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$$\frac{2}{ab}\frac{d^3}{d\theta^3}S_{true} = -2ab\left(1+m^2\right)\left(\frac{2\sin\theta\cos\theta}{L} - \frac{2abm\sin^3\theta}{L^2}\right) + \frac{dm}{d\theta}\left(-\frac{4abm\sin^2\theta}{L} + \cos\theta\right) - m\sin\theta - \cos\theta$$