

First model considered for adipocytes “growing”.

T triglycerides (= lipids) in the blood
 $u(t, r)$ adipocytes number at time t of radius r (containing l lipids)
The link between r and l is the following,

$$V_l l = \frac{4}{3} \pi r^3 - V_0$$

with $V_0 = \frac{4}{3} \pi r_0^3$ the minimum volume of adipocytes (r_0 is the minimum radius), so
 $\frac{dl}{dt} = \frac{4\pi}{V_l} \frac{dr}{dt} r^2$.

Model the lipogenesis and the lipolysis (fluxes of triglycerides l) :

$$\frac{dl}{dt} = ar^2 \frac{T}{T + T_\theta} \frac{r_\theta^n}{r^n + r_\theta^n} - (B + br^2) \frac{l}{l + \ell_\theta}$$

we rewrite with the variable r :

$$\frac{dr}{dt} = a \frac{V_l}{4\pi} \frac{T}{T + T_\theta} \frac{r_\theta^n}{r^n + r_\theta^n} - \frac{V_l}{4\pi} \frac{(B + br^2)}{r^2} \frac{\frac{4}{3} \pi r^3 - V_0}{\frac{4}{3} \pi r^3 - V_0 + V_l \ell_\theta} = \tau(r, T)$$

From these fluxes, the dynamics of the number of adipocytes u is described by

$$\partial_t u(t, r) + \partial_r (\tau(r, T) u) - D \partial_r^2 u = 0$$

with D a diffusion coefficient.

The intracellular quantity of triglycerides is $U(t) = \int l \rho_u dl$ with ρ_u adipocytes density. The total amount of triglycerides is assumed constant over time : $\frac{d}{dt}(T(t) + U(t)) = 0$ and $\frac{dT}{dt} = -\frac{dU}{dt}$ and we denote by Tg_0 the initial quantity of triglycerides so that $T(t) + U(t) = Tg_0$ for every time t .

boundary/initial conditions. $u(0, r) = \text{Gaussian density (minimum} = r_0)$, first test : unimodal (Q : can we recover the bimodal distribution that is observed).

$$T(t) = Tg_0 - U(t)$$

$$(\tau(r, T) u(t, r) - D \partial_r u(t, r))|_{r_{max}} = 0$$

Recruitment of new adipocytes. We assumed that when the level of triglycerides increases too largely, pre-adipocytes differentiate into adipocytes. This recruitment is modeled with the r_0 BC, as follows,

$$(\tau(r, T) u(t, r) - D \partial_r u(t, r))|_{r_0} = f(T)$$

with $f(T) = \alpha T$ or $f(T) = \alpha \frac{T}{(T + \kappa_\theta)}$