ML & Prolog

h_sakurai

MLとPrologの話をします

- Prolog入門
- Prolog でML
- MLTProlog

Shebang,演算子,lookup等

```
#!/usr/bin/env swipl --toplevel=halt --stand_alone=true -q
:- style_check(-singleton).
:- set_prolog_flag(double_quotes,codes).
:- initialization(main).
:- op(1200, xfx, [--]).
:- op(910, xfx, [ \vdash ]).
:- op(900, xfx, [ \downarrow, : ]).
:- op(892, xfy, [ then, else ]).
:- op(891, xfy, [ in ]).
:- op(890, fx, [ letrec, let, if ]).
:- op(888, xfy, ::).
= op(500, yfx, \$)
:- set_prolog_flag(report_error,true).
:- set_prolog_flag(unknown,error).
bool(true). bool(false).
lookup((\Gamma, X : V), X : V).
lookup((\Gamma, X1:V1), X : V) :- X1\==X, lookup(\Gamma, X : V).
term_expansion(A --- B, B :- A).
```

評価規則

```
% int, bool, if
integer(I),!
                           ----- (E-Int)
C ⊢ I ↓ I.
bool(B),!
                _____ (E-Bool)
C ⊢ B ↓ B.
C \vdash E1 \Downarrow true, C \vdash E2 \Downarrow V
--\%
C \vdash if E1 then E2 else E3 <math>\Downarrow V.
C ⊢ E1 ↓ false, C ⊢ E3 ↓ V (E-IfFalse)
C ⊢ if E1 then E2 else E3 ↓ V.
% 二項演算子
C \vdash E1 + E2 \downarrow V.
C ⊢ E1 ↓ V1, C ⊢ E2 ↓ V2, V is V1 − V2,!
C \vdash E1 - E2 \downarrow V.
C \vdash E1 \Downarrow V1, C \vdash E2 \Downarrow V2,
C \vdash E1 \Downarrow VI, C \vdash E2 \Downarrow V2,

(V1 \lt V2, V = true; V = false),!
C \vdash E1 < E2 \lor V.
```

評価規則

```
% 組み込み関数
C \vdash E \downarrow V
string_codes(S, V),!,write(S),!
                                                     (E-AppPrintString)
C ⊢ (print_string $ E) ↓ V.
C \vdash E \downarrow V, number_string(I, V),!
                                                   - (E-AppIntOfString)
C \vdash (int\_of\_string \$ E) \Downarrow I.
C \vdash E \downarrow V
string_codes(S, V),!,write(S),nl,!
                                                     (E-AppPrintlnString)
C ⊢ (println_string $ E) ↓ V.
C \vdash E \Downarrow V, write(V), nl,!
                                                     (E-AppPrintlnInt)
C ⊢ (println_int $ E) ↓ V.
C \vdash E \lor V, write(V), nl,!
                                                     (E-AppPrintlnBool)
C ⊢ (println_bool $ E) ↓ V.
% 関数とLet Rec
C \vdash E1 \Downarrow (C2 \vdash X \longrightarrow E0), C \vdash E2 \Downarrow V2,
(C2,X:V2) \vdash E0 \downarrow V
                                                     (E-App)
C \vdash (E1 + E2) \downarrow V.
(C,X:V1) \vdash E1 \Downarrow V1,(C,X:V1) \vdash E2 \Downarrow V2
C \vdash (letrec X = E1 in E2) \downarrow V2.
```

```
% リストとパターンマッチ
C \vdash E1 \Downarrow V, C \vdash E2 \Downarrow V2
                                                             - (E-Cons)
C \vdash (E1::E2) \downarrow [V \mid V2].
C \vdash E1 \Downarrow V, C \vdash E2 \Downarrow V2
                                                            -- (E-Cons2)
C \vdash [E1|E2] \downarrow [V|V2].
                                                          --- (E-Nil)
C ⊢ [] ↓ [].
C \vdash E1 \downarrow [], C \vdash E2 \downarrow V
                                                            — (E—MatchNil)
C \vdash match(E1 \mid [] \rightarrow E2 \mid \_) \downarrow V.
C \vdash E1 \downarrow [V1|V2],
((C,X : V1),Y : V2) \vdash E3 \downarrow V
                                                       ---- (E-MatchCons)
C \vdash match(E1 \mid \_ \mid X::Y->E3) \downarrow V.
```

型推論

```
% int,bool,if,二項演算子
integer(I)
                             _____ (T-Int)
\Gamma \stackrel{\circ}{\vdash} I : int.
bool(B)
                            _____ (T-Bool)
\Gamma \vdash B : bool.
\Gamma \vdash E1 : bool, \Gamma \vdash E2 : T, \Gamma \vdash E3 : T
\Gamma \vdash (if E1 then E2 else E3) : T.
\Gamma \vdash E1 : int, \Gamma \vdash E2 : int
                                         _____ (T-Plus)
\Gamma \vdash E1 + E2 : int.
\Gamma \vdash E1 : int, \Gamma \vdash E2 : int
                                      _____(T-Minus)
\Gamma \vdash E1 - E2 : int.
\Gamma \vdash E1 : int, \Gamma \vdash E2 : int
\Gamma \vdash (E1 < E2) : bool.
atom(X), lookup(\Gamma, X : T)
Γ ⊢ X : T.
(\Gamma, X:T) \vdash E : T2
\Gamma \vdash (X \rightarrow E) : (T \rightarrow T2).
\Gamma \vdash E1 : (T2 \rightarrow T), \Gamma \vdash E2 : T2
```

```
Γ ⊢ E1 $ E2 : T.
\Gamma \vdash E1 : T1, (\Gamma, X:T1) \vdash E2 : T2
\Gamma \vdash (\text{let } X = \text{E1 in E2}) : \text{T2.}
% Listとパターンマッチ
\Gamma \vdash E1 : T, \Gamma \vdash E2 : list(T)
                                                   ---- (T-List)
\Gamma \vdash (E1::E2) : list(T).
\Gamma \vdash E1 : T, \Gamma \vdash E2 : list(T)
                                             ----- (T-List2)
\Gamma \vdash [E1|E2] : list(T).
                                     ____ (T-Nil)
\Gamma \vdash [] : list(\_).
\Gamma \vdash E1 : list(T1), \Gamma \vdash E2 : T
((\Gamma,X : T1), Y : \text{list}(T1)) \vdash \text{E}3 : T
                                                    ____ (T_MatchCons)
\Gamma \vdash \mathsf{match}(\mathsf{E1} \mid [] \rightarrow \mathsf{E2} \mid \mathsf{X} :: \mathsf{Y} \rightarrow \mathsf{E3}) : \mathsf{T}.
(\Gamma, X:T1) \vdash E1 : T1, (\Gamma, X:T1) \vdash E2 : T2
\Gamma \vdash (letrec X = E1 in E2) : T2.
Γ⊢ E1 : "type error"
```

初期環境設定とMainプログラム

```
% 初期環境設定
add_{env}(V,E,E2) :- E2 = (E,V).
  add_env(print_string:(list(int)->list(int))),
  add_env(println_string:(list(int)->list(int))),
add_env(println_int:(int->int)),
add_env(println_bool:(bool->bool)),
  add_env(int_of_string:(list(int)->int)).
% メインプログラム
main :-
  current_prolog_flag(argv, ARGV),
  [File|_T=ARGV,
  close(In)), control catch(term_string(E,S),error(Err,string(ErrS,ErrPos)),(write(Err),write(':'),write(ErrS),halt)),
  maplist(string_codes, ARGV, ARGV2),
  env([],Env),
(Env,(argv:list(list(int)))) ⊢ E : T,
    T="type error", write('type error\n');
([],(argv:ARGV2)) ⊢ E ↓ _;
    write('runtime error\n')
  halt.
```

Prolog in ML syntax.ml

```
type v = string * int
type t =
                           アトム 例) a abc hoge
   Atom of string
  | Number of float
                                       123
                             数值
                                       "abc"
  | Str of string
                             文字列
  | Pred of string * t list 述語
                                       abc(1,2) add(int(1),var("a"))
  | Var of v
                             変数
                                       A B abc(A,B)
let rec show = function
   Atom(n)
   Number(v) -> string_of_float v
    Str(v)
                     -> V
   Pred(".", _) as t -> Printf.sprintf "[%s]" (show_list t)
   Pred(n, xs) -> Printf.sprintf "%s(%s)" n (String.concat ", " (List.map show xs))
Var(n, l) -> Printf.sprintf "%s_%d" n l
and show_list = function
   Pred(".", [t; Atom("[]")]) -> show t
   Pred(".", [t;(Pred(".", _) as u)]) -> show t ^ show_list u
   Pred(".", [t;u])
                                       -> show t ^ "|" ^ show u
                                       -> show t
```

Prolog in OCamle parser.mly

```
%{
                                                                          term DOT
                                                           query:
open Syntax
                                                                          sentence
                                                           seq:
let rec list args tail =
                                                                          term DOT
                                                           sentence:
 match args with
   [] -> tail
   x::xs -> Pred(".", [x; list xs tail])
%}
%token <string> ATOM
                                                           term:
%token <float> NUMBER
                                                                          term1
%token <string> STR
                                                           term1:
                                                                          exp1 term1
%token <string> VAR
%token <string> OP
                                                                          exp1
%token LPAREN RPAREN LBRACKET RBRACKET
                                                           exp1:
%token DOT OR SEMI COMMA LINE IIF
                                                                          exp
%token EOF
                                                           exp:
                                                                          MOTA
%right IIF
                                                                          VAR
%right COMMA
                                                                          NUMBER
%right OP
                                                                          STR
%start seq
%type <Syntax.t list> seq
                                                           exps:
                                                                          exp
%start query
                                                           listbody:
%type <Syntax.t> query
                                                                          exps
                                                          var_or_list:
```

```
{ $1 }
                            [$1] }
                             $1::$2 }
sentence seq
                             Pred(":-", [$1; Atom "nop"]) }
                             Pred(":-", [$2]) }
IIF term DOT
                             Pred(":-", [$2; Atom "nop"]) }
LINE term DOT
                             Pred(":-", [$3; $1]) }
term LINE term DOT
                             Pred(":-", [$1; $3]) }
term IIF term DOT
                             Pred(";", [$1; $3]) }
term1 SEMI term
                             $1 }
                             Pred(",", [$1; $3]) }
exp1 COMMA term1
                             Pred(",", [$1; $2]) }
                             $1 }
                             Pred($2, [$1; $3]) }
exp OP exp1
                             $1 }
                             Pred($1, $3) }
ATOM LPAREN exps RPAREN
                             Atom $1 }
                             Var($1, 0) }
                             Number $1 }
                             Str $1 }
                           { $2 }
LBRACKET listbody RBRACKET
                             $2 }
LPAREN term RPAREN
                             [$1] }
exp COMMA exps
                             $1::$3 }
                             list $1 (Atom "[]") }
exps OR var_or_list
                             list $1 $3 }
                            Var($1, 0) }
LBRACKET listbody RBRACKET { $2 }
```

Prolog in OCaml lexer.ml

```
rule token = parse
    [' ' '\t']
                          { token lexbuf }
    ln2 ln2+ '.'? ln2*
                           DOT }
                           token lexbuf }
    ln
    ";"
                           SEMI }
                          { COMMA }
    "("
                           LPAREN }
    ")"
                          { RPAREN }
    n [n
                           LBRACKET }
    "]"
                           RBRACKET }
    "." ln2*
                           DOT }
    min.
                           ATOM("!") }
    ":-"
                           IIF }
    '-' '-'+ com?
                          { LINE }
                           OP s }
           as s
    op
         as s
                          \{ ATOM s \}
    atom
                           VAR s }
           as s
    var
                          { NUMBER (float_of_string s) }
    number as s
    '''' (str <mark>as</mark> s) ''''
                          { STR (Scanf.unescaped s) }
    "'" (satom as s) "'"
                          { ATOM (Scanf.unescaped s) }
                           EOF }
    eof
    "%" nonendl
                           token lexbuf }
                          { token lexbuf }
```

```
let rec unify e t t2 =
  let rec unify r(t, t2) = match r with
     None -> None
     Some e ->
      let rec bind t v t2 =
       try match List.assoc v e with
         Var v as t3 -> if t == t3 then None else bind t v t2
                    -> if t2== t3 then r else mgu (t3, t2)
       with _ -> Some((v, t2) :: e)
     and mgu (t, t2) = match (t, t2) with
                t, Var v2 \rightarrow bind t2 v2 t
             Var v, t2 \rightarrow bind t v t2
         Pred(x, g), Pred(x2, g2) \rightarrow if x <> x2 then None else
                                    (try List.fold_left unify r (List.combine g g2)
                                    with _ -> None)
                             t2 -> if t = t2 then r else None
      in mgu (t, t2)
  in unify (Some e) (t, t2)
type g = t list (* goals *)
type d = t array (* database *)
type i = int
                        (* index *)
type s = (g * e * i * i) list (* stack *)
type m = g * d * i * s (* gdis machine *)
type ('a, 'b) res = Fail of 'a | Succ of 'b
```

```
type ('a, 'b) res = Fail of 'a | Succ of 'b
let trace = ref false
let e s = match s with
   [] -> []
   (_, e, _, _)::_ -> e
let el1 s = match s with
   [] \rightarrow [],1
   (_, e, l, _)::_ -> e,l+1
let pop m = match m with
     _, d, _, (g, _,_, i)::s -> Succ (g, d, i, s)
                         [] -> Fail d
let uni m s t t2 =
 match unify (e s) t t2, m with
   Some e, (_::g, d, _, (sg, _,l, i)::s) -> Succ (g, d, -1, (sg, e, l, i) :: s)
                                    m -> pop m
        _,
let rec eval e = function
   Number i -> i
   Pred("+", [x;y]) -> (eval e x) +. (eval e y)
   Pred("*", [x;y]) -> (eval e x) *. (eval e y)
   Pred("-", [x;y]) -> (eval e x) -. (eval e y)
   Pred("/", [x;y]) -> (eval e x) /. (eval e y)
   t -> failwith ("unknown term " ^ Syntax.show t)
let write1 e t = Printf.printf "%s%!" (Syntax.show (deref e t))
```

```
let rec assert1 d = function
   Pred(":-", [t]) -> process d t
                    -> Array.append d [| t |]
and consult1 d t =
  let filename = Syntax.show t in
  if !trace then Printf.printf "Loading %s\n" filename;
  let inp = open_in filename in
  let seq = Parser.seq Lexer.token (Lexing.from_channel inp) in
  List.fold_left assert1 d seq
and step = function
    Fail d -> Fail d
    Succ (g,d,i,s as m) ->
   if !trace then Printf.printf "i=%d g=[%s],e=[%s],s=%d\n"
     i (String.concat "; " (List.map Syntax.show g)) (show (e s)) (List.length s);
    match m with
                            [], d, i, s -> Succ m
                           g, d, -2, s -> Fail d
      Atom "halt"
                          ::g, d, -1, s -> exit 0
                          ::g, d, -1, s -> step (Succ(g,d,-1,s))
      Atom "nop"
      Atom "!"
                          ::g, d, -1, (g2,e,l,_)::s -> step (Succ(g, d, -1, (g2, e,l, -2)::s))
      Pred(",", [u;v]) ::g, d, -1, s -> step (Succ(u::v::g, d, -1, s))

Pred(";", [u;v]) ::g, d, -1, s -> let e,l1=el1 s in step (Succ( u::g, d, -1, (v::g, e,l1, -1)::s))
      Pred("=", [u;v]) ::g, d, -1, s -> step (uni m s u v)
      Pred("is", [u;v]) ::g, d, -1, s -> step (uni m s u (Number(eval (e s) (deref (e s) v))))
      Pred("assert", [t])::g, d, -1, s -> step (Succ(g, assert1 d (deref (e s) t), i, s))
      Pred("write", [t])::g, d, -1, s \rightarrow write1 (e s) t; step (Succ(g,d,-1,s))
      Pred("consult", [t]): g, d, -1, s -> step (Succ(g, consult1 d (deref (e s) t), i, s))
                             g, d, -1, s \rightarrow step (Succ(g, d, 0, s))
```

```
t::g, d, i, s ->
     if i >= Array.length d then step (pop m) else
     match d.(i) with
      Pred(":-", [t2; t3]) ->
       let e, l1 = el1 s in
       let rec gen_t = function
           Pred(n, ts) -> Pred(n, List.map (fun a -> gen_t a) ts)
           Var(n, _) -> Var(n, l1)
           t -> t
       begin match unify e t (gen_t t2) with
        Some e \rightarrow step (Succ(gen_t t3::g, d, -1, (t::g, e, l1, i+1) :: s))
       t -> Printf.printf "Database is broken. %s\n" (Syntax.show t); Fail d
and solve m =
 step (match m with
     [], _, _, _ -> pop m
                -> Succ m
and process d t =
 let rec prove m = match solve m with
     Fail d -> Printf.printf "No.\n"; d
     Succ (g, d, i, s as m) ->
     Printf.printf "%s\n" (show (e s));
     if s = [] \mid | i = -2 \text{ then (Printf.printf "Yes.\n"; d) else (}
       Printf.printf "More y/n";
       if "y" = read_line () then prove m else d
 in prove ([t], d, -1, [[],[],1,-2])
```

Prolog in OCaml main.ml

```
open Syntax
open Prolog
let welcome = "Beautiful Japanese Prolog Interpreter"
let parse str =
 Parser.query Lexer.token (Lexing.from_string str)
let help () =
 List.iter(fun (k,v) -> Printf.printf "%s\t%s\n%!" k v)
  ["q","quit"; "l","list"; "h","help";]
let rec repl d =
    Printf.printf("? %!");
   match read_line () with
     "q" -> ()
     "i" -> Array.iter (fun t ->
              Printf.printf "%s.\n%!" (Syntax.show t)
              ) d;
              repl d
      "h" -> help (); repl d
     "t" -> trace := not !trace;
              Printf.printf "Tracing %s.\n%!"
               (if !trace then "on" else "off");
              repl d
     line -> try repl (process d (parse line))
             with Parsing.Parse_error ->
                Printf.printf "Syntax error\n%!";
                repl d
```

```
#!/usr/bin/env swipl --toplevel=halt --stand_alone=true -q
:- initialization(main).
:- style_check(-singleton).
% prolog
pop((_, D, _, [(G, I)|S]), succ(G, D, I, S)).
pop((_, D, _,
                 []), fail(D)).
uni(M,T,T,M2) :- M=([\_|G], D, \_, S), M2=succ(G, D, D, S).
uni(M,_,_,M2) :- pop(M, M2).
assert1(':-'(T),D, R) :- process(D, [], T, R).
              ,D, R) :- append(D, [T], R).
assert1(T
read_stream_to_terms(Stream, RC, REnv) :-
  read_term(Stream, C, [variable_names(Env)]), !,
  ( C = end\_of\_file, RC = [], REnv = [],
  ; read_stream_to_terms(Stream, RC1, REnv1),
    RC = [C | RC1], append(Env, REnv1, REnv), !).
cnv2(A :- B, A :- B).
cnv2(:-B,:-B).
cnv2(T, T := nop).
consult1(Filename, D, D2) :-
  (flag(trace,1,1),write("Loading "),write(Filename),nl;!),!,
  setup_call_cleanup(open(Filename, read, In), read_stream_to_terms(In, Terms, Env), close(In)),
  maplist(cnv2,Terms,Terms2),!,
  foldl(assert1, Terms2, D, D2),!.
```

```
step(succ(G,D,I,S),R2):-(flag(trace,1,1),format("i=\sim G=\sim S=\sim N",[I,G,S]);!),!, step1((G,D,I,S),G,D,I,S,R2).
step(R, R).
step1(M, [], D, I,
                              S, R) :- R=succ([], D, I, S),!.
step1(M, [T|G], D, [T1=T2|_], S, R) :- copy_term(T1,T), call(T2,M,M,R).
step1(M, [T|G], D, [T_{II}], S, R) :- copy_term(T_{II}), step(succ([T3|G], D, D, [([T|G], I1)|S]), R).
step1(M, [T|G], D, [T_|I1], S, R) :- step(succ([T|G], D, I1, S), R).
                              S, R) = pop(M,M2), step(M2,R).
           G , D, I,
step1(M,
solve(M, R2) :- ([], _, _, _) = M, pop(M, R), step(R, R2).
solve(M, R2) :- (G, D, \overline{I}, \overline{S}) = M, step(succ(G,D,\overline{I},\overline{S}), R2).
read_line(P, A) :-
  prompt1(P), read_line_to_codes(user_input,R),atom_codes(A,R).
env_show_add_(K=V,R) :- format(atom(R),"~s=~p",[K,V]).
env_show(Vs,R) :- maplist(env_show_add_,Vs,E3), atomic_list_concat(E3,', ',R).
prove(Env,M,D2) :- solve(M, R),
  (R = fail(D2))
  ; R = succ(G, D, I, S),
    env_show(Env, X), write(X),nl,
    ( (S=[]; S=[(fail,D)]), write("Yes.\n"), D2=D
    ; ( read_line("More y/n", "y"), prove(Vs,(G, D, I, S), D2)
      ; D2=D))).
process(D, Env,T, D2) :- prove(Env,([T], D, D, [([fail],D)]), D2).
```

```
gen_builtin(T1 :- T2, T = N) :- T1 = .. [N,_,([T]],_,_,),_], assert(T1 :- T2).
init_db(Db) :- maplist(gen_builtin,[
    builtin_halt(
                   M,([
                              halt [G], D, _, S), R) :- halt,
                              fail|G], D, _, S), R) :- R=fail(D),
                   M,([
   builtin_fail(
                               nop[G], D, _, S), R) :- step(succ(G, D, D, S), R),
    builtin_nop(
                    M,([
                                 ! [G], D, _, S), R) :- step(succ(G, D, D, [([fail], D)]), R),
                   M, ([
   builtin_cut(
                                   [G], D, _, S), R) :- step(succ([U,V|G], D, D, S), R),
   builtin_comma( M,([(U,V)
                                   [G], D, _, S), R) :- step(succ([U|G], D, D, [([V|G], D)|S]), R),
    builtin_semi(
                   M,([(U;V)
                                   G], D, _, S), R) :- (uni(M,U,V,R1),step(R1, R)),
                   M, (\overline{(U=V)})
   builtin_eq(
                    M,([(U is V) | G], D, _, S), R) :- (N is V, !, uni(M,U,N,R1), step(R1,R)),
    builtin_is(
   builtin_write( M,([ write(T)|G], D, _, S), R) :- (write(T), step(succ(G, D, D, S), R)),
   builtin_assert( M, ([assert(T) G], D, M, M) :- (assert1(T, D, D2), step(succ(G, D2, D, S), R)),
    builtin_consult(M,([consult(T)|G], D, \overline{}, S), R) :- (consult1(T, D, D2), step(succ(G, D2, D, S),R))
  ], Db).
```

```
welcome("Beautiful Japanese Prolog Interpreter").
help :- maplist(format('~s\t~s\n'),[["e","exit"], ["l","list"],["h","help"]]).
syntax_print(T) :- write(T), write('.'), nl.
repl(D) :-
    read_line("? ", Y),!,
    (Y='e'
    ;Y='l', maplist(syntax_print, D),!, repl(D)
    ;Y='h', help,!, repl(D)
    ;Y='t', flag(trace,T,1-T),(T=0,S='on';S='off'),format('Tracing \sims\simn',[S]),!,repl(D)
            term_string(R,Y,[variable_names(Env)]),!,process(D,Env, R, D2),!, repl(D2)
            write('Syntax error\n'),!, repl(D)).optParse([
                                                                   ],Db,Db ).
optParse(['-t'|Args],Db,Db2) :- flag(trace,_,1), optParse(Args,Db,Db2).
             A|Args],Db,_ ) :- sub_atom(A,0,1,_,'-'), write("Usage: bjpl [-t] filename1 filename2 ...\n"), halt.
optParse([
optParse([ A|Args],Db,Db2) :- consult1(A,Db, Db1), optParse(Args, Db1, Db2).
main :-
  current_prolog_flag(argv, ARGV),
  flag(trace,_,0),
  init_db(Init_db),
  consult1('lib/initial.pl',Init_db, Db), % load files
  optParse(ARGV, Db, Db1),!,
  welcome(W),atom_length(W,L),
  (between(1, L, _), write(-), fail;nl),
  write(W), nl,
  (between(1, L, _), write(-), fail;nl),
  help,
  repl(Db1).halt.
```