

CSE 401: Computer Engineering (2)  
Fourth Year, Electronics & Communication Engineering

**Solution to Assignment #2**

1. Consider a 256 GB hard disk drive with the following parameters: 6.5 ms average seek time, ...  
(a) What is the spindle speed (in r.p.m)?

$$\text{Average rotational delay} = 1 / (2 * \text{spindle speed})$$

$$2.5 \text{ ms} = 1 / (2 * r)$$

$$\text{Spindle speed} = r = 1 / (2 * (2.5 * 10^{-3}) \text{ s}) = 200 \text{ r.p.s} = 200 * 60 \text{ r.p.m} = 12000 \text{ r.p.m}$$

- (b) What is the number of sectors per track?

$$\text{Maximum data rate} = \text{tracks per second} * \text{track capacity}$$

$$100 \text{ MB/s} = (200 \text{ track/s}) * \text{SPT} * (2048 \text{ B/sector})$$

$$\text{Number of sectors per track} = \text{SPT} = (100 * 2^{20} \text{ B/s}) / ((200 \text{ track/s}) * (2048 \text{ B/sector})) = 256$$

- (c) What is the number of heads per cylinder?

$$\text{Disk capacity} = \text{number of surfaces} * \text{tracks per surface} * \text{sectors per track} * \text{bytes per sector}$$

$$256 \text{ GB} = \text{HPC} * (65536 \text{ tr./surf.}) * (256 \text{ sect./tr.}) * (2048 \text{ B/sect.})$$

$$\text{Number of heads per cylinder} = \text{HPC} = (256 * 2^{30} \text{ B}) / (65536 * 256 * 2048 \text{ B/surf.}) = 8$$

- (d) Estimate the average percentage of the total time occupied by seek operations and rotational delays.

$$\text{Average transfer time} = \text{average file size} / (\text{track capacity} * \text{spindle speed})$$

$$= (0.1 * 2^{20} \text{ B}) / ((256 \text{ sect./tr.}) * (2048 \text{ B/sect.}) * (200 \text{ tr./s})) = 1 \text{ ms}$$

$$\text{Average \% of sk. \& rot. times} = (\text{sk. time} + \text{rot. time}) / (\text{sk. time} + \text{rot. time} + \text{tr. time}) * 100\%$$

$$= (6.5 \text{ ms} + 2.5 \text{ ms}) / (6.5 \text{ ms} + 2.5 \text{ ms} + 1 \text{ ms}) * 100\% = 90\%$$

2. A CD-ROM drive operates at a constant linear velocity of 1.2 m/s and a constant data rate of 150 KB/s.  
(a) What is the linear data density of the CD-ROM disk (in B/mm)?

$$\text{Linear data density} = \text{data transfer rate} / \text{linear velocity}$$

$$= (150 * 2^{10} \text{ B/s}) / (1.2 * 10^3 \text{ mm/s}) = 128 \text{ B/mm}$$

- (b) What is the storage capacity of the CD-ROM disk (in MB)?

$$\text{CD-ROM disk capacity} = \text{linear data density} * \text{track length}$$

$$= (128 * 2^{-20} / 10^{-6} \text{ MB/Km}) * (5.38 \text{ Km}) = 556.74 \text{ MB}$$

3. A RAID array is to be built using 12 disk drives. The storage capacity of each drive is 2 TB.

- (a) Block-level stripping with distributed parity.

$$\text{RAID level: } 5$$

$$\text{Number of data drives} = 12 - 1 = 11$$

$$\text{Total data capacity} = 11 * (2 \text{ TB}) = 22 \text{ TB}$$

- (b) Bit-level stripping with Hamming error correction codes (ECC).

$$\text{RAID level: } 2$$

Number of ECC drives =  $k$  (where  $12+k \leq 2^k \rightarrow k=4$ )

Number of data drives =  $12 - k = 8$

Total data capacity =  $8 * (2 \text{ TB}) = 16 \text{ TB}$

(c) Mirroring without stripping or parity.

RAID level: 1

Number of data drives =  $12 / 2 = 6$

Total data capacity =  $6 * (2 \text{ TB}) = 12 \text{ TB}$

4. A computer collects characters from  $n$  input devices while executing a program called PROG.

(a) Express the maximum value of  $n$  as a function of  $t$ .

$n$  is maximum when all the time is spent in polling!

CPU keeps executing POLL over and over 100% of the time!

$$t = 0.2 + 0.1 * n_{max}$$

$$n_{max} = 10 * t - 2$$

(b) Express the maximum value of  $r$  as a function of  $t$ .

$r$  is maximum when each device produces one character every polling round!

$$r_{max} = (1 \text{ char}) / (t \text{ ms}) = 1000 / t \text{ char/s}$$

(c) Express the percentage of time spent in servicing the devices as a function of  $n$  and  $t$ .

$$\begin{aligned} \%T_{serv} &= (\text{time to poll } n \text{ devices}) / (\text{time between pooling rounds}) * 100\% \\ &= (0.2 + 0.1 * n) / t * 100\% = (20 + 10 * n) / t \% \end{aligned}$$

(d) Which conditions need to be satisfied in order to prevent any loss of characters ...?

$$n = 8 \text{ and } \%T_{serv} \leq 10\%$$

$$(20 + 10 * 8) / t \leq 10$$

$$t \geq 10 \text{ ms}$$

$$r_{max} = 1000 / t \text{ char/s}$$

$$\text{Conditions: } t \geq 10 \text{ ms and } r \leq 1000 / t \text{ char/s}$$

5. Consider a system in which each bus cycle takes 200 ns. Transfer of bus control in either direction, from processor to I/O device or vice-versa, takes 75 ns. One of the I/O devices has a data transfer rate of 250 KB/s and employs DMA. Data are transferred one byte at a time.

(a) Suppose the DMA is employed in a burst mode. That is, the DMA controller gains bus mastership prior to the start of a block transfer and maintains control of the bus until the whole block is transferred. For how long would the DMA controller gain mastership of the bus in order to transfer a block of 1 KB?

$$\begin{aligned} \text{DMA time} &= \text{time to gain bus} + \text{time to transfer block} + \text{time to release bus} \\ &= 75 \text{ ns} + (1 \text{ KB}) / (250 \text{ KB/s}) + 75 \text{ ns} = 4000.15 \mu\text{s} \end{aligned}$$

(b) Repeat the calculation (from part (a)) for cycle-stealing mode.

$$\begin{aligned} \text{DMA time} &= (\text{time to gain bus} + \text{time to transfer byte} + \text{time to release bus}) * \text{block size} \\ &= (75 \text{ ns} + 200 \text{ ns} + 75 \text{ ns}) * 1024 = 358.4 \mu\text{s} \end{aligned}$$