1.

$$\int_{b}^{c} a(x-b)(x-c)dx = -\frac{a}{6}(c-b)^{3}$$