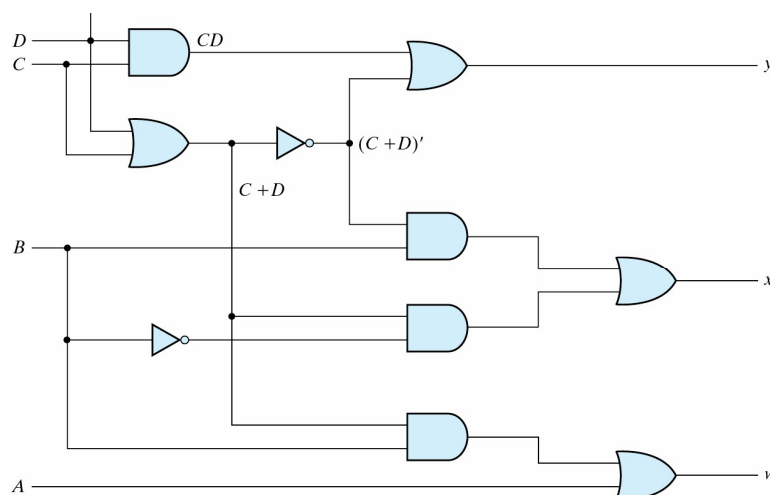


Department of Computer Science  
National Chiao Tung University  
**Digital System Design**

First Midterm Exam

11/1/2012

1. (10%) Convert decimal +47, +26 to binary using the *signed 2's complement* representation and enough bits to accommodate the numbers. Then perform the binary equivalent of  $(+26)+(-47)$ , and  $(-26)+(-47)$ . What is the minimum number of bits which is needed for correct results of these computations?
2. (10%) Represent the *unsigned* decimal numbers 53 and 69 in BCD, and then show the steps necessary to form their sum.
3. (6%) Find the *complement* of  $g(x,y,z) = w(x'+y'z)$ .
4. (10%) Show that  $(y+x)(y+z') = y+(xz')$  by using (i) truth table and (ii) algebraic manipulation (without using distributive laws).
5. (8%) Express the complement of function  $F(A,B,C,D) = A'(B'C+D') + B'CD$  in *product-of-maxterm* form.
6. (10%) Obtain the optimal *sum-of-product* (SOP) implementation of  $F(w,x,y,z) = \sum(3,4,6,10,12,14)$  with *don't care* conditions  $d(w,x,y,z) = \sum(1,8,9,13)$ .
7. (10%) Find all *prime implicants* for  $F(A,B,C,D) = \sum(0,2,4,5,7,8,10,13)$  and determine which are *essential*.
8. (18%) For the following circuit, obtain multiple-level NAND gate circuit for  $w$ , the optimal POS implementation of  $x$ , and the truth table of  $y$ .



9. (8%) Obtain the two-level NAND implementation of  $f(x,y,z) = y+(xy+z')(y'+z)$ .
10. (10%) Implement  $F = AB' + B'C + AC'D$  with OR and inverter gates.

$$1. (47)_{10} = (010111)_2 \rightarrow 101000 + 1 = 101001 (2's)$$

$$(26)_{10} = (001010)_2 \rightarrow 110101 + 1 = 110110 (2's)$$

①

$$\begin{array}{r} \text{sign} \quad 00011010 \\ +) (1111) + 1: 1(010001) \end{array}$$

2's complement

$$\begin{array}{r} 11101011 \rightarrow -1 \\ 11101010 \rightarrow \frac{1}{2} \times \frac{1}{2} \\ 00101010 \rightarrow \frac{1}{4} \times \frac{1}{4} \\ -(00010101) = -2 \frac{1}{4} \end{array}$$

②

$$\begin{array}{r} 11100110 \\ 11010001 \\ \hline 10110111 \end{array}$$

8 bits  $\rightarrow - ( \quad )$   
 $\rightarrow -73$

$$2. (53)_{10} = (01010011)_{BCD}$$

$$(69)_{10} = (01101001)_{BCD}$$

+)           

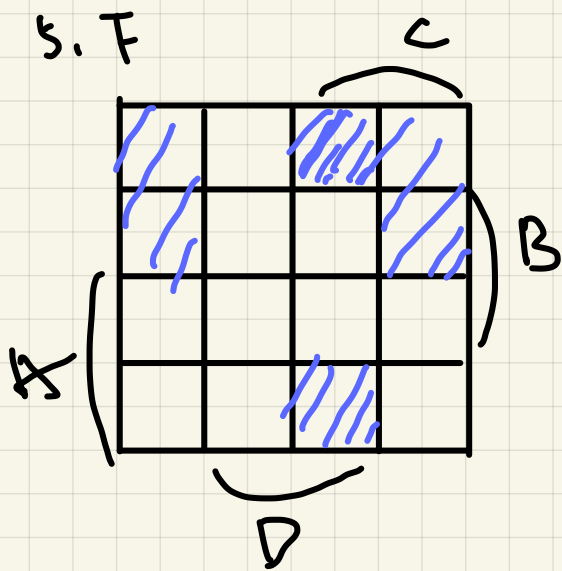
$$\begin{array}{r} 10111100 \\ +) 01100110 \\ \hline 10010010 \end{array}$$

1 2 2 #

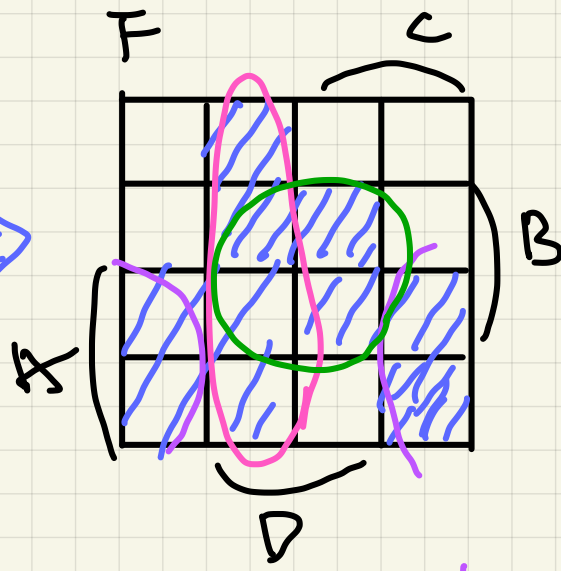
$$3. w' + (x(y+z'))$$

$$4(i) \quad x \quad y \quad z \quad (y+x) \quad (y+z') \quad (y+x)(y+z') \quad y+(xz')$$

$$(ii) \quad (y+x)(y+z')$$

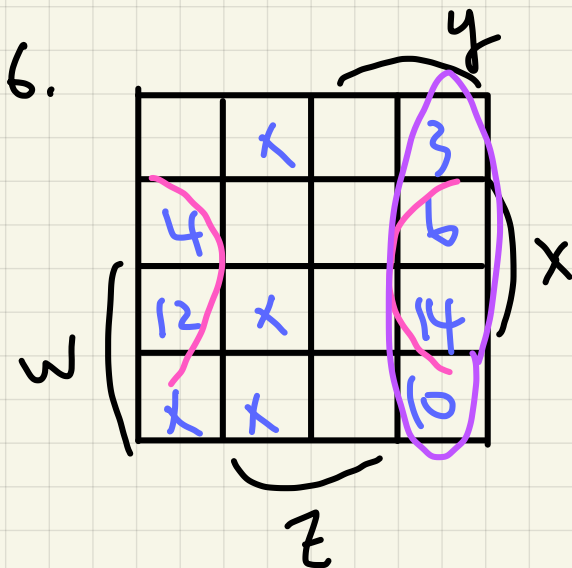


$\Rightarrow$

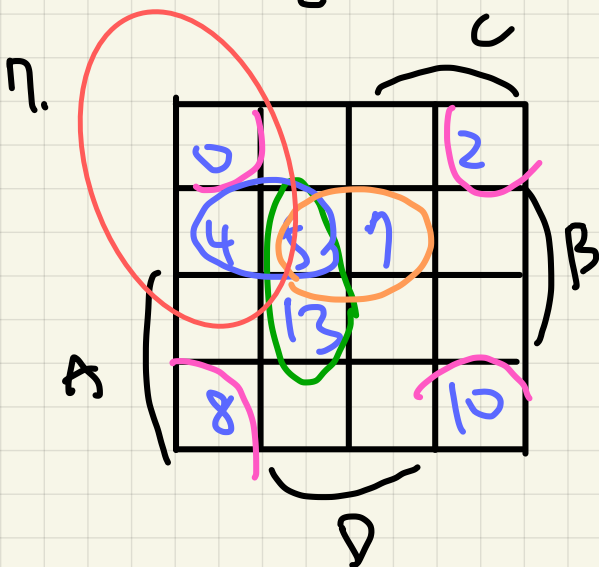


$$F' = C'D + AD' + BD$$

$$F = (C+D')(A+D)(B'+D')$$



$$F = XZ' + YZ'$$



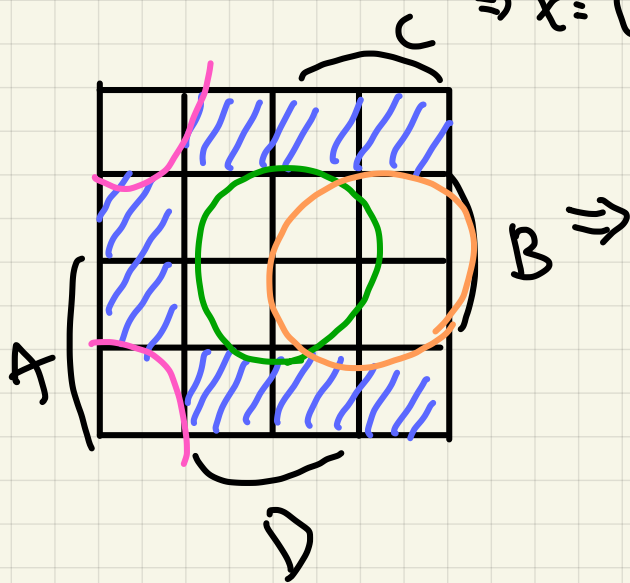
$$F = \underline{B'D'} + \underline{BC'D} + \underline{A'BC'} + \underline{A'BD}$$

essential

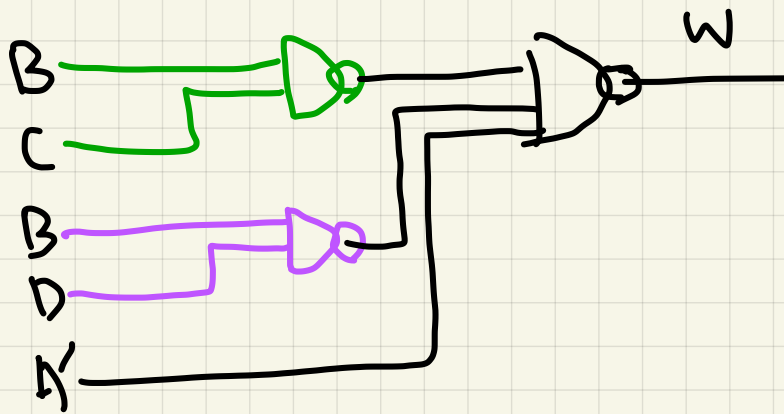
8.  $y$ : trivial

$$x = BC'D' + (C+D)B' \Rightarrow x' = B'C'D' + BD + BC$$

$$\Rightarrow x = (B+C+D)(B'+D')(B'+C')$$

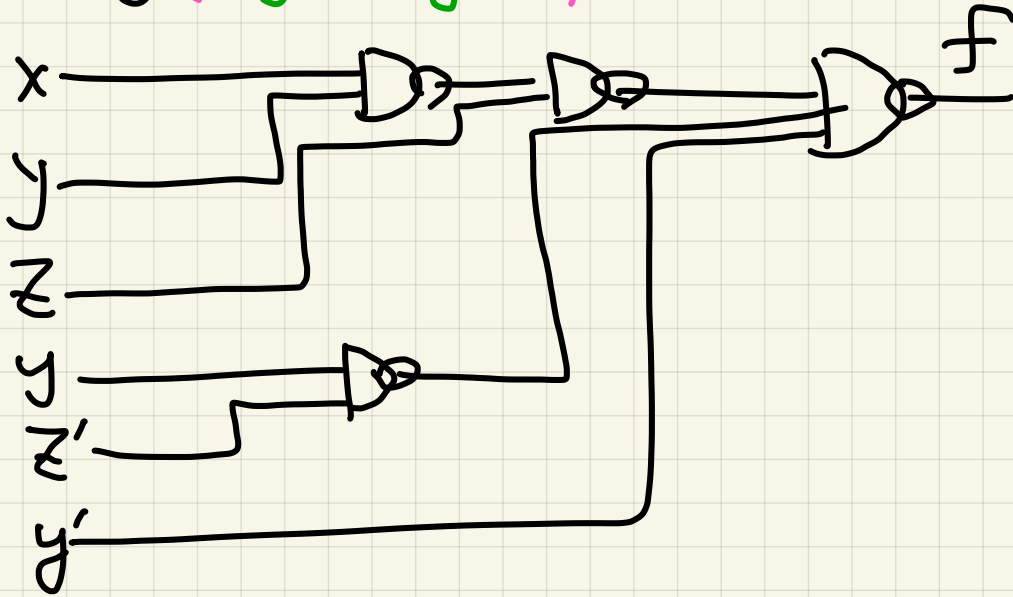


$$\begin{aligned} w &= A + B(C+D) \\ &= (A'(BC+BD))' \\ &= (A'(BC)'(BD)')' \end{aligned}$$



$$9. f = (y'((xy+z')(y'+z'))')'$$

$$= (y'(((xy)'z')(yz')'))'$$



$$10. F = (A'+B') + (B+C')' + (A'+C+D')'$$