

CSE 411: Artificial Intelligence (Elective Course #6)

400 Level, Mechatronics Engineering 2nd Term 2016/2017, Lecture #3

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March 13th, 2017

Credits to Dr. Mohamed El Abd for the slides

Adminstrivia

Notes

- Assignment #1:
 - Released today.
 - Due: **Monday, March 20, 2017**
 - Formulate two problems in Python.
 - Email Python files and hand in a printout!

Course Info:

- Website: <http://hshehata.github.io/courses/zu/cse411/>
- Office hours: Sunday 11:30am - 12:30pm

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 - Formulate two problems in Python.
 - Email Python files and hand in a printout!
- "Requirements & Reading Material" section:
 - Page numbers are based on 3rd US edition of AIMA.
 - Full TOC: <http://aima.cs.berkeley.edu/contents.html>.

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Introduction

- One approach to solve any problem is to formulate it in ***STATE-SPACE*** representation.

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Introduction

- One approach to solve any problem is to formulate it in **STATE-SPACE** representation.
- The problem is well-defined by defining:
 - An initial state.
 - A set of actions.
 - A transition model.
 - A goal test.
 - A concept of cost: step and path cost.

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- One approach to solve any problem is to formulate it in **STATE-SPACE** representation.
- The problem is well-defined by defining:
 - An initial state.
 - A set of actions.
 - A transition model.
 - A goal test.
 - A concept of cost: step and path cost.
- This is used to build a search tree to be traversed by a tree-search (or graph-search) algorithm.

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A puzzle example

6	2	
7	1	8
4	5	3

	1	2
3	4	5
6	7	8

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- **Initial state:** any arrangement of tiles.

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- **Transition model:** given a state and action, return a new state by switching one tile with the blank.
- **Goal test:** are the tiles in the goal state order?
- **Path cost:** each step costs 1, so path cost is the number of steps along the path.

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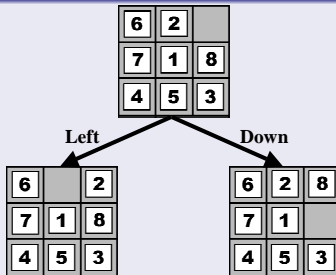
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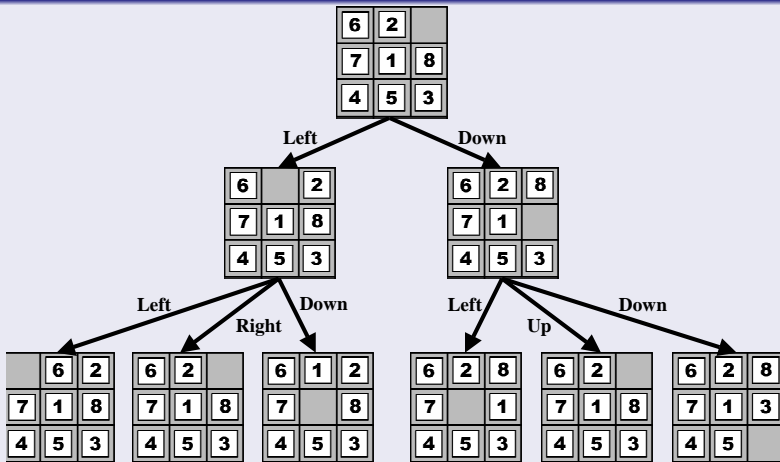
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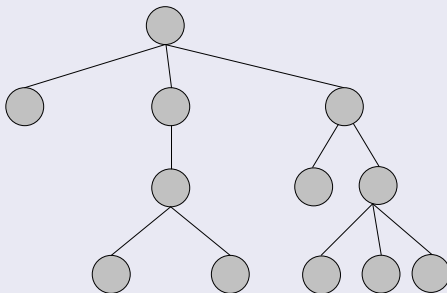
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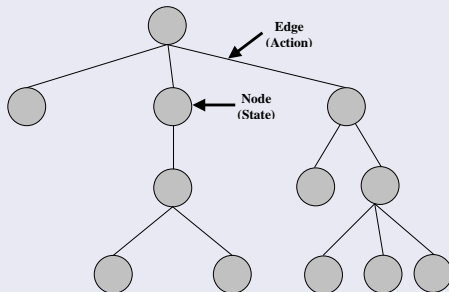
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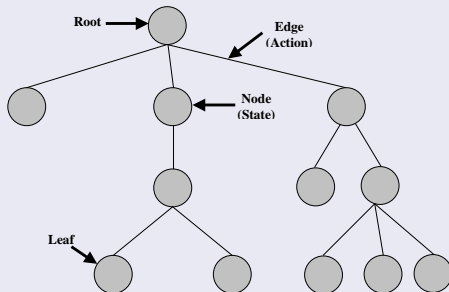
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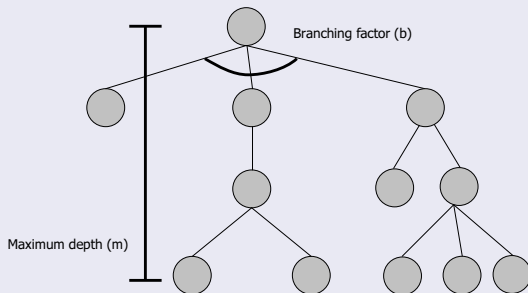
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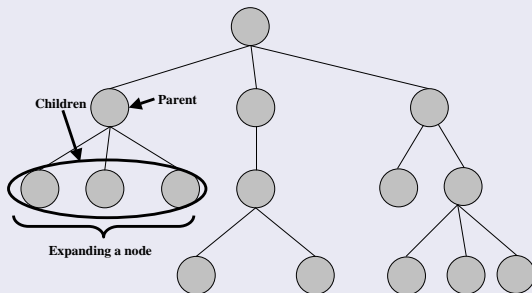
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General tree-search algorithm

TREE-SEARCH(*problem*) **returns** a solution, or failure

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General tree-search algorithm

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    if the frontier is empty then return failure
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    if the node contains a goal state then return the corresponding solution
    expand the chosen node, adding the resulting node to the frontier
  end
```

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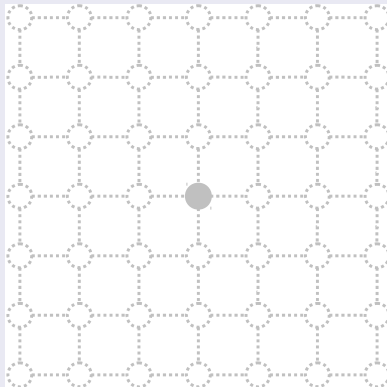
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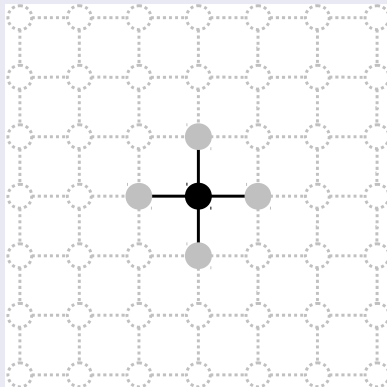
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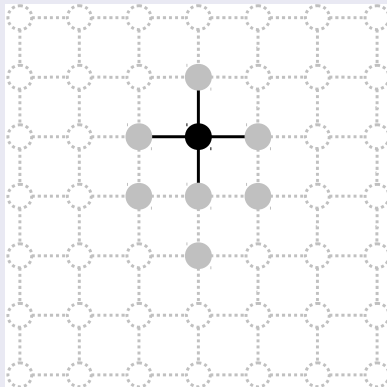
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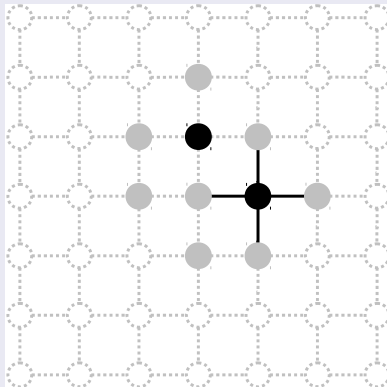
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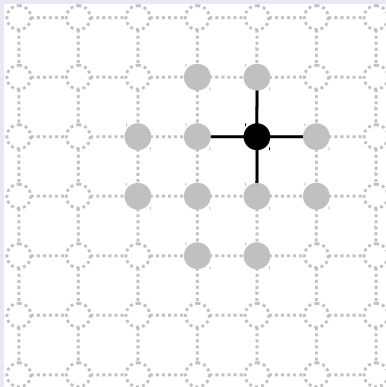
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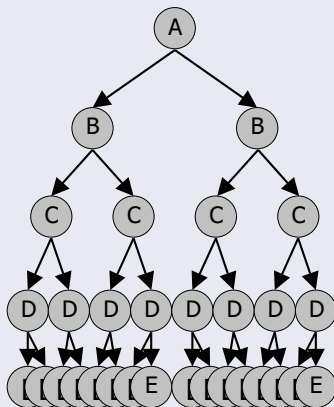
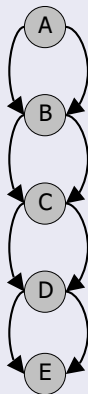
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Multiple paths to the same state



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Repeated states

- Unavoidable in problems where:
 - Actions are reversible (*e.g.*, , rectangular grid problems).
 - Multiple paths to the same state are possible.

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Repeated states

- Unavoidable in problems where:
 - Actions are reversible (*e.g.*, , rectangular grid problems).
 - Multiple paths to the same state are possible.
- Can greatly increase the number of nodes in a tree or even make a finite tree infinite.

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Repeated states

- Unavoidable in problems where:
 - Actions are reversible (*e.g.*, , rectangular grid problems).
 - Multiple paths to the same state are possible.
- Can greatly increase the number of nodes in a tree or even make a finite tree infinite.
- Can be solved by augmenting the tree search algorithm with a data structure called the **explored set** (a.k.a., the closed list) to keep track of the explored states.

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Repeated states

- Unavoidable in problems where:
 - Actions are reversible (*e.g.*, , rectangular grid problems).
 - Multiple paths to the same state are possible.
- Can greatly increase the number of nodes in a tree or even make a finite tree infinite.
- Can be solved by augmenting the tree search algorithm with a data structure called the **explored set** (a.k.a., the closed list) to keep track of the explored states.
- The tree search algorithm becomes a graph search algorithm.

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General graph-search algorithm

GRAPH-SEARCH(*problem*) **returns** a solution, or failure
initialize the frontier using the initial state of a *problem*

...

loop do

if the frontier is empty **then return** failure

 choose a leaf node and remove it from the frontier

if the node contains a goal state **then return** the corresponding solution

 ...

 expand the chosen node, adding the resulting node to the frontier

 ...

end

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General graph-search algorithm

```
GRAPH-SEARCH(problem) returns a solution, or failure
  initialize the frontier using the initial state of a problem
  initialize the explored set to be empty
  loop do
    if the frontier is empty then return failure
    choose a leaf node and remove it from the frontier
    if the node contains a goal state then return the corresponding solution
    ...
    expand the chosen node, adding the resulting node to the frontier
    ...
  end
```

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GRAPH-SEARCH(problem) returns a solution, or failure
  initialize the frontier using the initial state of a problem
  initialize the explored set to be empty
  loop do
    if the frontier is empty then return failure
    choose a leaf node and remove it from the frontier
    if the node contains a goal state then return the corresponding solution
    add the node to the explored set
    expand the chosen node, adding the resulting node to the frontier
    ...
  end
```

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General graph-search algorithm

```
GRAPH-SEARCH(problem) returns a solution, or failure
  initialize the frontier using the initial state of a problem
  initialize the explored set to be empty
  loop do
    if the frontier is empty then return failure
    choose a leaf node and remove it from the frontier
    if the node contains a goal state then return the corresponding solution
    add the node to the explored set
    expand the chosen node, adding the resulting node to the frontier
    only if not in the frontier and not in the explored set
  end
```

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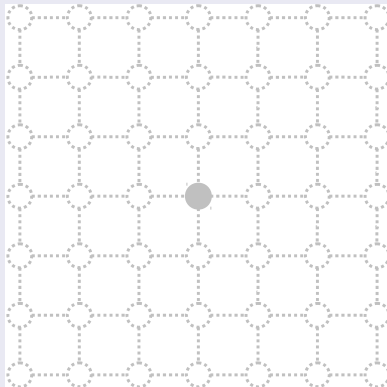
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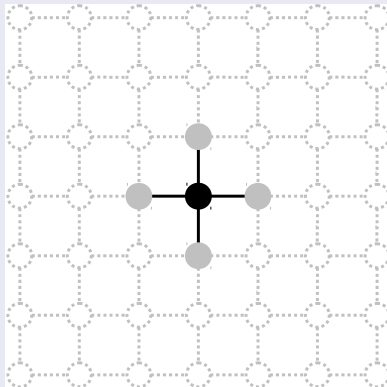
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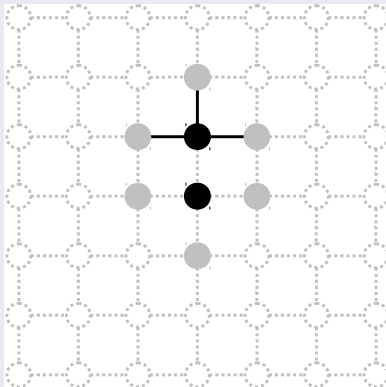
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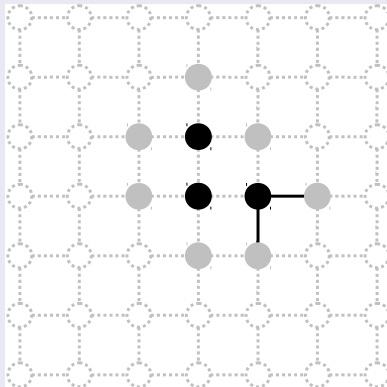
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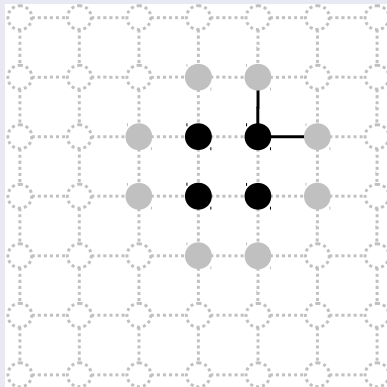
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Properties of search algorithms

- The method in which a search algorithm **traverses** the tree is known as the ***search strategy***.

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Properties of search algorithms

- The method in which a search algorithm **traverses** the tree is known as the ***search strategy***.
- The ***search strategy*** is defined by the method used by the algorithm for ***choosing*** the next node from the frontier (a.k.a., fringe or open list).

Search Algorithms

Properties of search algorithms

- **Completeness:**

Is the algorithm guaranteed to find a goal node, if one exists?

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Properties of search algorithms

- **Completeness:**

Is the algorithm guaranteed to find a goal node, if one exists?

- **Optimality:**

Is the algorithm guaranteed to find the best goal node, i.e. the one with the cheapest path cost?

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- **Completeness:**

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- **Optimality:**

Is the algorithm guaranteed to find the best goal node, i.e. the one with the cheapest path cost?

- **Time complexity:**

How many nodes are generated?

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Is the algorithm guaranteed to find a goal node, if one exists?

- **Optimality:**

Is the algorithm guaranteed to find the best goal node, i.e. the one with the cheapest path cost?

- **Time complexity:**

How many nodes are generated?

- **Space complexity:**

What is the maximum number of nodes stored in memory?

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Properties of search algorithms

Time and space complexities are measured in terms of:

- Branching factor, b ,

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Properties of search algorithms

Time and space complexities are measured in terms of:

- Branching factor, b ,
- Depth of least cost solution , d ,

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Properties of search algorithms

Time and space complexities are measured in terms of:

- Branching factor, b ,
- Depth of least cost solution , d ,
- Maximum depth of the search tree, m ,

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Infrastructure for search algorithms

- Special data structures are needed to represent: the **problem**, the **nodes**, the **frontier**, and the **explored** states.

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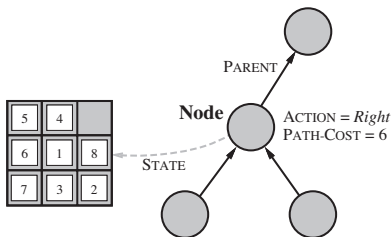
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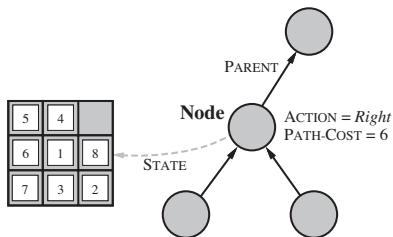
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Search Algorithms

Infrastructure for search algorithms

- Special data structures are needed to represent: the **problem**, the **nodes**, the **frontier**, and the **explored** states.
- Each node n has the following components:
 - $n.STATE$, $n.PARENT$, $n.ACTION$, $n.PATH-COST$, $n.CHILD-NODE(problem, action)$, and $n.SOLUTION()$



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Infrastructure for search algorithms

- Each problem p has the following components:
 - p .INITIAL-STATE, p .ACTIONS($state$), p .RESULT($state$, $action$), p .GOAL-TEST($state$), p .STEP-COST($state$, $action$).

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Infrastructure for search algorithms

- Each problem p has the following components:
 - p .INITIAL-STATE, p .ACTIONS($state$), p .RESULT($state$, $action$), p .GOAL-TEST($state$), p .STEP-COST($state$, $action$).
- Frontier f is represented as a (FIFO, LIFO, or priority) queue that has the following components:
 - f .EMPTY?(), f .INSERT($element$), and f .POP()

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Infrastructure for search algorithms

- Each problem p has the following components:
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 - f .EMPTY?(), f .INSERT($element$), and f .POP()
- Explored states are kept track of using a data structure that acts as a set.

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Types of search algorithms

- **Uninformed Search:**

Only has the information provided by the problem formulation (initial state, available actions, transition model, goal test, and step/path cost),

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Types of search algorithms

- **Uninformed Search:**

Only has the information provided by the problem formulation (initial state, available actions, transition model, goal test, and step/path cost),

- **Informed Search:**

Has additional information that allows it to judge the promise of an action, i.e. the estimated cost from a state to a goal.

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- Breadth-first search (BFS),
- Depth-first search (DFS),
- Depth-limited search,
- Iterative deepening search (IDS),
- Uniform-cost search

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- The frontier is implemented as a FIFO queue,
- The tree is traversed on a level-by-level basis.

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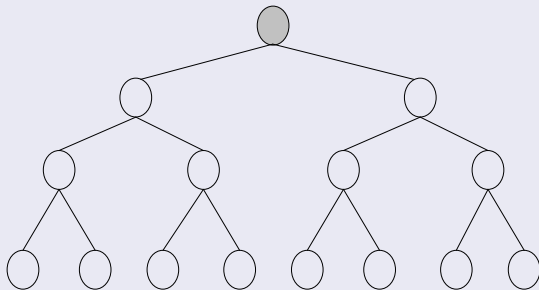
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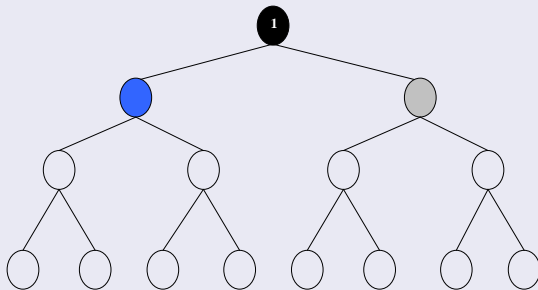
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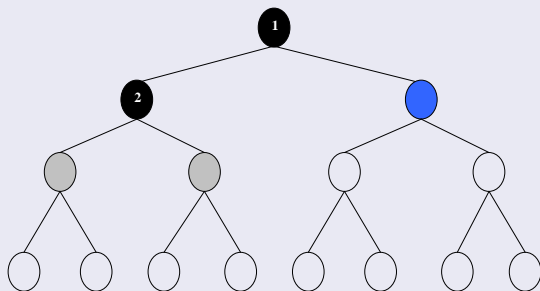
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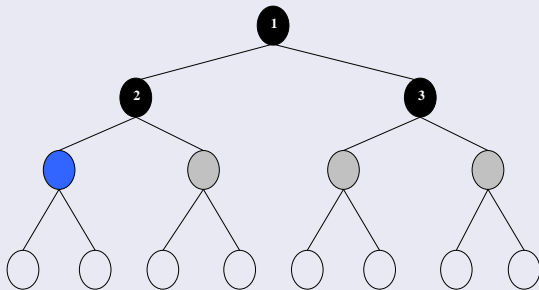
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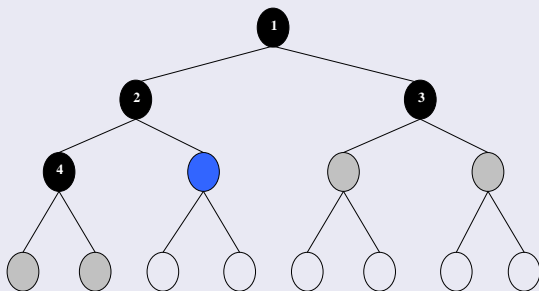
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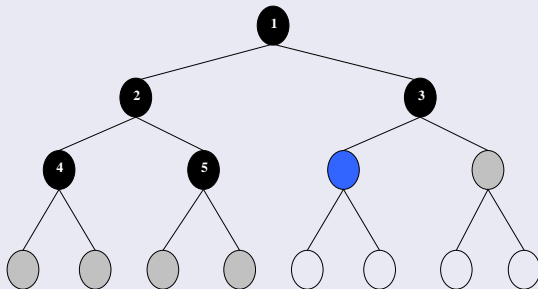
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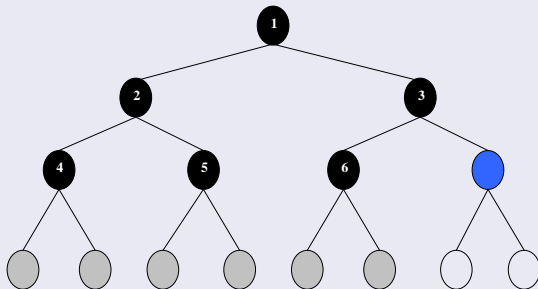
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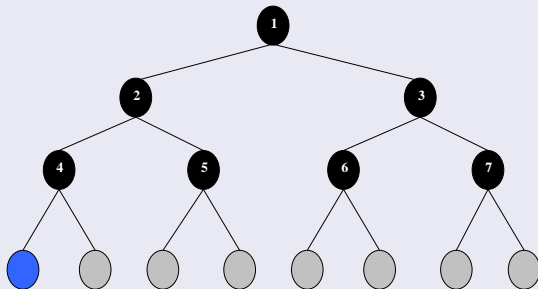
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Breadth-first search (tree version)

function BREADTH-FIRST-SEARCH(*problem*) **returns** a solution, or failure

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Search Algorithms

Breadth-first search (tree version)

function BREADTH-FIRST-SEARCH(*problem*) **returns** a solution, or failure
node \leftarrow a node with STATE=*problem*.INITIAL-STATE, PATH-COST=0

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Breadth-first search (tree version)

```
function BREADTH-FIRST-SEARCH(problem) returns a solution, or failure  
  node ← a node with STATE=problem.INITIAL-STATE, PATH-COST=0  
  if problem.GOAL-TEST(node.STATE) then return node.SOLUTION()
```

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Breadth-first search (tree version)

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function BREADTH-FIRST-SEARCH(problem) returns a solution, or failure  
  node ← a node with STATE=problem.INITIAL-STATE, PATH-COST=0  
  if problem.GOAL-TEST(node.STATE) then return node.SOLUTION()  
  frontier ← a FIFO queue with node as the only element
```

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Breadth-first search (tree version)

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  node ← a node with STATE=problem.INITIAL-STATE, PATH-COST=0
  if problem.GOAL-TEST(node.STATE) then return node.SOLUTION()
  frontier ← a FIFO queue with node as the only element
  loop do
```

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Breadth-first search (tree version)

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  if problem.GOAL-TEST(node.STATE) then return node.SOLUTION()
  frontier ← a FIFO queue with node as the only element
  loop do
    if frontier.EMPTY?() then return failure
```

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Breadth-first search (tree version)

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  node ← a node with STATE=problem.INITIAL-STATE, PATH-COST=0
  if problem.GOAL-TEST(node.STATE) then return node.SOLUTION()
  frontier ← a FIFO queue with node as the only element
  loop do
    if frontier.EMPTY?() then return failure
    node ← frontier.POP()          /* choose shallowest node in frontier */
```

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Breadth-first search (tree version)

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  if problem.GOAL-TEST(node.STATE) then return node.SOLUTION()
  frontier ← a FIFO queue with node as the only element
  loop do
    if frontier.EMPTY?() then return failure
    node ← frontier.POP()           /* choose shallowest node in frontier */
    for each action in problem.ACTIONS(node.STATE) do
```

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Breadth-first search (tree version)

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function BREADTH-FIRST-SEARCH(problem) returns a solution, or failure
  node ← a node with STATE=problem.INITIAL-STATE, PATH-COST=0
  if problem.GOAL-TEST(node.STATE) then return node.SOLUTION()
  frontier ← a FIFO queue with node as the only element
  loop do
    if frontier.EMPTY?() then return failure
    node ← frontier.POP()           /* choose shallowest node in frontier */
    for each action in problem.ACTIONS(node.STATE) do
      child ← node.CHILD-NODE(problem, action)
```

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Breadth-first search (tree version)

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    node ← frontier.POP()           /* choose shallowest node in frontier */
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      child ← node.CHILD-NODE(problem, action)
      if problem.GOAL-TEST(child.STATE) then return child.SOLUTION()
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Breadth-first search (tree version)

```
function BREADTH-FIRST-SEARCH(problem) returns a solution, or failure
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  frontier ← a FIFO queue with node as the only element
  loop do
    if frontier.EMPTY?() then return failure
    node ← frontier.POP()           /* choose shallowest node in frontier */
    for each action in problem.ACTIONS(node.STATE) do
      child ← node.CHILD-NODE(problem, action)
      if problem.GOAL-TEST(child.STATE) then return child.SOLUTION()
      frontier.INSERT(child)
```

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Breadth-first search (graph version)

```
function BREADTH-FIRST-SEARCH(problem) returns a solution, or failure
  node ← a node with STATE=problem.INITIAL-STATE, PATH-COST=0
  if problem.GOAL-TEST(node.STATE) then return node.SOLUTION()
  frontier ← a FIFO queue with node as the only element
  explored ← an empty set
  loop do
    if frontier.EMPTY?() then return failure
    node ← frontier.POP()           /* choose shallowest node in frontier */
    add node.STATE to explored
    for each action in problem.ACTIONS(node.STATE) do
      child ← node.CHILD-NODE(problem, action)
      if child.STATE is not in explored and not in frontier then
        if problem.GOAL-TEST(child.STATE) then return child.SOLUTION()
        frontier.INSERT(child)
```

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BFS properties:

- Complete (if b is finite).

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BFS properties:

- Complete (if b is finite).
- Optimal, if path cost is equal to depth:
 - Guaranteed to return the shallowest goal (depth d).

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BFS properties:

- Complete (if b is finite).
- Optimal, if path cost is equal to depth:
 - Guaranteed to return the shallowest goal (depth d).
- Time complexity = $O(b^d)$.

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BFS properties:

- Complete (if b is finite).
- Optimal, if path cost is equal to depth:
 - Guaranteed to return the shallowest goal (depth d).
- Time complexity = $O(b^d)$.
- Space complexity = $O(b^d)$.

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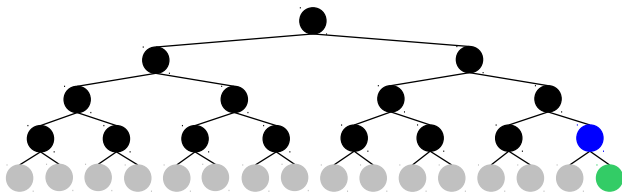
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BFS properties:

- Upper-bound case: when the goal node is the last node at depth d :



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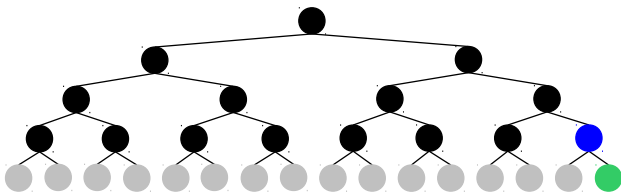
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BFS properties:

- Upper-bound case: when the goal node is the last node at depth d :
 - Goal is detected once goal node is generated.



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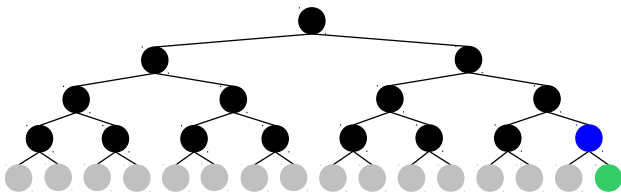
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BFS properties:

- Upper-bound case: when the goal node is the last node at depth d :
 - Goal is detected once goal node is generated.
 - Number of nodes generated:
$$b + b^2 + b^3 + \dots + b^d = O(b^d).$$



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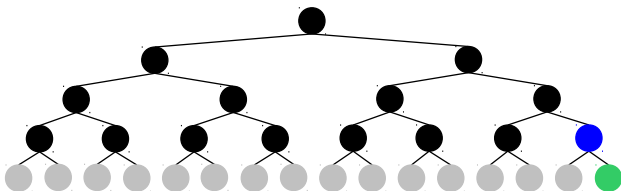
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BFS properties:

- Upper-bound case: when the goal node is the last node at depth d :
 - Goal is detected once goal node is generated.
 - Number of nodes generated:
 $b + b^2 + b^3 + \dots + b^d = O(b^d)$.
 - Space and time complexity: all generated nodes.



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- Algorithm is similar to BFS, except that the frontier is implemented as a LIFO queue (*i.e.*, stack).

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- Algorithm is similar to BFS, except that the frontier is implemented as a LIFO queue (*i.e.*, stack).
- Algorithm always expands deepest unexpanded node in current frontier.

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Depth-first search

- Algorithm is similar to BFS, except that the frontier is implemented as a LIFO queue (*i.e.*, stack).
- Algorithm always expands deepest unexpanded node in current frontier.
- Once a leaf is reached, the search backs up (*i.e.*, backtracks) to the next deepest node that still has unexplored successors.

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Depth-first search

- Algorithm is similar to BFS, except that the frontier is implemented as a LIFO queue (*i.e.*, stack).
- Algorithm always expands deepest unexpanded node in current frontier.
- Once a leaf is reached, the search backs up (*i.e.*, backtracks) to the next deepest node that still has unexplored successors.
- Search continues until reaching the goal or no frontier nodes are left for expansion.

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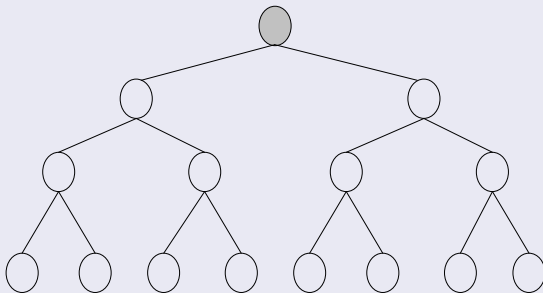
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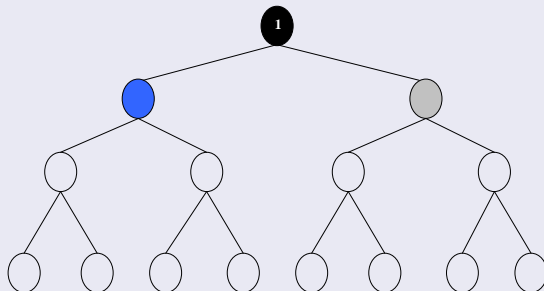
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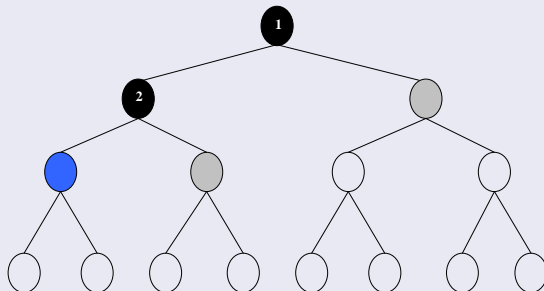
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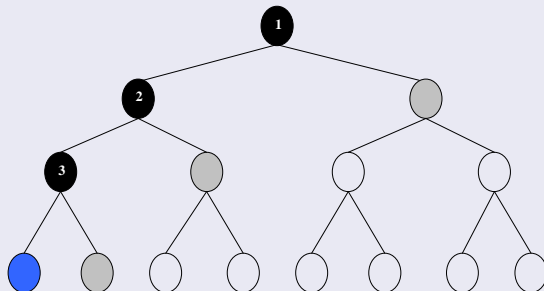
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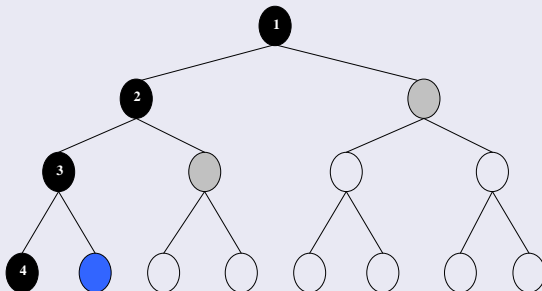
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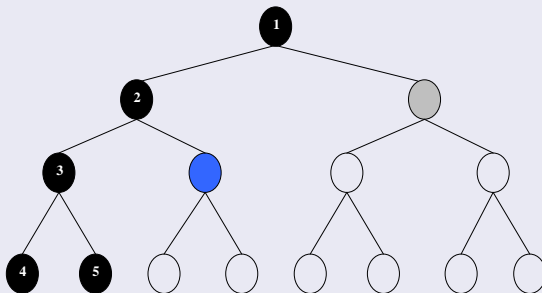
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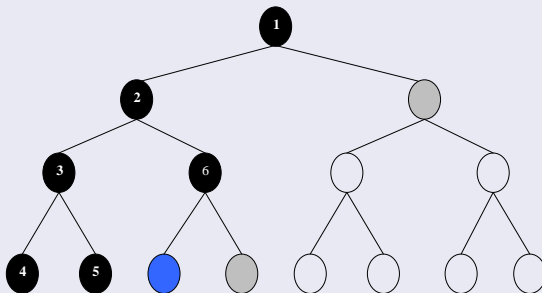
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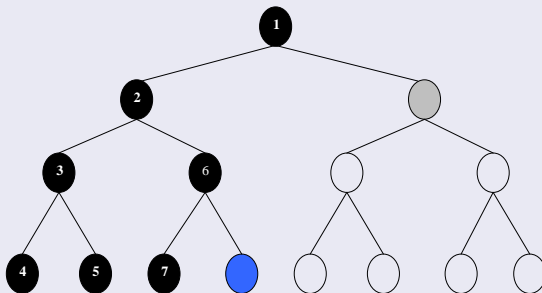
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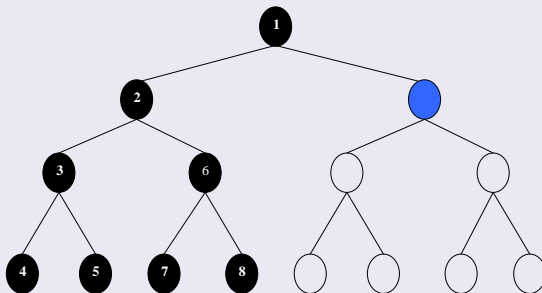
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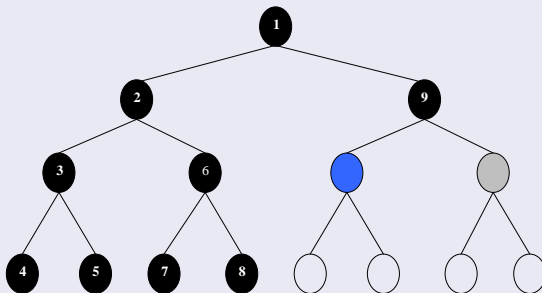
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DFS properties:

- Not complete (tree version).

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DFS properties:

- Not complete (tree version).
- Not Optimal.

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DFS properties:

- Not complete (tree version).
- Not Optimal.
- Time complexity = $O(b^m)$.

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DFS properties:

- Not complete (tree version).
- Not Optimal.
- Time complexity = $O(b^m)$.
- Space complexity = $O(bm)$.

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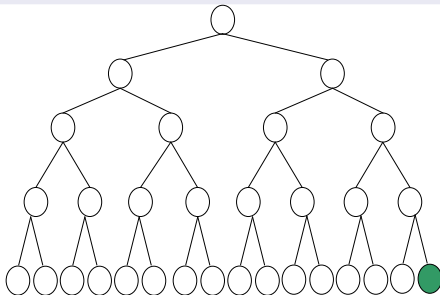
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DFS properties:

- Upper-bound case for time: goal is last node of last branch:



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Search
Algorithms

Problem solving by
searching
Search Algorithms

Uninformed
Search

Algorithms
Breadth-first search
Depth-first search

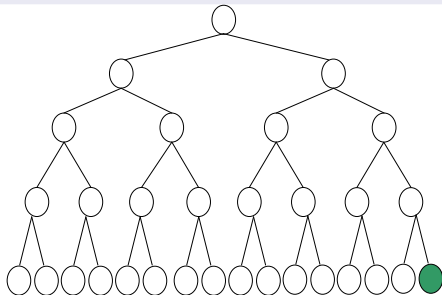
Requirements
& Reading
Material

Uninformed Search

Depth-first search

DFS properties:

- Upper-bound case for time: goal is last node of last branch:
- Number of nodes generated: b nodes for each node of m levels (entire tree).



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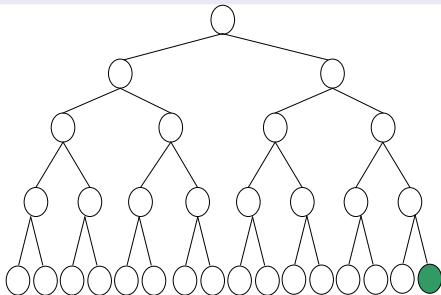
Requirements
& Reading
Material

Uninformed Search

Depth-first search

DFS properties:

- Upper-bound case for time: goal is last node of last branch:
- Number of nodes generated: b nodes for each node of m levels (entire tree).
- Time complexity: all generated nodes $O(b^m)$.



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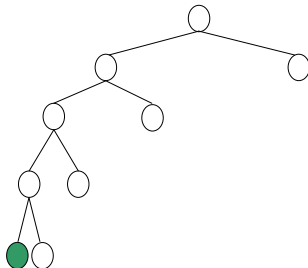
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Uninformed Search

Depth-first search

DFS properties:

- Upper-bound case for space: goal is last node of first branch:



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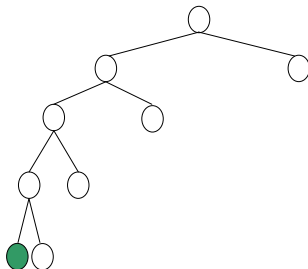
Requirements
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Material

Uninformed Search

Depth-first search

DFS properties:

- Upper-bound case for space: goal is last node of first branch:
 - Number of generated nodes: b nodes at each of m levels.



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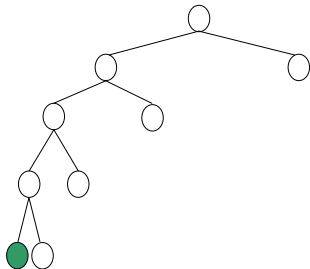
Requirements
& Reading
Material

Uninformed Search

Depth-first search

DFS properties:

- Upper-bound case for space: goal is last node of first branch:
 - Number of generated nodes: b nodes at each of m levels.
 - Space complexity: all generated nodes = $O(bm)$.



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2 Uninformed Search

3 Requirements & Reading Material

Requirements

What do I need from you

- When given a certain problem you should be able to:

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Requirements & Reading Material

Requirements

What do I need from you

- When given a certain problem you should be able to:
 - Build the search tree up to a given depth.

Requirements

What do I need from you

- When given a certain problem you should be able to:
 - Build the search tree up to a given depth.
 - Traverse the search tree according to a given strategy.

Requirements

What do I need from you

- When given a certain problem you should be able to:
 - Build the search tree up to a given depth.
 - Traverse the search tree according to a given strategy.
- Answer descriptive questions.

Reading Material

Which parts of the textbook are covered

- Russell-Norvig, Chapters 3:
 - Pages 75 - 83.
 - Pages 85 - 87.