Real-time resolving assembly graph by ONT long reads data

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Abstract: A real-time assembly pipeline for Oxford Nanopore Technology (ONT) data is important for either saving sequencing resources or reducing turnaround time for data analyses. The previous approach from npScarf provided a greedy fast-response, auto-correct streaming algorithm for such task but was relatively prone to mis-assemblies compared to other graph-based methods. Here we present npGraph, a real-time hybrid assembly software using the assembly graph instead of the separated pre-assembly contigs. It is able to produce more complete genome assembly by resolving the path finding problem on the assembly graph using long reads as the traversing guide. The application on synthetic and real data set of isolate genomes show improved accuracy while still maintaining the required computational cost extremely low. On top of that, we apply npGraph on mock community in the very first application to improve metagenomics assembly in real-time with nanopore data. With npScarf, the built-in graphical user interface (GUI) can provide users a comprehensive look-and-feel of the whole assembly process. The tool and source code is available at https://github.com/hsnguyen/assembly.

Keywords: hybrid assembly, assembly graph, real-time analysis, nanopore sequencing

Introduction

Streaming assembly methods had been proven to be useful in saving time and resources compared to the conventional batch algorithms with examples included e.g. Faucet [1] and npScarf [2]. The first method allows the assembly graph to be constructed incrementally as long as reads are retrieved and processed. This practice is helpful dealing with huge short-read data set because it can significantly reduce the local storage for the reads, as well as save time for a De Bruijn graph (DBG) construction while waiting for the data being retrieved. npScarf, on the other hand, is a hybrid assembler working on a pre-assembly set of short-read assembly contigs. It functions by scaffolding the contigs using nanopore sequencing which is well-known by the real-time property. The completion of genome assembly in parallel with the sequencing run provides explicit benefits in term of resource control and turn-around time for analysis [2].

Hybrd approaches are still common practice in genome assembly and data analyses when Illumina sequencing remains the most favoured option in terms of cost and accuracy to date. On the other hand, the third-generation sequencing methods such as Pacbio or Oxford Nanopore Technology are well-known for the ability to produce much longer reads that can further complete the Illumina assembly. As the consequence, it is rational to combine two sources of data together in a hybrid method that can offer accurate and comptete genomes at the same time. npScarf, following that philosophy, had been developed and deployed on real microbial genomes.

However, due to the greedy bridging approach of the contigs-based streaming algorithm, npScarf's results might suffer from mis-assemblies [3, 4]. A default setting were optimized for microbial genomes input but cannot fit for all data from various experiments in practice. Also, the gap filling step has to rely on the low quality nanopore reads thus the accuracy of the final assembly is affected as well. To tackle the quality issue while maintaining its streaming feature, a bridging method by assembly graph traversing is proposed. In which, after the construction of a compact DBG assembly graph, the next step is to traverse the graph, resolve the repeats and identify the longest possible un-branched paths that would represents contigs for the final assembly.

Hybrid assembler using nanopore data to resolve the graph has been implemented in hybridSPAdes [5] or Unicycler [3]. In general, the available tools employ batch-mode algorithms on the whole long-read data set to generate the final genome assembly. In which, the SPAdes hybrid assembly module, from its first step, exhaustively looks for the most likely paths (with minimum edit distance) on the graph for each of the long read given but only ones supported by at least two reads are attained. In the next step, these paths will be subjected to a decision-rule algorithm, namely exSPAnder [6], for repeat resolution by step-by-step expansion, before output the final assembly. On the other hand, Unicycler's hybrid assembler will initially generate a consensus long read for each of the bridge from the batch data. The higher quality consensus reads are used to align with the assembly graph to find the best paths bridging pairs of anchored contigs. While the latter method employs the completeness of the data set from the very beginning for a consensus step, the former only iterates over the batch of possible paths and relies on a scoring system for the final decision of graph traversal. For that reason, the first direction is more suitable for a real-time pipeline.

Nonetheless, the challenge to adapt this approach into a real-time mechanism is obvious, mainly from building a progressive implementation for path-finding and graph reducing module which are essential for a streaming graph assembler. To achieve that, we apply a modified DFS (depth-first search) mechanism and a dynamic voting algorithm

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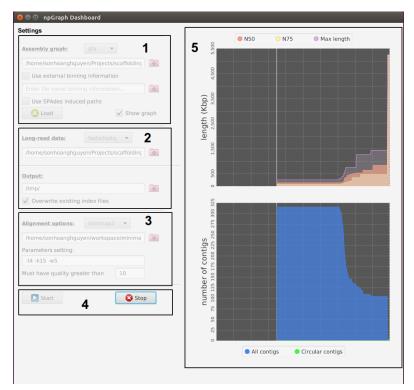
into an on-the-fly graph resolver. The method is implemented in npGraph, a user-friendly tool with GUI that can traverse the assembly graph and bridge its components in real-time as long as the nanopore sequencing process is still running.

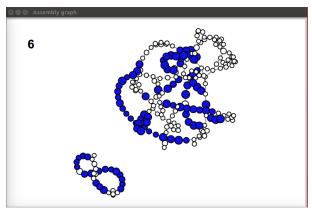
We use different hybrid data sets to study the npGraph's performance and compare with other available tools with similar functionality, such as npScarf, Unicycler and hybridSPAdes. Even though all data were from microbial genomes, the complexity of the input graphs range from few hundred to ten thousands of components, synthesized in silico or sequenced from in vitro samples. Particularly, for the first time, we employ a pipeline in an attempt to complete metagenomics assembly in real-time. We aim to develop a simple approach on top of npGraph to adapt with metagenomics while minimizing additional processing steps. In fact, only one more step for population binning is needed to make npGraph functions on genomes of a mock community. Despite a rather straightforward methodology, the pipeline has shown consecutively enhanced assembly from the fragmented short-read DBG graph.

Results

npGraph - a tool to resolve assembly graph in real-time

npGraph's input consists of Illumina assembly graph resulted from running assembler, e.g. SPAdes [7], Velvet [8], AbySS [9] on Illumina short reads, together with long reads from third generation sequencing technology (Oxford Nanopore Technology, Pacbio). The long reads will be aligned with the contigs in the assembly graph to indicate longer paths that should be traversed. These local paths, given sufficient data, are expected to untangle the complicated graph and guide to the global Eulerian paths (or cycles if possible) that represent the entire genomic sequences. npGraph can be invoked and fully function from the command-line interface. In addition, in order to aid the visualization of the assembly process, a GUI has been developed as well.





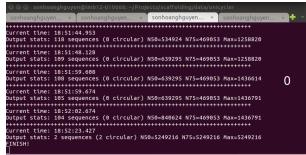


Figure 1: npGraph user interface including Console (0) and GUI components (1-6). The GUI consists of the Dashboard (1-5) and the Graph View (6). From the Dashboard there are 5 components as follow: 1 the assembly graph input field; 2 the long reads input field; 3 the aligner settings field; 4 control buttons (start/stop) to monitor the real-time scaffolding process; 5 the statistics plots for the assembly result.

The GUI includes the dashboard for control the settings of the program and another pop-up window for a simple visualization of the assembly graph in real-time (Figure 1). In this interface, the assembly graph loading stage is separated from the actual assembly process so that users can check for the graph quality first before carry out any further tasks. The box numbered 1 on Figure 1 is designed for this task. Only after an assembly graph is loaded successfully, users can move to box 2 to specify the nanopore input data. Settings for an aligner (BWA-MEM or minimap2) in box 3 is required if the input is the raw sequences in FASTA/FASTQ format. Another option is to run the alignment independently and provide SAM/BAM input for the next stage of bridging and assembly. This stage is controlled by buttons in box 4: the START button ignites the process while the STOP button can prematurely terminate it

and output the assembly result till that moment. The plots from the right panel (5) depicts real-time statistics of the assembly contigs inferred from the graph. From the second window (6), the colored vertices imply unique contigs while the white ones involve either unspecified or repetitive elements. The number of different colors (other than white) indicates the amount of abundant groups being detected as population bins (e.g. chromosome versus different plasmids, or different bins in metagenomics).

A proper combination of command line and GUI can provide an useful streaming pipeline that copes well with MinION output data. The practice is similar to the previous developed pipelines [2, 10, 11] that allow the analysis to take place abreast to a nanopore sequencing run.

Evaluation using synthetic data

To evaluate the performance of the method, npGraph was tested against SPAdes with its hybrid assembly module [5], npScarf with/without assembly graph integrated, and Unicycler version 0.4.6 on Unicycler's synthetic data set [3]. The data set is a simulation of Illumina and MinION raw data, generated *in silico* based on random and available microbial references. We ran all hybrid assembly methods in batch-mode and the reciprocal results were examined by QUAST 5.0.2 [14].

Table 1: Comparison of assemblies produced in batch-mode using npGraph and the comparative methods on 5 Unicycler's synthetic data sets downloaded from https://cloudstor.aarnet.edu.au/plus/index.php/s/dzRCaxLjpGpfKYW

| | Assembly | | N50 | Mis- | Error | Run times | | | |
|---|-----------------------------------|-----------|--------|------------|---------------|-------------|--|--|--|
| Method | size (Mbp) | # Contigs | (Kbp) | assemblies | (per 100 Kbp) | (CPU hrs) | | | |
| Mycobacterium tuberculosis H37Rv: 4,411,532bp | | | | | | | | | |
| SPAdes | 4.376 | 66 | 150.7 | 0 | 0.23 | 1.42 | | | |
| SPAdes hybrid | 4.411 | 1 | 4410.5 | 0 | 0.86 | 1.61 | | | |
| Unicycler | 4.412 | 1 | 4411.5 | 0 | 2.56 | 5.52 | | | |
| npScarf | 4.432 | 4 | 4402.2 | 7 | 6.61 | 1.42 + 0.7 | | | |
| npGraph (bwa) | 4.411 | 1 | 4411.4 | 0 | 2.63 | 1.42 + 0.64 | | | |
| npGraph (minimap2) | 4.412 | 1 | 4411.5 | 0 | 0.68 | 1.42 + 0.02 | | | |
| Saccharomyces cerevisiae S288c: 12,157,105 bp | | | | | | | | | |
| SPAdes | 11.675 | 194 | 260.5 | 0 | 1.57 | 3.61 | | | |
| SPAdes hybrid | 11.910 | 45 | 770.5 | 5 | 34.52 | 4.15 | | | |
| Unicycler | 11.837 | 29 | 909.1 | 0 | 22.83 | 16.34 | | | |
| npScarf | 11.990 | 22 | 796.8 | 53 | 85.5 | 3.61 + 4.35 | | | |
| npGraph (bwa) | 12.000 | 151 | 913.1 | 3 | 38.68 | 3.61 + 4.12 | | | |
| npGraph (minimap2) | 12.008 | 148 | 913.1 | 5 | 25.32 | 3.61 + 0.13 | | | |
| Shigella sonnei 53G: 5,22 | Shigella sonnei 53G: 5,220,473 bp | | | | | | | | |
| SPAdes | 4.796 | 392 | 27.7 | 0 | 0.44 | 1.1 | | | |
| SPAdes hybrid | 5.218 | 8 | 2195.5 | 2 | 41.98 | 1.36 | | | |
| Unicycler | 5.221 | 5 | 4988.5 | 0 | 7.91 | 9.64 | | | |
| npScarf | 6.426 | 20 | 1293.8 | 84 | 366.04 | 1.1 + 0.52 | | | |
| npGraph (bwa) | 5.293 | 97 | 4988.5 | 3 | 14.87 | 1.1 + 0.57 | | | |
| npGraph (minimap2) | 5.293 | 97 | 4988.5 | 3 | 8.31 | 1.1 + 0.08 | | | |
| Shigella dysenteriae Sd197: 4,560,911 bp | | | | | | | | | |
| SPAdes | 4.096 | 534 | 14.4 | 1 | 0.68 | 1.19 | | | |
| SPAdes hybrid | 4.486 | 23 | 821.2 | 96 | 10.99 | 1.89 | | | |
| Unicycler | 4.561 | 3 | 4369.2 | 0 | 12.96 | 8.46 | | | |
| npScarf | 4.649 | 174 | 41.8 | 65 | 372.87 | 1.19 + 0.62 | | | |
| npGraph (bwa) | 4.553 | 3 | 4369.1 | 6 | 91.03 | 1.19 + 0.76 | | | |
| npGraph (minimap2) | 4.548 | 3 | 4364.1 | 8 | 83.68 | 1.19 + 0.14 | | | |

Table 1 shows comparative results running different methods on 5 synthetic data sets, report for the whole comparison can be found in Supplementary Table 1. In the first column of applied methods, beside Unicycler and hybridSPAdes, the original scaffolder npScarf was included as well as npScarf_wag – its modified version with assembly graph integrated. On the other hand, npGraph can use 2 different aligners, BWA-MEM and minimap2, for its bridging phase thus both practices were included in this comparison.

In general, the graph version of npScarf improved the assembly results in terms of mis-assemblies and error reduction while virtually consuming similar resources compared to the original version. The only exception where the number of mis-assemblies being increased was the simulation of a random sequence with many repeats. There were 10 more mistakes detected using the later version npScarf_wag. However, with additional investigations, we found that the number of mis-assemblies on the true positive circular sequences (3 from the reference) has been significant reduced by

applying assembly graph for npScarf. The errors mostly came from redundant sequences output from the software due to the failure in estimation of contig multiplicity. Even though using assembly graph for gap fillings, there were no changes in the way npScarf_wag determine if a contig is unique or not. Its implementation still relied on the length and coverage statistics, i.e. Astats [15] to find anchors that were critical for the backbone construction of the assembly. Redundant path findings for false positive replicons consequently returned additional wrong translocations in the final contigs which were reported by QUAST. Other than that, the method had successfully produced better assemblies than the original. Regarding Mycobacterium tuberculosis H37Rv, the number of mis-assembled breakpoints had been trimmed down from 12 to 2, while the number of final contigs had reduced from 4 to only one as in the reference. Results in cases of E. coli O25b H4ST131 and Streptococcus suis BM407 also showed enhancements in terms of those categories as well as N50 statistics. There was improvements considering the nucleotide errors (mismatches and indels) as well from aforementioned data sets, except for the E. coli when slightly more mismatches had been detected. However, these errors can be corrected by running polishing tools with the raw Illumina data afterward.

For Acinetobacter AB30 synthetic data, it was an deficiency for npScarf_wag in traversing the graph to find candidate paths for a bridge of long distance due to particular large search space. The exhaustive, naive DFS implementation for this version of npScarf required a lot of memory to traverse a complex assembly graph that usually exceed a normal desktop's capacity. This issue has been fixed in npGraph when Algorithm 1 was used on the definitive graph. This resulted in completed runs of the assembly process for all data sets with the similar number of mis-assemblies compared to the best figures in this category. As shown in Table 1 and 1, the assembly graph based methods offered significant improvements when compared to npScarf. Not only because of the clear drops with respect to mis-assemblies and errors, but it was also reflected by the number of final contigs and their N50 as well.

To align the long reads to the assembly graph components, either BWA-MEM [16] or minimap2 [17] was invoked in npGraph. The former option was inherited from npScarf pipeline with the intact parameters while the latter was used with the recommended settings (-k15 -w5) for the best sensitivity working on MinION data. Even though, BWA-MEM normally reported more hits than minimap2 but at the same time, was responsible for more false positive alignments. For instance, regarding the last data set from Table 1, the assembly of npGraph using BWA-MEM was suffered from the ambiguous alignments thus more fragmented than the other counterparts. On the other hand, referring to more complicated graphs from Acinetobacter A1 and the yeast Saccharomyces cerevisiae S288c from Table 1, the number of mis-assemblies from using minimap2 were increased due to the lacks of appropriate alignments to support accurate bridging process. However, under almost circumstances, using either aligners would result in final assemblies with similar qualities. Furthermore, in terms of running time and resources required, minimap2 proved to be the best option. The total CPU hours had been cut down drastically with the new aligner, making npGraph the fastest hybrid assembler available. This feature is certainly more favoured for a real-time assembly pipeline that normally requires quick responses in very short intervals. Because minimap2 is expected to replace BWA-MEM for long-read sequencing data alignment, it likewise being chosen as the default aligner for npGraph pipeline.

To evaluate assembly errors, we considered the measure of the total mismatches and indels per 100 Kbp from the assembly sequences when mapping to the reference. As expected from hybrid assembly methods embedding Illumina data, the figures were hardly bigger than 100 (equivalent to 0.1% error rate) in almost every cases. Furthermore, the indels errors, which mainly caused by TGS data, were found relatively low in the final contigs (Table 1). The majority of the differences accounted for the mismatched nucleotides caused by the alternative paths connecting the unique anchors from the backbone of the assembly. This phenomenon may root from homologous repeats or sequencing errors of the genome. From all the hybrid assemblers, hybridSPAdes reported results with highest fidelity. This meant that the performance its decision-rule algorithm exSPAnder [6] was the most accurate amongst all path finding methods. As the trade-off, there were fewer connections satisfying its quality threshold, resulting in the fragmented assemblies in cases of Streptococcus suis or Acinetobacter samples (Table 1 and 1). Unicycler, which employs an algorithm based on 45 semi-global (or glocal) alignments [18] with the consensus long reads, returned the second best reliable and at the same time, closest-to-complete results overall. npScarf, on the other hand, employed the long reads for the gap filling thus inherited the high error rates from them. By integrating the assembly graph for the task, the errors were reduced in general (random sequences, M. tuberculosis, S. suis from Table 1) but not completely since the mis-placed contigs were still not resolved in other circumstances. npGraph significantly reduced the errors compared to npScarf, however the 50 figures were still higher than the those of the best counterparts. This implied a more robust decision making system is needed in npGraph's real-time path finding module for even better output's accuracy.

Hybrid assembly for real data sets

A number of sequencing data sets from *in vitro* bacterial samples [19] were used in this scenario. The data included both Illumina paired-end reads and MinION sequencing based-call data for each sample. Due to the unavailability of reference genomes, there were fewer statistics being reported by QUAST for the comparison of the results. Instead, we investigated the number of circular sequences and PlasmidFinder 1.3 [20] mappings to obtain an evaluation on the accuracy and completeness of the assemblies. Table 2 shows the benchmark results of npGraph (using minimap2) against Unicycler on three data sets of bacterial species Citrobacter freundii, Enterobacter cloacae and Klebsiella oxytoca.

From the first data set, there was high similarity between final contigs generated by two assemblers. They shared the same number of circular ultimate sequences, including the chromosomal and other six replicons contigs. The only

Table 2: Assembly of real data sets using Unicycler and npGraph with the optimized SPAdes output. Circular contigs are highlighted in **bold**, fragmented assemblies are presented as X|Y where X is the total length and Y is the number of supposed contigs making up X.

| | Unicycler npGraph | | Replicons (based on PlasmidFinder 1.3) | |
|----------------------|-----------------------|-----------------|--|--|
| Citrobacter freundii | 5,029,534 5,029,486 | | Chromosome | |
| CAV1374 | 109688 109688 | | IncFIB(pHCM2)_1_pHCM2_AL513384 | |
| | 100,873 | $100,\!873$ | IncFIB(pB171)_1_pB171_AB024946 | |
| | 85,575 | $85,\!575$ | IncL/M(pMU407)_1_pMU407_U27345 | |
| | 43,621 | 43,621 | repA_1_pKPC-2_CP013325 | |
| | 3,223 | 3,223 | - | |
| | 1,916 | 1,916 | ColRNAI_1_DQ298019 | |
| | 14,464 3 | 14,456 2 | - | |
| Enterobacter cloacae | 4,806,666 2 | 4,858,438 2 | Chromosome | |
| CAV1411 | 90,451 | 90,693 2 | IncR_1_DQ449578 | |
| | 33,610 | 33,610 | repA_1_pKPC-2_CP013325 | |
| | 13,129 2 | 14,542 4 | - | |
| Klebsiella oxytoca | 6,153,947 5 | $6,\!155,\!762$ | Chromosome | |
| CAV1015 | 113,105 | 113,105 | IncFII(SARC14)_1_SARC14_JQ418540; | |
| CAV 1019 | 113,103 | | IncFII(S)_1CP000858 | |
| | 111,395 | $111,\!395$ | - | |
| | 108,418 | 109,209 13 | IncFIB(K)_1_Kpn3_JN233704 | |
| | 76,183 | $76,\!186$ | IncL/M(pMU407)_1_pMU407_U27345 | |
| | 11,638 | 11,892 2 | - | |

divergence lied on the biggest sequence ($\simeq 5.029 \mathrm{Mbp}$) when the Unicycler's chromosome was 48 nucleotides longer than that of npGraph. Five out of six identical replicons were confirmed as plasmids based on the occurences of appropriate Origin of replication sequences (PlasmidFinder database). In detail, two megaplasmids (longer than 100Kbp) were classified as IncFIB while the other two mid-size replicons, 85.6Kbp and 43.6Kbp, were incL and repA respectively, leaving the shortest one with 2Kbp of length as ColRNAI plasmid. The remaining circular sequence without any hits to the database was 3.2Kbp long suggesting that it could be phage or newly replicon's DNA. Lastly, there were still 14.5Kbp unfinished sequences resulted in 3 linear contigs from Unicycler and 2 for npGraph respectively.

The assembly task for *Enterobacter cloacae* was observed more challenging as the chromosomal DNA sequence not been fully resolved using either method. The chromosome size was estimated to be approximately 4.8Mbp but had been broken into two smaller pieces. npGraph returned longer stretches of length 3.324Mbp and 1.534Mbp while the figures were 2.829Mbp and 1.978Mbp from Unicycler's output. However, the number of circular sequences detected by Unicycler was one more than the other (2 versus 1). They were corresponding to 2 plasmids, namely IncR and repA. While the latter were recognized by both methods, the longer plasmid sequence was fragmented running npGraph. Similar to the previous data set, there were around 14Kbp of data were unable to be finished by the assemblers.

Finally, assembly for Klebsiella oxytoca saw fragmented chromosome using Unicycler but it was a fully complete contig for npGraph with 6.156Mbp of size. The two assemblers shared 3 common circular sequences where two of them were confirmed plasmids. The first identical sequences represented a megaplasmid ($\simeq 113 \mathrm{Kbp}$) with two variations of IncFII's origin of replication DNA being identified. The other agreed plasmid were IncL/M with 76Kbp of length. Particularly, there was one circular contig with length greater than 100Kbp but returned no hits to the plasmid database, suggesting the importance of de novo replicon assembly in combination with further interrogations. Unicycler detected another megaplasmid of size 108.4Kbp which was fractured by npGraph. The dissolution was also observed in npGraph for the final contig of length 11.6Kbp where it failed to combine two smaller sequences into one.

In addition to what presented in Table 2, dot plots for the pair-wise alignments between the assembly contigs were generated and can be found in Appendix Figure 1. Interestingly, beside all other agreements, there was a structural difference using two methods for *E. cloacae* CAV1411 genome assembly. This was caused by the inconsistency of a fragment's direction on the final output contigs. However, when compare to a reference genome of the same bacteria strain (GenBank ID: CP011581.1 [21]), contigs generated by npGraph demonstrated a consistent alignment which was not the case for Unicycler results (Appendix Figure 2). Even though this might reflect a novel variation between bacterial samples of the same strain, it was more likely a mis-assembly by using Unicycler.

Overall, by testing with synthetic and real data, npGraph proved to be able to generate assemblies of comparative quality compared to other powerful batch-mode hybrid assemblers, such as hybridSPAdes or Unicycler. Furthermore, similar to npScarf, it has the advantage in term of supporting real-time assembly. The next section will address this utility and the interactive GUI bundled in npGraph.

Assembly performance on streaming data

Figure 2 demonstrates the real-time mode performance of npScarf and npGraph via N50 statistics during the assembly of 4 example data sets. This experiment would discover the rate of completing genome assemblies of the new method, set aside the accuracy aspect which had already been discussed previously. npScarf_wag basically scaffolds the pre-assembly contigs in the same manner with the original version thus was not discussed here.

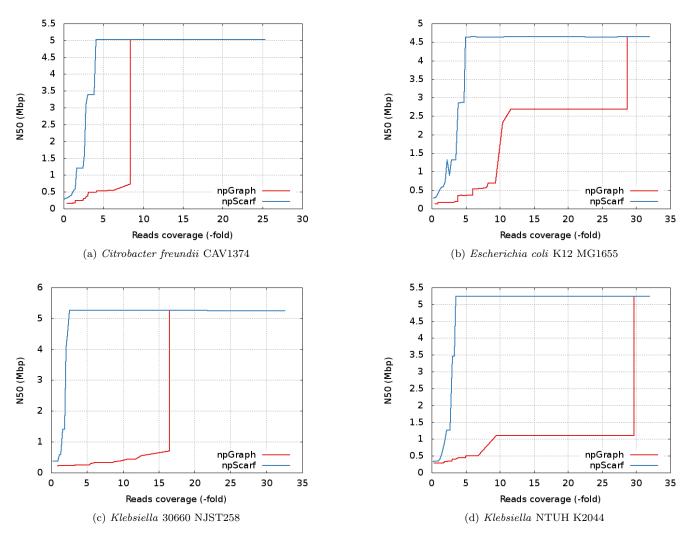


Figure 2: N50 statistics of real-time scaffolding by npScarf versus npGraph.

As can be observed from all the plots, npGraph and npScarf both converged to the same ultimate completeness but with different paces and patterns. Apparently it took more data for npGraph to finish the same genome than the other. The reason stems from the fact that the new algorithm implemented a more 'conservative' approach of bridge construction with at least 3 supporting long-reads for each to prevent any potential mis-bridging. Unlike npScarf when the connections could be undone and rectified later if needed, a bridge in npGraph will remain unchanged once created. The plot for $E.\ coli$ data clarifies this behaviour when a fluctuation can be observed in npScarf assembly at \simeq 3-folds data coverage. On the other hand, the N50 length of npGraph is always a monotonic increasing function. The sharp jumping patterns suggested that the linking information from long-read data had been stored and exploited at certain time point decided by the algorithm. Once a unique path has been determined, the bridge can be formed to connect the fragments together into longer sequences.

Metagenomics assembly on mock community

We further employed npGraph on mock community data to study the performance of our method in metagenomics co-assembly problem. In this application, sequencing data (including both short and long reads) from mixtures of ten microbial species of ZymoBIOMICS Microbial Community Standards [22] were used as input for npGraph. The total genome size was estimated as 61.96 Mbp. There were two settings for the input depending on the distribution of cell abundances in the mixture itself, namely even and log population. On the other hand, 8 out of 10 genomes being sequenced were reconstructed by using PacBio sequencing (RSII and Sequel) previously [23], including Bacillus subtills, Enterococcus faecalis, Escherichia coli, Listeria monocytogenes, Pseudomonas aeruginosa, Saccharomyces cerevisiae,

Salmonella enterica and Staphylococcus aureus. We evaluated the coassembly results by running metaQUAST given 8 PacBio assembly as references.

Table 3: Assembly improvement, in terms of NGA50 statistics, from metaSPAdes to npGraph contigs on two mock communities ZymoLog and ZymoEven [22]. The statistics were generated by metaQUAST v3.2 with 8 (out of 10) available PacBio isolate assemblies used as reference [23].

| Community | Zymol | Even | ZymoLog | |
|------------------|------------|-----------|------------|---------|
| Community | metaSPAdes | npGraph | metaSPAdes | npGraph |
| B. subtilis | 23,386 | 382,368 | 35,390 | 433,078 |
| E. coli | 34,776 | 1,108,989 | _ | _ |
| E. faecalis | 23,340 | 217,908 | _ | _ |
| L. monocytogenes | 26,480 | 520,012 | 23, 146 | 130,284 |
| P. aeruginosa | 59,372 | 1,753,658 | 161,816 | 444,495 |
| S. aureus | 26,058 | 175,908 | _ | _ |
| S. cerevisiae | _ | _ | _ | _ |
| S. enterica | 33,363 | 4,242,458 | _ | _ |

To run npGraph on the metagenomics data set, we firstly augmented binning information from using metaBAT [24] on the Illumina raw reads, before applying our method to the assembly graph generated by metaSPAdes. The default parameter setting was remained as it was for isolate assembly.

In terms of Illumina data, Even community had been sequenced by MiSeq platform which generated about 43-fold coverage while the Log community's short-read data had been obtained from an Illumina HiSeq 1500, for about 156X coverage. Even though the total amount of base coverage from the latter was almost four-times richer than the former, its metaSPAdes assembly quality was lesser. This happened due to the fact of under-presented microbial cells from rare species in the Log population that require much more input for their reads to be sequenced, resulting in significant smaller size of assembly contigs and more fragmented assembly graph (Supplementary Figure 3). The assembly size for the two population are approximately 41 Mbp (66%) and 22 Mbp (36%). During pre-processing step, npGraph disregarded nodes which represent short, unconnected and extremely-low-coverage contigs which were indistinguishable from sequencing errors, artifacts or the actual rare species' genomes without additional works.

Despite of the input graph quality, table 3 shows the assembly improvement in terms of NGA50 after running npGraph on the metaSPAdes initial graph. As expected from better quality assembly graph, the results for the Even community indicated significant more complete genomes recovered. There were 7 isolate genomes had been identified for this community, compared to only 3 from the more complicated log population. npGraph had been able to resolve the assembly graph efficiently for Even community, with the maximum NGA50 improvement for S. enterica boosted from 33 Kbp to 4.2 Mbp. On the other hand, genomes from the Log community witnessed increasing length of aligned contigs as well, but not as distinct as for the balanced colony. The longest NGA50 contigs belongs to P.aeruginosa of 445 Kbp, however, the counterpart from the Even community was 4-fold than that, at 1.75 Mbp. The only exception was B. subtilis, where npGraph can only resolved 382 Kbp correct length from the zymo even while the respective statistics was 433 Kbp for the zymo log. However for this isolate, the initial metaSPAdes assembly of the former was slightly better compared to the latter's.

Conclusion

Due to the limits of current sequencing technology, application of hybrid methods should remain a common practice in whole genome assembly for the near future. On the other hand, the ONT platforms are evolving quickly with significant improvement in terms of data accuracy and yield, however, the sequencing cost per base is still high. Beside, the real-time property of this technology has not been sufficiently exploited to match its potential benefits. npScarf had been introduced initially to address these issues, however, the accuracy of the assembly output was affected by its greedy alignment-based scaffolding approach. Here we present npGraph, a streaming hybrid assembly method working on the DBG assembly graph that is able to finish short-read assembly in real-time while minimizing the errors and mis-assemblies drastically.

Compared to npScarf, npGraph algorithm employs a less greedy approach based on graph traversal. This might reduce the bridging rate when the linking conditions become more strict, but the concurrent results reported are more reliable. The performance of npGraph is comparable to Unicycler while consuming much less computational resources so that it can work on streaming mode. Also, the integrated GUI allows users to visualize its animated output in a more efficient way.

In the very first attempt to run real-time assembly on metagenomics data, npGraph proved that its method can adapt to scaled-up data and complexity. The assembler was able to handle the De Bruijin assembly graph from Illumina data generated by metaSPAdes and simplify it using a minimal input stream of long reads. The result has shown more complete isolate genomes reconstructed out of the graph, but the overall communities' genome coverage were dropped

with several strains omitted comparing to the reference. The issue is caused by the shortage of short-read sequencing input to cover underpresented species in the mixture, especially for the Log community.

As a hybrid assembler, similar to Unicycler, npGraph relies on the initial assembly graph to generate the final assembly. The algorithm operates on the assumption of a high quality assembly from a well-supplied source of short-read data for a decent assembly graph to begin with. It then consumes a just-enought amount of data from a streaming input of nanopore reads to resolve the graph. Finally, extra pre-processing and comprehensive binning on the initial graph could further improve the performance of the streaming assembler.

Methods

The work flow of npGraph mainly consists of 3 stages: (1) assembly graph preprocessing; (2) graph resolving and simplifying; (3) postprocessing and reporting results. The first step is to load the graph of Illumina contigs and retrieve their metadata which are helpful for the next steps, e.g. binning and multiplicity estimation. The second step works on the processed input and augmented information from the previous one. In combination with path inducing from long reads, the assembly graph is then traversed and resolved in real-time. Finally, the graph is subjected to the last attempt of resolving and cleaning, as well as output the final results. The whole process can be managed by using either command-line interface or GUI. Among three phases, only the first one must be performed prior to the MinION sequencing process in a streaming setup. The algorithm works on the assembly graph of Illumina contigs, so the terms contigs and nodes if not mentioned specifically, would be used interchangable throughout this context.

Contigs binning

Contigs from each completed genome are expected to be assigned to an unique group, or *bin*, that would represent the final assembly unit, *e.g.* chromosome, plasmids, or even particular species genome in a metagenomic community. As a result, the binning phase would assist the multiplicity estimation submodule that can differentiate repetitive contigs from unique ones.

Each contig is embeded in a single node in the assembly graph and an edge between two nodes indicates their overlap (link) properties. This step is to cluster the biggest nodes (contigs longer than 10Kbp) into different sets, namely *core* groups, based on the their degree (number of connections) and coverage values. DBSCAN clustering algorithm [25] is applied for this task by default. The rationale is to approximate a coverage value of an extremely long contig (which can be splitted into more than $10,000 \ k\text{-mers}$) to be a sampled mean of a Poisson distribution (of k-mers count). The metric is a distance function based on Kullback-Leibner divergence [26], or relative entropy, of two Poisson distributions.

Assuming there are 2 Poisson distributions P_1 and P_2 with density functions

$$p_1(x, \lambda_1) = \frac{e^{-\lambda_1} \lambda_1^x}{\Gamma(x+1)}$$

and

$$p_2(x, \lambda_2) = \frac{e^{-\lambda_2} \lambda_2^x}{\Gamma(x+1)}$$

The Kullback-Leibner divergence from P_2 to P_1 is defined as:

$$D_{KL}(P_1||P_2) = \int_{-\infty}^{\infty} p_1(x) \log \frac{p_1(x)}{p_2(x)} dx$$

or in other words, it is the expectation of the logarithmic difference between the probabilities P_1 and P_2 , where the expectation is taken with regard to P_1 . The log ratio of the density functions is

$$\log \frac{p_1(x)}{p_2(x)} = x \log \frac{\lambda_1}{\lambda_2} + \lambda_2 - \lambda_1$$

take expectation of this expression with regard to P_1 with mean λ_1 we have

$$D_{KL}(P_1||P_2) = \lambda_1 \log \frac{\lambda_1}{\lambda_2} + \lambda_2 - \lambda_1$$

The metric we used is the distance defined as

$$D(P_1,P_2) = \frac{D_{KL}(P_1||P_2) + D_{KL}(P_2||P_1)}{2} = \frac{1}{2}(\lambda_1 - \lambda_2)(\log \lambda_1 - \log \lambda_2)$$

We implemented a simple binning algorithm based on the clustered contigs, the graph topology as well as statistics calculated by length and coverage of each contigs. Additional binning step is taken place in real-time using the long reads as well. In this context, the repetition or uniquess of ambigous nodes are determined with sufficient supporting evidence from the long-spanning reads. Generally, the algorithm performs well for isolate or simple simulated metagenomics, but

ineffective for complicated community. In that case, external binning tools can be employed for more comprehensive binning task and the results can be augmented to npGraph input. If external binning algorithm is employed, the resulting output must be converted into a text file that specifies the corresponding bin of every contigs, just like output from MetaBAT. By that, each line of the file would be: $< contig_ID > < bin_ID > where bin_ID = 0$ indicates unspecified binned contigs.

Multiplicity estimation

Due to the possible divergence of sequencing coverage relative to the real abundance of sequences, especially for the shorter contigs, an optimization step is carried out to alleviate this issue. The re-estimation is basically carried out by following two steps.

1. From nodes coverage, estimate edges' value by quadratic unconstrained optimization of the least-square function:

$$\frac{1}{2} \sum_{i} l_{i} ((\sum e_{i}^{+} - c_{i})^{2} + (\sum e_{i}^{-} - c_{i})^{2})$$

where l_i and c_i is the length and coverage of a node i in the graph;

 $\sum e_i^+$ and $\sum e_i^-$ indicates sum of the values of incoming and outgoing edges from i respectively. The above function and be rewritten as:

$$f(x) = \frac{1}{2}x^T Q x + b^T x + r$$

and then being minimized by using gradient-based method.

2. Update nodes' coverage based on itself and its neighbor edges' measures.

The calibration is iterative until no further improvements are made or a threshold loop count is reached. The coverage measures of nodes (which represent contigs) are propated throughout the graph via connecting edges for calibrations prior to the multiplicity estimation.

Based on the coverage values of all the edges and the graph's topology, we induce the copy numbers of every significant nodes (long contigs) in the final paths. For each node, this could be done by investigating its adjacent edges and answering the questions of how many times it should be visited, from which abundance groups. Multiplicities of insignificant nodes (of sequences with length less than 1,000 bp) can be estimated in the same way but usually with less confident due to more complicated connections and greater variation of coverage values. For that reason, in npGraph's algorithm, they are only used as augmented information to calculate likelihood scores of candidate paths containing corresponding nodes.

Building bridges in real-time

Bridge is the data structure designed for tracking the possible connections between two anchored nodes (of unique contigs) in the assembly graph. A bridge must start from a unique contig, or *anchor* node, and end at another when completed. Located inbetween are nodes known as *steps* and distances between them are called *spans* of the bridge. Stepping nodes are normally repetitive contigs and indicative for a path finding operation later on. In a complicated assembly graph, the more details the bridge, *a.k.a.* more steps inbetween, the faster and more accurate the linking path it would resolve. A bridge's function is complete when it successfully return the ultimate linking path between 2 anchors.

The real-time bridging method considers the dynamic aspect of multiplicity measures for each node, meaning that a n-times repetitive node might become a unique node at certain time point when its (n-1) occurrences have been already identified in other distinct unique paths. Furthermore, the streaming fashion of this method allows the bridge constructions (updating steps and spans) to be carried out progressively so that assembly decisions can be made immediately after having sufficient supporting data. A bridge in npGraph has several completion levels. When created, it must be rooted from an $anchor\ node$ which represents a unique contig (level 1). A bridge is known as fully complete (level 4) if and only if there is a unique path connecting its two anchor nodes from two ends.

At early stages (level 1 or 2), a bridge is constructed progressively by alignments from long reads that spanning its corresponding anchor(s). In an example from Figure 3, bridges from a certain anchor (highlighted in red) are created by extracting appropriate alignments from incoming long reads to the contigs. Each of the steps therefore is assigned a weighing score based on its alignment quality. Due to the error rate of long reads, there should be deviations in terms of steps found and spans measured between these bridges, eventhough they represent the same connection. A continuous merging phase, as shown in the figure, takes advantage of a pairwise Needleman-Wunsch dynamic programming to generate a consensus list based on weight and position of each of every stepping nodes. The spans are calibrated accordingly by averaging out the distances. On the other hand, the score of the merged steps are accumulated over time as well. Whenever a consensus bridge is anchored by 2 unique contigs at both ends and hosting a list of steps with sufficient coverage, it is ready for a path finding in the next step.

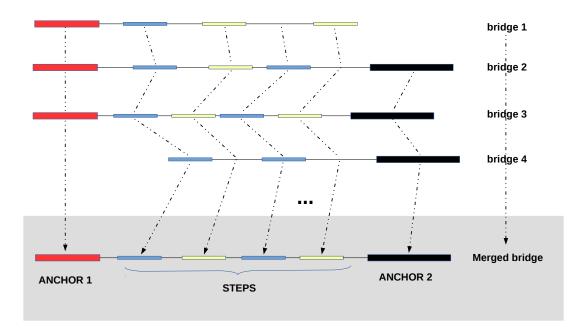


Figure 3: Bridge merging progressively in real-time. Sequencing long reads induce alignments to the contigs where new bridges are created respectively. Bridges sharing same anchors can be merged together to form the ultimate, more comprehensive bridge (with more step nodes and better approximation of spans between them).

Path finding algorithm

Given a bridge with 2 anchors, a path finding algorithm is invoked to find all candidate paths between them. Each of these paths is given a score of alignment-based likelihood which are updated immediately as long as there is an appropriate long read being generated by the sequencer. As more nanopore data arrives, the divergence between candidates' score becomes greater and only the top-scored ones are kept for the next round. We implement a modified stack-based version utilizing Dijkstra's shortest path finding algorithm [27] to reduce the search space when using Depth-First Search.

Due to false alignments from shorter contigs to the long reads, not all of the reported step nodes are neccessary to be appeared in the ultimate path resolved by the bridge. In most cases, the accumulated score of each step indicates its likelihood to be the true component of the final solution. For that reason, a strategy similar to binary searching is employed to find a path across 2 anchors of a bridge as shown in Algorithm 2.

Before that, we define Algorithm 1 to demonstrates the path finding algorithm for two nodes given their estimated distance. In which, function $\mathtt{shortestTree}(\overrightarrow{vertex}, distance) : (V, Z) \to V^n$ from line 3 of the algorithm's pseudo code builds a shortest tree rooted from \overrightarrow{v} , following its direction until a distance of approximately d (with a tolerance regarding nanopore read error rate) is reached. This task is implemented based on Dijkstra algorithm. This tree is used on line 4 and in function includedIn() on line 19 to filter out any node or edge with ending nodes that do not belong to the tree

Basically, the algorithm keeps track of a stack that contains sets of candidate edges to discover. During the traversal, a variable d is updated as an estimation for the distance to the target. A hit is reported if the target node is reached with a reasonable distance i.e. close to zero, within a given tolerance (line 21). A threshold for the traversing depth is set (150) to ignore too complicated and time-consuming path searching.

Note that the length() functions for node and edge are totally different. While the former returns the length of the sequence represented by the node, *i.e.* contig from short-read assembly, the latter is usually negative because an edge models a link between two nodes, which is normally an overlap (except for composite edges). For example, in a k-mers SPAdes assembly graph, the value of an edge is -k + 1.

In many cases, due to dead-ends, there not always exist a path in the assembly graph connecting two anchors as suggested by the alignments. In this case, if enough long reads coverage (20X) are met, a consensus module is invoked and the resulting sequence is contained in a *pseudo* edge.

Graph simplification in real-time

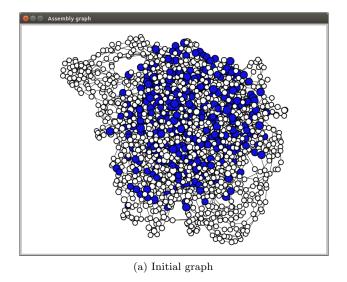
³⁰ npGraph resolves the graph by reducing its complexity perpetually using the long reads that can be streamed in real-time. Whenever a bridge is finished (with a unique linking path), the assembly graph is *transformed* or *reduced* by replacing its unique path with a composite edge and removing any unique edges (edges coming from unique nodes) along the path. The assembly graph would have at least one edge less than the original after the reduction. The nodes located on the reduced path, other than 2 ends, also have their multiplicities subtracted by one and the bridge is marked as finally resolved without any further modifications.

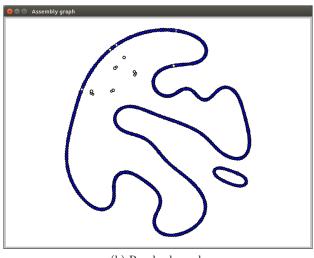
Algorithm 1: Pseudo-code for finding paths connecting 2 nodes given their estimated distance.

```
Data: Assembly graph G\{V, E\}
    Input: Pair of bidirected nodes \overrightarrow{v_1}, \overrightarrow{v_2} and estimated distance d between them
    Output: Set of candidate paths connecting \overrightarrow{v_1} to \overrightarrow{v_2} with reasonable distances compared to d
 1 Function DFS (\overrightarrow{v_1}, \overrightarrow{v_2}, d):
        P:=new List()
 2
        M:=\mathtt{shortestTree}(\overrightarrow{v_2},d)
                                                                                               // build shortest tree from \overrightarrow{v_2} with range d
 3
        if M.contain(\overrightarrow{v_1}) then
 4
             S:=\text{new } Stack()
                                                                                                       // stack of sets of edges to traverse
 5
             edgesSet := getEdges(\overrightarrow{v_1})
                                                                                                  // get all bidirected edges going from \overrightarrow{v_1}
 6
             S.push(edgesSet)
 7
             p := \text{new } Path(\overrightarrow{v_1})
                                                                                                           // init a path that has \overrightarrow{v_1} as root
             while true do
                 edgesSet := S.peek()
10
                 if edgesSet.isEmpty() then
11
                      if p.size() \leq 1 then
                       break
                                                                                // stop the loop when there is no more edge to discover
13
                      S.pop()
14
                      d+=p.peekNode.length() + p.popEdge().length()
15
                  else
16
                      curEdge := edgesSet.remove()
17
                      \overrightarrow{v}:=curEdge.getOpposite(p.peekNode())
18
                      S.push(getEdges(\overrightarrow{v}).includedIn(M))
19
                      p.add(curEdge)
20
                      if reach \overrightarrow{v_2} with reasonable d then
21
                         P.add(p)
22
                      d = \overrightarrow{v}.length() + curEdge.length()
23
        return P
24
```

Algorithm 2: Recursive binary bridging to connect 2 anchor nodes.

```
Data: Assembly graph G\{V, E\}
  Input: Brigde B: \{\overrightarrow{v_0}, ... \overrightarrow{v_k}, ..., \overrightarrow{v_n}\} with \overrightarrow{v_0} and \overrightarrow{v_n} are two anchors, \{\overrightarrow{v_k}\}, k = 1 \dots (n-1) are steps inbetween
   Output: Set of candidate paths connecting \overrightarrow{v_0} to \overrightarrow{v_2} that maximize the likelihood of the step list.
1 Function BinaryBridging(B):
       /* search for the contig with maximum score from the step list (two ends excluded)
       m := \operatorname{argmax}_{k}(\overrightarrow{v_{k}}.score())
2
       /* if there is no step inbetween, run path finding algorithm above directly and return the result
       if M.size() \equiv 2 then
3
        | return DFS(B.start(), B.end().B.distance())
4
       /* divide the original bridge B into 2 bridges by v_m\colon \ BL and BR
       BL := \{B.start(), ..., \overrightarrow{v_m}\}
5
       BR := \{\overrightarrow{v_m}, ..., \overrightarrow{B}.end()\}
       /* Return the join of running recursive function on two sub-bridges
       return BinaryBridging(BL) \bowtie BinaryBridging(BR)
```





(b) Resolved graph

Figure 4: Assembly graph of Shigella dysenteriae Sd197 synthetic data being resolved by npGraph and displayed on the GUI Graph View. The SPAdes assembly graph contains 2186 nodes and 3061 edges, after the assembly shows 2 circular paths representing the chromosome and one plasmid.

Figure 3 presents an example of the results before and after graph resolving process in the GUI. The result graph, after cleaning, would only report the significant connected components that represents the final contigs. Smaller fragments, even unfinished but with high remaining coverage, are also presented as potential candidates for further downstream analysis. Further annotation utility can be implemented in the future better monitoring the features of interests as in 5 npScarf.

Result extraction and output

npGraph reports assembly result in real-time by decomposing the assembly graph into a set of longest straight paths (LSP), each of the LSP will spell a contig in the assembly report. The final assembly output contains files in both FASTA and GFAv1 format (https://github.com/GFA-spec/GFA-spec). While the former only retains the actual genome 10 sequences from the final decomposed graph, the latter output file can store almost every properties of the ultimate graph such as nodes, links and potential paths between them.

A path $p = \{v_0, e_1, v_1, \dots, v_{k-1}, e_k, v_k\}$ of size k is considered as straight if and only if each of every edges along the path $e_i, \forall i = 1, ..., k$ is the only option to traverse from either v_{i-1} or v_i , giving the transition rule. To decompose the graph, the tool simply mask out all incoming/outgoing edges rooted from any node with in/out degree greater than 1 as 15 demonstrated in Figure 2. These edges are defined as branching edges which stop straight paths from further extending.

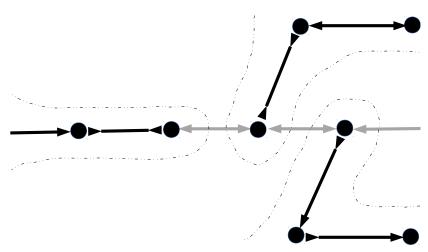


Figure 5: Example of graph decomposition into longest straight paths. Branching edges are masked out (shaded) leaving only straight paths (bold colored) to report. There would be 3 contigs extracted by traversing along the straight paths here.

The decomposed graph is only used to report the contigs that can be extracted from an assembly graph at certain time point. For that reason, the branching edges are only masked but not removed from the original graph as they

would be used for further bridging.

Other than that, if GUI mode is enabled, basic assembly statistics such as N50, N75, maximal contigs length, number of contigs can be visually reported to the users in real-time beside the Dashboard. The progressive simplification of the assembly graph can also be observed at the same time in the Graph view.

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