## **BEBI5009 Homework4**

## Due 12/01/2016: before class(9:10am)

1. Consider the reaction network

$$A \xrightarrow{k_1} B + C \qquad B + C \xrightarrow{k_{-1}} A$$

- (a) Suppose that the system starts with two molecules of A, one molecule of B, and no molecules of C, that is  $(N_A, N_B, N_C) = (2, 1, 0)$ . Determine the set of possible states the system can adopt and write the chemical master equation that describes the corresponding probability distribution.
- (b) Take  $k_1 = 1$  (time<sup>-1</sup>) and  $k_{-1} = 1$  (time<sup>-1</sup>), and solve for the steady-state probability distribution.
- (c) Simulate sample paths of  $N_A$ ,  $N_B$ , and  $N_C$  using stochastic simulation algorithm (SSA).

Set the initial condition of  $N_A$ ,  $N_B$ , and  $N_C = (2,1,0)$  or (10, 5, 0) or (100, 50, 0)

R1: A  $\rightarrow$  B+C propensity:  $k_1N_A$ 

R2: B+C  $\rightarrow$  A propensity  $k_{-1}N_BN_C$ 

Note1: To calculate the waiting time, you will need to generate values of a random variable distributed according to an exponential distribution.

You could simply generate a random variable U drawn from the uniform distribution on the unit interval (0, 1), and T=-ln(U)/ $\lambda$ will be an exponential random variable, where  $\lambda$  is the rate parameter of the exponential distribution. In this example,  $\lambda$  would be the sum of the reaction propensities.

Another way to generate exponential random number is to use Matlab function **exprnd(\mu)**, where  $\mu$  is the mean of the exponential distribution  $\mu$ =1/ $\lambda$ .

Note2: You might need to change the value of  $k_1$  and  $k_{-1}$  for different initial conditions due to the volume changes. Use  $(k_1, k_{-1}) = (1,1)$ , (1, 1/5) and (1, 1/50) (time<sup>-1</sup>) for I.C.= (2,1,0), (10,5,0), and (100,50,0).

- (d) Set the initial condition of  $N_A$ ,  $N_B$ , and  $N_C$ =(2, 1, 0). Analyzed the statistics of your ensemble, and compare to the steady state probability distribution in (b).
- (e) Write down a deterministic model for the chemical reaction following the mass action law. Simulate the concentration changes of A, B C with the parameter  $k_1 = 1$  (s<sup>-1</sup>) and  $k_{-1} = 1$  (mM<sup>-1</sup> s<sup>-1</sup>). Set initial concentrations [A],[B],[C] as 2,1, and 0mM. Compare simulation results in (c).