

Concepts

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Constraint Based Production Scheduling



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Key Points



- We introduce the core concepts used in scheduling
- Different layers of description
 - What we are doing (jobs, tasks, resources)
 - Why we are scheduling (orders, products, processes)
- Temporal Relations
- Process description
- Problem classification
- Visualization

Most basic description of scheduling problem



- *Job*
 - Collection of activities required to manufacture one object/lot/order
 - Overall start/end determined by starts and ends of its tasks
- *Task*
 - Individual activities required for manufacture
 - Have defined start, end (typical: variables) and duration (sometimes fixed)
 - Often performed on one specific resource (more on that later)
- *Resources*
 - Resources are needed to perform the tasks
- Very compact representation of scheduling problem
- But, where does that information come from?

Scheduling orders



- An *order* specifies a need for a certain *product* at a given time in a specific quantity
- There may be multiple ways of making the *product* (multiple *processes*)
- We assume that the process to use is decided when placing the order
- Each order corresponds to a job, with its constituent tasks
- There may be limited visibility of future orders

Process Description



- Each *process* consists of one or more *process steps*
- A process step contains a duration formula to describe how long it lasts
- The order of *process steps* is defined by *process sequences*
- The resources needed are defined by *resource needs* (described later on)
- Tasks are created for each process step, their duration is based on the duration formula and order quantity

Where do the orders come from?



- Made to order
 - Each order is caused by a customer request
 - Defines due date, release date often implied
- Made to stock
 - Orders are satisfied from stock
 - Inventory control strategy decides when to make product
 - Often called stock orders
 - More complex variant integrates production planning and detailed scheduling
 - Example later in course

Temporal Relations



- Temporal constraints between tasks and/or jobs
- Defined by the manufacturing process
- In simple cases
 - A single sequence of process steps performed in that order
 - Each task must finish before the next one can start



Annotations on Features

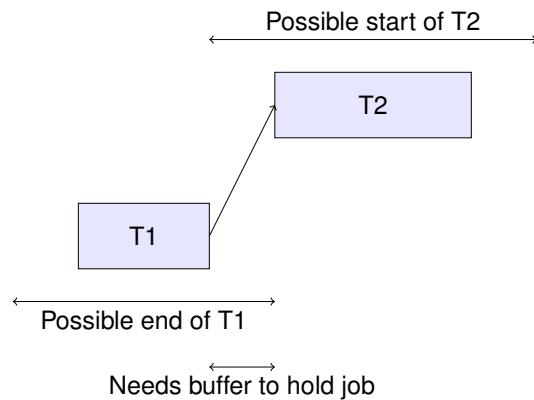


- ✓Currently available in scheduling tool
- (✓)Will be available shortly
- ✗Currently not available, may be added in future version

The Most Common Relation: EndBeforeStart ✓



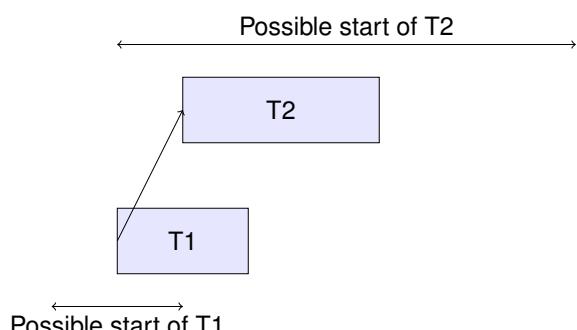
- States that one task (T1) must end before the next one (T2) can start
- Typical for manufacturing process based on the same item
- Addition: offset
 - Wait at least offset units between end and start
 - For example cooling, drying time outside a machine



Less Common: StartBeforeStart ✓



- States that one task (T2) can start any time after the start of another task (T1)
- Uncommon in manufacturing, occurs in project management
- Example later on on assembly line balancing

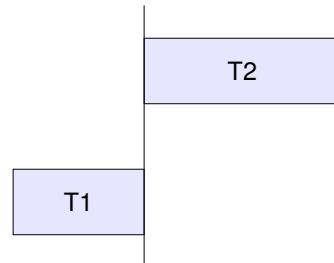


NoWait ✓



- Sometimes, two steps must follow each other immediately
- The item made would spoil
 - Product specific
- There is no space to hold item
 - Machine specific, buffers
- End of one task (T1) must be equal to start of next task (T2)
- May mean delay of start of task T1

Start of T2 is equal to End of T1

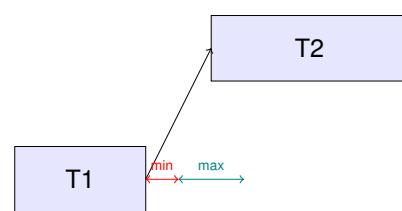


MaxWait (✓)



- Limit how long we can wait between tasks
 - Cooling enough, but not too much
 - Baking: rise time
- Impose both lower and upper waiting time limit
- Makes it more difficult to find solutions

Possible start of T2



Possible end of T1

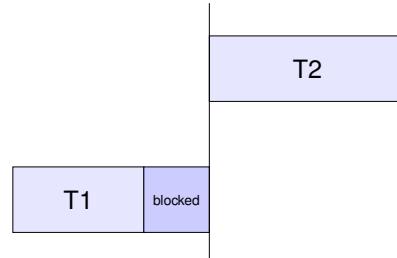
Needs buffer to hold job

Blocking ✓



- Sometimes, two steps must follow each other immediately
- There is no space to store item between machines
- Keep item on previous machine until needed
- That machine is now *blocked*
- Duration of task T1 is extended until start of T2
- *Use with caution! Easy to deadlock*

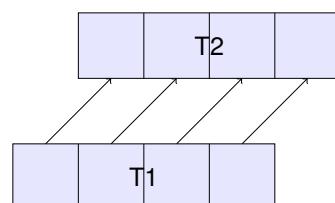
Start of T2 is equal to End of T1



Special Case: Pipelining ✗

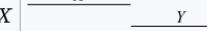


- Sometimes, we can start on the next task while the first is still running
- Possible if one job produces multiple items (lots,...)
- As soon as the first item is finished, take it to the next machine to process it there
- Overlaps T1 and T2 as much as possible
- Details can get complex



More General: Relations between Intervals

- First introduced by Allen (1983)
- 13 relations between intervals
- Allows composition of relations
- Constraint reasoning on sets of relations

Relation	Illustration	Interpretation
$X < Y$ $Y > X$		X precedes Y Y is preceded by X
$X \text{ m } Y$ $Y \text{ mi } X$		X meets Y Y is met by X (i stands for inverse)
$X \text{ o } Y$ $Y \text{ oi } X$		X overlaps with Y Y is overlapped by X
$X \text{ s } Y$ $Y \text{ si } X$		X starts Y Y is started by X
$X \text{ d } Y$ $Y \text{ di } X$		X during Y Y contains X
$X \text{ f } Y$ $Y \text{ fi } X$		X finishes Y Y is finished by X
$X = Y$		X is equal to Y

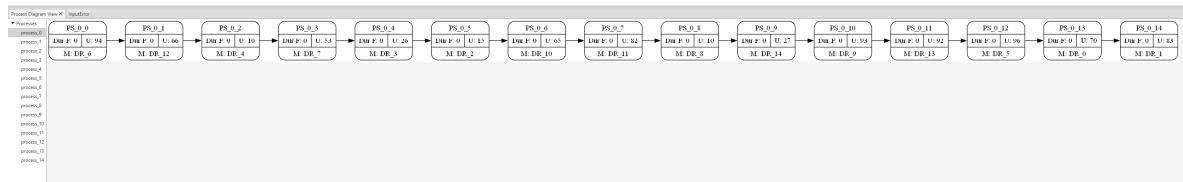
from Wikipedia: https://en.wikipedia.org/wiki/Allen%27s_interval_algebra

Start and End of Jobs



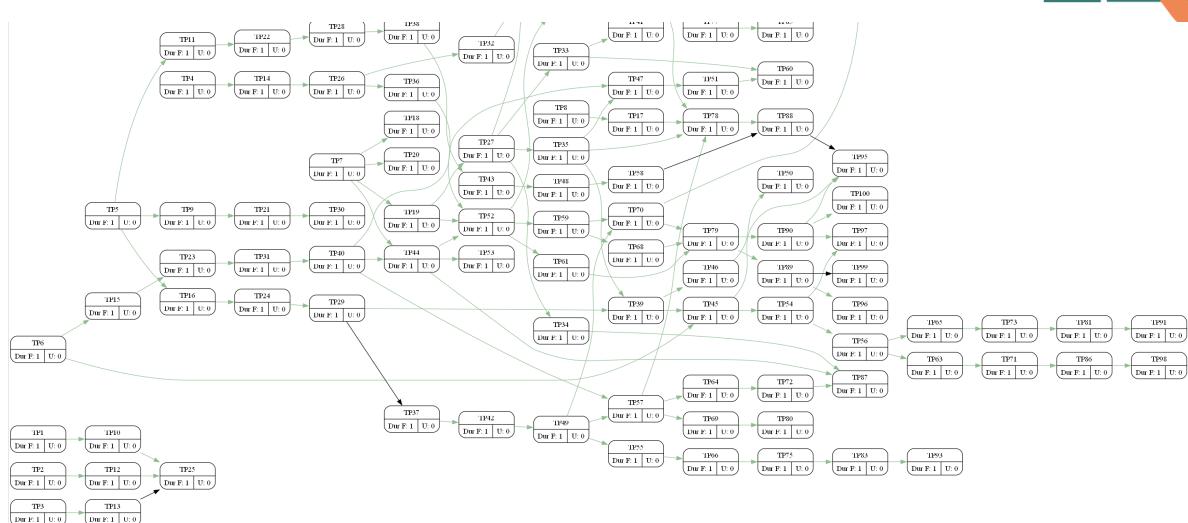
- The start of a job is equal to the start of the earliest task of the job
- The end of a job is equal to the latest end of any of its tasks
- Also called: the job *spans* its tasks
- Sometimes very simple
 - Start of job is start of first process step
 - End of job is end of last process step
 - But, do we know which steps will be first or last?

An Example of a Simple Process



- The steps form a precedence chain
- Easy to identify first and last step

An Example of a More Complex Process

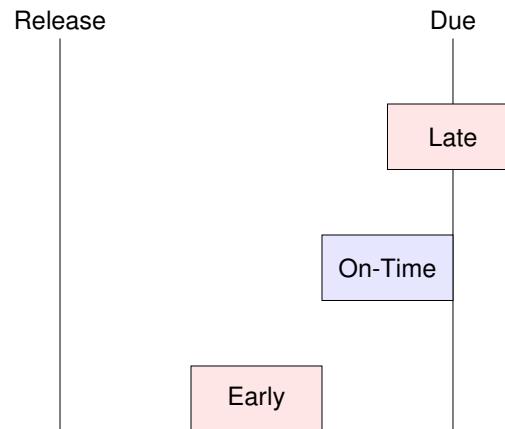


- There is no clear first or last process step

Jobs: Release and Due Dates ✓



- The execution of a job may be constrained in time
- *Release dates* states earliest time a job can start
- *Due dates* states latest time a job can end
- These may or may not be hard constraints!
- A job will be *late* if it ends after the due date
- A job will be *early* if it ends before the due date
- A job will be *on-time* if it ends at the due date



Relations between Jobs ✗



- There may be relations between jobs as well
- For example, jobs for the same product may be arranged by due date
- Do not allow to run job for a later due date before any job with an earlier due date
- Orders for the same customer, but different products, may be constrained
- Most common:
 - Jobs for intermediate products must finish in time for their use later on

More Complexity



- We have ignored a lot of potential complications
 - Alternative processes
 - Alternative process paths
 - Alternative resources
- Intermediate products
- Impact of raw material availability

Intermediate products



- Some production operations are assembly steps
- Combine multiple intermediate products together
- These intermediate products need to be made as well
- There are processes for those products

Raw materials X



- Sometimes, a process step needs certain raw materials
- These are not made within the scheduled part of the plant
- They come from stock, inventory control problem
- Do we schedule production and then order raw materials?
- Do we schedule based on the available raw materials?

Bill of Materials (BoM), Bill of Processes X



- Enterprise systems will describe which items are needed to make a product
- Tree like structure, indicates the intermediate product/raw material needed and its quantity
- *BoM explosion* derive all required input materials for a given set of orders
- We may want to know at which step of process we need which materials (Bill of processes)
- This is where you use SAP, big database, trivial calculation
- Becomes hard if processes not fixed

Problem Classification



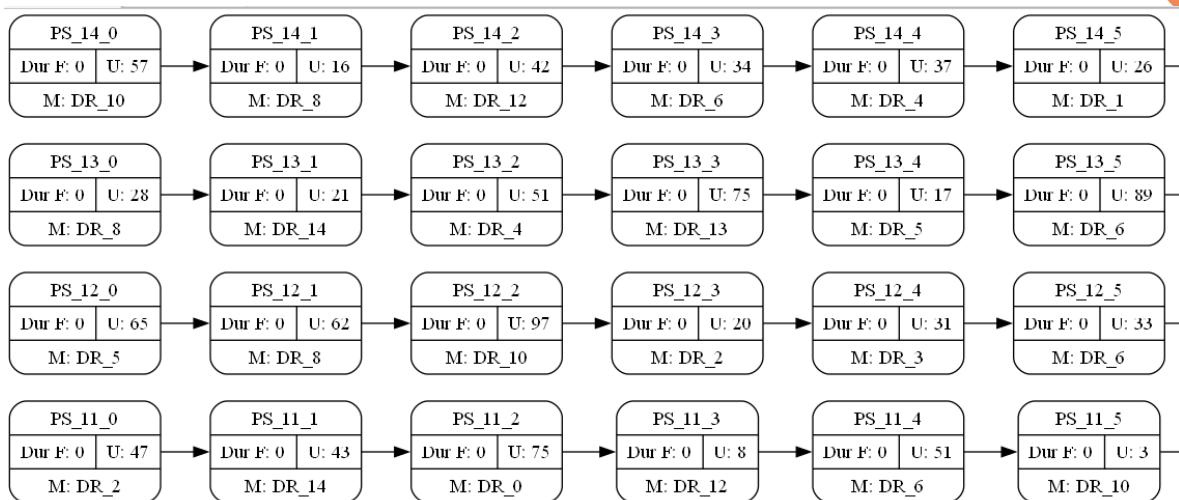
- Most real-world problems are messy, with many special conditions and exceptions
- Academic research prefers well-structured problems
- Scheduling research often focuses on well-structured problem types
 - Easier to understand
 - Possible to exploit structure
 - Easier to compare results
- A small number of problem types are very common in research

Job-Shop ✓



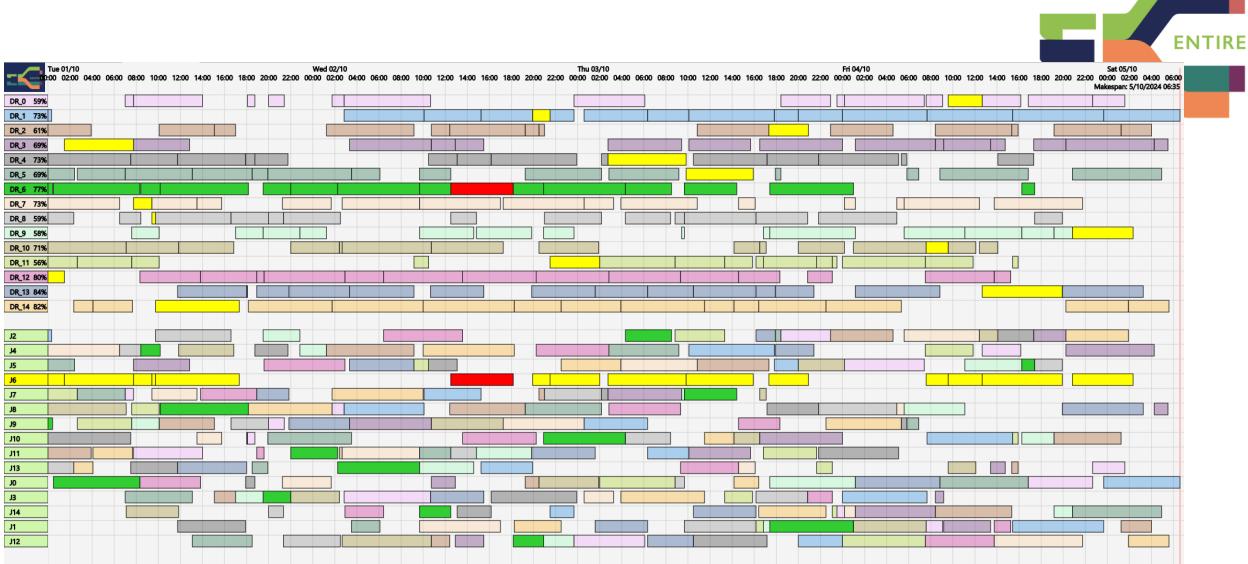
- Consists of a number of jobs and a number of machines
- Each job visits each machine, but possibly in a different order, depending on process
- Tasks of a job are linked as a precedence chain
- Objective is to minimize overall end, the *makespan*

Example Job-Shop Process



- Note that the order of machines visited is different for each process

Example Job-Shop Solution



- One task is selected (in red), in both Machine and Job Gantt Chart
- Tasks are colored by machine, note coloring in jobs is different for each job

Flow-Shop ✓

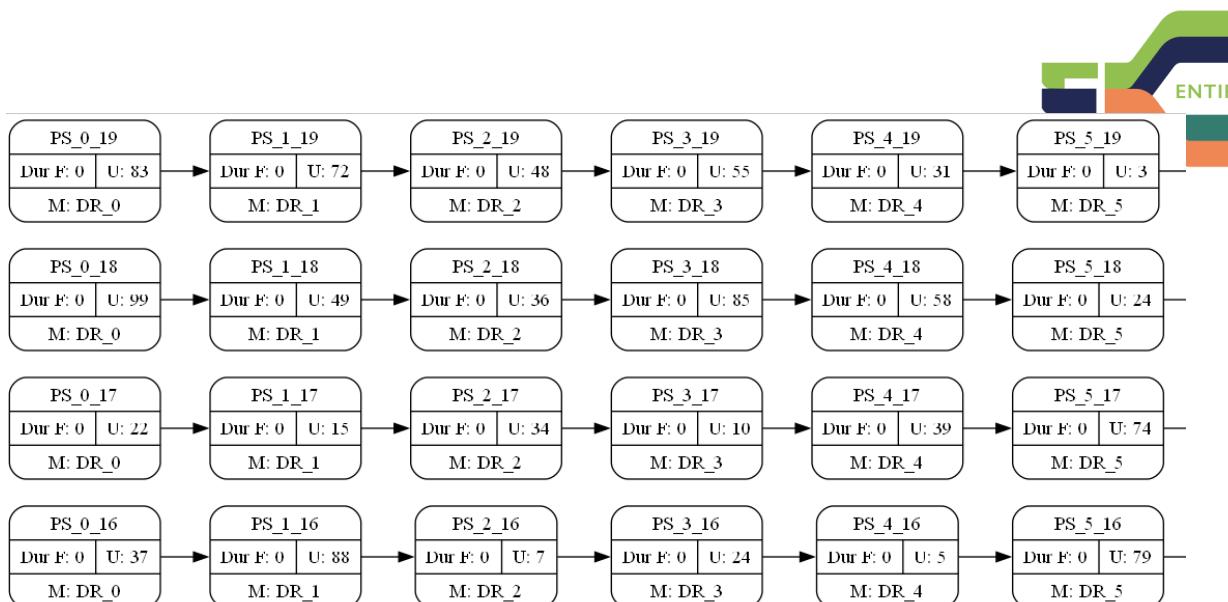


- Consists of a number of jobs and a number of machines
- Each job visits each machine, all jobs in the same order
- Tasks of a job are linked in a precedence chain
- Objective is to minimize overall end, the *makespan*

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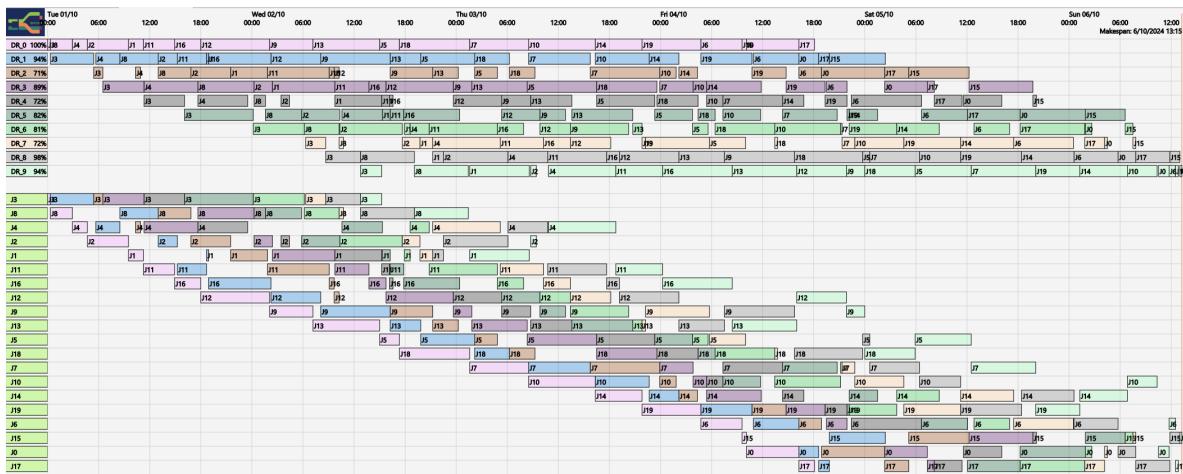
- Note that each process visits the machines in order DR_0, DR_1, ...

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Example Flow-Shop Solution



- Tasks are colored by machine, note the regular pattern in the Job Gantt Chart

Open-Shop ✓



- Consists of a number of jobs and a number of machines
- Each job visits each machine, we have to choose the sequence individually for each order
- There are no temporal constraints between tasks, but tasks of the same job cannot overlap
- Objective is to minimize overall end, the *makespan*

Open Shop Example Process



- Only showing details of one process
- No prescribed sequence between process steps
- Easier to find a task to run next
- Much larger search space

▼ Processes	PS_0_6
process_0	Dur F: 0 U: 56
process_1	M: DR_4
process_2	
process_3	
process_4	
process_5	
process_6	

▼ Processes	PS_0_5
process_0	Dur F: 0 U: 92
process_1	M: DR_5
process_2	
process_3	
process_4	
process_5	
process_6	

▼ Processes	PS_0_4
process_0	Dur F: 0 U: 71
process_1	M: DR_0
process_2	
process_3	
process_4	
process_5	
process_6	

▼ Processes	PS_0_3
process_0	Dur F: 0 U: 34
process_1	M: DR_6
process_2	
process_3	
process_4	
process_5	
process_6	

▼ Processes	PS_0_2
process_0	Dur F: 0 U: 54
process_1	M: DR_3
process_2	
process_3	
process_4	
process_5	
process_6	

▼ Processes	PS_0_1
process_0	Dur F: 0 U: 39
process_1	M: DR_1
process_2	
process_3	
process_4	
process_5	
process_6	

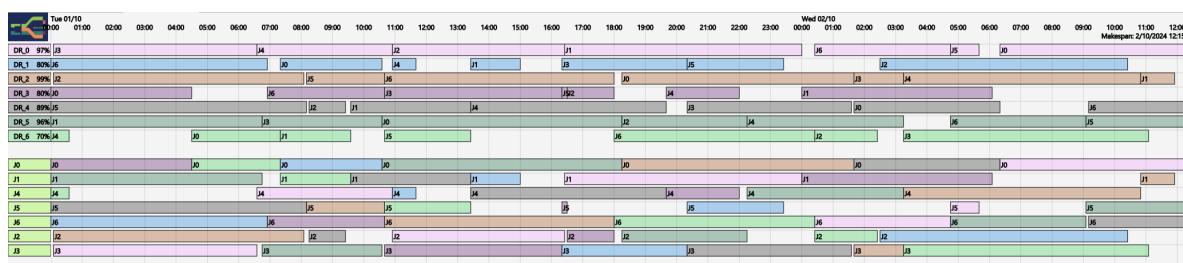
▼ Processes	PS_0_0
process_0	Dur F: 0 U: 89
process_1	M: DR_2
process_2	
process_3	
process_4	
process_5	
process_6	

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Open-Shop Example Solution



- Example solution for 7x7 open shop example
- Order of tasks within jobs not constrained
- Note that machines are still idle in optimal solution

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Resource Constrained Project Scheduling Problem (RCPSP) (✓)



- Problem class from project management
- One project (one job), many tasks
- Precedence graph is arbitrary DAG
- Cumulative as well as disjunctive resources
- Variants with process alternatives

$\alpha/\beta/\gamma$ Notation



- The previous classes are good for algorithm research, but not very practical
- General scheme to describe problem type introduced in 1979
- Based on three parameters
 - α resource structure, stages
 - β temporal relations
 - γ objective
- $P2/r_j, \bar{d}_j/C_{\max}$: One stage, two identical parallel machines, hard release and due dates, objective makespan
- More detailed description at
<https://encyclopedia.pub/entry/30497>

Visualization



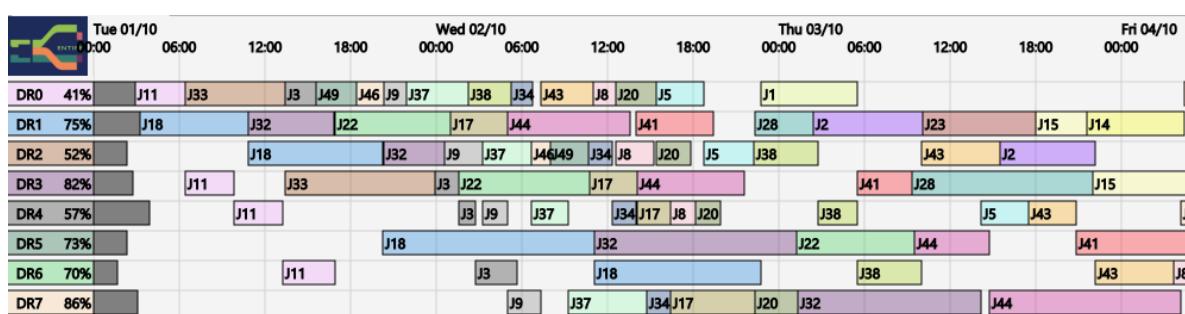
- Visualization is key to present and to understand results
- Many different ways to give an overview of schedule, and highlight problems
- Some diagrams types are used a lot, and are provided in our generic scheduling tool
- Customization is key

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Machine Gantt Chart ✓



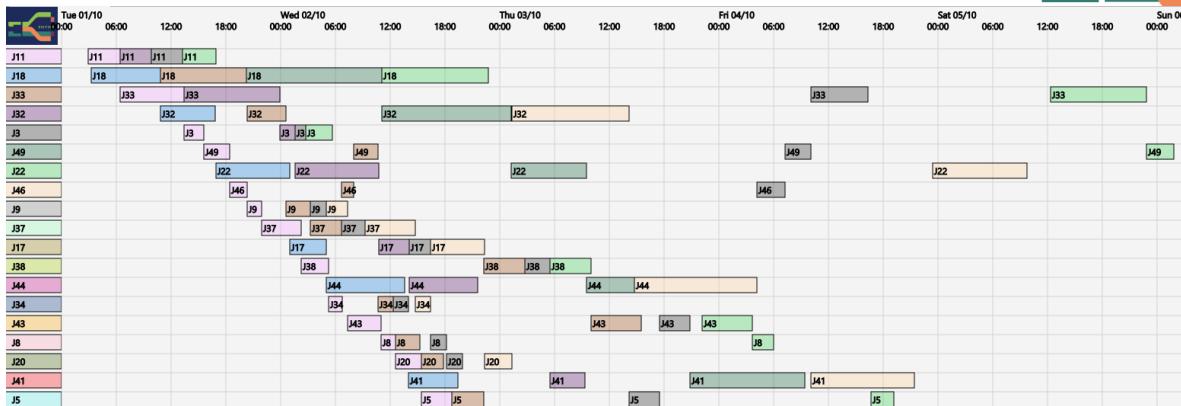
- Shows all tasks that are assigned to each machine
- Tasks should not overlap
- Also shows work in progress (WiP), down-times
- Optional display of setup and idle times

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Job Gantt Chart ✓



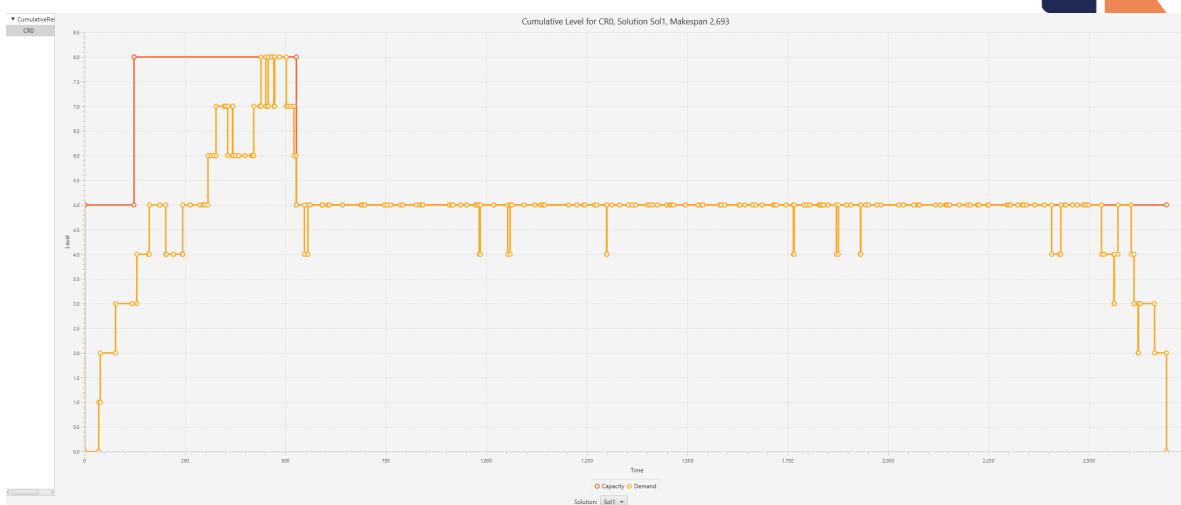
- Shows all tasks of a job in one line
- Only works for single chain of process steps
- Possible display of earliness, lateness
- Optional display of waiting and transport times

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Cumulative Resource Chart ✓



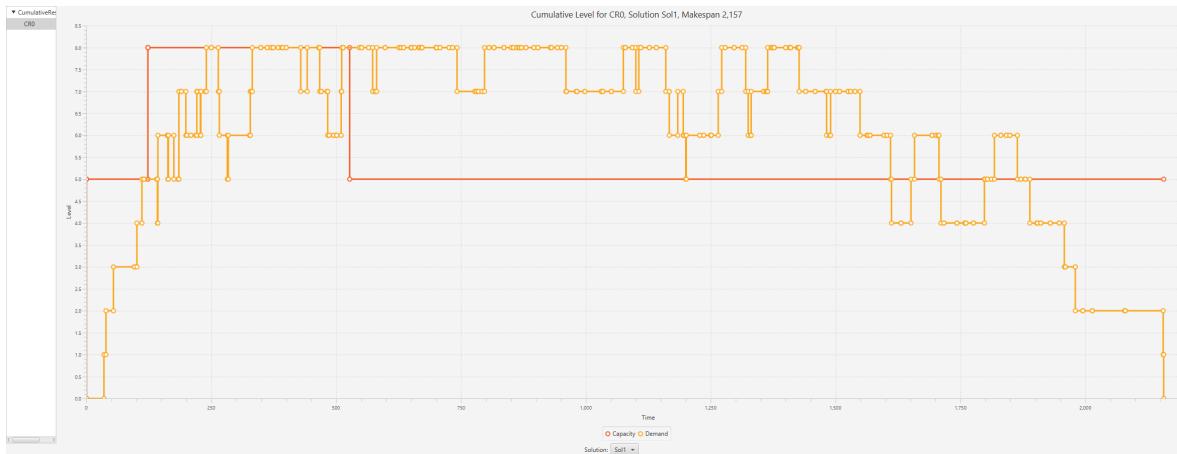
- Shows resource utilization of cumulative resource over time
- Utilization should be below capacity profile
- Unless we relax the cumulative resource constraint

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Cumulative Resource Constraint Relaxed

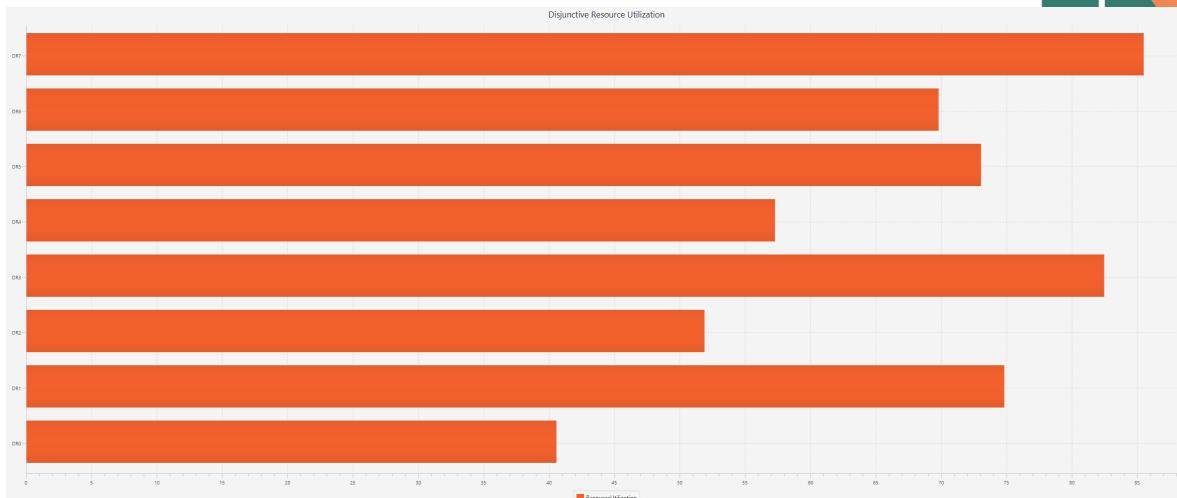


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Resource Utilization ✓



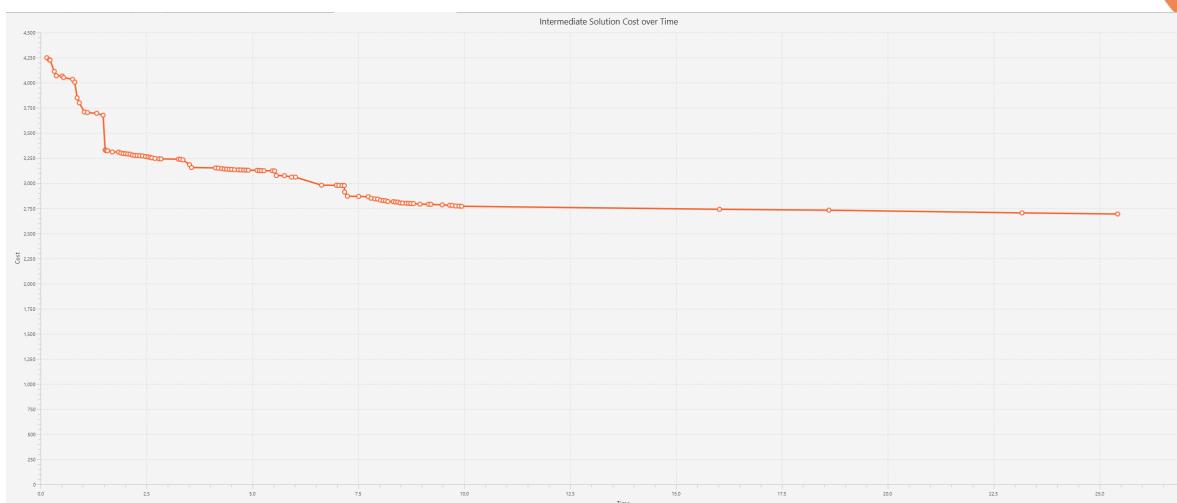
- Shows utilization of machines as percentage of active time
- Helpful to identify bottleneck machines
- Information also shown in Machine Gantt

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Intermediate Solutions ✓



- Shows intermediate solutions found over time
- Useful to see if enough/too much time is allocated

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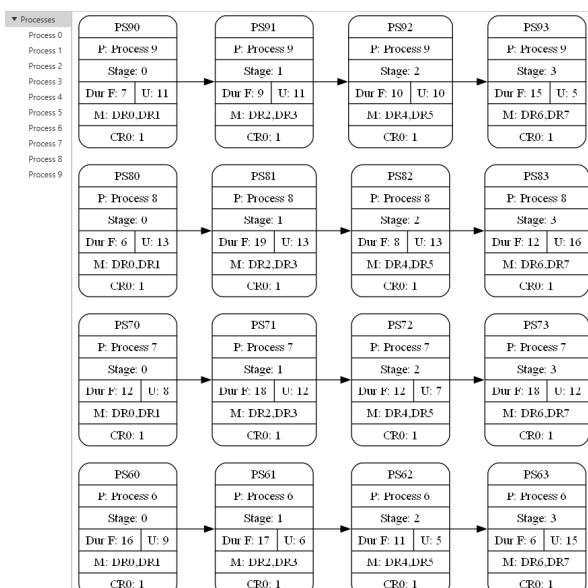
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Process Diagram ✓



- See all details of one process in one image
- Can also look at all processes in one diagram
- Options to show/hide different fields

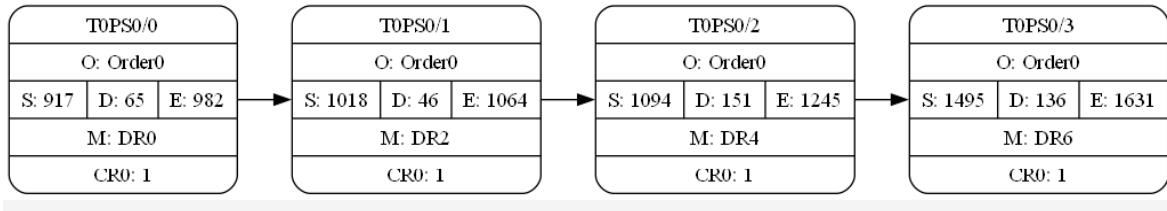


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PERT Chart(Program Evaluation Review Technique) ✓



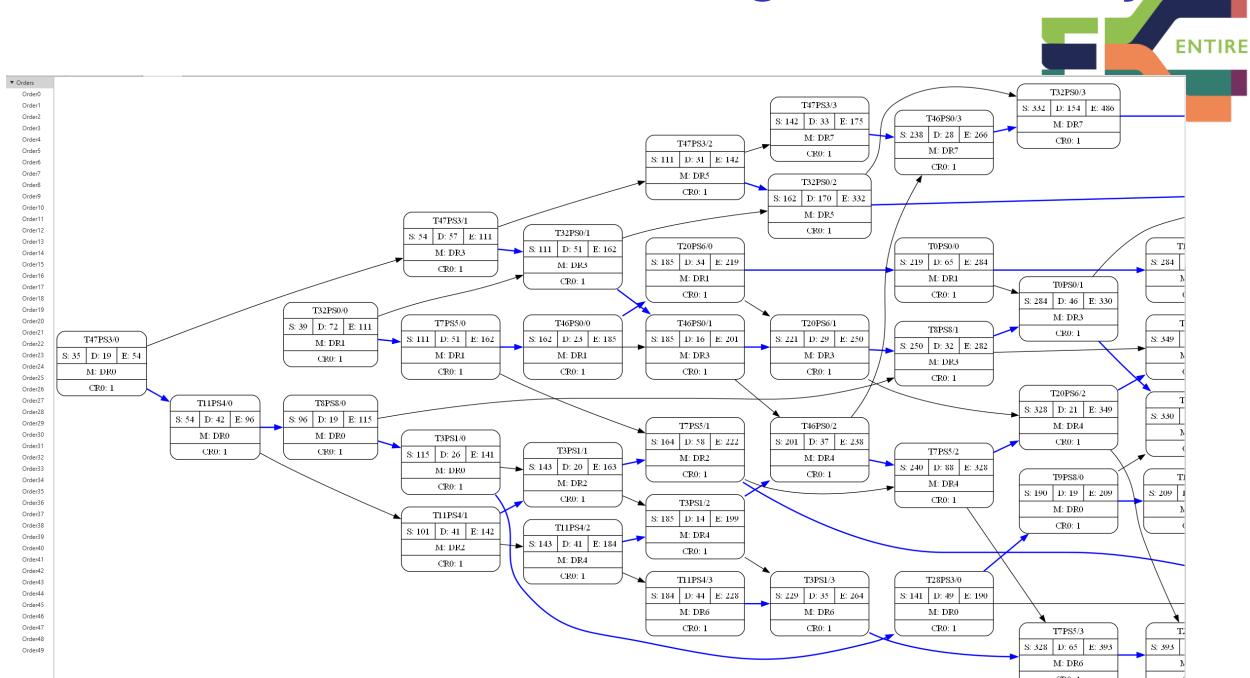
- Show details of job as a graph
- Useful if task graph is not a chain
- Often used in project management

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PERT Charts become Confusing Quite Quickly



- Especially if all resource dependencies are included (in blue)

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Calendars X



- Shows weekly structure for one or more years
 - Indicates public holidays, shut-downs, etc
 - Indicating working days, KPI for each day

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Summary



- We introduced the key concepts for scheduling problems
 - Orders, products, processes
 - Jobs and tasks
 - Existing problem classifications
 - Academic
 - Limited practical usefulness
 - Used for benchmarking
 - Key visualization ideas

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