CS 496: Homework Assignment 5

Due: 1 May 2022, 11:59pm

# 1 Assignment Policies

Under absolutely no circumstances code can be exchanged between students from different groups. Excerpts of code presented in class can be used.

# 2 Assignment

In this assignment you are asked to extend the type-checker for the language REC with references, pairs, lists and trees. This assignment is organized in three parts:

- 1. Part 1. Add type-checking for references.
- 2. Part 2. Add type-checking for lists.
- 3. Part 3. Add type-checking for trees.

The new language including all these constructs will be called CHECKED\_PLUS.

# 3 Type-Checking References

One new grammar production, which is added to the parser for CHECKED\_PLUS, is needed for the concrete syntax of expressions.

```
\langle \mathsf{Expression} \rangle ::= ()
```

The concrete syntax of types must be extended so as to allow the typing rules described below to be implemented. Two new productions are added, the one for unit and for ref:

```
<Type> ::= int

<Type> ::= bool

<Type> ::= unit

<Type> ::= ref(<Type>)

<Type> ::= <Type> -> <Type>

<Type> ::= (<Type>)
```

The typing rules are:

Note the use of the type unit to indicate that the return result of the assignment operation is not important.

#### 3.1 Task

You have to update the code for the type checker by adapting the file checker.ml so that type\_of\_expr can handle:

```
let rec type_of_expr : expr -> texpr tea_result =
  fun e ->
  match e with

4    ...
  | Unit -> failwith "Implement me!"
  | NewRef(e) -> failwith "Implement me!"
  | DeRef(e) -> failwith "Implement me!"
  | SetRef(e1,e2) -> failwith "Implement me!"
  | BeginEnd([]) -> failwith "Implement me!"
  | BeginEnd(es) -> failwith "Implement me!"
```

Here are some examples:

```
# chk "let x = newref(0) in deref(x)";;
   - : texpr Checked.ReM.result = Ok IntType
   # chk "let x = newref(0) in x";;
   - : texpr Checked.ReM.result = 0k (RefType IntType)
   # chk "let x = newref(0) in setref(x,4)";;
   - : texpr Checked.ReM.result = Ok UnitType
   # chk "newref(newref(zero?(0)))";;
   - : texpr Checked.ReM.result =Ok (RefType (RefType BoolType))
   # chk "let x = 0 in setref(x,4)";;
   - : texpr Checked.ReM.result = Error "setref: Expected a reference type"
10
   # chk "begin 1;2;zero?(3) end";;
  - : texpr Checked.ReM.result = Ok BoolType
12
   # chk "begin end";;
- : texpr Checked.ReM.result = Ok UnitType
```

## 4 Lists

## 4.1 Concrete syntax

The concrete syntax for expressions should be extended with the following productions:

```
 \begin{array}{lll} <\mathsf{Expression}> & ::= & \mathrm{emptylist} <\mathsf{Type}> \\ <\mathsf{Expression}> & ::= & \mathrm{cons} \; (<\mathsf{Expression}>, <\mathsf{Expression}>) \\ <\mathsf{Expression}> & ::= & \mathrm{nullL?} \; (<\mathsf{Expression}>) \\ <\mathsf{Expression}> & ::= & \mathrm{hd} \; (<\mathsf{Expression}>) \\ <\mathsf{Expression}> & ::= & \mathrm{tl} \; (<\mathsf{Expression}>) \\ \end{aligned}
```

The concrete syntax for types includes one new production (the last one listed below):

```
<Type>
            ::=
                  int
<Type>
            ::=
                  bool
<Type>
           ::=
                  unit
<Type>
           ::= ref(<Type>)
<Type>
           ::= <Type> -> <Type>
           ::= \langle \mathsf{Type} \rangle * \langle \mathsf{Type} \rangle
<Type>
<Type>
           ::= list(<Type>)
<Type>
          ::= (\langle \mathsf{Type} \rangle)
```

The new type constructor is for typing lists. For example,

- 1. list(int) is the type of lists of integers
- 2. int -> list(int) is the type of functions that given an integer produce a list of integers.

Here are some sample expressions in the extended language. They are supplied in order to help you understand how each constructor works.

```
# chk "emptylist int";;
2 -: texpr Checked.ReM.result = Ok (ListType IntType)
# chk "cons(1, emptylist int)";;
4 -: texpr Checked.ReM.result = Ok (ListType IntType)
# chk "hd(cons(1, emptylist int))";;
6 -: texpr Checked.ReM.result = Ok IntType
# chk "tl(cons(1, emptylist int))";;
8 -: texpr Checked.ReM.result = Ok (ListType IntType)
# chk "cons(nullL?(emptylist int), emptylist int)";;
10 -: texpr Checked.ReM.result =
Error "cons: type of head and tail do not match"
12 # chk "proc(x:int) { proc (1:list(int)) { cons(x,1) } }";;
-: texpr Checked.ReM.result =
14 Ok (FuncType (IntType, FuncType (ListType IntType, ListType IntType)))
```

Here are the typing rules:

## 4.2 Typing rules

```
 \begin{array}{ll} & \Gamma \vdash e1:t & \Gamma \vdash e2:list(t) \\ \hline \Gamma \vdash emptylist & t:list(t) & \hline \Gamma \vdash cons(e1,e2):list(t) \\ \hline \frac{\Gamma \vdash e:list(t)}{\Gamma \vdash t1(e):list(t)} & \frac{\Gamma \vdash e:list(t)}{\Gamma \vdash hd(e):t} \\ \hline \frac{\Gamma \vdash e:list(t)}{\Gamma \vdash nullL?(e):bool} \end{array}
```

#### 4.3 Task

Extend the type-checker to del with the new constructs:

```
let rec type_of_expr : expr -> texpr tea_result = function
...
| EmptyList(t) -> failwith "Implement me!"
| Cons(he, te) -> failwith "Implement me!"
| IsNullL(e) -> failwith "Implement me!"
| Hd(e) -> failwith "Implement me!"
| Tl(e) -> failwith "Implement me!"
```

## 5 Trees

## 5.1 Concrete syntax

The concrete syntax for expressions should be extended with the following productions:

```
 \begin{array}{lll} <\mathsf{Expression}> & ::= & \mathrm{emptytree} < \mathsf{Type}> \\ <\mathsf{Expression}> & ::= & \mathrm{node} \ (<\mathsf{Expression}>, <\mathsf{Expression}>, <\mathsf{Expression}>) \\ <\mathsf{Expression}> & ::= & \mathrm{nullT?} \ (<\mathsf{Expression}>) \\ <\mathsf{Expression}> & ::= & \mathrm{getData} \ (<\mathsf{Expression}>) \\ <\mathsf{Expression}> & ::= & \mathrm{getLST} \ (<\mathsf{Expression}>) \\ <\mathsf{Expression}> & ::= & \mathrm{getRST} \ (<\mathsf{Expression}>) \\ \end{aligned}
```

The concrete syntax for types includes one new production (the last one listed below):

```
<Type>
              int
         ::=
<Type>
         ::=
              bool
<Type>
              unit
         ::=
<Type>
              ref(<Type>)
         ::=
<Type>
              <Type> -> <Type>
         ::=
              <Type> * <Type>
<Type>
         ::=
<Type>
         ::=
              list(<Type>)
<Type>
         ::=
              tree (<Type>)
<Type>
              (<\mathsf{Type}>)
         ::=
```

Here is a sample program that assumes you have implemented the append operation on lists. Note that you will not be able to run this program unless you have extended the interpreter to deal with lists and trees. This assignment only asks you to write the typechecker, not the interpreter. You are, of course, encouraged to write the interpreter too!

Here is another example. It should type-check with result Ok (ListType IntType) and evaluate to Ok (ListVal [NumVal 1; NumVal 2; NumVal 3]):

## 5.2 Typing rules

#### 5.3 Task

Extend the type-checker to del with the new constructs:

```
let rec type_of_expr : expr -> texpr tea_result = function
...
| EmptyTree(t) -> failwith "Implement me!"
| Node(de, le, re) -> failwith "Implement me!"
| IsNullT(t) -> failwith "Implement me!"
| GetData(t) -> failwith "Implement me!"
| GetLST(t) -> failwith "Implement me!"
| GetRST(t) -> failwith "Implement me!"
```

Here are some sample expressions in the extended language. They are supplied in order you to help you understand how each construct works.

```
# chk "emptytree int";;
- : texpr Checked.ReM.result = Ok (TreeType IntType)
# chk "nullT?(node(1, node(2, emptytree int, emptytree int), emptytree int))";;
- : texpr Checked.ReM.result = Ok BoolType
# chk "getData(node(1, node(2, emptytree int, emptytree int), emptytree int))";;
- : texpr Checked.ReM.result = Ok IntType
# chk "getLST(node(1, node(2, emptytree int, emptytree int), emptytree int))";;
- : texpr Checked.ReM.result = Ok (TreeType IntType)
```

## 6 Submission instructions

Submit a file named HW5.zip through Canvas which includes all the source files from the original stub. Your grade will be determined as follows, for a total of 100 points:

Section	Grade
References	30
List	35
Tree	35