

# CSE 620: Selective Topics

# Introduction to Formal Verification

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Master Studies in CSE  
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**Lecture #8**



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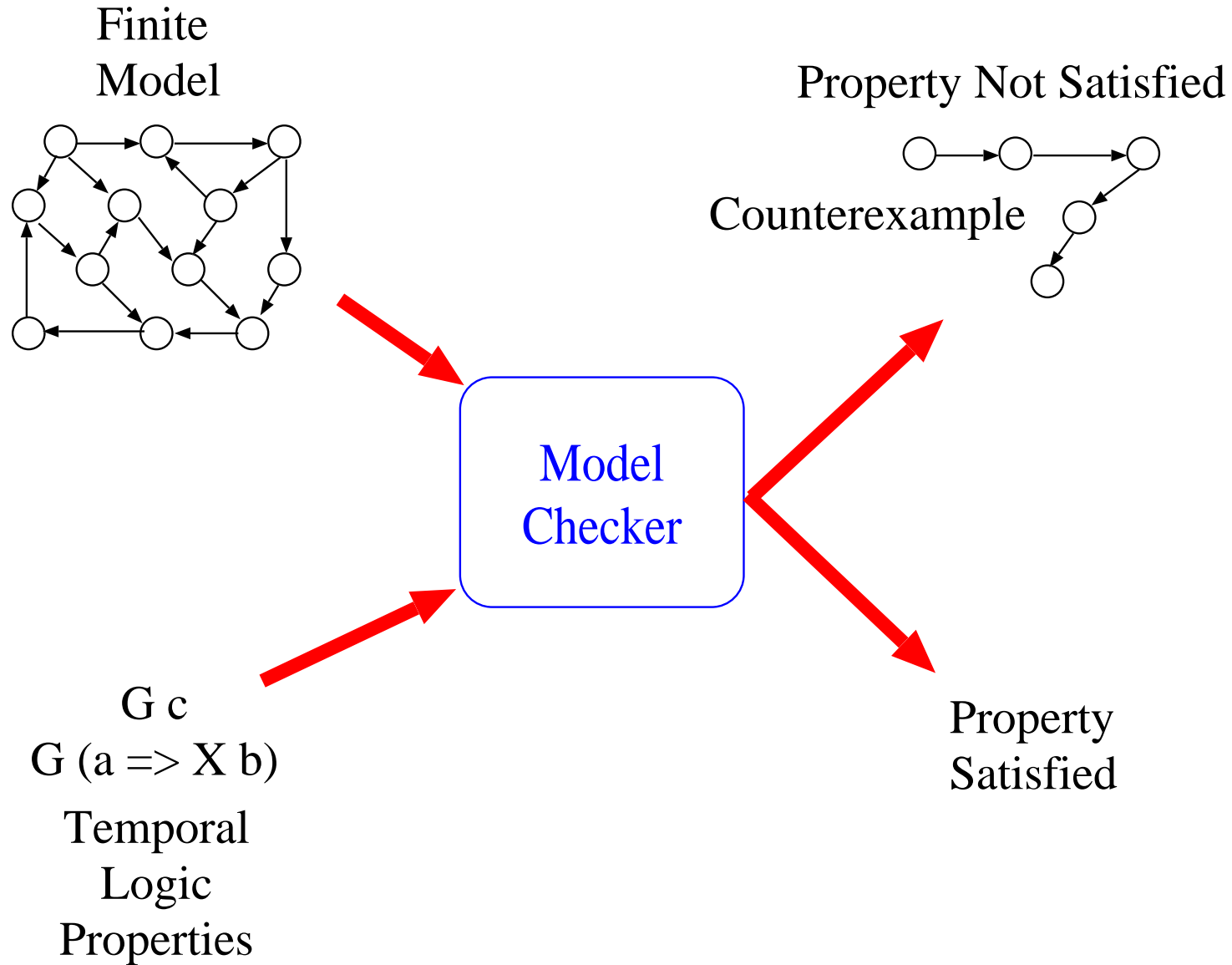
# Course Outline

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- Computational Boolean Algebra
  - Basics
    - Shannon Expansion
    - Boolean Difference
    - Quantification Operators
      - + Application to Logic Network Repair
  - Validity Checking (Tautology Checking)
  - Binary Decision Diagrams (BDD's)
  - Satisfiability Checking (SAT solving)
- Model Checking
  - Temporal Logics → LTL - CTL
  - **SMV: Symbolic Model Verifier**
  - Model Checking Algorithms → Explicit CTL



# Model Checking



# Symbolic Model Verifier (SMV)

SMV is a program that checks  $\mathcal{M} \models \phi$  for a  $\phi$  that is a property in the temporal logics LTL and CTL. We will be using LTL.

- ▶ Developed to verify synchronous circuits
- ▶ Extended to verify asynchronous circuits
- ▶ Successfully used to verify models of **reactive systems**

Next we are going to talk about modelling systems using SMV. The SMV symbolic model checking algorithm will be described next week.

# Getting and installing SMV

Cadence SMV (extended SMV) can be found at:

[http://www.cadence.com/webforms/cbl\\_software/index.aspx](http://www.cadence.com/webforms/cbl_software/index.aspx)

You have to fill in a registration form. You can get SMV for various platforms.

Run the executable `vw`. Like HOL, you edit your model description as a text file and load it into SMV.

Look in `smv/doc/smv` for a tutorial, and SMV examples.

# Reactive Systems

- ▶ System interacts with its environment, monitoring and responding to environmental events
- ▶ Computation may not terminate
- ▶ System behaviour changes over time, in reaction to history of inputs
- ▶ Complexity is due to **concurrency and interactions** among components
- ▶ **Examples:** operating systems, embedded systems, process-control systems, financial trading systems, automated banking machines, etc.

# Compared to Transformational Programs

- ▶ Program computes a function from inputs to outputs
- ▶ Complexity is in **data transformations**
- ▶ **Examples:** compilers, filters, payroll systems, scientific computations

# SMV Modelling

- ▶ Goal is to describe **control and interaction**. Hence, no complex data structures, not much data manipulation.
- ▶ SMV Language: **Communicating Finite State Machines** (FSMs with variables)
- ▶ System may consist of several **modules**
- ▶ Modules consist of several simple **parallel assignments**
- ▶ Model may also specify **constraints on environment's behaviour**



# SMV Modelling

A system is described as a **set of modules**. Each module is a reactive system interacting with other modules and the system's environment.

Each modules has **variables** that it reacts to, and that is manipulates.

In each module, there are variable declarations, assignments to variables, and properties that we want to check.

The **main** module is like a main program. In the simplest SMV descriptions we use only the main module, and no sub-modules.

Modules can be parameterized and the main module can creating instances of modules to describe the system.

# Example Specification (echo1.smv)

```
MODULE main ()
{
    signal : boolean;
    echo   : boolean;

    init(echo) := 0;

    next(echo) := signal;

    mypropname: assert G (signal <-> X (echo));

}
```

# Example Specification (echo1.smv)

## Example Traces:

```
signal: 01001000100001...  
echo:   001001000100001...
```

```
signal: 11001100110011...  
echo:   011001100110011...
```

At the prompt, type “vw echo1.smv &”

# Example Specification (echo2.smv)

```
MODULE main ()
{
    signal : boolean;
    echo   : boolean;

    init(echo) := 0;

    next(echo) := signal & 1 ;

    mypropname: assert G (signal <-> X (echo));
}
```

See [echo2.smv](#)

# Example Specification (echo3.smv)

```
MODULE main ()
{
    signal : boolean;
    echo   : boolean;

    init(echo) := 0;

    next(echo) := signal & 0 ;

    mypropname: assert G (signal <-> X (echo));
}
```

See [echo3.smv](#)

# SMV Modelling

Recall that the SMV modelling notation is used to describe communicating finite state machines.

It consists of a set of modules, with one **main** module.

In each module there are:

- ▶ variables declarations,
- ▶ variable initialization,
- ▶ assignments, and
- ▶ properties that we want to check.

# Variables

Variables can be boolean, enumerated types, integer subranges, user-defined modules, or an array of any of these:

```
var1 : {on, off};  
var2 : array 2..5 of {on, off};  
var3 : array 1..10 of array 2..5 of boolean;  
var4 : Inverter(1);  
var5 : array on..off of boolean;    -- error  
var6 : {enabled, active, off};      -- error  
var7 : 0..6;
```

# Variables

- ▶ Enumerated values must be distinct, from each other and from integer values
- ▶ Boolean values are 0 and 1
- ▶ Boolean operations are:  $\sim$  (not),  $\&$  (and),  $|$  (or),  $\wedge$  (xor),  $\rightarrow$  (implies),  $\leftrightarrow$  (iff)
- ▶ Array subscripts must evaluate to integers (preferably constants)
- ▶ Comments are delimited by `--` and a newline



# Execution Model

- ▶ System state  $\mathcal{S}$  is defined by the variables' values

$$v_1:T_1; \ v_2:T_2; \ \dots; \ v_n:T_n;$$

$$\mathcal{S} \in T_1 \times T_2 \times \dots \times T_n$$

- ▶ Each variable is either **controlled by the system** (i.e., the model explicitly assigns values to the variable) or is **controlled by the environment** (i.e., can be thought of as an input variable).

# Execution Model

- ▶ **Round-based execution**: initialization round followed by a sequence of update rounds. In each round
  - ▶ the environment-controlled variables **non-deterministically change value**
  - ▶ the system executes its **parallel assignment statements**
  - ▶ the result is a **new system state**
- ▶ Variable assignments may either take effect in the next system state (**sequential/unit delay**)  
     $\text{next}(x) := y + 3;$   
or be effective immediately (**combinational/derived**)  
     $x := y + 3;$

# Assignments

**Conditional Assignments:** if-then-else returns the value assigned.  
The condition or guard is a Boolean expression over variables.

## Examples:

In a case statement  
the conditions are  
evaluated in order.

```
next(y) := (a | b) ? x : x+1;
```

```
next(k) := case {  
    c1 : x1;  
    c2 : x2;  
    ...  
    default : z;  
};
```

## Example: Thermostat (See therm1.smv)

```
MODULE main()
{
    temp : {hot, cold, justright}; -- room temperature
    active : boolean;               -- is thermostat on?
    heat : boolean;                 -- is furnace on?
    aircond : boolean;             -- is aircond on?

    init(heat) := 0;
    next(heat) := case {
        active & (temp=cold) : 1 ;
        ~active | ~(temp=cold) : 0;
    };
    init(aircond) := 0;
    next(aircond) := case {
        active & (temp=hot) : 1 ;
        ~active | ~(temp=hot) : 0 ;
    };
};
```

# Example: Thermostat

Better properties:

```
prop2: assert G
        ((active & temp=hot) -> X aircond);
```

```
prop3: assert G
        ((active & temp=cold) -> X heat);
```

See [therm2.smv](#)

# Case Statements

Case statements are evaluated in top-down order. In the thermostat example, the guards are mutually exclusive. Let's add a user override:

```
input turnheattoff: boolean;
next(heat) := case {
    active & (temp=cold): 1;
    ~active | ~(temp=cold) : 0;
    turnheattoff : 0;
};
prop4: assert G (turnheattoff -> X ~heat);
```

Can we prove prop3 and prop4?

See [therm3.smv](#), [therm4.smv](#), [therm5.smv](#)

# Non-Determinism

**Non-determinism:** more than one outcome possible.

Ways to have non-determinism in SMV models:

- ▶ **Input:** A variable is not assigned any value.

- ▶ **Non-deterministic assignments**

$$x := \{1, 2, 3, 4\};$$

- ▶ **Undefined assignments**

A variable of undefined value may take on any value in its type. See examples next page. Note: undefined assignments are **not** a good idea!

# Undefined Assignments

- ▶ **Example:** A variable that is assigned a value outside the range of its declared type:

```
on : boolean;  
on := 4;
```

- ▶ **Example:** If a conditional assignment is not total (i.e., there exists a condition not covered by any clause):

```
y := c1 ? x;           z := case {  
                        c1 : x1;  
                        c2 : x2;  
                        c3 : x3;  
                        };
```

where  $c1 \vee c2 \vee c3$  isn't a tautology.



# Environmental Assumptions

- ▶ Some counter-examples exhibit undesirable system behaviour **in response to invalid environmental input**. These are called **infeasible paths**.
- ▶ Sometimes we need to constrain how environmental variables change value, in order to model a realistic environment. One option is include a model of the environment in your system description:

```
next(temp) := case {  
  temp=hot : {justright, hot};  
  temp=justright : {cold, justright, hot};  
  temp=cold : {cold, justright}  
};
```

The verification is valid as long as environmental assumptions are true.

# Common Errors

SMV must be able to compute set of possible next states

## Single Assignment Rule

Can only have one assignment statement for each variable

- ▶ The following is invalid

```
next(x) := y;  
next(x) := z;
```

- ▶ Can assign value to:
  - ▶ x, or
  - ▶ next(x) and init(x),but not both.

# Common Errors

## Circular Dependency Rule

Cannot have a cycle of dependencies all of whose assignments take effect immediately. That is, the system can't have a set of variables whose current values depends on the current values of each other and vice versa (can't have a combinational loop):

```
x := y;  
y := z;  
z := x;
```

SMV should give you a syntax error for all of these mistakes.

# SMV Models and Kripke Structures

An SMV model represents a Kripke structure.

```
MODULE main()  
{  
    request: boolean;  
    status: {ready, busy};  
  
    init(status) := ready;  
    next(status) := case {  
        request : busy;  
        default: {ready, busy};  
    };  
}
```

From: Huth and Ryan [R18].

# SMV Modules

So far, we've only been using the “main” module.

A **module** bundles together definitions (type declarations and assignments). These definitions can then be reused.

Modules have three kinds of variables: **input**, **output**, **private**.

Input and output variables are labelled as such (keywords: INPUT and OUTPUT) and included in the list of formal parameters of the module. These variables are pass by reference.

# SMV Modules

The input variables of the main module are the environmental variables.

All module variables are visible to other modules and to the environment.

However, for modularity. modules shouldn't refer to each other's private variables directly!

# Example Module

```
MODULE half_adder(a, b, cout, sum)
{
  INPUT a, b : boolean;
  OUTPUT cout, sum : boolean;

  -- combinational
  sum := (a & ~b) | (~a & b);  -- corrected here
  cout := a & b;
}
```

# Module Instantiations

ADD1:

```
input in1, in2, cin1: boolean;  
output sum1, cout1: boolean;  
w1,w2,w3: boolean;
```

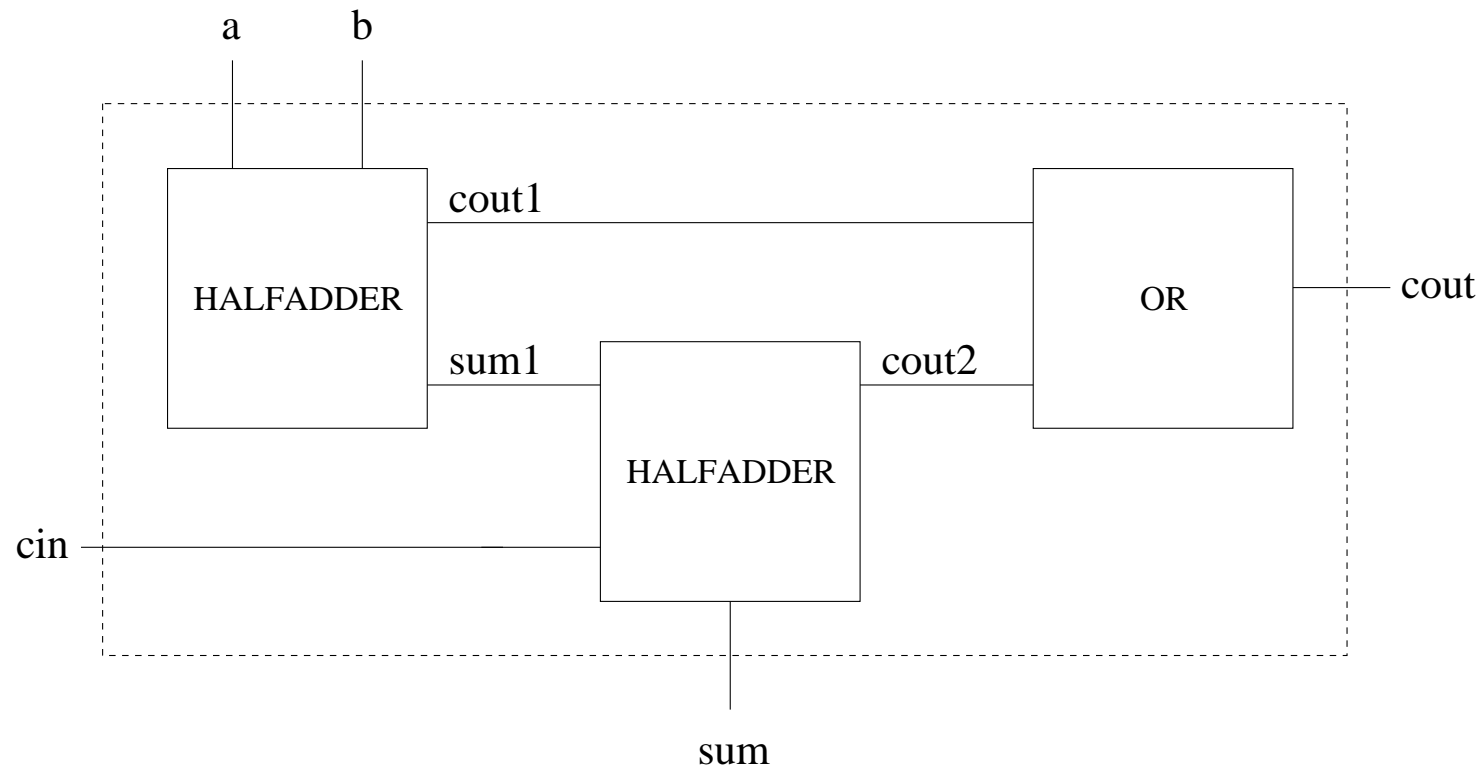
```
bit0 : half_adder(in1, in2, w1, w2);  
bit1 : half_adder(w2, cin1, w3, sum1);
```

Then we can use: bit0.a, bit0.cout, etc.

(Don't forget we'd also need an OR-gate.)



# Full Adder



Make outputs “sum” and “cout” unit delayed.

See [adder.smv](#)

Note: in our properties, we can't refer to the value at the previous time step, so we have to write more properties to describe the behaviour of an adder.

# Modules with Types

“A module with only type declarations and no parameters or assignments acts like a structured data type.” (SMV Language Reference Manual, 2001)

```
MODULE point(start)
{
    x,y: start..6;
}
```

```
MODULE main()
{
    mypt: point(1);
    j: 0..6;

    next(j) := mypt.x;
}
```