

## Note

- This is a document which combines all materials from the Scheduling course
- Files are also available individually in separate directories

# Part I

## Introduction

### Key Points

- AI is more than LLM
- Stochastic vs. deductive AI methods
- Constraint Based Scheduling and its alternatives
- Key advantages
  - Compositional
  - Reusable
  - Explainable
- Course structure

## 1 Artificial Intelligence

## 2 Scheduling

### 2.1 Constraint-Based Scheduling

#### Constraint Programming - in a nutshell

- Declarative description of problems with
  - *Variables* which range over (finite) sets of values
  - *Constraints* over subsets of variables which restrict possible value combinations
  - A *solution* is a value assignment which satisfies all constraints
- Constraint propagation/reasoning
  - Removing inconsistent values for variables
  - Detect failure if constraint can not be satisfied
  - Interaction of constraints via shared variables
  - Incomplete
- Search
  - User controlled assignment of values to variables
  - Each step triggers constraint propagation
- Different domains require/allow different methods

## Constraint Programming is Different

- Declarative Programming
  - Concentrate on what you want
  - Not how to get there
  - Program != Algorithm
  - Program = Model
- Applied to Combinatorial Problems
  - No complete polynomial algorithms known (exist?)
  - CP less ad-hoc than heuristics
  - Models can evolve



## A Subtractive Process

“Oh, bosh, as Mr. Ruskin says. Sculpture, per se, is the simplest thing in the world. All you have to do is to take a big chunk of marble and a hammer and chisel, make up your mind what you are about to create and chip off all the marble you don’t want.”-Paris Gaulois.

Source: <https://quoteinvestigator.com/2014/06/22/chip-away/>

## 2.2 Other Solution Approaches

### Other Technologies

- Heuristics
- Integer Programming
- Local search
- Deep neural networks

## 3 Course Structure

### 3.1 What is not covered?

#### How does it all work?

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## 3.2 A Short History

### Summary

- Why use Constraint Based Scheduling?
- Compared to other AI methods
- Compared to other solution approaches

# Part II

# Concepts

### Key Points

- We introduce the core concepts used in scheduling
- Different layers of description
  - Why we are scheduling (orders, products, processes)
  - What we are doing (jobs, tasks)
- Temporal Relations
- Process description
- Problem classification
- Visualization

## 4 Core Concepts

### 4.1 Orders, Products, Processes

### 4.2 Jobs and Tasks

## 5 Temporal Relations

### 5.1 Release and Due Date

## 6 Processes, Bill of Materials

## 7 Problem Classification

### 7.1 Job-Shop

### 7.2 Flow-Shop

### 7.3 Open-Shop

### 7.4 RCPSP

### 7.5 $\alpha, \beta, \gamma$ Notation

## 8 Key Visualization Methods

## 9 Summary

### Summary

- We introduced the key concepts for scheduling problems
- Orders, products, processes
- Jobs and tasks
- Existing problem classifications
  - Academic
  - Limited practical usefulness
- Key visualization methods

## **Part III**

# **Machines and Resources**

### **Key Points**

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## **10 Disjunctive Resources**

## **11 Cumulative Resources**

## **12 Machine Choice**

### **12.1 Identical Machines**

### **12.2 Machine Dependent Speed**

### **12.3 Machine Preferences**

## **13 Work in Progress and Planned Downtimes**

## **14 Calendars**

## **15 Summary**

### **Summary**

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## **Part IV**

# **Experiments**

### **Key Points**

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## **16 The Scheduling Tool**

### **17 Data Input**

### **18 Result Output**

### **19 Instance Generator**

## **20 Predefined Problem Sets**

### **20.1 Taillard**

### **20.2 SALBP**

### **20.3 Test Scheduling**

### **20.4 Hybrid Flexible Flowshop**

## **21 Creating Your Own Tests**

## **22 Summary**

Summary

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## **Part V**

# **Objectives**

Key Points

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## **23 Why Have an Objective?**

### **23.1 Cost vs. Profit Based Objectives**

## **24 Objective Types**

### **24.1 Makespan**

### **24.2 Flowtime**

### **24.3 Lateness**

### **24.4 Earliness**

### **24.5 Just-In-Time**

### **24.6 Hybrid**

### **24.7 Resource Levels**

## **25 Multi-Level**

## **26 Interactive Scheduling**

Summary

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## **Part VI**

# **Advanced Concepts**

Key Points

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- 27 Sequence Dependent Setup**
- 28 Transportation Time**
- 29 Human Resource Constraints**
- 30 Energy Cost Aware Scheduling**
- 31 Preemption**
- 32 Inventory**
- 33 Alternative Processes/Process Paths**
- 34 Explainability**
- 35 Summary**

#### **Summary**

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## **Part VII**

# **Case Studies**

#### **Key Points**

- We provide a number of scheduling case studies
- Use the methodology developed to describe problems
- Use scheduling tool to provide solutions
- Generic tool provides good, but not always best solutions
- Two case studies are not handled by scheduling tool (yet)

#### **Case Studies Overview**

- Production Planning and Detailed Scheduling
  - How to use detailed scheduling in a wider context
- Assembly Line Balancing
  - Scheduling to plan design of an assembly line
- Test Scheduling
  - Scheduling tests on resources
- Factory Design
  - Location of resources affects scheduling outcome

- Oven Scheduling
  - Solving one detailed scheduling problem is not enough
- Blades and Vanes
  - Capacity and production planning over a multi-year period

### **Summary**

- See how the methodology can be applied to solve real-world problems
- Generic tool provides immediate solution of good quality
- Visualization of results is also provided
- Tool will be available in a few weeks time

## **Part VIII**

# **Production Planning Case Study**

### **Key Points**

- Case study from industry
- Production planning and detailed scheduling
- Based on project with medical devices company in Cork
  - Real problem
  - Realistic data
- Solved in two stages
  - Production planning based on run-out days and safety stock levels
  - Scheduling using our generic scheduling tool

### **Product List**

Name	ShortName	Nr	DailySales	InventoryAtStart	CalcDaysCover	LotSize	CycleTime	LotDuration	Machine	ProductType	SafetyStock	SafetyAlert
P1	P1	1	3.20	877	274.06	163	1.33	217	8	pt1	66	253.44
P2	P2	2	11.40	1,011	88.68	240	1.20	288	8	pt2	774	20.79
P3	P3	3	796.20	26,204	32.91	420	2.10	882	5,7,9,10,13,14,16	pt3	12,108	17.70
P4	P4	4	233.80	7,877	33.69	420	2.00	840	5,7,9,10,13,14,16	pt4	3,358	19.33
P5	P5	5	267.30	7,152	26.76	350	2.30	805	5,7,9,10,13,14,16	pt5	3,906	12.14
P6	P6	6	606.20	18,654	30.77	350	2.30	805	5,7,9,10,13,14,16	pt6	9,293	15.44
P7	P7	7	137.30	4,939	35.97	420	2.00	840	5,7,9,10,13,14,16	pt7	1,979	21.56
P8	P8	8	88.30	3,152	35.70	350	2.30	805	5,7,9,10,13,14,16	pt8	1,342	20.50
P9	P9	9	77.20	2,688	34.82	420	2.10	882	5,7,9,10,13,14,16	pt9	1,082	20.80
P10	P10	10	165.60	5,971	36.06	420	2.10	882	5,7,9,10,13,14,16	pt10	2,649	20.06
P11	P11	11	60.70	2,310	38.06	420	2.10	882	5,7,9,10,13,14,16	pt11	877	23.61
P12	P12	12	51.80	1,928	37.22	350	2.30	805	5,7,9,10,13,14,16	pt12	883	20.17
P13	P13	13	79.00	2,231	28.24	320	2.30	736	5,7,9,10,13,14,16	pt13	1,193	13.14
P14	P14	14	271.20	8,951	33.01	432	2.10	908	5,7,9,10,13,14,16	pt14	3,732	19.24
P15	P15	15	86.60	3,244	37.46	336	2.00	672	5,7,9,10,13,14,16	pt15	1,454	20.67
P16	P16	16	42.40	2,110	49.76	420	2.10	882	5,7,9,10,13,14,16	pt16	875	29.13
P17	P17	17	17.60	681	38.69	420	2.00	840	5,7,9,10,13,14,16	pt17	290	22.22
P18	P18	18	217.50	5,710	26.25	336	2.00	672	5,7,9,10,13,14,16	pt18	2,814	13.31
P19	P19	19	56.30	2,450	43.52	420	2.00	840	5,7,9,10,13,14,16	pt19	804	29.24
P20	P20	20	13.60	506	37.21	480	2.00	960	5,7,9,10,13,14,16	pt20	272	17.21
P21	P21	21	10.80	977	90.46	360	2.10	756	5,7,9,10,13,14,16	pt21	293	63.33
P22	P22	22	21.80	1,538	70.55	420	2.00	840	5,7,9,10,13,14,16	pt22	349	54.54
P23	P23	23	189.10	5,195	27.47	360	2.30	828	5,7,9,10,13,14,16	pt23	2,941	11.92
P24	P24	24	9.50	886	93.26	350	2.30	805	5,7,9,10,13,14,16	pt24	191	73.16
P25	P25	25	7.50	326	43.47	120	2.30	276	5,7,9,10,13,14,16	pt25	210	15.47
P26	P26	26	11.60	418	36.03	360	2.10	756	5,7,9,10,13,14,16	pt26	187	19.91
P27	P27	27	16.50	1,388	84.12	480	2.10	1,008	5,7,9,10,13,14,16	pt27	218	70.91

### Product List (Sorted by Daily Sales)

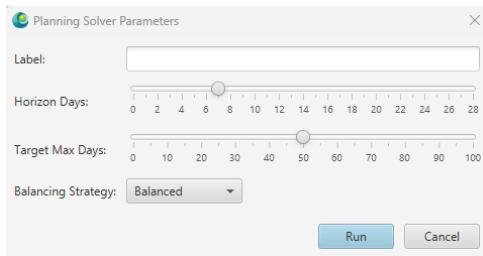
Product X														
Name	ShortName	Nr	DailySales	InventoryAtStart	CalcDaysCover	LotSize	CycleTime	LotDuration	Machine	ProductType	SafetyStock	SafetyAlert		
P3	P3	3	796.20	26,204	32.91	420	2.10	882	5,7,9,10,13,14,16	pt3	12,108	17.70		
P6	P6	6	606.20	18,654	30.77	350	2.30	805	5,7,9,10,13,14,16	pt6	9,293	15.44		
P14	P14	14	271.20	8,951	33.01	432	2.10	908	5,7,9,10,13,14,16	pt14	3,732	19.24		
P53	P53	53	267.70	8,264	30.87	504	1.20	605	1,2,3,8	pt2	3,734	16.92		
P5	P5	5	267.30	7,152	26.76	350	2.30	805	5,7,9,10,13,14,16	pt5	3,906	12.14		
P124	P124	124	242.70	16,503	68.00	240	5.00	1,200	15,18,19	pt65	3,595	53.19		
P4	P4	4	233.80	7,877	33.69	420	2.00	840	5,7,9,10,13,14,16	pt4	3,358	19.33		
P123	P123	123	223.40	7,600	34.02	490	2.33	1,142	1,2,3,8	pt51	3,738	17.29		
P18	P18	18	217.50	5,710	26.25	336	2.00	672	5,7,9,10,13,14,16	pt18	2,814	13.31		
P23	P23	23	189.10	5,195	27.47	360	2.30	828	5,7,9,10,13,14,16	pt23	2,941	11.92		
P56	P56	56	168.20	4,824	28.68	504	1.20	605	1,2,3,8	pt2	2,660	12.87		
P10	P10	10	165.60	5,971	36.06	420	2.10	882	5,7,9,10,13,14,16	pt10	2,649	20.06		
P59	P59	59	152.80	5,666	37.08	420	1.33	559	1,2,3,8	pt51	3,095	16.83		
P7	P7	7	137.30	4,939	35.97	420	2.00	840	5,7,9,10,13,14,16	pt7	1,979	21.56		
P57	P57	57	134.80	5,358	39.75	588	1.10	647	1,2,3,8	pt53	2,294	22.73		
P36	P36	36	133.50	3,895	29.18	336	2.00	672	5,7,9,10,13,14,16	pt36	2,057	13.77		
P54	P54	54	122.40	5,059	41.33	480	1.33	639	1,2,3,8	pt51	1,965	25.28		
P121	P121	121	98.10	4,334	44.18	588	1.10	647	1,2,3,8	pt53	1,524	28.64		
P8	P8	8	88.30	3,152	35.70	350	2.30	805	5,7,9,10,13,14,16	pt8	1,342	20.50		
P125	P125	125	86.90	8,593	98.88	240	5.00	1,200	15,18,19	pt65	1,022	87.12		
P15	P15	15	86.60	3,244	37.46	336	2.00	672	5,7,9,10,13,14,16	pt15	1,454	20.67		
P100	P100	100	85.20	2,665	31.28	420	1.33	559	1,2,3,8	pt56	1,115	18.19		
P55	P55	55	79.50	2,876	36.18	441	2.33	1,028	1,2,3,8	pt52	1,367	18.98		
P13	P13	13	79.00	2,231	28.24	320	2.30	736	5,7,9,10,13,14,16	pt13	1,193	13.14		
P9	P9	9	77.20	2,688	34.82	420	2.10	882	5,7,9,10,13,14,16	pt9	1,082	20.80		
P47	P47	47	74.60	5,391	72.27	160	6.84	1,095	2,11	pt47	1,132	57.09		
P11	P11	11	60.70	2,310	38.06	420	2.10	882	5,7,9,10,13,14,16	pt11	877	23.61		
P61	P61	61	60.30	2,758	45.74	490	1.33	652	1,2,3,8	pt56	1,073	27.94		
P78	P78	78	57.60	2,234	38.78	588	1.10	647	1,2,3,8	pt59	824	24.48		
P19	P19	19	56.30	2,450	43.52	420	2.00	840	5,7,9,10,13,14,16	pt19	804	29.24		

### Product List (Sorted by Days Cover)

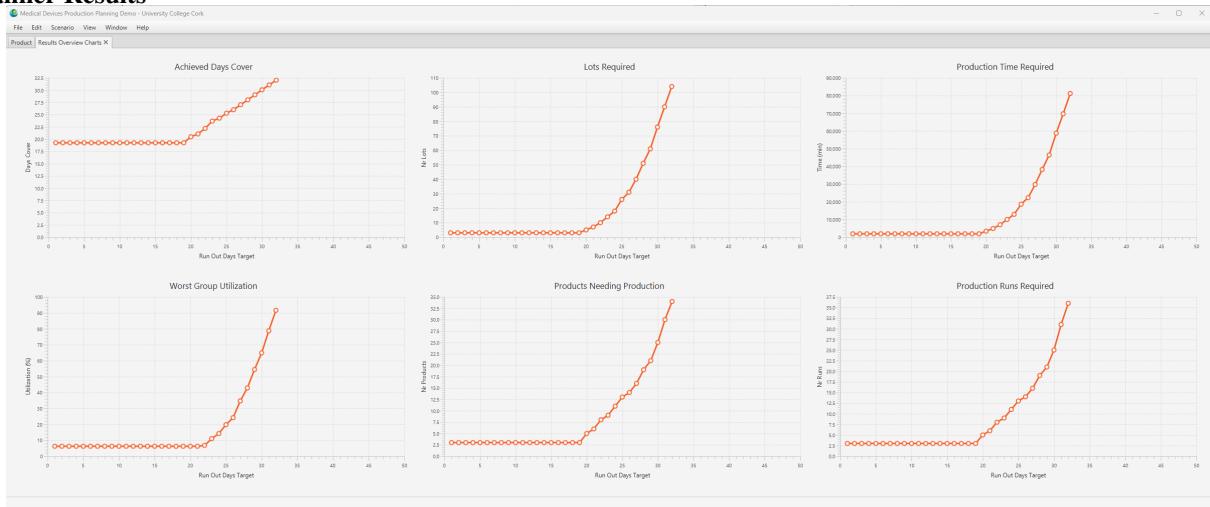
Product X														
Name	ShortName	Nr	DailySales	InventoryAtStart	CalcDaysCover	LotSize	CycleTime	LotDuration	Machine	ProductType	SafetyStock	SafetyAlert		
P35	P35	35	1.30	26	20.00	120	2.30	276	5,7,9,10,13,14,16	pt35	33	0.00		
P18	P18	18	217.50	5,710	26.25	336	2.00	672	5,7,9,10,13,14,16	pt18	2,814	13.31		
P5	P5	5	267.30	7,152	26.76	350	2.30	805	5,7,9,10,13,14,16	pt5	3,906	12.14		
P23	P23	23	189.10	5,195	27.47	360	2.30	828	5,7,9,10,13,14,16	pt23	2,941	11.92		
P13	P13	13	79.00	2,231	28.24	320	2.30	736	5,7,9,10,13,14,16	pt13	1,193	13.14		
P56	P56	56	168.20	4,824	28.68	504	1.20	605	1,2,3,8	pt2	2,660	12.87		
P58	P58	58	55.00	1,590	28.91	420	2.33	979	1,2,3,8	pt54	1,208	6.95		
P36	P36	36	133.50	3,895	29.18	336	2.00	672	5,7,9,10,13,14,16	pt36	2,057	13.77		
P6	P6	6	606.20	18,654	30.77	350	2.30	805	5,7,9,10,13,14,16	pt6	9,293	15.44		
P53	P53	53	267.70	8,264	30.87	504	1.20	605	1,2,3,8	pt2	3,734	16.92		
P100	P100	100	85.20	2,665	31.28	420	1.33	559	1,2,3,8	pt56	1,115	18.19		
P122	P122	122	45.40	1,421	31.30	490	1.33	652	1,2,3,8	pt56	725	15.33		
P3	P3	3	796.20	26,204	32.91	420	2.10	882	5,7,9,10,13,14,16	pt3	12,108	17.70		
P14	P14	14	271.20	8,951	33.01	432	2.10	908	5,7,9,10,13,14,16	pt14	3,732	19.24		
P4	P4	4	233.80	7,877	33.69	420	2.00	840	5,7,9,10,13,14,16	pt4	3,358	19.33		
P123	P123	123	223.40	7,600	34.02	490	2.33	1,142	1,2,3,8	pt51	3,738	17.29		
P77	P77	77	33.00	1,146	34.73	336	1.20	404	1,2,3,8	pt61	565	17.61		
P9	P9	9	77.20	2,688	34.82	420	2.10	882	5,7,9,10,13,14,16	pt9	1,082	20.80		
P8	P8	8	88.30	3,152	35.70	350	2.30	805	5,7,9,10,13,14,16	pt8	1,342	20.50		
P7	P7	7	137.30	4,939	35.97	420	2.00	840	5,7,9,10,13,14,16	pt7	1,979	21.56		
P26	P26	26	11.60	418	36.03	360	2.10	756	5,7,9,10,13,14,16	pt26	187	19.91		
P10	P10	10	165.60	5,971	36.06	420	2.10	882	5,7,9,10,13,14,16	pt10	2,649	20.06		
P55	P55	55	79.50	2,876	36.18	441	2.33	1,028	1,2,3,8	pt52	1,367	18.98		
P63	P63	63	42.40	1,565	36.91	490	1.33	652	1,2,3,8	pt51	689	20.66		
P59	P59	59	152.80	5,666	37.08	420	1.33	559	1,2,3,8	pt51	3,095	16.83		
P20	P20	20	13.60	506	37.21	480	2.00	960	5,7,9,10,13,14,16	pt20	272	17.21		
P12	P12	12	51.80	1,928	37.22	350	2.30	805	5,7,9,10,13,14,16	pt12	883	20.17		
P44	P44	44	5.50	205	37.27	360	2.10	756	5,7,9,10,13,14,16	pt44	126	14.36		
P15	P15	15	86.60	3,244	37.46	336	2.00	672	5,7,9,10,13,14,16	pt15	1,454	20.67		

### Product List (Sorted by Safety Alert)

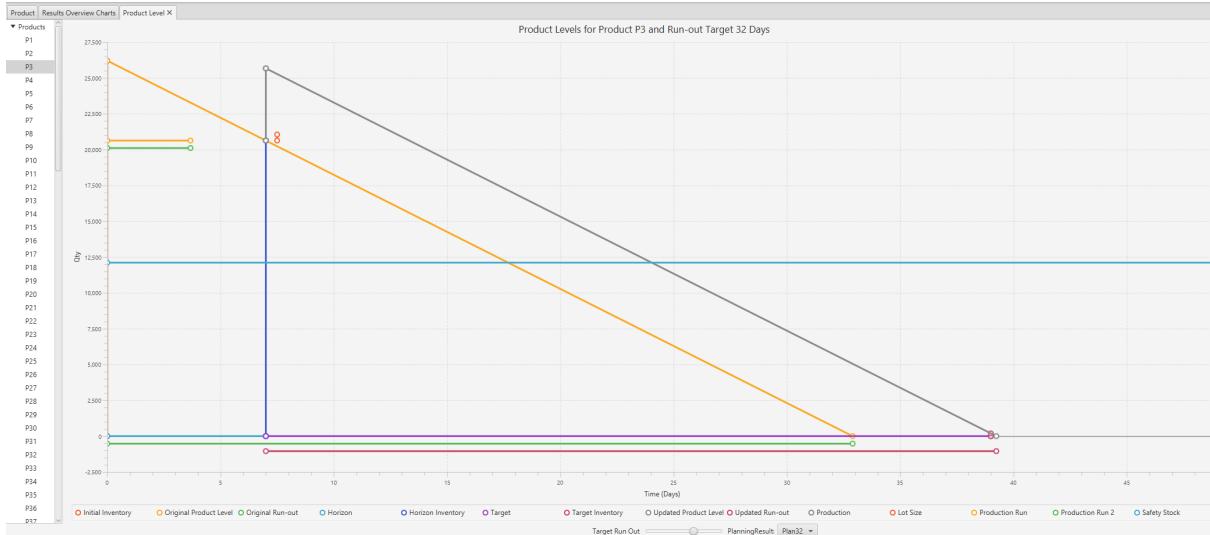




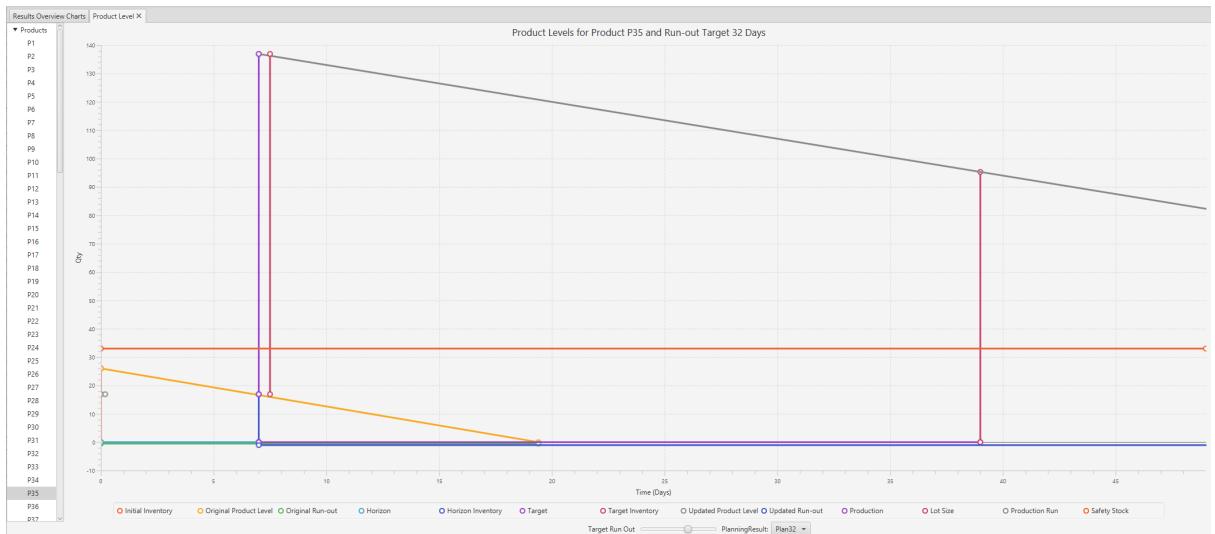
## Planner Results



## Product Level Chart for Product P3



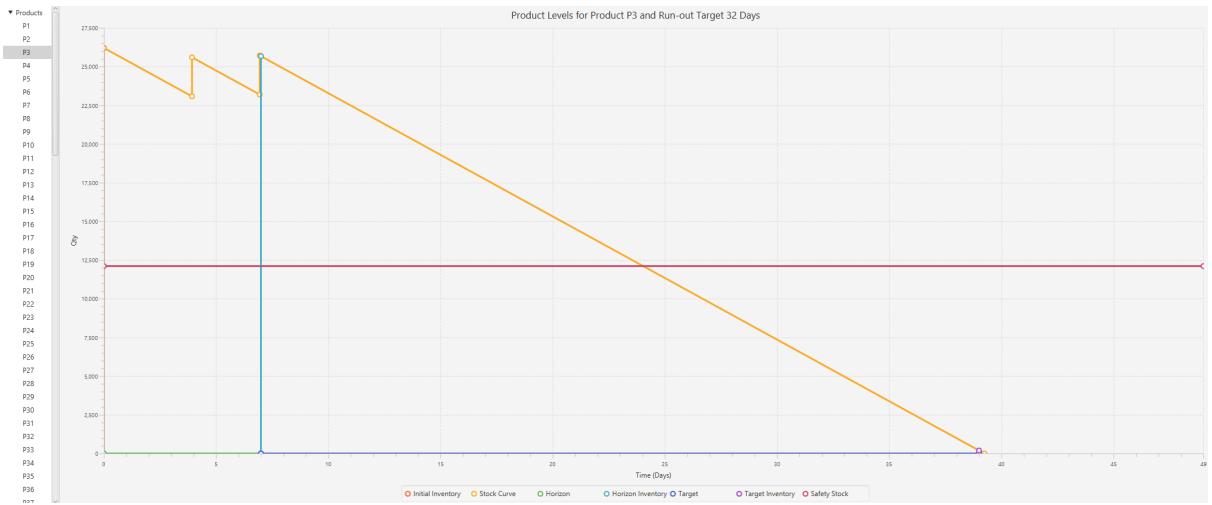
## Product Level Chart for Product P35



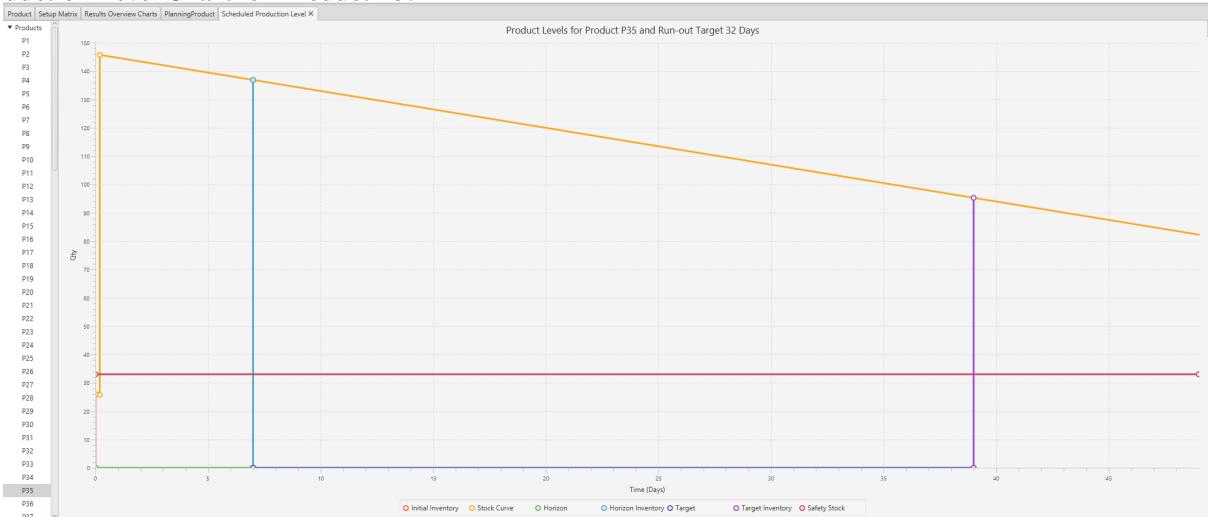
### Scheduled Production Runs

Product	Results Overview Charts		Product Level		Scheduled Production Level		ProductionRun X		
Name	Product	NrLots	Qty	Due	Start	End	Duration	StartDay	EndDay
job3_0	P3	6	2,520	10,080	366	5,658	5,292	0.25	3.93
job3_1	P3	6	2,520	10,080	4,712	10,004	5,292	3.27	6.95
job4_0	P4	3	1,260	10,080	0	2,520	2,520	0.00	1.75
job5_0	P5	10	3,500	10,080	1,794	9,844	8,050	1.25	6.84
job6_0	P6	7	2,450	10,080	4,224	9,859	5,635	2.93	6.85
job6_1	P6	8	2,800	10,080	0	6,440	6,440	0.00	4.47
job7_0	P7	1	420	10,080	7,442	8,282	840	5.17	5.75
job8_0	P8	1	350	10,080	816	1,621	805	0.57	1.13
job9_0	P9	1	420	10,080	3,282	4,164	882	2.28	2.89
job10_0	P10	2	840	10,080	0	1,764	1,764	0.00	1.23
job11_0	P11	1	420	10,080	6,500	7,382	882	4.51	5.13
job12_0	P12	1	350	10,080	1,651	2,456	805	1.15	1.71
job13_0	P13	3	960	10,080	0	2,208	2,208	0.00	1.53
job14_0	P14	4	1,728	10,080	0	3,632	3,632	0.00	2.52
job15_0	P15	1	336	10,080	2,580	3,252	672	1.79	2.26
job17_0	P17	1	420	10,080	5,718	6,558	840	3.97	4.55
job18_0	P18	9	3,024	10,080	3,144	9,192	6,048	2.18	6.38
job20_0	P20	1	480	10,080	3,692	4,652	960	2.56	3.23
job23_0	P23	7	2,520	10,080	2,516	8,312	5,796	1.75	5.77
job26_0	P26	1	360	10,080	0	756	756	0.00	0.53
job35_0	P35	1	120	0	0	276	276	0.00	0.19
job36_0	P36	4	1,344	10,080	6,618	9,306	2,688	4.60	6.46
job44_0	P44	1	360	10,080	2,298	3,054	756	1.60	2.12
job46_0	P46	1	350	10,080	8,372	9,177	805	5.81	6.37
job51_0	P51	1	140	6,064	0	630	630	0.00	0.44
job53_0	P53	5	2,520	10,080	707	3,732	3,025	0.49	2.59
job55_0	P55	1	441	10,080	2,580	3,608	1,028	1.79	2.51
job56_0	P56	4	2,016	10,080	7,218	9,638	2,420	5.01	6.69
job58_0	P58	2	840	10,002	3,668	5,626	1,958	2.55	3.91
job59_0	P59	1	420	10,080	464	1,023	559	0.32	0.71
job63_0	P63	1	490	10,080	0	652	652	0.00	0.45
job77_0	P77	1	336	10,080	0	404	404	0.00	0.28
job78_0	P78	1	588	10,080	0	647	647	0.00	0.45

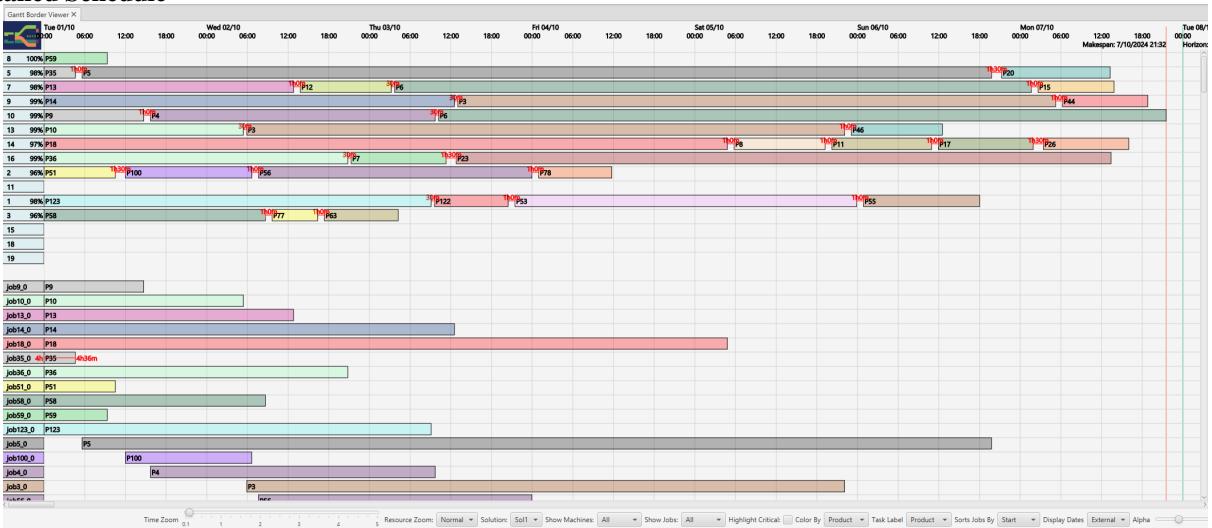
### Production Level Chart for Product P3



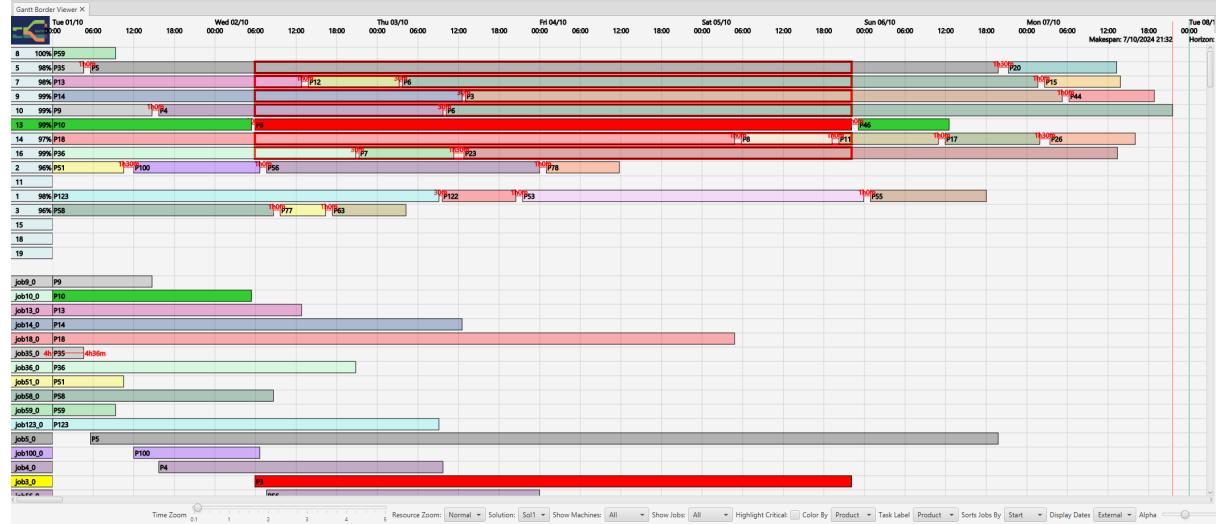
Production Level Chart for Product P35



Detailed Schedule



## Showing Alternative Machines in Gantt Chart



## Summary

- We demonstrated the use of our scheduling tool inside a production planning problem from industry
- Production planning decides which products to make in which quantity
  - Balance stock levels against projected demand
  - Allow for product specific safety stock levels
- Uses estimate of production capacity over planning horizon
- Use detailed scheduling to validate plan

# Part IX

## Assembly Line Balancing Case Study

### Key Points

- 

### Problem Description

### Feature Overview

### Summary

- 

# Part X

## Test Scheduling Case Study

### Key Points

-

### **Problem Description**

The problem arises in the context of a testing facility. A number of tests have to be performed in minimal time. Each test has a given duration and needs to run on one machine. While the test is running on a machine, no other test can use that machine. Some tests can only be assigned to a subset of the machines, for others you can use any available machine. For some tests, additional, possibly more than one, global resources are needed. While those resources are used for a test, no other test can use the resource. The objective is to finish the set of all tests as quickly as possible, i.e. all start times should be non-negative, and makespan should be minimized.

### **Feature Overview**

#### **Summary**

- 

## **Part XI**

# **Factory Design Case Study**

### **Key Points**

- 

### **Problem Description**

### **Feature Overview**

#### **Summary**

- 

## **Part XII**

# **Oven Scheduling Case Study**

### **Key Points**

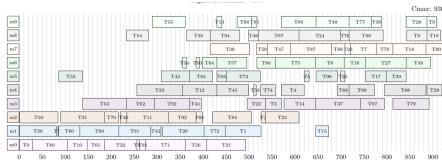
- Discusses two topics:
  - Solve a very specific industrial scheduling problem from the ASSISTANT EU project
  - Discuss the general issue of short-term scheduling vs. long-term objectives

### **Research Challenge**

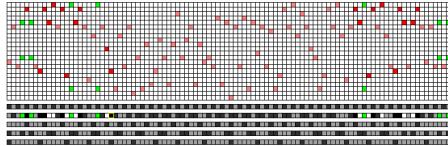
- Often the long-term business objectives are not visible in the operational decision problem
- We optimize a short-term objective without understanding the impact in the long term
- What choices should we make in short-term to improve overall result?
- Especially important when future data not yet visible
- Surprisingly, this problem is rarely discussed in literature

## Examples

- Production Scheduling
- Nearly all scheduling benchmarks use  $c_{max}$  (makespan) as objective
- Why?
- Do we want to close factory as rapidly as possible?

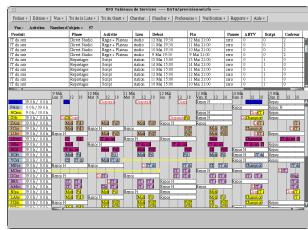


- Car Sequencing
- The best heuristics push difficult cars to the edge of schedule
- Because they are easier to schedule this way
- But: It makes it hard to schedule next day



## Examples

- Personnel Rostering
- Satisfy working rules and demands for period
- But: rules apply on a rolling horizon
- Easy to over-constrain problem for next period



- Transportation Planning
- Build daily delivery tours, optimizing cost
- Where are your trucks at 10PM?
- Also, avoid cherry-picking at start of week



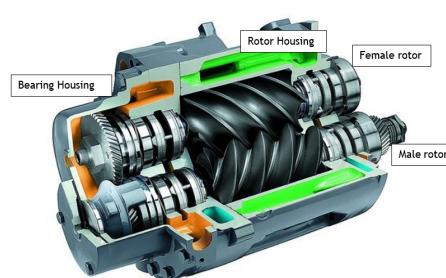
## Problem Studied Here

- Example from the ASSISTANT EU project (ended last year)
- Oven schedule for one of the industrial partners
- Schedule tasks on a set of ovens
- Tasks can share oven only if they are compatible
- Conflicting objectives
  - Energy use of ovens very significant, reduce when ovens are used
  - Waiting for an oven affects quality of product
- Jobs only visible when previous process step starts
- Currently scheduled by hand, industry partner expressed strong need for change

## What does this look like in the real world?



Industrial Oven



Rotors in Compressor

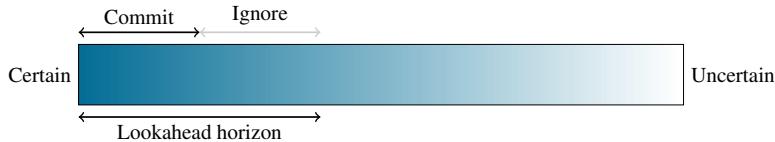
## Solution Approach: Constraint Programming

- Declarative modelling approach for combinatorial problems
  - Problem expressed in terms of variables and constraints
- Global constraints
  - Combines expressive modelling abstractions and powerful reasoning
  - Examples: disjunctive, cumulative, global\_cardinality
- Compositional: Add constraints as required
- Main application areas
  - Scheduling, rostering, transportation
  - Also: test generation, verification, configuration



### Overall Decomposition (Standard)

- We can only see that far into future
- We do not want to take decisions now that we might regret later
- We have to make some decisions now otherwise we never do anything
- *Rolling horizon* decomposition
  - We schedule up to *lookahead horizon* units into the future
  - We commit to implement resulting schedule only to up *commitHorizon*
  - We reschedule when we receive new information, or we reach the end of commitment
  - We solve each short-term sub problem based on short-term objectives



### Short-Term Schedule Modelling

- Challenge: There is no global constraint to express the oven resource constraint
- We are not able to invest a lot of time/resources to develop such a constraint
- Two choices:
  - Two traditional models with variables linking them (Lackner et al, Constraints 2023)
  - Direct model expressing conditions as disjunctions of basic constraints

## The Standard Pieces

- Jobs  $N$  consisting of multiple stages  $Q$ , tasks for each stage of each job, running on machines  $M$
- Release dates  $r_i$  of jobs given by up-stream schedule
- WiP  $w_k$  on certain machines resulting from earlier schedule
- Machine  $m_{ij}$  and start variables  $s_{ij}$  for each task
- Precedence constraints between tasks of each jobs, with total waiting time  $c_i$  when waiting for resource
- Total number of ovens used in schedule  $nrOvens$  by *nvalue* constraint

$$nvalue(nrOvens, [m_{ij} | i \in N, j \in Q] \text{++} [k | k \in M \text{ s.t. } w_k > 0])$$

## Resource Constraints

We start from the basic decomposition of the disjunctive machine choice constraint

$$\begin{aligned} \forall_{i_1, i_2 \in N} \forall_{j_1, j_2 \in Q \text{ s.t. } <i_1, j_1> \neq <i_2, j_2>} : \quad m_{i_1 j_1} \neq m_{i_2 j_2} \vee \\ s_{i_1 j_1} \geq s_{i_2 j_2} + d_{i_2 j_2} \vee \\ s_{i_2 j_2} \geq s_{i_1 j_1} + d_{i_1 j_1} \end{aligned}$$

Express case where tasks share an oven (only when types and stages are the same)

$$\begin{aligned} \forall_{i_1, i_2 \in N \text{ s.t. } i_1 \neq i_2} \forall_{j \in Q} : \quad m_{i_1 j} \neq m_{i_2 j} \vee \\ s_{i_1 j} \geq s_{i_2 j} + d_{i_2 j} \vee \\ s_{i_2 j} \geq s_{i_1 j} + d_{i_1 j} \vee \\ (t_{i_1 j_1} = t_{i_2 j_2} \wedge m_{i_1 j} = m_{i_2 j} \wedge s_{i_1 j} = s_{i_2 j}) \end{aligned}$$

## Limit stacking

Need binary variables  $b_{i_1 i_2 j}$  to state that two jobs  $i_1$  and  $i_2$  share oven in stage  $j$

$$\begin{aligned} \forall_{i_1, i_2 \in N \text{ s.t. } i_1 < i_2} \forall_{j \in Q} : \quad (b_{i_1 i_2 j} = 0 \wedge (m_{i_1 j} \neq m_{i_2 j} \vee \\ s_{i_1 j} \geq s_{i_2 j} + d_{i_2 j} \vee \\ s_{i_2 j} \geq s_{i_1 j} + d_{i_1 j}) \vee \\ (b_{i_1 i_2 j} = 1 \wedge t_{i_1 j_1} = t_{i_2 j_2} \wedge m_{i_1 j} = m_{i_2 j} \wedge s_{i_1 j} = s_{i_2 j})) \end{aligned}$$

Count how many jobs share stage  $j$  with job  $i$

$$\forall_{i \in N} \forall_{j \in Q} : \quad z_{ij} = \sum_{i_1=1}^{i-1} b_{i_1 ij} + \sum_{i_2=i+1}^n b_{ii_2 j}$$

Limit how many tasks can be stacked together

$$\forall_{i \in N} \forall_{j \in Q} : \quad z_{ij} < \text{maxStacked}$$

## This should not work!

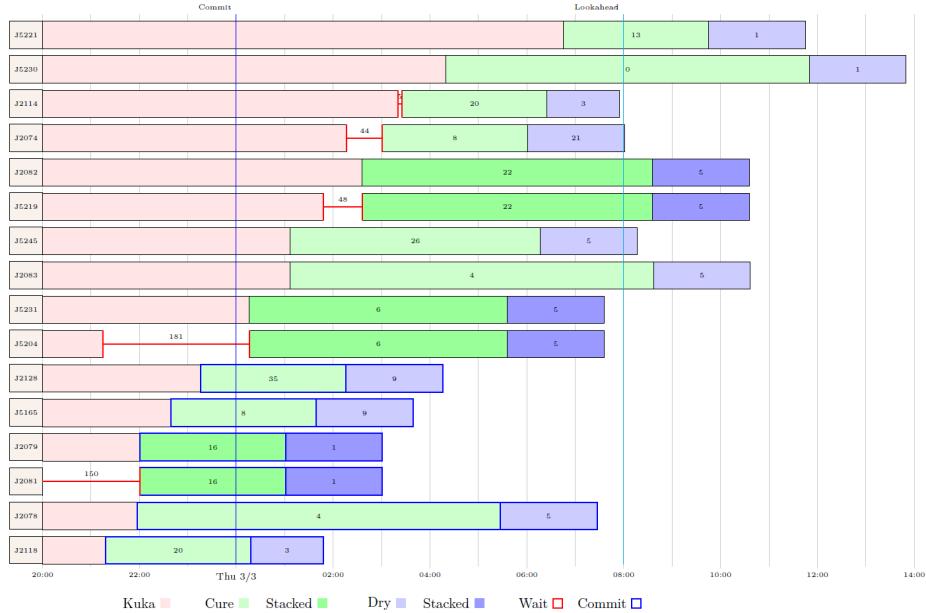
- Weakness of basic decomposition model was the reason to develop the scheduling constraints in the first place
- Does not scale well to thousands of tasks
- But model is well suited to some solvers
  - SAT based solvers, Chuffed, CP-SAT (OR-Tools)
  - MIP solvers
- This works (only) as long as problem size stays manageable

## Compound Objective

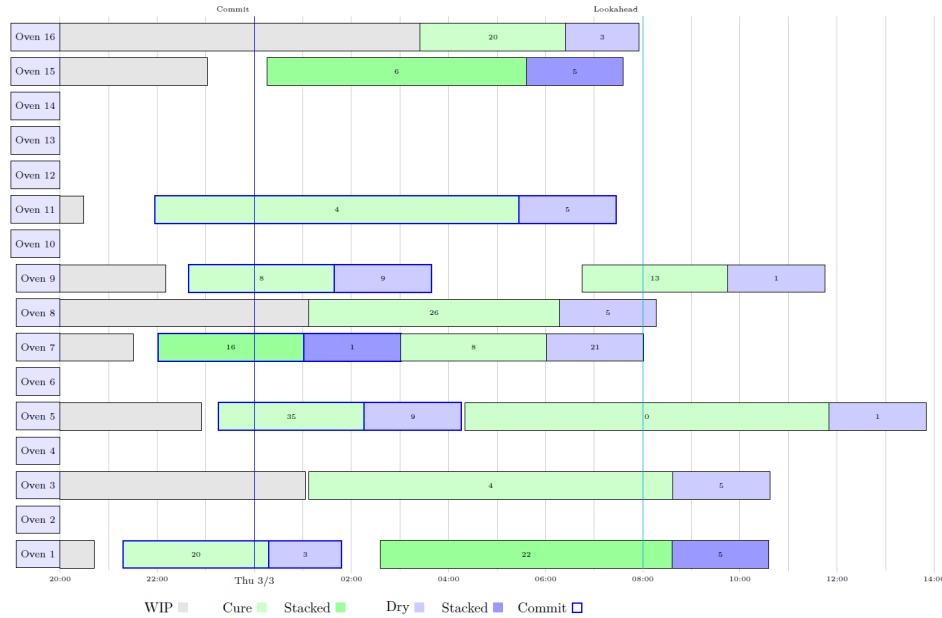
$$\min \alpha_1 \sum_{i \in N} c_i + \alpha_2 \text{nrOvens} + \alpha_3 \sum_{i \in N, j \in Q} z_{ij}$$

- Three conflicting elements
  - Total waiting time for jobs
  - Number of ovens used
  - Number of tasks stacked (negative coefficient)
- Reducing waiting time requires using more ovens
- Improved stacking will require for one job to wait until second is ready

## Short-Term Schedule: Job View



## Short Term Schedule: Resource View



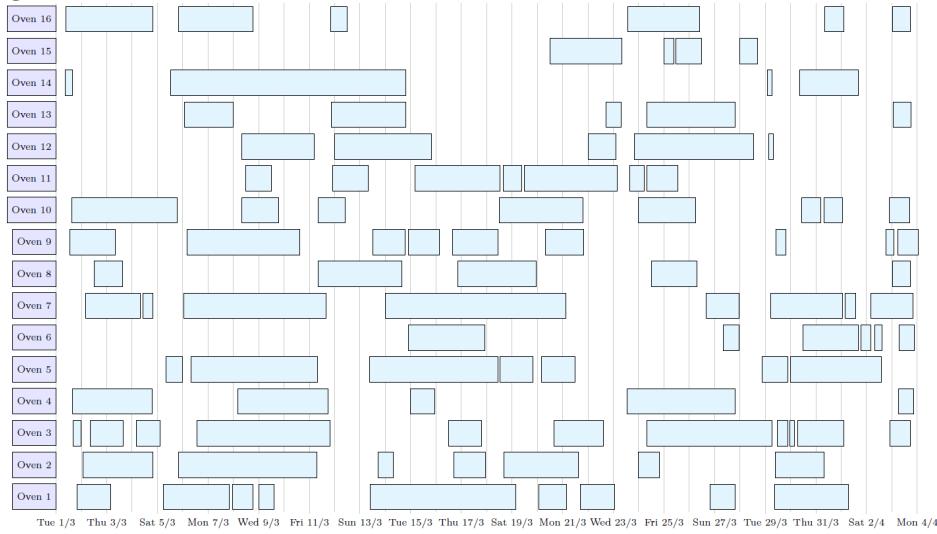
## Are the short-term solutions good?

- We solve many problems to optimality, depending on solver
- Optimality gap is small, increasing search time helps a bit
- But are we optimizing the best possible objective?

## Long Term Schedule: Detailed Schedule



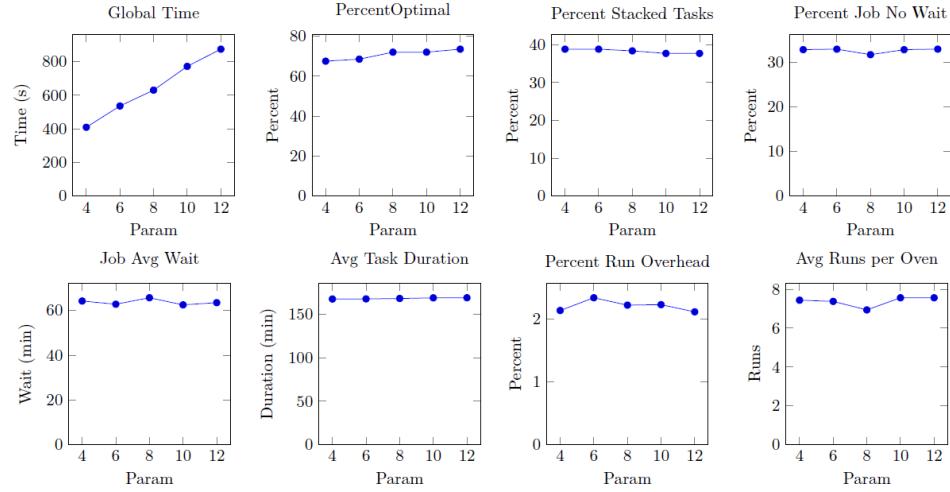
## Long Term Schedule: Abstracted Oven Runs



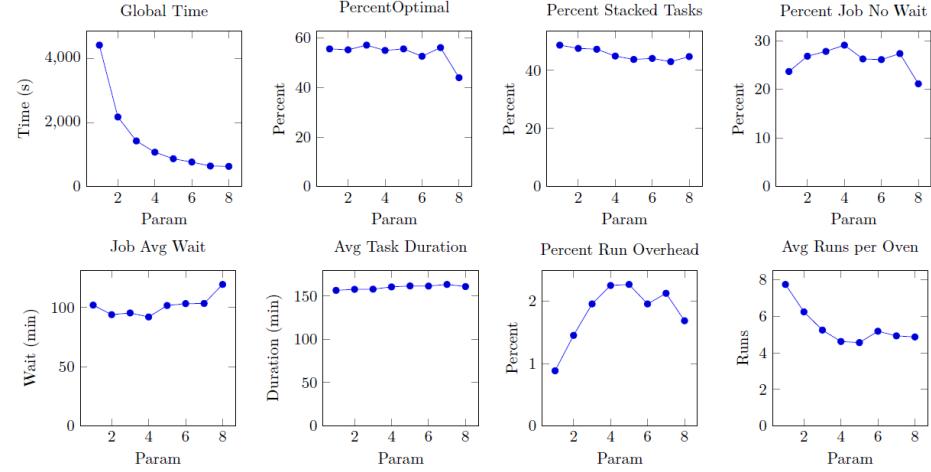
## Is that a good global schedule? KPIs

Name	Unit	Explanation
Global Time	Seconds	Total time for solving all sub problems
Nr Jobs	-	Total number of jobs scheduled
Nr Tasks	-	Total number of tasks scheduled
Percent Optimal	Percentage (0-100)	How many sub problems were solved to optimality
Percent Stacked Tasks	Percentage (0-100)	Percentage of all tasks scheduled that were stacked
Percent Jobs No Wait	Percentage (0-100)	Percentage of jobs that were scheduled without any waiting time
Job Average Wait	Minutes	Average wait time over all jobs
Job Maximal Wait	Minutes	Largest waiting time for any job scheduled
Ovens Used	-	Total number of ovens used during period
Avg Task Duration	Minutes	Average tasks duration (influenced by stacking)
Oven Runs	-	Number of oven runs over total horizon
Run Overhead Percent	Percentage (0-100)	Overhead during oven runs when machine is idle
Avg Runs per Oven Used	-	Average number of oven runs per oven used

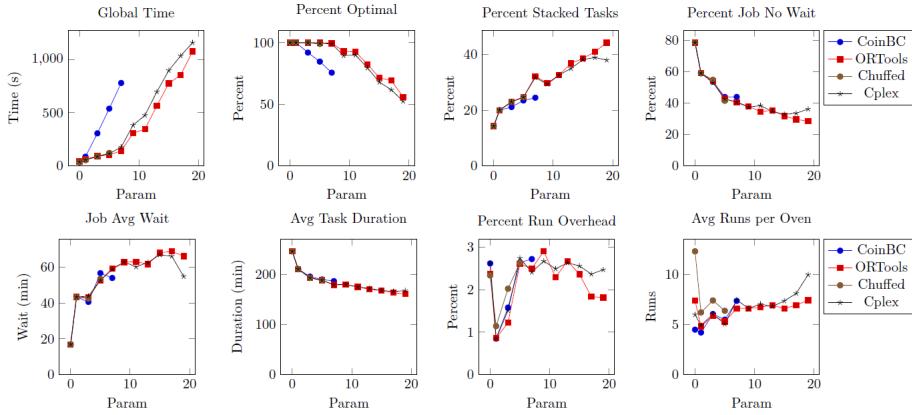
### Impact of Lookahead Parameter



### Impact of CommitHorizon Parameter



### Comparing Different Solvers



### Is the global solution really good?

- We schedule with limited information
- Hindsight is 20/20, we cannot expect best possible solution from partial information
- Process Challenge: Can we improve data visibility?
- Demand is variable over time, no steady-state solution
- Modelling Challenge: Can we define a short-term objective that produces better long-term solutions?
- Algorithm Challenge: Can we solve the global problem to optimality?
  - Assumes "a priori" visibility of data
  - This would provide a lower bound
  - But we need optimality to use as bound

### Summary

- Discussed a non-standard oven scheduling problem from industry
- Models with decomposition of resource constraints
- Good/very good short-term solutions
- But is the overall schedule close to the global optimum?
- In any case, industry partner was happy with solution and analysis

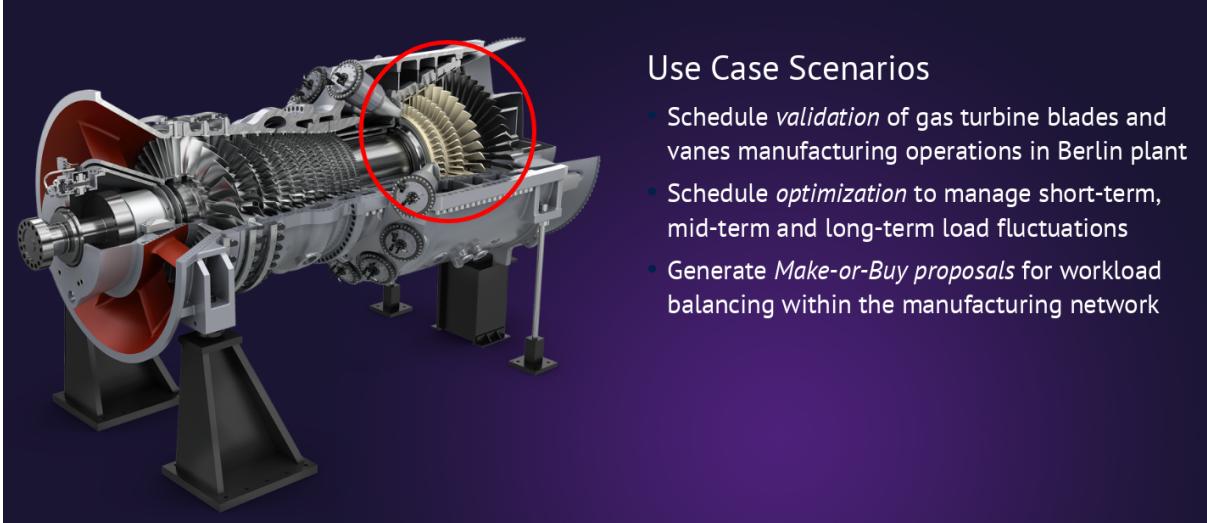
## Part XIII

# Blades and Vanes Production Case Study

### Key Points

- Scheduling/Planning tool for manufacturing industry
- Developed as part of European ASSISTANT project
- Focused on key make-or-buy decisions
- Complex manufacturing process with alternative process paths
- Outperforms both current in-house tool and commercial simulator
- Key Technology: Optimization and Constraint Programming

## Assistant Siemens Energy Use Case

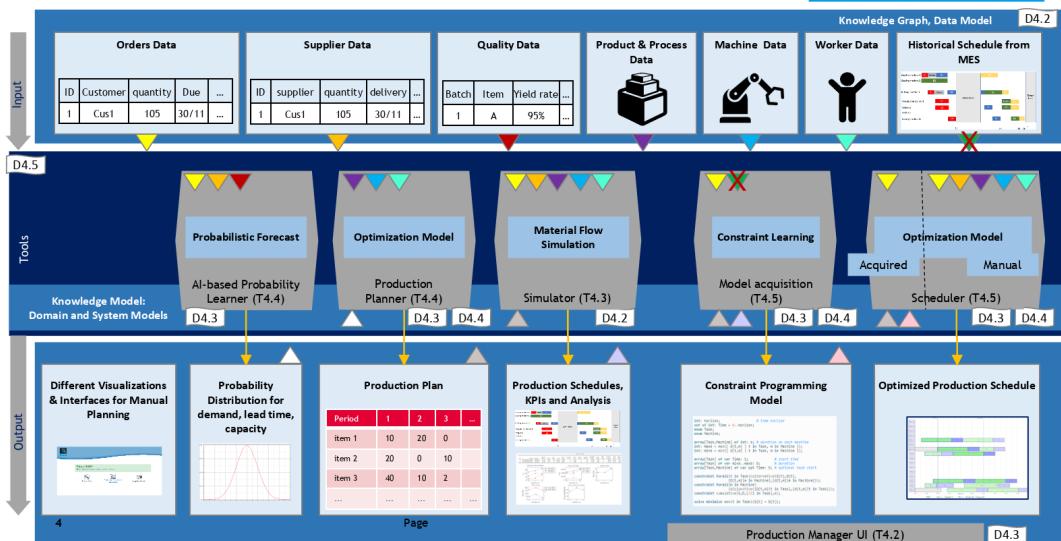


### Use Case Scenarios

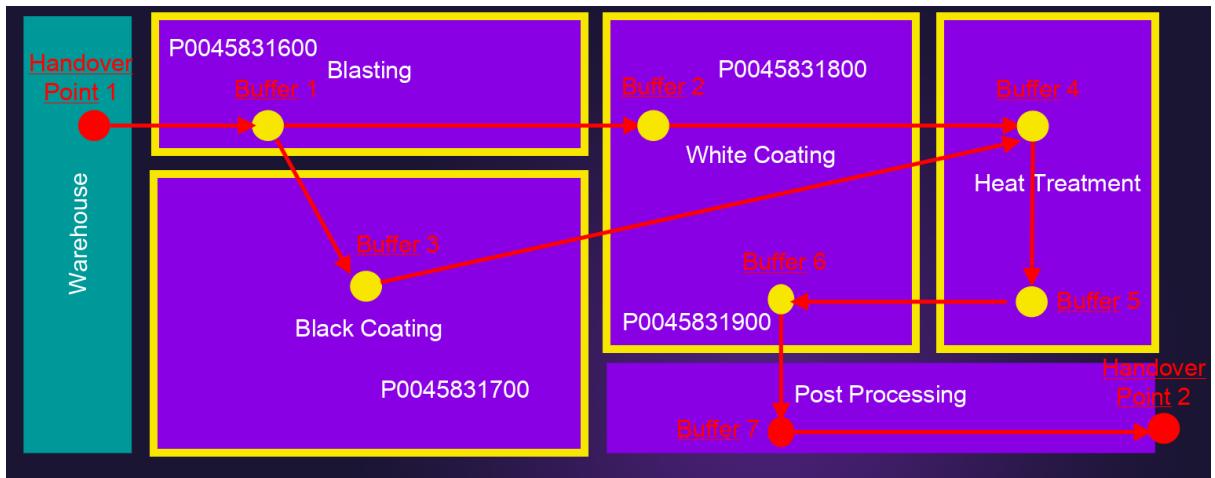
- Schedule validation of gas turbine blades and vanes manufacturing operations in Berlin plant
- Schedule optimization to manage short-term, mid-term and long-term load fluctuations
- Generate Make-or-Buy proposals for workload balancing within the manufacturing network

## ASSISTANT Project Overview

### Intelligent digital twin for process planning and scheduling



## SE Product Routing



## Test Datasets

### Full Scale Datasets

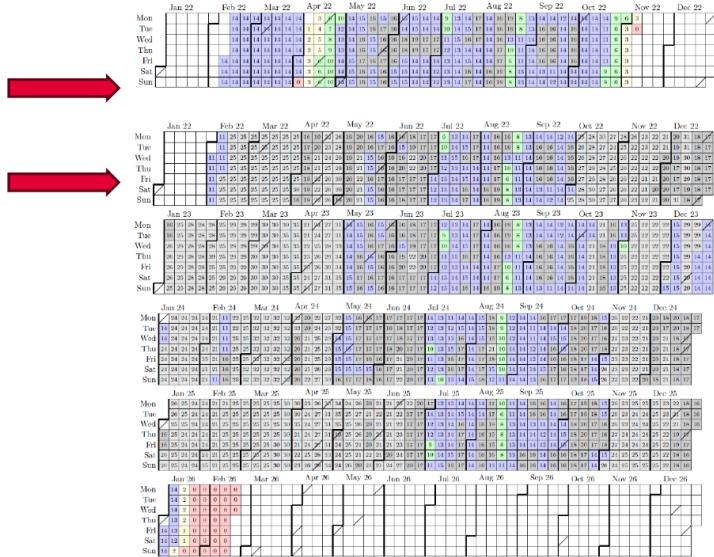
Berlin06: 96 orders, 9 months horizon, previous review

Berlin07: 450 orders, 4 years horizon

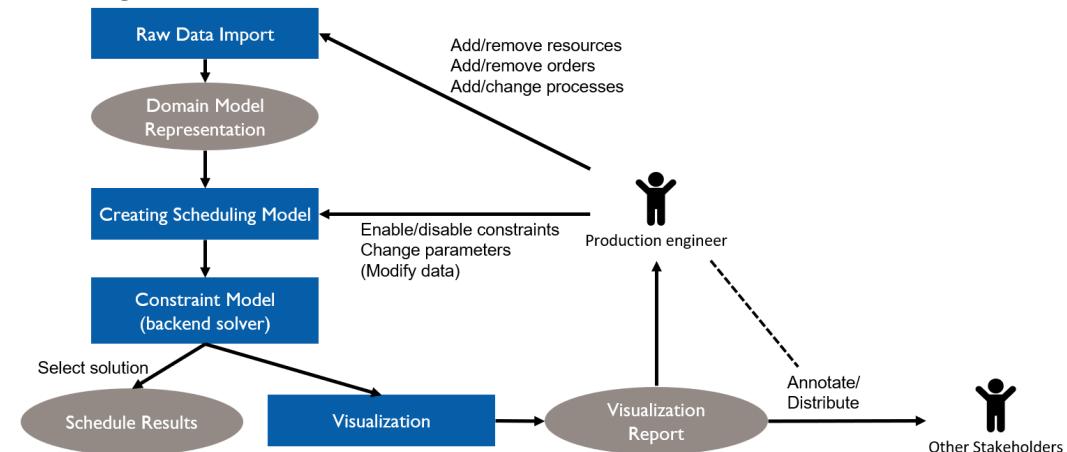
Berlin08: 559 orders, Christmas gap added

Berlin08a: 670 orders, filling gaps

Value in cell indicates active orders  
Yellow and red colors indicate low order volume



## Optimizer High Level Structure

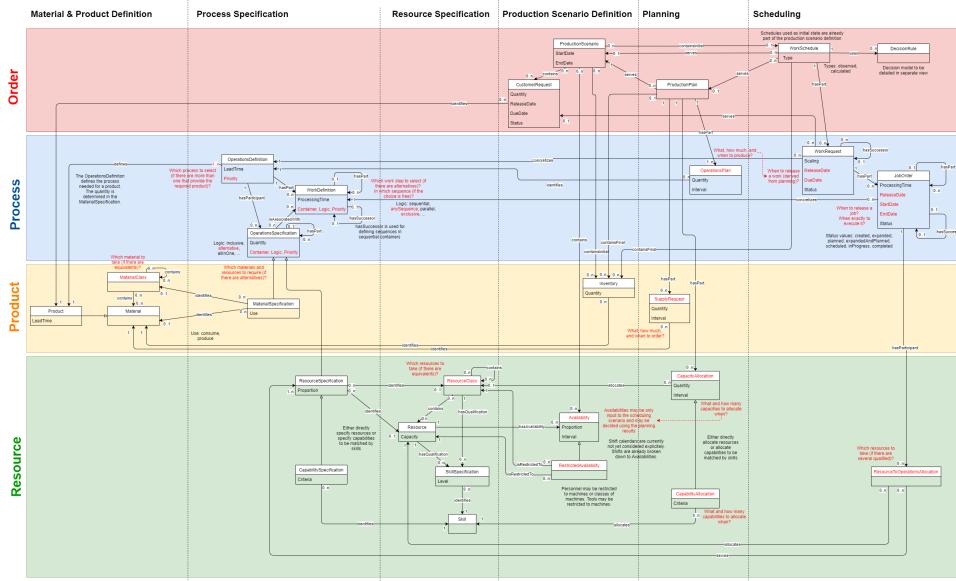


## Raw Data - Manual Data Entry Causes Problems

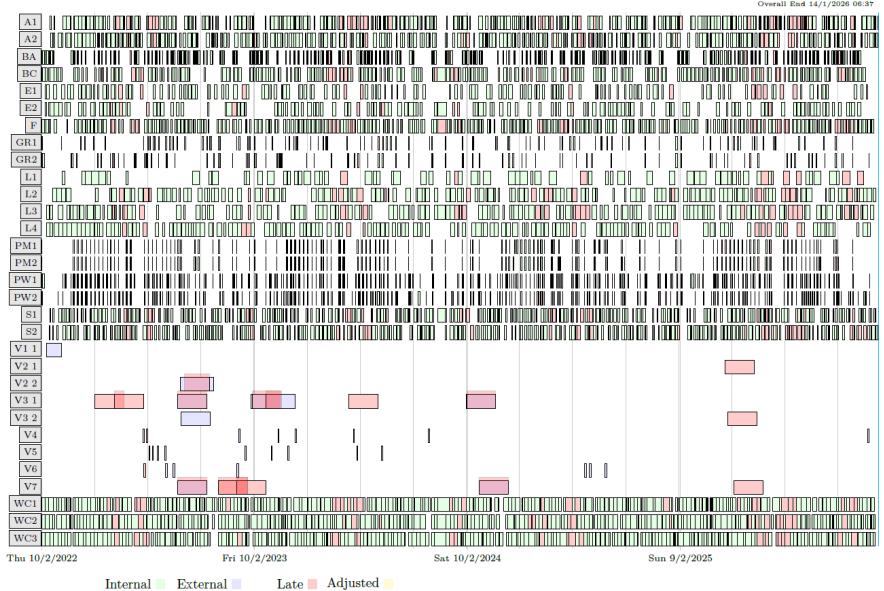
- Raw data come from spreadsheet
  - 20 tabs
- Excel is a particularly bad input data format
- Realistic, not real data
- Created by hand/automatically from existing test scenarios
- Series of files Berlin01 - Berlin05 were too inconsistent to run
- Berlin06 still contains some errors
- Optimizer explains all issues that it finds

Name	Severity	Sheet	RowNr	ColNr	Description
Issue1	Major	t_Load	129	11	DateTime not formatted correctly, found 2022-02-2800:00:00 format yyyy-MM-dd'T'HH:mm:ss
Issue2	Minor	t_Products	1	15	Extra Empty Header
Issue3	Minor	t_Availabilities	1	8	Extra Empty Header
Issue4	Minor	t_Unavailabilities	1	8	Extra Empty Header
Issue5	Minor	t_Shift_Segments	1	6	Extra Empty Header
Issue6	Major	t_Shift_Segments	1	1	TimeOnly not formatted correctly, found 0.250000, format H:mm:ss
Issue7	Major	t_Shift_Segments	1	2	TimeOnly not formatted correctly, found 0.583333, format H:mm:ss
Issue8	Major	t_Shift_Segments	2	1	TimeOnly not formatted correctly, found 0.291667, format H:mm:ss
Issue9	Major	t_Shift_Segments	2	2	TimeOnly not formatted correctly, found 0.302083, format H:mm:ss
Issue10	Major	t_Shift_Segments	3	1	TimeOnly not formatted correctly, found 0.458333, format H:mm:ss
Issue11	Major	t_Shift_Segments	3	2	TimeOnly not formatted correctly, found 0.479167, format H:mm:ss
Issue12	Major	t_Shift_Segments	4	1	TimeOnly not formatted correctly, found 0.583333, format H:mm:ss
Issue13	Major	t_Shift_Segments	4	2	TimeOnly not formatted correctly, found 0.916667, format H:mm:ss
Issue14	Major	t_Shift_Segments	5	1	TimeOnly not formatted correctly, found 0.666667, format H:mm:ss
Issue15	Major	t_Shift_Segments	5	2	TimeOnly not formatted correctly, found 0.677083, format H:mm:ss
Issue16	Major	t_Shift_Segments	6	1	TimeOnly not formatted correctly, found 0.770833, format H:mm:ss
Issue17	Major	t_Shift_Segments	6	2	TimeOnly not formatted correctly, found 0.791667, format H:mm:ss
Issue18	Major	t_Shift_Segments	7	1	TimeOnly not formatted correctly, found 0.916667, format H:mm:ss
Issue19	Major	t_Shift_Segments	7	2	TimeOnly not formatted correctly, found 0.250000, format H:mm:ss
Issue20	Major	t_Shift_Segments	8	1	TimeOnly not formatted correctly, found 0.000000, format H:mm:ss
Issue21	Major	t_Shift_Segments	8	2	TimeOnly not formatted correctly, found 0.010417, format H:mm:ss
Issue22	Major	t_Shift_Segments	9	1	TimeOnly not formatted correctly, found 0.083333, format H:mm:ss
Issue23	Major	t_Shift_Segments	9	2	TimeOnly not formatted correctly, found 0.104167, format H:mm:ss
Issue24	Minor	t_Shift_Segments	10	0	First Column Empty
Issue25	Minor	t_Shift_Segments	11	0	First Column Empty
Issue26	Minor	t_Shift_Segments	12	0	First Column Empty
Issue27	Minor	t_Shift_Segments	13	0	First Column Empty
Issue28	Minor	t_Shift_Segments	14	0	First Column Empty
Issue29	Minor	t_Shift_Segments	15	0	First Column Empty
Issue30	Minor	t_Shift_Segments	16	0	First Column Empty
Issue31	Minor	t_Shift_Segments	17	0	First Column Empty
Issue32	Minor	t_Shift_Segments	18	0	First Column Empty
Issue33	Minor	t_Shift_Patterns	1	9	Extra Empty Header
Issue34	Minor	t_Shift_Patterns	7	0	First Column Empty
Issue35	Minor	t_Shift_Patterns	8	0	First Column Empty

## Domain Model - Knowledge Graph



### Solution for Berlin 08a - Shows Only 20% of Tasks in Model



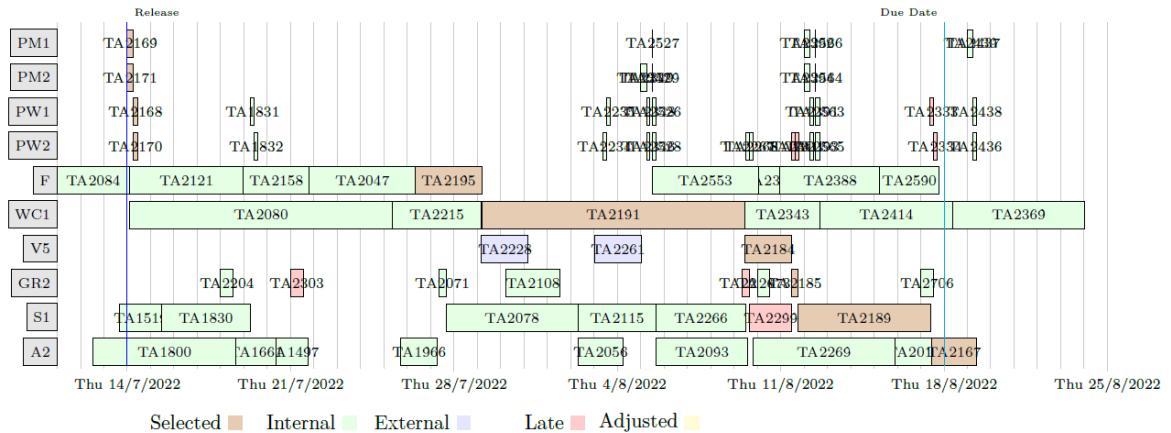
### Implementation

- Requirement capture done inside project
- Data checking/cleaning most time consuming aspect
- Some specified functionality was rejected by Betriebsrat
- Built in Java
- Uses IBM's CPOptimizer back-end
- 120k LoC, 110k generated, 3k solver
- Outperforms both
  - Current in-house tool

- Simulation based tool based on commercial simulator
- System installed at SE site, but not in daily use

### Explaining Late Delivery

- Explain why some orders are delivered late
- Find root-cause, show schedule in context



### Evaluation - KPIs

KPI	Baseline	Optimizer
OTD	> 80 %	92 %
Bottleneck machine utilization	99.5 %	100 %
Manufacturing defects	10-15 %	< 10 %
Scenarios in 8 hours	15-20	> 100,000

### Conclusion by Siemens Energy

*“Within less than eight hours the ASSISTANT tools provided us thousands of manufacturing scenarios including different make-or-buy recommendations for making deliberate decisions on the way to proceed for strategic planning.”*

from ASSISTANT final project review: Siemens Energy assessment

### Summary

- Scheduling/Planning tool for manufacturing industry
- Developed as part of European ASSISTANT project
- Focused on key make-or-buy decisions
- Complex manufacturing process with alternative process paths
- Outperforms both current in-house tool and commercial simulator
- Key Technology: Optimization and Constraint Programming

# Part XIV

## Where to Go from Here

### Key Points

- We are working on a survey of the existing CP & Scheduling literature
- Considers over 1200 papers
- Current version of survey available at <https://hsimonis.github.io/pthg24>

## 36 CP and Scheduling Literature Survey

### A Survey of the Existing Literature

- Joint work with Cemalettin Ozturk, MTU
- What is out there
- Where to start
- Where to publish
- I'm interested in some specific topic, what is relevant

### 36.1 Methodology

#### Methodology

- Manually curated list of works, somewhat inclusive
- Starting with bibtex files
- Citation links through OpenCitations (open access)
- Content analysis on local copies of pdf files
- Closure of domain by analyzing missing cited and citing works
- Limited manual analysis of works (datasets, code)
- Results presented as LaTeX documents
- Open source analysis on git: <https://hsimonis.github.io/pthg24/>

### 36.2 Analysis Results

#### Overall Analysis (Based on 671 Works)



Table 5: Works from bibtex (Total 274)

Key	Authors	Title	LC	Cite	Year	Conference /Journal	Pages	Nr Cites	Nr Refs	b	c
ForbesHJST24	M. Forbes [T. Taimre]	Combining optimisation and simulation using logic-based Benders decomposition	Yes	[217]	2024	European Journal of Operational Research	15	0	26	1314	1496
ForbesHJST24											
PrataAN23	Bruno A. Prata [Levi R. Abreu] [Marcelo S. Nagano]	Applications of constraint programming in production scheduling problems: A descriptive bibliometric analysis	Yes	[509]	2024	Results in Control and Optimization	17	0	0	1427	1497
abs-2402-00459	S. Nguyen [Dhananjay R. Thiruvady] [Y. Sun] [M. Zhang]	Genetic-based Constraint Programming for Resource Constrained Job Scheduling	Yes	[169]	2024	CoRR	21	0	0	1495	1498
AbreuNP23	AbreuNP23 [Levi Ribeiro de Abreu] [Marcelo Seido Nagano] [Bruno A. Prata]	Two-stage constraint programming approach for open shop scheduling problem with machine blocking	Yes	[168]	2023	International Journal of Production Research	20	1	47	1243	1499
AbreuPNF23	Levi R. Abreu [Bruno A. Prata] [Marcelo S. Nagano] [José M. Framinan]	A constraint programming-based iterated greedy algorithm for the open shop with sequence-dependent processing times and makespan minimization	Yes	[3]	2023	Computers & Operations Research	12	0	46	1244	1500
Adelgren2023	N. Adelgren [Christofer T. Maravillas]	Optimization of production scheduling formulations including resource constraints	Yes	[7]	2023	Computers & Industrial Engineering	12	0	43	1245	1501
AksarVP23	S. Aksar [Camino R. Vela] [Juan José Palacios] [L. González-Rodríguez]	Mathematical models and benchmarking for the fuzzy job shop scheduling problem	Yes	[8]	2023	Computers & Industrial Engineering	14	0	50	1246	1502
AkramNHSA23	Hilal Omar Akrami [Nor Kamariah Noordin] [F. Hashmi] [Mold Fadlee A. Rasid] [Mustafa Ismail] [Salman Abdulrahman M. Abdulghani]	Joint Scheduling and Routing Optimization for Deterministic Hybrid Traffic in Time-Sensitive Networks Using Constraint Programming	Yes	[13]	2023	IEEE Access	16	0	0	1248	1503
AffieriGPS23	A. Affieri [M. Garrappa] [E. Pastore] [F. Salassa]	Permutation flowshop problems minimizing core processing time and core idle time	Yes	[15]	2023	Computers & Industrial Engineering	13	0	37	1249	1504
AffieriGPS23		Scheduling through logic-based tools	Yes	[127]	2023	Constraints An. Int.	1	0	0	1287	1505
Caballer023	Jordi Coll Caballero	Constraint Programming for Flexible Flow Shop Scheduling Problem with Repeated Jobs and Repeated Operations	Yes	[159]	2023	Advances in Science and Technology Research Journal	14	0	0	1297	1506
CzerniachowskaW23	K. Czerniachowska [R. Wiczniarek] [K. Zywicki]	Overload-Checking and Edge-Finding for Robust Cumulative Scheduling	No	[207]	2023	INFORMS Journal on Computing	null	0	16	No	1507
FahimiQ23	H. Fahimi [C. Quimper]	Cumulative Hybrid Job Shop Systems in Dynamic Environments: Mixed-Integer Linear Programming and Constraint Programming Approaches	Yes	[212]	2023	Omega	15	7	60	1312	1508
GhasemiMH23	S. Ghasemi [R. Tavakkoli-Moghaddam] [M. Hamidi]	Operating room scheduling by emphasizing human factors and dynamic decision-making styles: a constraint programming method	No	[242]	2023	International Journal of Systems Science: Operations Logistics	null	0	104	No	1509
GuoZ23	P. Guo [J. Zhu]	Capacity reservation for humanitarian relief: A logic-based Benders decomposition method with subgradient cut	Yes	[269]	2023	European Journal of Operational Research	29	0	112	1325	1510
GurPAE23	S. Gür [M. Pinarbası] [Haci Mehmet Alakas] [T. Eren]	Operating room scheduling with surgical team: a new approach with constraint programming and goal programming	Yes	[270]	2023	Central. Eur. J. Oper. Res.	25	1	40	1327	1511
IsikYA23	Eyüp Ensar Isik [Seyda Topaloğlu Yıldız] [Özge Satır Akpunar]	Constraint programming models for the hybrid flow shop scheduling problem and its extensions	Yes	[321]	2023	Soft Comput.	28	0	127	1350	1512
JuviniHL23a	C. Juvini [L. Housset] [P. Lopez]	Logic-based Benders decomposition for the preemptive flexible job-shop scheduling problem	Yes	[331]	2023	Computers & Operations Research	17	0	40	1355	1513
LacknerMMWW23	M. Lackner [C. Mrkvicka] [N. Musliu] [D. Walkiewicz] [F. Winter]	Exact methods for the Oven Scheduling Problem	Yes	[374]	2023	Constraints An. Int.	42	0	32	1371	1514

## Automatically Extracted Article Features

Table 6: Automatically Extracted ARTICLE Properties (Requires Local Copy)

Work	Pages	Concepts	Classification	Constraints	Prog Languages	CP Systems	Areas	Industries	Benchmarks	Algorithm	a	c
Laborie03 [369]	38	task, precedence, order, cmax, machine, job, activity, re-scheduling, setup-time, release-date, inventory, preempt, job-shop, resource, scheduling, make-span		cycle, table constraint, cumulative, disjunctive	C++, Ilog	Sched- ule			benchmark	edge- finding, not-last, energetic reasoning, not-first, time-tabling	1201	1731
LaborieRSV18 [372]	41	release-date, job-shop, resource, activity, precedence, sequence dependent setup, earliness, scheduling, machine, inventory, transportation, manpower, due-date, setup-time, batch process, order, tardiness, flow-shop, job, make-span, re-scheduling, task, distributed	peplib, parallel machine, RCPSP	alternative constraint, cumulative, disjunctive, span constraint, cycle, alwaysIn, endBeforeStart	C , Python, C++, Java	CHIP, Geodec, Ilog Solver, Cplex, Ilog Scheduler, OPL, Choco Solver, CPO	semiconductor railway, container terminal, satellite, robot, pipeline, aircraft, shipping	chemical industry, petro-chemical industry	real-world, CSPlib, benchmark	edge- finding	1080	1610
LacknerMMWW23 [374]	42	release-date, batch process, setup-time, job, order, due-date, tardiness, scheduling, make-span, machine, task, lateness, job-shop, earliness	parallel machine, OSP, single machine	alternative constraint, disjunctive, bin-packing, noOverlap, cumulative, endBeforeStart		Chuffed, Cplex, OPL, CPO, OR-Tools, MiniZinc, Gurobi	oven conductor scheduling	electronics industry, steel industry, manufacturing industry	random instance, industrial partner, benchmark, instance generator, zenodo, real-life real-life	time-tableting	984	1514
LammaMM97 [377]	15	Job-shop, resource, scheduling, precedence, order, task, job, distributed, no-wait		circuit, disjunction	C++, Prolog	ECLIPSe, OPL, CHIP	railway				1230	1760
LetortCB15 [385]	52	machine, make-span, job, precedence, resource, scheduling, task, order	psplib	cumulative, cycle, bin-packing	Java, Prolog	Choco Solver, CPLEX, SICSSolver			generated instance, Roadef, benchmark, random instance	energetic reasoning, sweep, edge-finding	1110	1640
LiW08 [386]	18	precedence, activity, resource, completion-time, setup-time, make-span, scheduling, machine, preempt, job-shop, no preempt, job, re-scheduling, open-shop, due-date, task, order	RCPSP	disjunctive, cycle, bin-packing		OZ, ECLIPSe, OPL, CHIP		real-world			1178	1708
LiessM08 [388]	12	precedence, resource, scheduling, machine, job, activity, precedence, job-shop, task, make-span, order, cmax	RCPSp, pepib	disjunctive, cu- mulative	C++	OZ			benchmark	edge-finding	1179	1709
LimtanyakulS12 [393]	32	release-date, scheduling, order, completion-time, job, resource, activity, tardiness, machine, due-date, precedence		table constraint, disjunctive, bin-packing, cumulative	OZ, Ilog Scheduler, Cplex	robot, automotive	automotive industry	random instance, real-life, generated instances, industrial partner, benchmark	not-last, energetic reasoning, not-first, edge-finding		1133	1603
LombardiM10a [402]	30	due-date, distributed, order, job, make-span, release-date, re-scheduling, task, completion-time, resource, activity, precedence, preempt, scheduling, machine	TCSP	cyclo, constraint, span constraint, cumulative, disjunctive, table constraint	C	Cplex		real-world, benchmark, real-life	sweep		1160	1690

## Manually Extracted Article Features

Table 4: Manually Defined PAPER Properties

Key	Title (Local Copy)	CP System	Bench	Links	Data Avail	Sol Avail	Code Avail	Related To	Classification	Constraints	a	b
AaslanPG23	Optimization of Short-Term Underground Mine Planning Using Constraint Programming	CP Opt	real-world	1	n	n	n	-	?	1	325	
AaslanPG23 [1]	Enhancing Hybrid CP-SAT Search for Disjunctive Scheduling	ARIES	real-world, github, OR-Tools	1	y	y	-	JSSP OSSP	-	2	371	
Bit-Monnot23	Predicting the Optimal Period for Cyclic Hoist Scheduling Problems	Mistral OR-Tools	benchmark, random instance, generated instance, real-life industrial instance	3	n	n	-	CHSP	-	3	415	
EftymiouY23	An Efficient Constraint Programming Approach to Preemptive Job Shop Scheduling	CP Opt	supplementary material, github, benchmark	6	ref	y	PJSSP	endBeforeStart span noOverlap	4	476		
JuvinHHL23	Constraint Programming for the Robust Two-Machine Flow-Shop Scheduling Problem with Budgeted Uncertainty	CP Opt Cplex	real-world	0	ref	n	-	Perm FSSP	endBeforeStart noOverlap sameSequence cumulative	5	477	
KameugneFND23	Horizontally Elastic Edge Finder Rule for Cumulative Constraint Based on Slack and Density	?	benchmark	5	BL PSPLib	n	-	RCPSPs	6	480		
KimCMILLP23	Iterated Greedy Constraint Programming for Scheduling Steelmaking Continuous Casting	Gurobi OR-Tools	real-world, benchmark, zenodo	0	y	n	-	SCC	alternative noOverlap	7	485	
Mehdizadeh-Somarin23	A Constraint Programming Model for a Constrained Job Shop Scheduling Problem with Machine Availability	CP Opt	random instance	0	n	n	-	JSSP RMS	8	529		
Mehdizadeh-Somarin23 [430]	A Constraint Programming Model for Scheduling the Unloading of Trains in Ports	custom	real-world, generated instance	0	n	n	-	SUTP	9	553		
PerezGSL23	Partially Preemptive Multi Skill/Mode Resource-Constrained Project Scheduling with Generalized Precedence Relations and Calendars	CP Opt MiniZinc Chuffed	real-world, benchmark, industrial instance, real-life	4	y	y	PP-MS-MMRCPSp/maximal disjunctive	10	557			
SquillaciPR23	Scheduling Complex Observation Requests for a Constellation of Satellites: Large Neighborhood Search Approaches	Cplex Studio	github, benchmark	2	y	n	-	EOSP	11	584		
TardivoDFMP23	Constraint Propagation on GPU: A Case Study for the Cumulative Constraint	MiniCPP MiniZinc	bitbucket, github, benchmark, real-world	9	PSPLib BL Pack	y	-	RCPSp	cumulative	12	590	
TasselGS23	An End-to-End Reinforcement Learning Approach for Job-Shop Scheduling Problems Based on Constraint Programming	custom Choco	industrial instance, real-world, supplementary material, github, benchmark	0	ref	y	-	JSSP	noOverlap	13	591	
WangB23	Dynamic All-Different and Maximal Cliques Constraints for Fixed Job Scheduling	FaCtLe	real-world, random instance	0	(y)	n	[628]	FJS	-	14	620	
WangB23 [629]	A competitive constraint programming approach for the group shop scheduling problem	CP Opt	github, benchmark	0	ref	n	-	GSSP	noOverlap endBeforeStart	15	633	
YuraszeczkMC23												
YuraszeczkMC23 [649]												

## Extracted Features: Application Areas

Table 16: Works for Concepts of Type ApplicationAreas

Type	Keyword	High	Medium	Low
ApplicationAreas	COVID	GuoZ23 [269]	GelbingerKMMW21 [234]	Patomi-AnarakiTFV23 [212], Mehdizadeh-Somarin23 [430], GunPA123 [210], JuvinHHL23a [331], OujanaYB22 [437], Lemos21 [351]
ApplicationAreas	HVAC	LimHTB16 [390], LimBTBB15 [391], GrimesIOS14 [260]		AkramNIRSA23 [13], BenderWS21 [84], HamPK21 [275], AstrandO21 [35], QinWLSLS21 [611], AstrandO21 [36], MejiaY20 [28]
ApplicationAreas	agriculture			
ApplicationAreas	aircraft	PohlAK22 [502], WangB20 [628], TranDRFWOWB16 [506], Ishiumi16 [205], BajestaniB13 [42], LombardiM12 [405], BajestaniB11 [41], FrankK05 [219], Arttouchine93 [34], Simons09 [558]	WangB23 [629], GombolayWS18 [253], Ham18 [273], Simons07 [559], SakkoutW03 [523], Simons05a [558]	PovedaA23 [509], PovedaA23 [509], Adelgren2023 [7], EttimaniesabaniCNMS22 [202], ElecOH22 [195], ZarandiASC20 [654], HauderBRPA20 [283], abs-1902-09244 [282], Hooker19 [312], LaborieRSV18 [372], HookerH17 [314], TranAB16 [594], LombardiL0 [389], Laborie09 [370], KovacsS08 [355], KrogLP1107 [608], MartinPY01 [327], SimonsCK00 [660], GrulianQ98 [264], Darby-DowlingLMZ07 [163], Wallace96 [625], Simons08 [557]
ApplicationAreas	automotive		GuoZ23 [269], YuraszeczkMPV22 [650], EmdeD22 [169], Groloca21 [261], LimtanayakulS12 [393], [SunLYL10] [567], Lombarddi10 [398], BarlaatCCG08 [52], SchildW00 [532]	PovedaA23 [509], NaderIR23 [460], CzernachowskaV22 [159], NaderIB22 [457], NaderIB22a [456], AntiorHHEN21 [22], HubnerCSV21 [318], AbreuAPM21 [166], KoehlerBFPHFSS21 [348], VilkHT21 [623], BarzegaranZP20 [601], GelbingerMM19 [236], abs-1911-04769 [235], BonfettiZLM16 [113], Siala5m [552], SchneiHT15 [533], [AlesioNBG14] [181], HarjunkoskiMBC14 [279], BenniBCM06 [88], KovacsV06 [369], Wallace96 [625]
ApplicationAreas	cable tree	KoehlerBFFHPSS21 [348]		
ApplicationAreas	car manufacturing	QinDCS20 [512], SacramentoSP20 [528]	AntuoriHHEN21 [22], LaborieHSV18 [372]	BeldiceanuC04 [78], abs-2312-13682 [497], PerezGSL23 [496], ToumtBT22 [592], CauwelaertDS20 [142], Wallace96 [627], ZarandiASC20 [654], FallahiAC20 [209], Hooker19 [312], CauwelaertDMS16 [140], Dejemeppe16 [172], DejemeppeCS15 [172], Novash12 [476], CorreaR02 [155], LimtanayakulS12 [393], Adelgren2023 [7], EttimaniesabaniCNMS22 [202], NaderIB22a [456], NaderIB22 [457], HeinzNV22 [295], ElecOH22 [195], Lemos21 [351], MokhtarzadehTNF20 [443], TranLWSK18 [574], HookerH17 [314], DoulaibRP16 [190], LipovetzkyBPS14 [304], HachenGIH11 [272], MilanoW09 [441], WuB309 [643], MilanoW06 [440], BeldiceanuC02 [79], JainG01 [323], SimonsCK00 [560]
ApplicationAreas	container terminal			
ApplicationAreas	crew-scheduling	ZarandiASC20 [654], PourDERB18 [505]	BourreauGGLT22 [118], Zahout21 [652], CombelayWS18 [253], Mason01 [429], Touralvane05 [503]	BeldiceanuC04 [78], abs-2312-13682 [497], PerezGSL23 [496], ToumtBT22 [592], CauwelaertDS20 [142], Wallace96 [627], ZarandiASC20 [654], FallahiAC20 [209], Hooker19 [312], CauwelaertDMS16 [140], Dejemeppe16 [172], DejemeppeCS15 [172], Novash12 [476], CorreaR02 [155], LimtanayakulS12 [393], Adelgren2023 [7], EttimaniesabaniCNMS22 [202], NaderIB22a [456], NaderIB22 [457], HeinzNV22 [295], ElecOH22 [195], Lemos21 [351], MokhtarzadehTNF20 [443], TranLWSK18 [574], HookerH17 [314], DoulaibRP16 [190], LipovetzkyBPS14 [304], HachenGIH11 [272], MilanoW09 [441], WuB309 [643], MilanoW06 [440], BeldiceanuC02 [79], JainG01 [323], LetortBC12 [383]
ApplicationAreas	dairies			
ApplicationAreas	dairy	EscobarPQPRA19 [201]	PrataAN23 [509], HarjunkoskiMBC14 [279]	Grolier22 [261], Zainou21 [552], GalleguillosSB19 [225], Madl-WambalaLOBM17 [418], Letort13 [582], IfrimOS12 [320], LetortBC12 [383]
ApplicationAreas	datacenter	HermenierDL11 [500]		
ApplicationAreas	datacentre		HurleyOS16 [319]	
ApplicationAreas	day-ahead market			
ApplicationAreas	deep space			
ApplicationAreas	drone	MontemannD23a [446], MontemannD23 [447], Ham18 [273]		HeberardALLCMR22 [852], Grolier22 [261], JuvinHHL23a [331], Adelgren2023 [7], ShahidK23 [547], LamteD23 [169], AstrandO21 [35], AstrandO21 [36], AntuoriHHEN21 [22], ZarandiASC20 [654], Ham18a [274]

## Prolific Authors

Table 8: Co-Authors of Articles/Papers

Author	Nr Works	Nr Cites	Entries
J. Christopher Beck	49	701	LuoB22 [416], ZhangBB22 [658], TangB20 [573], RoshanaiBAUB20 [521], TranPZLDB18 [597], TranVNB17 [599], TranVNB17a [600], CohenHB17 [154], BoothNB16 [113], KuiB16 [365], TranAB16 [594], TranWDRFOVB16 [601], LuoVLM16 [415], TranDRFWOB16 [596], BajestaniB15 [43], KoschB14 [839], TerekhovTDB14 [831], LouieVN14 [412], HeinzB13 [294], HeinzKB13 [291], BajestaniB13 [42], TranTDB13 [598], HeinzB12 [290], TerekhovDOB12 [580], ZandariB12 [595], KovacsB11 [356], BeckFW11 [66], HeckmanB11 [289], BajestaniB11 [41], WuLB09 [643], BidotVLB09 [94], CarchraeB09 [131], WatsonB08 [632], KovacsB08 [553], BeckW07 [73], Beck07 [64], KovacsB07 [354], Beck06 [63], CarchraeBF06 [132], WuBBo5 [642], BeckW05 [72], BeckW04 [71], Beckf03 [70], BeckPS03 [69], BeckF00 [68], Beck99 [62], BeckF98 [67].
Michela Milano	31	297	
Andreas Schutt	27	322	YangSS19 [141], KreterSSZ18 [86], CifuentesS18 [251], MusinSS18 [455], KreterS17 [363], YoungSS17 [250], SchuttS16 [543], SchuttiW16 [544], SchuttiW15 [545], SchuttiW14 [546], SchuttiW13 [547], SchuttiW12 [548], SchuttiW11 [549], SchuttiW10 [544], abs-1009-0347 [539], SchuttiSW10 [538], SchuttiWS10 [545].
Michele Lombardi	25	194	BorghesiBLMB18 [115], BonfettiZLM18 [113], BridiBLMB16 [120], BridiBLBM16 [121], LombardiBM15 [399], BartoliniBLBM14 [60], BonfettiBLM14 [111], BonfettiBLBM14 [109], BonfettiLM13 [110], LombardiM13 [406], LombardiMB13 [407], LombardiM12 [405], BonfettiBLBM12 [108], LombardiM12a [404], BonfettiM12 [112], BonfettiLBMB11 [107], LombardiLBMB11 [400], BeniniLMR11 [60], Milano11 [438], LombardiM10 [403], LombardiM10a [402], LombardiMRB10 [408], LombardiM09 [401], RuggieroBMA09 [525], MilanoW09 [441], BeniniLMR08 [89], BeniniBG06 [88].
Peter J. Stuckey	24	453	YangSS19 [644], DemirovićS18 [177], KreterSSZ18 [364], MuslimSS18 [455], KreterS17 [363], SchuttiS16 [543], BlomPS16 [100], KreterSS17 [363], BlomPS16 [100], KreterS16 [543], BlomPS15 [124], SchuttiFSW14 [542], BlomPS14 [542], LipovetzkyBPS14 [394], GuSSW14 [266], SchuttiS13 [536], GuSS13 [265], SchuttiFSW13 [541], SchuttiCSW12 [532], GuSW12 [267], SchuttiFSW11 [540], BandaSC11 [170], abs-1009-0347 [539], SchuttiFSW09 [538], OhrimenkoC09 [483].
John N. Hooker	19	1316	EliOH22 [195], HookerI17 [312], Hooker17 [311], HookerH17 [314], HochenigH16 [288], CireCH16 [150], HarjunkoskiMBC14 [270], CireCH13 [149], CobanH11 [153], CobanH10 [152], Hooker10 [310], Hooker09 [309], Hooker08 [308], Hooker07 [307], Hooker06 [306], Hooker05 [305], Hooker03 [313], HookerY02 [315], Hooker02 [304].
Emmanuel Hebrard	17	71	JuvinHH123 [328], HebrardALLCMR22 [285], AntuoriHHEN21 [22], ArtiguesHQ721 [32], GodetLHS20 [247], AntuoriHHEN20 [21], Hebrard-HJMPV16 [286], SimoninAHL15 [555], SinalAH15 [563], GrimesH15 [581], BessiereHMQW14 [63], SimoninAHL12 [554], BilautHL12 [65].
Pierre Lopez	17	90	JuvinHH123 [328], JuvinHH123 [331], JuvinHL23 [330], HebrardALLCMR22 [285], JuvinHL22 [329], Polo-MejiaALB20 [503], NattaHHKA19 [466], NattaALH17 [463], NattaALR16 [464], SimoninAHL15 [555], NattaAL15 [462], SimoninAHL12 [564], BillautHL12 [65], LahimerHL11 [375], TrojetHL11 [662], LopezAKYG00 [410], TorresL00 [591].
Christian Artigues	16	203	PovedaA23 [152], PohLA22 [502], HebrardALLCMR22 [285], ArtiguesHQ721 [32], Polo-MejiaALB20 [503], NattaHHKA19 [466], NattaALH17 [463], NattaALR16 [464], SimoninAHL15 [555], NattaAL15 [462], SinalAH15 [563], SimoninAHL12 [554], NeronABCDD06 [481].
Pierre Schaus	15	79	CauwelaertDS20 [112], ThomasKS20 [656], HoumtJSW19 [316], CappartTSR18 [130], CauwelaertLS18 [141], CappartS17 [129], CauwelaertDMS16 [120], DujougenotCS15 [173], SchauM18 [530].
Helmut Simonis	15	154	ArmstrongCO22 [271], ArmstrongGOS21 [26], AntunesABD20 [20], AntunesABD18 [19], HurleyOS16 [310], GrimesOS14 [260], IfrimOS12 [320], SimonisH11 [662], SimonisH10 [559], SimonisK09 [560], Simonis99 [558], Simonis95 [561], Simonis95 [557], Simonis95a [556], DinebachSH90 [184].
Nicolas Beldiceanu	13	274	Madz-WamilaLOB17 [418], Madz-WamilaHB [617], LetortCB15 [385], LetortCB13 [384], LetortCB12 [383], ClercqPB34 [151], BeldeceanuCDP11 [80], BeldeceanuCP08 [81], PoderB08 [500], BeldeceanuCP07 [82], PoderBS04 [501], BeldeceanuCP02 [79], AggounB93 [9].
Luca Benini	13	146	BorghesiBLMB18 [115], BridiBLMB16 [120], BridiBLMB16 [121], BonfettiBLMB16 [109], LombardiMB13 [407], BonfettiBLMB12 [108], BonfettiBLMB11 [107], LombardiLBMB11 [400], BeniniLMR11 [60], LombardiMRB10 [408], RuggieroBMA09 [525], BeniniLMR08 [89], BeniniBG06 [88].
Philippe Laborie	12	513	LunardiBLRV20 [413], LaborieRSV18 [372], Laborie18a [371], MelgarejoS15 [11], VilimS15 [621], Laborie09 [370], BidotVLB09 [94], BaptisteLPN06 [17], NeronABCDD06 [481], GodardLN05 [245], Laborie03 [369], FocaceLN00 [215].
Philippe Baptiste	11	403	BaptisteB18 [46], Baptiste09 [45], BaptisteLPN06 [47], NeronABCDD06 [481], ArtiouchnicheB05 [34], Baptiste02 [44], BaptistePN01 [50], BaptisteLP00 [49], PapazB98 [492], BaptisteP97 [48], PapeB97 [49].
Roman Barták	11	88	SvancaraB22 [569], JelmekB16 [325], BartakV15 [59], Bartak14 [55], BartakS11 [57], BartakCS10 [56], BartakSR10 [58], VilimBC05 [620], VilimBC04 [619], Bartak02 [54], Bartak02a [53].

### 36.3 Limitations

#### Limitations

- Limited coverage by OpenCitations
- Difficult to have local access to some publication types (book, incollection)
- Heavily biased towards publications in English
- More powerful NLP analysis of works possible?

#### Problem: Count for Most Cited Papers

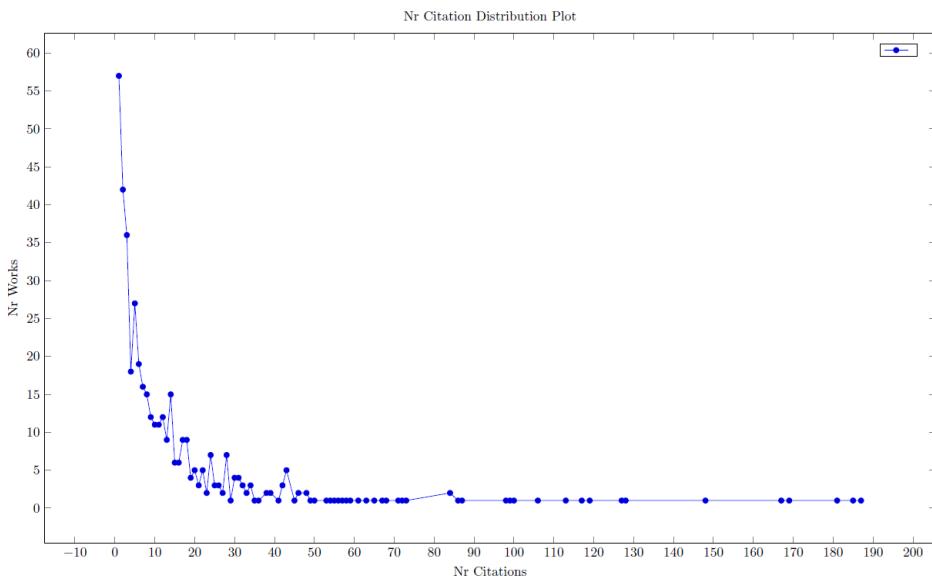
Table 9: Works from bibtex (Total 30)

Key	Authors	Title	LC	Cite	Year	Conference /Journal	Pages	Nr Cites	Nr Refs	b	c
JainM99 JainM99	A. Jain, S. Meeran	Deterministic job-shop scheduling: Past, present and future	Yes	[322]	1999	European Journal of Operational Research Computers Chemical Engineering	45	490	150	1352	1753
HarjunkoskiMBC14 HarjunkoskiMBC14	I. Harjunkoski, Christos T. Maravelias, P. Bongers, Pedro M. Castro, S. Engell, Ignacio E. Grossmann, John N. Hooker, C. Méndez, G. Sand, L. Wassek	Scope for industrial applications of production scheduling models and solution methods	Yes	[279]	2014	European Journal of Operational Research Computers Chemical Engineering	33	381	176	1335	1649
BlazewiczDP96 BlazewiczDP96	J. Blazewicz, W. Domschke, E. Pesch	The job shop scheduling problem: Conventional and new solution techniques	Yes	[125]	1996	European Journal of Operational Research Mathematical Programming Book	33	344	127	1278	1762
HookerO03 HookerO03	John N. Hooker, G. Ottosson	Logic-based Benders decomposition	Yes	[319]	2003	European Journal of Operational Research Mathematical Programming Book	28	317	0	1347	1729
BaptistePN01 BaptistePN01	P. Baptiste, Claude Le Pape, W. Nuijten	Constraint-Based Scheduling	No	[50]	2001	European Journal of Operational Research Mathematical Programming Book	null	296	0	No	n/a
JainG01 JainG01	V. Jain, Ignacio E. Grossmann	Algorithms for Hybrid MILP/CP Models for a Class of Optimization Problems	Yes	[233]	2001	INFORMS Journal on Computing Mathematical and Computer Modelling	19	279	23	1351	1738
AggounB93 AggounB93	A. Aggoun, N. Beldiceanu	Extending CHIP in order to solve complex scheduling and placement problems	Yes	[9]	1993	INFORMS Journal on Computing Mathematical and Computer Modelling	17	187	11	1247	1767
Hooker00 Hooker00	John N. Hooker	Logic-Based Methods for Optimization: Combining Optimization and Constraint Satisfaction	No	[304]	2000	Operations Research Planning and Scheduling by Logic-Based Benders Decomposition	null	185	0	No	n/a
Hooker07 Hooker07	John N. Hooker	Decomposition techniques for multistage scheduling problems using mixed-integer and constraint programming methods	Yes	[309]	2007	Operations Research Computers Chemical Engineering	29	181	19	1345	1715
HarjunkoskiG02 HarjunkoskiG02	I. Harjunkoski, Ignacio E. Grossmann	Introducing Global Constraints in CHIP	Yes	[278]	2002	Operations Research Computers Chemical Engineering	20	169	11	1334	1733
BeldiceanuC94 BeldiceanuC94	N. Beldiceanu, E. Contejean	IBM ILOG CP optimizer for scheduling - 20+ years of scheduling with constraints at IBM/ILOG	Yes	[372]	2018	Constraints An Int. J.	41	148	35	1370	1610
LaborieRSV18 LaborieRSV18	P. Laborie, J. Rogerie, P. Shaw, P. Vilim	Algorithms for propagating resource constraints in AI planning and scheduling: Existing approaches and new results	Yes	[369]	2003	Artificial Intelligence	38	128	10	1369	1731
OhrimenkoSC09 OhrimenkoSC09	O. Ohrimenko, Peter J. Stuckey, M. Codish	Propagation via lazy clause generation	Yes	[483]	2009	Constraints An Int. J.	35	127	15	1417	1702
Kuhi16 Kuhi16	W. Ku, J. Christopher Beck	Mixed Integer Programming models for job shop scheduling: A computational analysis	Yes	[365]	2016	Computers Operations Research	9	119	17	1367	1630
Rodriguez07 Rodriguez07	J. Rodriguez	A constraint programming model for real-time train scheduling at junctions	Yes	[520]	2007	Transportation Research Part B: Methodological	15	117	6	1430	1716
LiW08 LiW08	H. Li, K. WOMER	Scheduling projects with multi-skilled personnel by a hybrid MILP/CP-benders decomposition algorithm	Yes	[386]	2008	Journal of Scheduling	18	113	31	1374	1708
CorreaLR07 CorreaLR07	Ayoub Inna Corrêa, A. Langevin, L. Rousseau	Scheduling and routing of automated guided vehicles: A hybrid approach	Yes	[158]	2007	Computers Operations Research	20	106	20	1296	1714
MengZRZL20 MengZRZL20	L. Meng, C. Zhang, Y. Ren, B. Zhang, C. Lv	Mixed-Integer linear programming and constraint programming formulations for solving distributed flexible job shop scheduling problem	Yes	[355]	2020	Computers Industrial Engineering	13	100	62	1393	1574
BensanaLV99 BensanaLV99	E. Bensana, M. Lemaitre, G. Verfaillie	Earth Observation Satellite Management	Yes	[91]	1999	Constraints An Int. J.	7	99	0	1276	1752

## OpenCitation Count Compared to Google Scholar

Key	Type	Google	OC	Ratio
JainM99	article	1116	490	2.28
HarjunkoskiMBC14	article	588	381	1.54
BlazewiczDP96	article	796	344	2.31
BaptistePN01	book	1039	296	3.51
AggounB93	article	502	187	2.68
LaborieRSV18	article	309	148	2.09
BensanaLV99	article	251	99	2.54
DincbasSH90	article	271	86	3.15
Thorsteinsson01	paper	205	67	3.06
DincbasSH88	paper	287	0	∞

## Problem: Citation Count Distribution



## 37 Summary

### Summary

- Use the survey to find
  - Most important works on Constraint Based Scheduling
  - Specialized papers on the constraint reasoning for scheduling
  - Works in specific application domains or specific industries