

ntusat and ntusatbreak

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Abstract—This document is brief description of solver ntusat and ntusatbreak entering the SAT Competition 2014.

I. INTRODUCTION

ntusat is based on Simpsat in SAT Competition 2012 which is an enhanced version of CRYPTOMINISAT 2.9.2 [1] with new technique for gaussian elimination described in [2]. ntusatbreak is ntusat with preprocessing technique described in [3] and [4] of SAT Competition 2013. The additional technique compared to Simpat in 2012 is pure literal detection and learning [5]. Adding pure literal implication clauses from time to time could make the theory not functional equivalent but reduce the search space to help the solver solve faster. The other technique is to find more XOR-clauses by improving XOR-recovery. If no XOR-clauses found, do the clause resolution procedure to find more information. The detail technique would be described in algorithm and datastructure part.

II. MAIN TECHNIQUES

ntusat and ntusatbreak are CDCL solver with simplification techniques subsumption, block literal, and inprocessing technique literal probing, hyper-binary resolution applied by CRYPTOMINISAT 2.9.2. Since there are XORclauses extraction and equivalent variable replacement, part of the pure literal detection technique is different from MINIPURE [5] last year. If any variable of literal β is in the XORclause, β would not be detected as pure literal. If literal α is replaced by literal β , then all the clause ID in vector litcontain [5] of α should be moved to litcontain(β). For other inprocessing techniques which causes variable elimination, clause subsumption and clause elimination, the clause watch and litcontain datastructure should also be checked.

III. MAIN PARAMETERS

Most of parameters are the same as SIMPSAT in SAT Competition 2012. Since improved XOR-recovery from time to time is time consuming, NTUSAT do not apply that technique after 700 seconds. The pure literal detection and learning is applied every eight restarts. Empirically, for some cases, adding too much pure literal implication clauses would make it harder to find solution for SAT cases. If the difference between max and min decision level of variables in pure literal implication clauses is less than 25, the clauses is added to the database as irredundant clauses. Otherwise, the solver drop the clause.

Add-XORs(add new learnt xor for each restart)

input: Solver data: watch, original clauses ϕ

output: NEWXOR and LEARNTCLAUSE

begin

```

01 for each original and learnt clause  $C$  size $\geq 5$  and  $C$  not found
02   match-clauses :=  $\phi$ ;
03   for each literal  $L$  in  $C$ 
04     candidate-clauses := watch( $\neg L$ )+watch( $L$ )
05                       +cache( $\neg L$ )+cache( $L$ );
06   match-clauses := match-clauses+
07   check-all-literal(candidate-clauses);
08 end
09 if foundallxor( $C$ , match-clauses);
10   newxor.push( $C$ );
11 else
12   learntclause:=Getmoreinfo( $C$ ,match-clauses);
13 end
end

```

Fig. 1. Algorithm: ADDXOR

IV. SPECIAL ALGORITHMS, DATA STRUCTURES, AND OTHER FEATURES

During the simplification procedure, NTUSAT would detect XORclauses by Figure 1. If there is no XOR-clauses found, the solver would apply the resolution method to find more information. For example, the clause set $\Omega = \{ (x_1 \vee x_2 \vee x_3), (x_1 \vee \neg x_2 \vee x_3), (x_1 \vee x_2 \vee \neg x_3), (x_1 \vee \neg x_2 \vee \neg x_3) \}$ these clauses can not form a XOR clause, but these clauses imply $x_1=1$ directly. The other clause set $\Gamma = \{ (x_1 \vee x_2 \vee \neg x_3), (x_1 \vee \neg x_2 \vee x_3), (\neg x_1 \vee \neg x_2 \vee \neg x_3), (\neg x_1 \vee \neg x_2 \vee x_3) \}$ can neither form a XOR clause, but $x_2 = x_3$ can be implied from the set. The detail of the algorithm is in Figure 2. The solver generates clauses by resolution which would reduce the clause size by 1. In line 2, the solver implements this process until size is equal to three and in this loop the generating clauses would be binary clauses. In line 15, the vector candidate-learnt will store the binary clauses of the same variables, e.g. $\{ (\neg a \vee b), (\neg a \vee \neg b) \}$ would be push into candidate-learnt (a,b)={ 1,0 } . $(\neg a, b)$ the sign of the variables in binary bits form is equal to 1 and $(\neg a, \neg b)$ is equal to 0. In line 22, k.size() means how many binary clauses with the same variables. k.size() equal to 4 means conflict, k.size() equal to 3 means the two variables are assigned. k.size() equal to 2 means the two variable are equivalent or one variable is assigned. The solver could get more information even there is no XOR-clauses found.

Getmoreinfo**input:** C, match-clauses**output:** learntclauses**begin**

```
01 even:=  $\phi$ , odd :=  $\phi$ , candidate1learnt :=  $\phi$ ;  
02 for sz= match-clauses.size down to 3  
03   for each clause  $i$  in match-clauses and C  
04     match-clauses.popup( ) ;  
05     if xor all the literal in  $i$  is true  
06       even.pushback(i);  
07     else  
08       odd.pushback(i);  
09     end  
10   for each  $i$  in even  
11     for each  $j$  in odd  
12       if sign of literals in  $i, j$  has only one difference  
13         learnt:= resolve(i,j);  
14         if sz equal 3  
15           candidate-learnt[learnt].pushback(signs of learnt);  
16         else  
17           match-clauses.pushback(learnt);  
18         end  
19     end  
20   end  
21 for each  $k$  in candidate-learnt and  $k.size() > 0$   
22   learntclause.pushback(learn clauses according to k.size())  
23 end  
end
```

Fig. 2. Algorithm: GETMOREINFO

V. IMPLEMENTATION DETAILS

ntusat and ntusatabreak are implemented in C++. Both of them are based on SIMPSAT and CRYPTOMINISAT2.9.2. ntusatabreak applies saucy and breakID as preprocessor before solving.

VI. SAT COMPETITION 2013 SPECIFICS

Both of the solvers are submitted to hard combinatorial SAT and UNSAT, Application SAT and UNSAT, Random SAT and UNSAT. The compiler version is 4.7.1., O3 used for compiling and 64-bit binary. There is no command-line option. All the parameters are locked in the solver. More information about parameters is in Main Parameters part.

VII. AVAILABILITY

Solver NTUSAT is available upon request for research purpose. Send email to the authors. For preprocessor of BreakID [3] and Saucy <http://vlsicad.eecs.umich.edu/BK/SAUCY/>

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REFERENCE

- [1] K. N. M. Soos and C. Castelluccia, "Extending sat solvers to cryptographic problems." *Proc. Int'l Conf. on Theory and Applications of Satisfiability Testing*, pp. 244–257, 2009.
- [2] C.-S. Han and J.-H. R. Jiang, "When boolean satisfiability meets gaussian elimination in a simplex way." *Proc. Int'l Conf. on Computer Aided Verification*, pp. 410–426, 2012.
- [3] J. Devriendt and B. Bogaerts, "Shatterglucose and breakidglucose," *Proc. of SAT-13*, pp. 12–13, 2013.
- [4] K. A. S. H. Katebi and I. L. Markov, "Graph symmetry detection and canonical labeling: Differences and synergies," *Proc. Turing-100*, 2012.
- [5] H.-S. Wang, "minipure," *Proc. of SAT-13*, pp. 57–58, 2013.