

Deep Probabilistic Graphical Models

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About VinAI Research

- Lab Location: Hanoi, Vietnam. <https://www.vinai.io/>
- Funded by VinGroup, the largest private company in Vietnam.
- Publication focused.
- The first of its kind in South East Asia (not counting Singapore).
- We're hiring scientists, engineers and AI Residents.

Roadmap

- Motivation
- Deep Probabilistic Graphical Models
- Training Deep PGMs via Variational Inference
- Representation Learning with Deep PGMs
 - Disentangled Representations
 - Planning in Representation Space

Motivation: Unsupervised Learning, Generative Modeling



where can i buy an affordable stationary bike ? try this place , they have every type imaginable with prices to match . http :
UNK </s>

if our economy collapses , will canada let all of us cross their border ? no , a country would have to be stupid to let that
many people cross their borders and drain their resources . </s>

does the flat earth society still exist ? i 'm curious to know whether the original society still exists . i 'm not especially interested
in discussion about whether the earth is flat or round . although there is no currently active website for the society , someone (
apparently a relative of samuel UNK) maintains the flat earth society forums . this website , which offers a discussion forum and
an on-line archive of flat earth society UNK from the 1970s and 1980s , represents a serious attempt to UNK the original flat
earth society . </s>



Brock, Andrew, Jeff Donahue, and Karen Simonyan. "Large scale gan training for high fidelity natural image synthesis." arXiv preprint arXiv:1809.11096 (2018).

Kim, Yoon, et al. "Semi-amortized variational autoencoders." arXiv preprint arXiv:1802.02550 (2018).

Van Den Oord, Aaron, et al. "WaveNet: A generative model for raw audio." SSW 125 (2016).

Motivation: Representation Learning



Motivation: Representation Learning



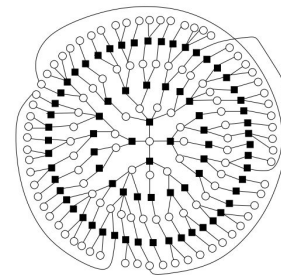
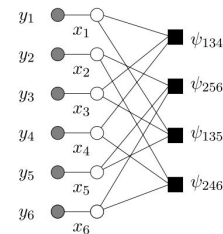
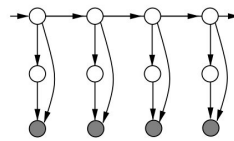
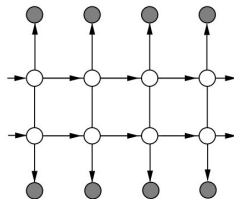
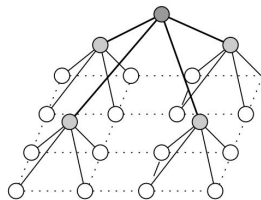
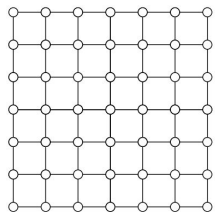
Varying the code of tense

i thought the movie was too bland and too much
i guess the movie is too bland and too much
i guess the film will have been too bland

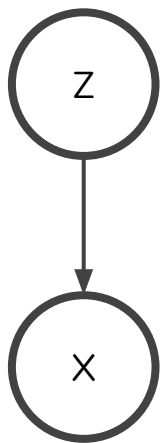
this was one of the outstanding thrillers of the last decade
this is one of the outstanding thrillers of the all time
this will be one of the great thrillers of the all time

Probabilistic Graphical Models

Graphical representation of probabilistic dependency in joint probability distributions



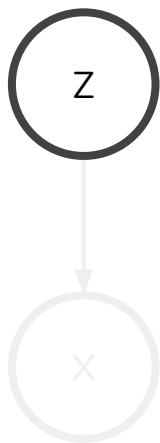
Latent Variable Models



Node denotes an unconditional probability distribution
 $\Pr(Z)$

Linked Node denotes a conditional probability distribution
 $\Pr(X \mid Z = z)$

Latent Variable Models



Node denotes an unconditional probability distribution
 $\Pr(Z)$

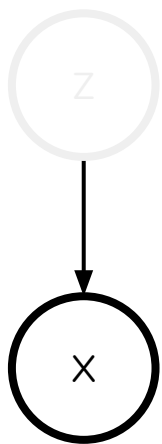
How to represent an unconditional probability distribution:

Parametric distributions $\Pr(Z ; \gamma)$

Discrete: Categorical, Binomial, Bernoulli, etc

Continuous: Gaussian, Gamma, Beta, Dirichlet, etc

Latent Variable Models



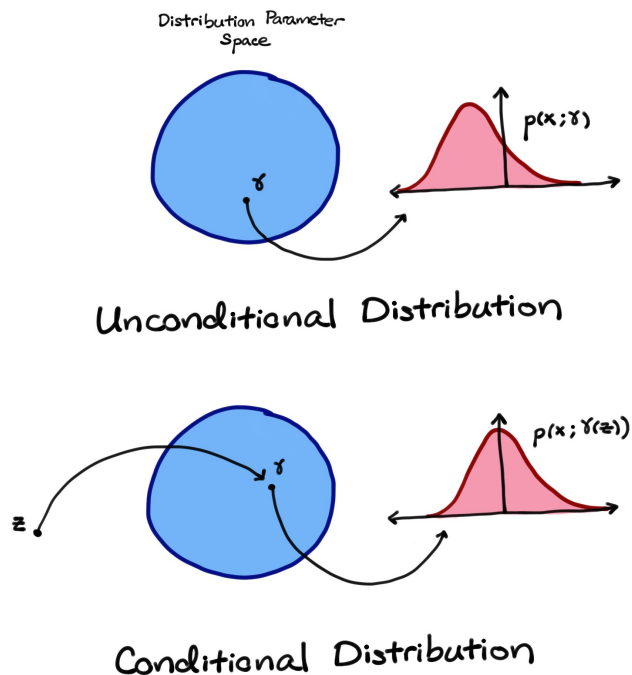
Linked Node denotes a conditional probability distribution
 $\Pr(X \mid Z = z)$

How to represent a conditional probability distribution:

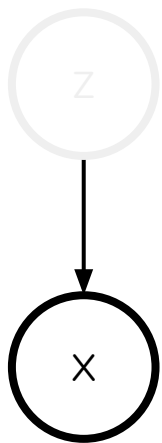
- A mapping function $f: z \rightarrow \gamma$
- A parametric distribution $\Pr(X; \gamma)$

$$\Pr(X \mid Z = z) := \Pr(X; f(z))$$

Probabilistic Graphical Models



Deep Probabilistic Graphical Models



Linked Node denotes a conditional probability distribution
 $\Pr(X \mid Z = z)$

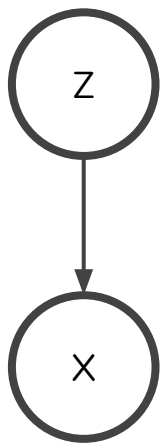
How to represent a conditional probability distribution:

- A mapping function $f: Z \rightarrow \gamma$
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f is a neural network

Deep Probabilistic Graphical Models

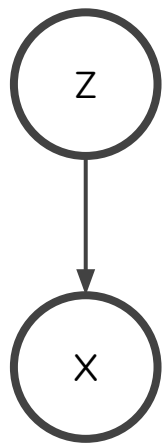


Node denotes an unconditional probability distribution
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f is a neural network

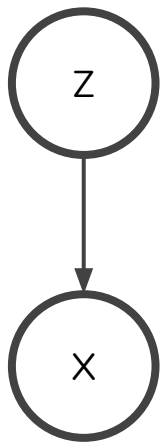
Training a Deep PGM



Given a dataset (D), and a deep PGM (P)

Minimize “distance” between D and P

Training a Deep PGM



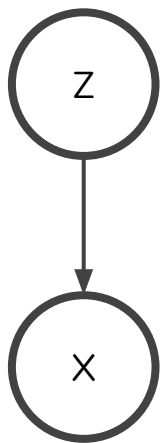
Given a dataset (D), and a deep PGM (P)

Minimize “distance” between D and P

Choices of distance:

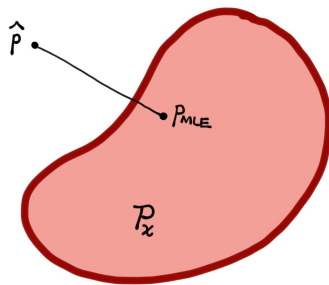
- Kullback-Leibler Divergence
- Jensen-Shannon Divergence
- Wasserstein Distance
- etc

Training a Deep PGM: Kullback-Leibler

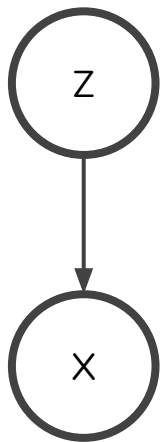


Given a dataset (D), and a deep PGM (P)

Minimize KL divergence between D and P



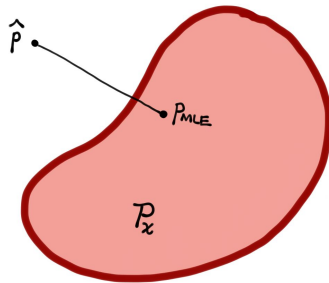
Training a Deep PGM: Kullback-Leibler



Given a dataset (D), and a deep PGM (P)

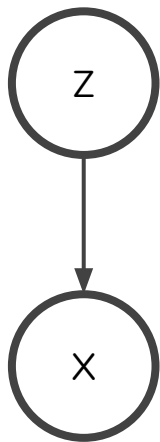
Minimize KL divergence between D and P is equivalent to

Maximize log-likelihood of $\ln P(x)$ where x is sampled from D



Training a Deep PGM: Kullback-Leibler

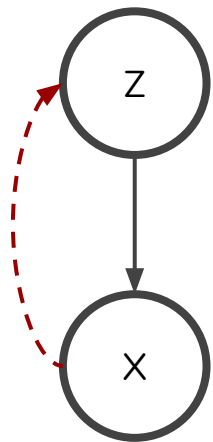
Computing $\ln P(x)$ is intractable



$$\ln p(x) = \ln \int p(x, z) dz \geq \mathbb{E}_{q(z|x)} \ln \frac{p(x, z)}{q(z | x)}$$

Training a Deep PGM: Kullback-Leibler

Computing $\ln P(x)$ is intractable

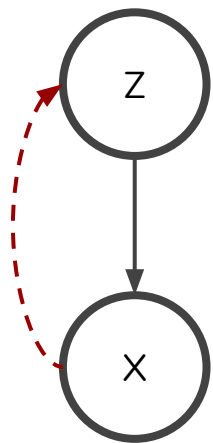


$q(z | x)$ is the variational approximation

$$\ln p(x) = \ln \int p(x, z) dz \geq \mathbb{E}_{q(z|x)} \ln \frac{p(x, z)}{q(z | x)}$$

Training a Deep PGM: Kullback-Leibler

Computing $\ln P(x)$ is intractable



$q(z | x)$ is the variational approximation

$$\ln p(x) = \ln \int p(x, z) dz \geq \mathbb{E}_{q(z|x)} \ln \frac{p(x, z)}{q(z | x)}$$

$$\underset{p}{\text{maximize}} \quad \ln p(x) \quad \longrightarrow \quad \underset{p, q}{\text{maximize}} \quad \mathbb{E}_{q(z|x)} \ln \frac{p(x, z)}{q(z | x)}$$

Evidence Lower Bound (ELBO)

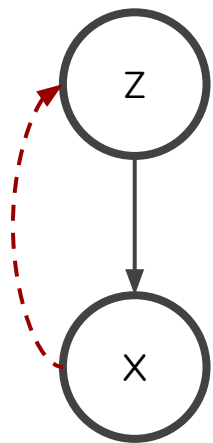
$$\mathbb{E}_{q_{\phi}(z|x)} \ln \frac{p_{\theta}(x, z)}{q_{\phi}(z|x)}$$

$$\mathbb{E}_{q_{\phi}(z|x)} \ln p_{\theta}(x|z) - D_{KL}(q(z|x)||p(z))$$

$$\ln p_{\theta}(x) - D_{KL}(q(z|x)||p(z|x))$$

Training a Deep PGM: Kullback-Leibler

Computing $\ln P(x)$ is intractable



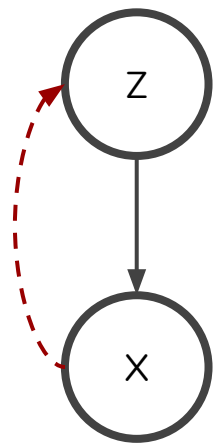
$q(z | x)$ is the variational approximation

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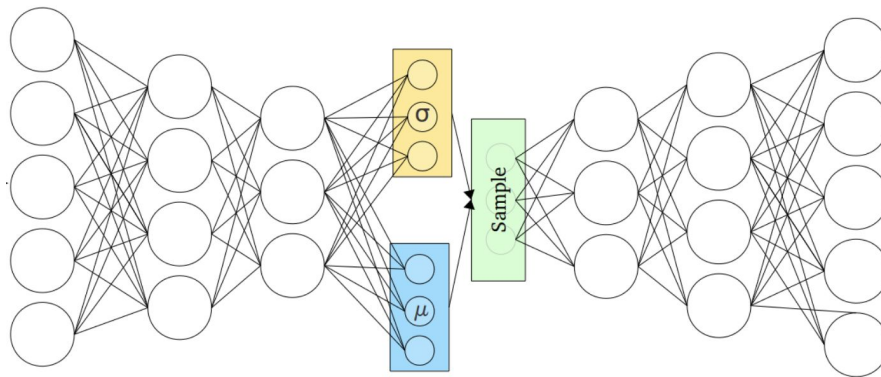
$$\underset{p}{\text{maximize}} \quad \ln p(x) \quad \longrightarrow \quad \underset{p, q}{\text{maximize}} \quad \mathbb{E}_{q(z|x)} \ln \frac{p(x, z)}{q(z | x)}$$

Variational Autoencoder

Training a Deep PGM: Kullback-Leibler



$q(z | x)$ is the variational approximation



$$\underset{p}{\text{maximize}} \ln p(x) \longrightarrow \underset{p, q}{\text{maximize}} \mathbb{E}_{q(z|x)} \ln \frac{p(x, z)}{q(z | x)}$$

Variational Autoencoder

Reparameterization Trick

$$\nabla_{\phi} \mathbb{E}_{q_{\phi}(x)} f(x, \phi)$$

Cannot push the gradient operator
inside the expectation

$$\epsilon \sim q_0, x = r(\epsilon, \phi)$$

Reparameterize the distribution

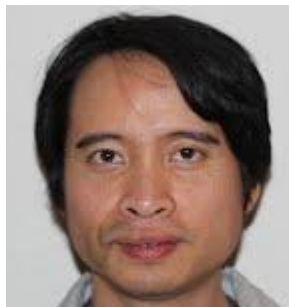
Rewrite the gradient, push gradient operator inside

$$\nabla_{\phi} \mathbb{E}_{\epsilon \sim q_0} f(r(\epsilon, \phi), \phi) = \mathbb{E}_{\epsilon \sim q_0} \nabla_{\phi} f(r(\epsilon, \phi), \phi)$$

Toward Disentangled Face Representations



Toward Disentangled Face Representations

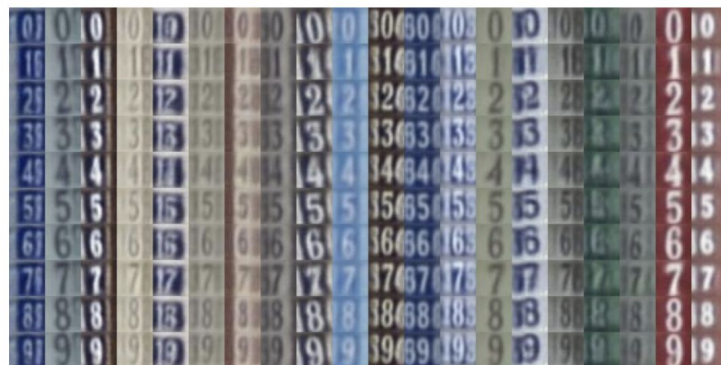


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Style and Content Disentanglement

Model 1



Model 2

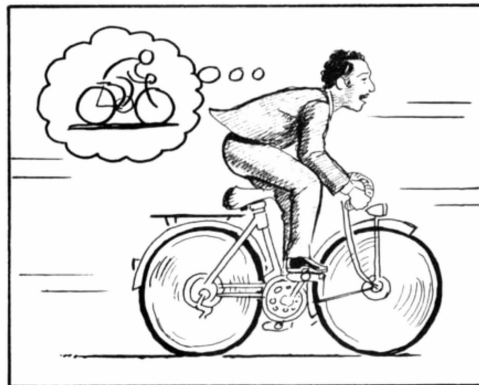


1. Why does our optimizer coincide with human preference?
2. How do we modify the loss function so that the loss function favors Model 1?

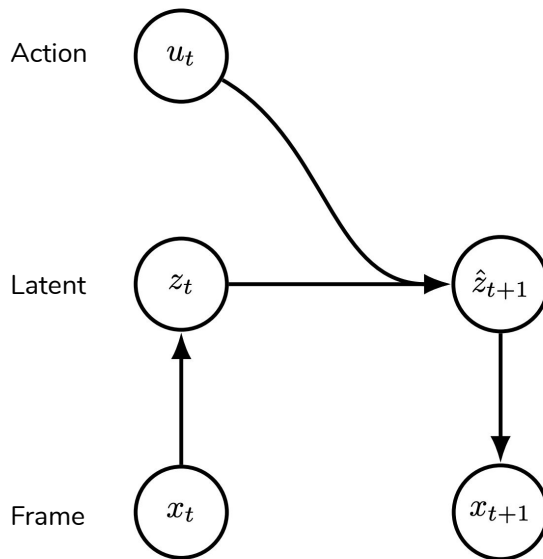
Planning in Representation Space

If you can **predict** what will happen if you perform an action, then you can **plan** ahead

- (Prediction) Use a generative model to do prediction in representation space
- (Planning) Apply optimal control algorithm in representation space



Planning in Representation Space

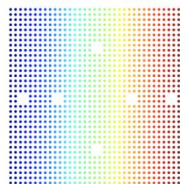


Predict next frame via a bottlenecked model

Planning in Representation Space



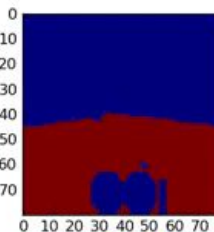
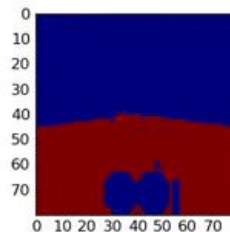
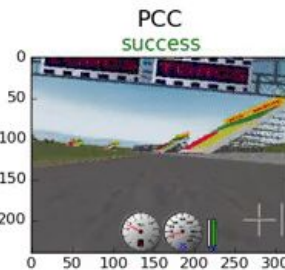
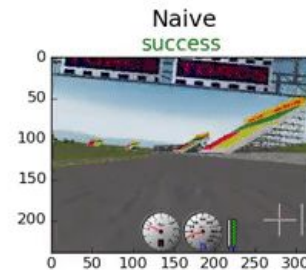
True map



Learned latent space

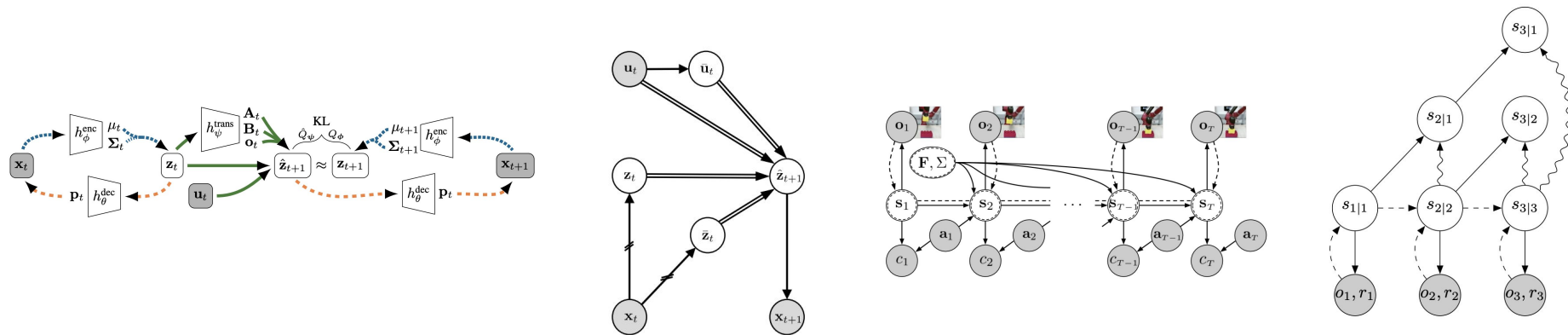


Planar System Environment



TORCS Environment

Planning in Representation Space



1. What is the best way to learn a representation space for control?
2. Should our choice of controller influence how we choose to learn the representation space?

Recap

- Motivation
 - Generative modeling
 - Representation learning
- Deep Probabilistic Graphical Models
 - A neural network mapping function
- Training Deep PGMs
 - Variational Inference
- Representation Learning with Deep PGMs
 - Disentangled Representations
 - Planning in Representation Space