1 Gradient Descent

Gradient descent, or back propagation, is a first order iterative optimization algorithm used to minimize the cost function when training artificial neural networks.

Cost Function,
$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^{m} [h_\theta(x_i) - y_i]^2$$

Gradient Descent,
$$\theta_j = \theta_j - \alpha \frac{\partial}{\partial \theta_j} J(\theta_0, \theta_1)$$

It follows,
$$\frac{\partial}{\partial \theta} J_\theta = \frac{\partial}{\partial \theta} \frac{1}{2m} \sum_{i=1}^{m} [h_\theta(x_i) - y_i]^2$$

$$= \frac{1}{m} \sum_{i=1}^{m} (h_\theta(x_i) - y_i) \frac{\partial}{\partial \theta} (\theta x_i - y)$$

$$= \frac{1}{2m} (h_\theta(x_i) - y_i) x_i$$

Therefore,
$$\theta_j := \theta_j - \frac{\alpha}{m} \sum_{i=1}^{m} [(h_\theta(x_i) - y) x_i]$$