

1 Gradient Descent

Gradient descent, or back propagation, is a first order iterative optimization algorithm used to minimize the cost function when training artificial neural networks.

Cost Function,

$$J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m [h_{\theta}(x_i) - y_i]^2$$

Gradient Descent,

$$\theta_j = \theta_j - \alpha \frac{\partial}{\partial \theta_j} J(\theta_0, \theta_1)$$

It follows,

$$\begin{aligned} \frac{\partial}{\partial \theta} J_{\theta} &= \frac{\partial}{\partial \theta} \frac{1}{2m} \sum_{i=1}^m [h_{\theta}(x_i) - y_i]^2 \\ &= \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x_i) - y_i) \frac{\partial}{\partial \theta} (\theta x_i - y) \\ &= \frac{1}{m} \sum_{i=1}^m [(h_{\theta}(x_i) - y) x_i] \end{aligned}$$

Therefore,

$$\theta_j := \theta_j - \frac{\alpha}{m} \sum_{i=1}^m [(h_{\theta}(x_i) - y_i) x_i]$$