

[8 points] Consider a single-platter disk with the following parameters: rotation speed: 3600 rpm; number of tracks on one side of platter: 15,000; number of sectors per track: 300; seek time: 2 ms for every hundred tracks traversed. Let the disk receive a request to read 5 consecutive sectors starting at a random sector on a random track and assume the disk head starts at track 0.

- (a) What is the average seek time?
- (b) What is the average rotational latency?
- (c) What is the transfer time for one sector?
- (d) What is the total average time to satisfy the request?

Solution

2, (a) ~~14,999~~/2 tracks are traversed on average
 (8) \Rightarrow Av. seek time = $\frac{14,999}{2} \times \frac{2 \text{ ms}}{100} = 149.99 \text{ ms}$

(b) Av. rot. delay = $\frac{1}{2r} = \frac{60 \times 10^3}{2 \times 3600} = 8.33 \text{ ms}$

(c) Transfer time for a sector = $\frac{\text{Transfer time for a track}}{300}$
 $= \frac{60 \times 10^3 / 3600}{300} = 0.056 \text{ ms}$

(d) Time to satisfy request =
 $149.99 + 8.33 + 5 \times 0.056$
 $= 158.603$

[6 points] Consider a magnetic disk in which the physical addresses (2,4,9) and (3,5,4) are mapped to the logical addresses 1288 and 1859, respectively.

- What is the number of sectors per track?
- What is the number of heads per cylinder?
- What is the disk capacity (in GB) knowing that the capacity of each sector is 512 byte, and each platter surface has 16384 tracks.
- What is the maximum data transfer rate (in Mbps) knowing that the spindle speed is 5400 rpm.

Solution

(a) $\star (2, 4, 9) \rightsquigarrow 1288$

$$\Rightarrow ((2 * HPC) + 4) * SPT + 9 - 1 = 1288$$

$$\Rightarrow HPC * SPT = 640 - 2 * SPT \rightarrow \textcircled{1}$$

$\star (3, 5, 4) \rightsquigarrow 1859$

$$\Rightarrow ((3 * HPC) + 5) * SPT + 4 - 1 = 1859$$

$$\Rightarrow HPC * SPT = \frac{1}{3} (1856 - 5 * SPT) \rightarrow \textcircled{2}$$

From $\textcircled{1}, \textcircled{2}$: $640 - 2 * SPT = \frac{1}{3} (1856 - 5 * SPT)$

$$SPT = 640 * 3 - 1856 = \boxed{64}$$

(b) From $\textcircled{1}$: $HPC = \frac{640 - 2 * 64}{64} = \boxed{8}$

(c) Disk Capacity = $\frac{\text{total \# of tracks/disk}}{\text{heads/cylinder}} * \text{sectors/track} * \text{byte/sector}$

$$= 16384 \text{ (cylinder)} * 8 \text{ heads/cylinder} * 64 \text{ sectors/track} * 512 \text{ byte/sector}$$

(d) Maximum data rate =

$$\begin{aligned}
 & \# \text{ of tracks/sec} \times \text{track capacity} \\
 & = \frac{5400 \text{ track/min}}{60 \text{ sec/min}} \times 64 \text{ sector/track} \times 512 \text{ B/sector} \\
 & = 2,949,120 \text{ B/s} \\
 & = 2,949,120 \times \frac{8}{10^6} \text{ Mb/s} \quad \leftarrow \text{Mega bit per second (Mbps)} \\
 & = 2,949,120 \times \frac{8}{2^{20}} \text{ Mib/s} \quad \leftarrow \text{Mebi bit per second}
 \end{aligned}$$

[9 points] Consider a magnetic disk with the following parameters: 300 GB capacity; 3 double-sided platters; 7200 rpm spindle speed; 32768 tracks per side; 4096 bytes per sector; 1 ms seek time for

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each thousand tracks traversed.

- (a) What is the number of heads per cylinder?
- (b) What is the number of sectors per track?
- (c) Suppose the heads are initially positioned at cylinder 0 and then the disk receives a request to read a 120 KB block of data stored on consecutive sectors starting at logical address 4800499.
 - i. What is the physical address of the starting sector of the block?
 - ii. What is the seek time taken to satisfy this read request?
 - iii. What is the transfer time taken to satisfy this read request?

Solution

$$\begin{aligned} 2. (a) & \text{ 3 double-sided platters } \Rightarrow HPC = 3 * 2 = 6 \\ (b) & \text{ Capacity} = HPC * \text{Tracks per side} * SPT * \text{bytes per sector} \\ 300 * 2^{30} \text{ B} &= 6 * 32768 * SPT * 4096 \text{ B} \\ SPT &= 400 \end{aligned}$$

2) i. The physical address (C, H, S) of the starting sector (whose LBA = 4800499)

$$C = \text{LBA} \div_{\text{int}} (\text{SPT} * \text{HPC}) = 2000$$

$$H = (\text{LBA} \div_{\text{int}} \text{SPT}) \bmod \text{HPC} = 1$$

$$S = (\text{LBA} \bmod \text{SPT}) + 1 = 100$$

iii. Transfer time = $\frac{b}{rN}$

$$= \frac{\overbrace{120 * 2^{10}}^b}{\underbrace{(7200/60)}_r * \underbrace{400 * 4096}_N}$$

$$= 625 \text{ } \mu\text{sec}$$
