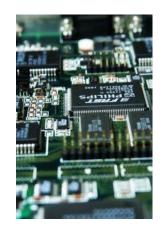
### **CSE 321b**

# Computer Organization (2)

تنظيم الحاسب (2)



3<sup>rd</sup> year, Computer Engineering
Winter 2016
Lecture #11



Dr. Hazem Ibrahim Shehata Dept. of Computer & Systems Engineering

Credits to Dr. Ahmed Abdul-Monem Ahmed for the slides

#### **Adminstrivia**

- Midterm:
  - —New date: Thursday, May 5, 2016
  - —New time: 12:30pm 2:00pm
  - —Location: classroom #27309
  - —Coverage: lectures #1 → #7
- Assignment #3 (optional):
  - —Assignments mark = max(A1+A2, A2+A3, A1+A3)
  - —To be released early next week
- Final:
  - **—**???

Website: <a href="http://hshehata.github.io/courses/zu/cse321b/">http://hshehata.github.io/courses/zu/cse321b/</a> Office hours: Sunday 11:30am – 12:30pm

## Chapter 9. Computer Arithmetic (Cont.)

#### **Outline**

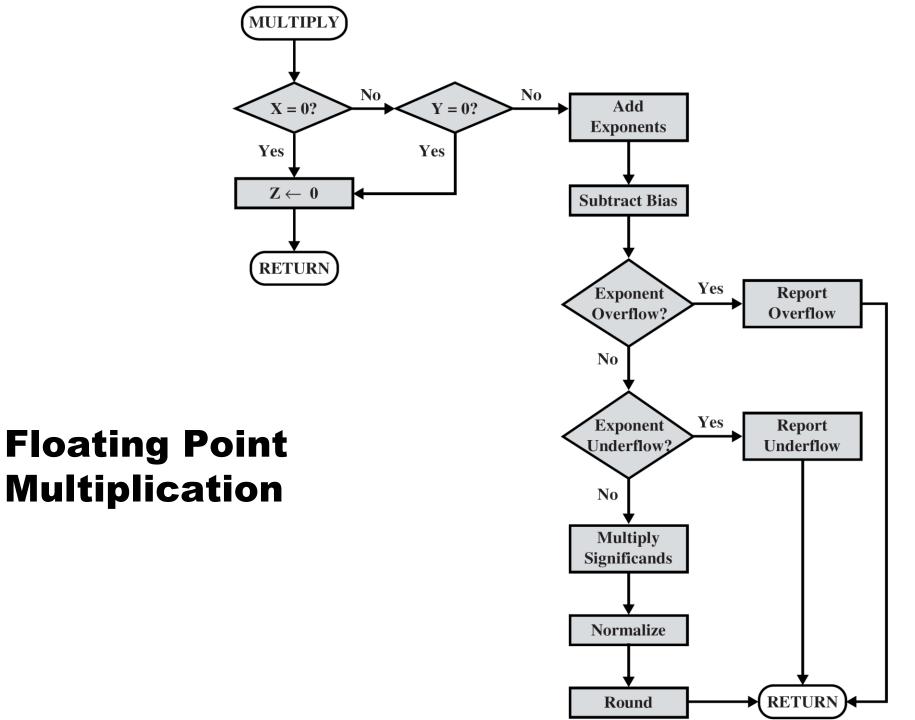
- Integer Representation
  - -Sign-Magnitude, Two's Complement, Biased
- Integer Arithmetic
  - —Negation, Addition, Subtraction
  - -Multiplication, Division
- Floating-Point Representation
  - —IEEE 754
- Floating-Point Arithmetic
  - —Addition, Subtraction
  - —Multiplication, Division
  - —Rounding

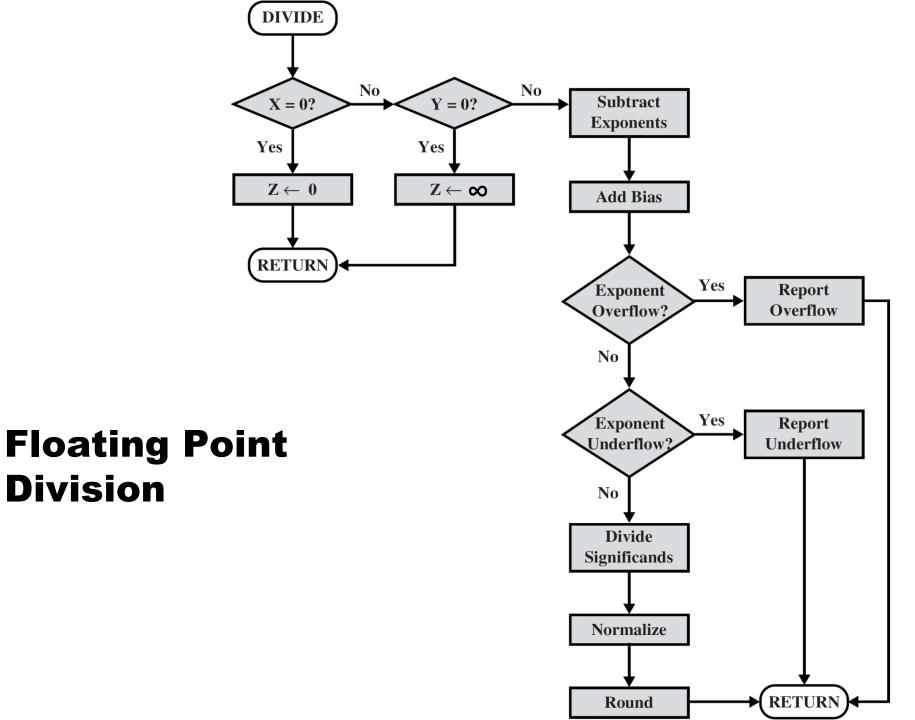
#### **FP Arithmetic +/-**

- Algorithm:
  - 1. Check for zeros (and other special cases, e.g., NaN).
  - 2. Align significands (adjusting exponents).
  - 3. Add or subtract significands.
  - 4. Normalize result.
  - Round result.

#### **FP Arithmetic** x/÷

- Algorithm:
  - 1. Check for zeros (and other special cases, e.g., NaN).
  - 2. Add/subtract exponents.
  - Multiply/divide significands (watch sign).
  - 4. Normalize result.
  - 5. Round result.
- All intermediate results should be in double length storage.





**Division** 

#### **Guard Bits**

- Extra bits added to the right of the mantissa during intermediate calculations.
- Maintains good precision.

$$1.000...00 \times 2^{1}$$
  
 $-1.111...11 \times 2^{0}$ 

$$1.000...00000 \times 2^{1}$$
 $-1.111...110000 \times 2^{0}$ 

$$1.000...000...2^{1}$$
  
 $-0.111...1110000 \times 2^{1}$ 

$$0.000...001...00 \times 2^{1}$$

$$= 2^{-24} \times 2^1 = 2^{-23}$$

## Rounding

- The result of any operation on significands is stored in a longer register.
- When the result is to be stored as an FP number, extra bits have to be dropped off → rounding.
- Round to nearest representable number.
- Round toward  $+\infty$ : **round up** to the next number.
  - $\triangleright$  Ex.: +1.1...001 001  $\rightarrow$  +1.1...010
  - $\rightarrow$  Ex.:  $-1.1...001 001 \rightarrow -1.1...001$
- Round toward -∞: round down to the next number.
  - $\rightarrow$  Ex.: +1.1...001 001  $\rightarrow$  +1.1...001
  - $\rightarrow$  Ex.:  $-1.1...001 001 \rightarrow -1.1...010$
- Round toward zero: truncate the extra bits.
  - $\triangleright$  Ex.: +1.1...001 001  $\rightarrow$  +1.1...001
  - $\rightarrow$  Ex.:  $-1.1...001 001 \rightarrow -1.1...001$

#### **Round to Nearest**

- Default technique listed in the IEEE standard.
- Deliver the representable value nearest to the infinitely precise result. If the two nearest representable values are equally near, the one with LSB 0 will be delivered.
- Examples:
  - If the guard bits are 10010 → they amount to more than one half of the last representable bit position → Round away from zero.
  - If the guard bits are 01111 → they amount to less than one half of the last representable bit position → Truncate.
  - If the guard bits are 10000 → midway
    - If we always truncate → biased toward zero.
    - If we choose randomly → not predictable/deterministic results.
    - IEEE standard:
      - + Force the result to be even.
      - + If last bit is 1, round away from zero, else, truncate.

#### Round to ±∞

- Useful in implementing interval arithmetic.
- Interval arithmetic: produce two values for every result. These two values correspond to the lower and upper endpoints of an interval that contains the true result.
- Used in monitoring and controlling errors.

# **Reading Material**

- Stallings, Chapter 10:
  - —Pages 352-356