

CSCI 3336 Organization of Programming Languages

DESCRIBING SYNTAX

Topics

- Introduction
- The General Problem of Describing Syntax
- Formal Methods of Describing Syntax
- Context-Free grammars

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Introduction

- **Syntax:** the form or structure of the expressions, statements, and program units
- **Semantics:** the meaning of the expressions, statements, and program units
- Syntax and semantics provide a language's definition
 - Example


```
while (<boolean_expr>) <statement>
```

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The General Problem of Describing Syntax

- A *sentence* is a string of characters over some alphabet
- A *language* is a set of sentences
- A *lexeme* is the lowest level syntactic unit of a language (e.g., `*`, `sum`, `begin`)
- A *token* is a category of lexemes (e.g., `identifier`)

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Example: Lexemes and tokens

- Consider the following Java statement:


```
index = 2 * count + 17;
```

Lexemes	Tokens
index	identifier
=	equal_sign
2	int_literal
*	mult_op
count	identifier
+	plus_op
17	int_literal
;	semicolon

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Formal Definition of Languages

- **Recognizers**
 - A recognition device reads input strings of the language and decides whether the input strings belong to the language
 - Example: syntax analysis part of a compiler
- **Generators**
 - A device that generates sentences of a language
 - One can determine if the syntax of a particular sentence is correct by comparing it to the structure of the generator

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Formal Methods of Describing Syntax

- Backus–Naur Form and Context-Free Grammars
 - Most widely known method for describing programming language syntax
- Extended BNF
 - Improves readability and writability of BNF

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BNF and Context-Free Grammars



Noam Chomsky

- Context-Free Grammars
 - Developed by Noam Chomsky in the mid-1950s
- $G=(V,T,P,S)$
 - » V and T are disjoint finite sets of *variables* and *terminals*
 - » P is a finite set of productions of the form $A \rightarrow \alpha$, where A is a variable and α is a string of symbols from $(V \cup T)^*$
 - » Finally, S is a special variable called the *start symbol*.
- Language generators
- Define a class of languages called context-free languages

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Backus–Naur Form (BNF)

- Backus–Naur Form (1959)
 - Invented by John Backus to describe Algol 58
 - BNF is equivalent to context-free grammars
 - BNF is a *metalanguage* used to describe another language
 - In BNF, abstractions are used to represent classes of syntactic structures—they act like syntactic variables (also called *nonterminal symbols*)



John Backus



Peter Naur

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Context-Free Grammar

- Context-free grammars are powerful enough to describe the syntax of most programming languages; in fact, the syntax of most programming languages is specified using context-free grammars.
- On the other hand, context-free grammars are simple enough to allow the construction of efficient parsing algorithms which, for a given string, determine whether and how it can be generated from the grammar.

Grammars

- Grammars express languages
- Example: The English language grammar
 - $\langle sentence \rangle \rightarrow \langle noun_phrase \rangle \langle predicate \rangle$
 - $\langle noun_phrase \rangle \rightarrow \langle article \rangle \langle noun \rangle$
 - $\langle predicate \rangle \rightarrow \langle verb \rangle$

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The English language grammar

$$\langle article \rangle \rightarrow a$$

$$\langle article \rangle \rightarrow the$$

$$\langle noun \rangle \rightarrow cat$$

$$\langle noun \rangle \rightarrow dog$$

$$\langle verb \rangle \rightarrow runs$$

$$\langle verb \rangle \rightarrow sleeps$$

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Derivation of string "the dog sleeps"

$$\begin{aligned}
 \langle \text{sentence} \rangle &\Rightarrow \langle \text{noun_phrase} \rangle \langle \text{predicate} \rangle \\
 &\Rightarrow \langle \text{noun_phrase} \rangle \langle \text{verb} \rangle \\
 &\Rightarrow \langle \text{article} \rangle \langle \text{noun} \rangle \langle \text{verb} \rangle \\
 &\Rightarrow \text{the} \langle \text{noun} \rangle \langle \text{verb} \rangle \\
 &\Rightarrow \text{the dog} \langle \text{verb} \rangle \\
 &\Rightarrow \text{the dog sleeps}
 \end{aligned}$$

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Derivation of string "a cat runs"

$$\begin{aligned}
 \langle \text{sentence} \rangle &\Rightarrow \langle \text{noun_phrase} \rangle \langle \text{predicate} \rangle \\
 &\Rightarrow \langle \text{noun_phrase} \rangle \langle \text{verb} \rangle \\
 &\Rightarrow \langle \text{article} \rangle \langle \text{noun} \rangle \langle \text{verb} \rangle \\
 &\Rightarrow \text{a} \langle \text{noun} \rangle \langle \text{verb} \rangle \\
 &\Rightarrow \text{a cat} \langle \text{verb} \rangle \\
 &\Rightarrow \text{a cat runs}
 \end{aligned}$$

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Grammar for the English Language

$G_L = (S, V, T, P)$, where
 $S = \langle \text{sentence} \rangle$
 $V = \{ \langle \text{sentence} \rangle, \langle \text{noun_phrase} \rangle, \langle \text{predicate} \rangle, \langle \text{article} \rangle, \langle \text{noun} \rangle, \langle \text{verb} \rangle \}$
 $T = \{ \text{a, the, cat, dog, runs, sleeps} \}$
 $P = \{$
 $\quad \langle \text{sentence} \rangle \rightarrow \langle \text{noun_phrase} \rangle \langle \text{predicate} \rangle$
 $\quad \langle \text{noun_phrase} \rangle \rightarrow \langle \text{article} \rangle \langle \text{noun} \rangle$
 $\quad \langle \text{predicate} \rangle \rightarrow \langle \text{verb} \rangle$
 $\quad \langle \text{article} \rangle \rightarrow \text{a} \mid \text{the}$
 $\quad \langle \text{noun} \rangle \rightarrow \text{cat} \mid \text{dog}$
 $\quad \langle \text{verb} \rangle \rightarrow \text{runs} \mid \text{sleeps} \}$

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Language of grammar G_L

$L = \{$
 $\quad \text{"a cat runs"},$
 $\quad \text{"a cat sleeps"},$
 $\quad \text{"the cat runs"},$
 $\quad \text{"the cat sleeps"},$
 $\quad \text{"a dog runs"},$
 $\quad \text{"a dog sleeps"},$
 $\quad \text{"the dog runs"},$
 $\quad \text{"the dog sleeps"} \}$

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A grammar example for a small language L1

$\langle \text{program} \rangle \rightarrow \text{begin} \langle \text{stmts} \rangle \text{end}$
 $\langle \text{stmts} \rangle \rightarrow \langle \text{stmt} \rangle \mid$
 $\quad \langle \text{stmt} \rangle ; \langle \text{stmts} \rangle$
 $\langle \text{stmt} \rangle \rightarrow \langle \text{var} \rangle = \langle \text{expr} \rangle$
 $\langle \text{var} \rangle \rightarrow A \mid B \mid C$
 $\langle \text{expr} \rangle \rightarrow \langle \text{var} \rangle + \langle \text{var} \rangle \mid$
 $\quad \langle \text{var} \rangle - \langle \text{var} \rangle \mid$
 $\quad \langle \text{var} \rangle$

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Derivation

- Every string of symbols in the derivation is a sentential form
- A sentence is a sentential form that has only terminal symbols
- A leftmost derivation is one in which the leftmost nonterminal in each sentential form is the one that is expanded

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An example of derivation

Given the following program:

```
begin
A = B + C
end
```

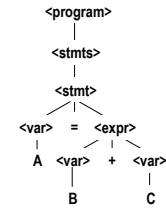
A derivation of the program in L1 follows:

```
<program> => begin <stmts> end
=> begin <stmt> end
=> begin <var> = <expr> end
=> begin A = <expr> end
=> begin A = <var> + <var> end
=> begin A = B + <var> end
=> begin A = B + C end
```

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Parse Tree

- A hierarchical representation of a derivation



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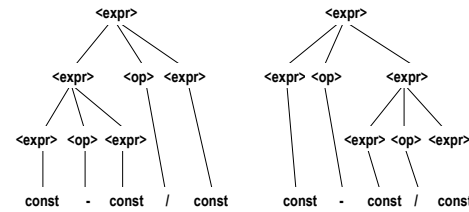
Ambiguity in Grammars

- A grammar is *ambiguous* if and only if it generates a sentential form that has two or more distinct parse trees

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An Ambiguous Expression Grammar

```
<expr> -> <expr> <op> <expr> | const
<op> -> / | -
```

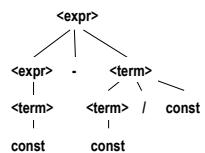


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An Unambiguous Expression Grammar (cont' d)

- If we use the parse tree to indicate precedence levels of the operators, we cannot have ambiguity

```
<expr> -> <expr> - <term> | <term>
<term> -> <term> / const | const
```

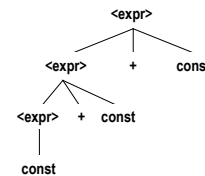


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Associativity of Operators

- Operator associativity can also be indicated by a grammar

```
<expr> -> <expr> + <expr> | const (ambiguous)
<expr> -> <expr> + const | const (unambiguous)
```



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Extended BNF

- Optional parts are placed in brackets []
`<proc_call> -> ident [(<expr_list>)]`
- Alternative parts of RHSs are placed inside parentheses and separated via vertical bars
`<term> -> <term> (+|-) const`
- Repetitions (0 or more) are placed inside braces { }
`<ident> -> letter {letter|digit}`

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BNF and EBNF

- BNF
`<expr> -> <expr> + <term>`
`| <expr> - <term>`
`| <term>`
`<term> -> <term> * <factor>`
`| <term> / <factor>`
`| <factor>`
- EBNF
`<expr> -> <term> { (+ | -) <term> }`
`<term> -> <factor> { (* | /) <factor> }`

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Summary

- BNF and context-free grammars are equivalent meta-languages
 - Well-suited for describing the syntax of programming languages
- An attribute grammar is a descriptive formalism that can describe both the syntax and the semantics of a language
- Three primary methods of semantics description
 - Operation, axiomatic, denotational

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