

# Lecture 9

Name: Harsh Sanjay Roniyar

Roll Number: 22B3942

---

## Convex Functions

Convex Functions are defined mathematically, as follows-

$$\alpha L(w_1) + (1 - \alpha)L(w_2) \geq L(\alpha w_1 + (1 - \alpha)w_2),$$

where,  $\alpha$  is between 0 and 1.

In L2 regularization, we work under the assumption that  $L(w)$  is convex.

Adding two convex functions, with a positive multiplier for each, the resulting function is also a convex function. (Jensen's Inequality).

## Gradient Descent Algorithm

A very important technique in all of modern AI-ML tasks.

Basic intuition - Even if we can't calculate the exact minimum, we can still get closer to the minimum iteratively in small steps.

Randomly initialize  $w$

Until we reach terminal condition.

$$w_{\text{new}} \leftarrow w_{\text{old}} - \eta \nabla L_w$$

$$w_{\text{old}} \leftarrow w_{\text{new}}$$

$\eta$  is the learning rate (or step size) and needs to be tuned properly in real-world systems.

Perform this in all components of  $w$  (dimension of  $w$ ).

Now, the terminal conditions could be one (or a combination) of the following -

1. `max_iter` has been reached
2.  $L(w_o) - L(w_n) < \epsilon$
3.  $(w_o - w_n)^T (w_o - w_n) < \delta$

Since, from the last lecture [Lecture 8](#), we have the expressions for  $E_D$  and  $E_W$ , hence we can compute the gradient for those expressions and we would get the update-iterate step.