

### 3.lab\_session

September 19, 2023

Import relevant packages here.

```
[1]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
```

Load the data and verify it is loaded correctly.

Print it (head, tail, or specific rows, choose a sensible number of rows).

Compare it to the source file.

```
[8]: data = pd.read_csv('cf_data.csv')

print(data.head())
print(data.tail())
```

	dv	s	a
0	-0.743240	53.5427	1.242570
1	-0.557230	53.6120	1.777920
2	-0.454769	53.6541	0.544107
3	-0.525396	53.7030	-0.294755
4	-0.601285	53.7592	-0.290961

  

	dv	s	a
73903	5.19874	116.139	-0.795081
73904	5.10428	115.627	-0.314263
73905	5.13764	115.118	0.232283
73906	5.15348	114.599	0.262078
73907	5.25868	113.112	-0.612440

In the ensuing, you will use numpy.

Let's create a grid for the values to plot. But first create two arrays named dv and s using numpy.linspace that hold the grid values at the relevant indices in their respective dimension of the grid.

Create a grid named a with zeros using numpy.zeros in to which calculated acceleration values can be stored. Let the grid span:

Speed difference dv [m/s]

From -10 till 10

With 41 evenly spaced values

```
</li>
<li>Headway <code>s</code> [m]
  <ul>
    <li>From 0 till 200</li>
    <li>With 21 evenly spaced values</li>
  </ul>
</li>
```

```
[3]: dv = np.linspace(-10, 10, 41)
      s = np.linspace(0, 200, 21)
      a = np.zeros((len(s), len(dv)))
```

Create from the imported data 3 separate numpy arrays for each column dv, s and a. (We do this for speed reasons later.)

Make sure to name them differently from the arrays that belong to the grid as above.

You can access the data of each column in a DataFrame using data.xxx where xxx is the column name (not as a string).

Use the method to\_numpy() to convert a column to a numpy array.

```
[4]: DV = data['dv'].to_numpy()
      S = data['s'].to_numpy()
      A = data['a'].to_numpy()
```

Create an algorithm that calculates all the acceleration values and stores them in the grid. The algorithm is described visually in the last part of the lecture. At each grid point, it calculates a weighted mean of all measurements. The weights are given by an exponential function, based on the 'distance' between the grid point, and the measurement values of dv and s. To get you started, how many for-loops do you need? For this you will need math. Use an epsilon of 1.5m/s and a sigma of 30m. Warning: This calculation may take some time. So:

Print a line for each iteration of the outer-most for-loop that shows you the progress.

Test your code by running it only on the first 50 measurements of the data.

```
[5]: epsilon = 1.5
      sigma = 30
      for i in range(len(s)):
          for j in range(len(dv)):
              weights = np.exp(-((DV - dv[j]) ** 2 + (S - s[i]) ** 2) / (2 * sigma ** 2))
              a[i, j] = np.sum(weights * A) / np.sum(weights)
              print(f"Progress: Row {i+1}/{len(s)}, Column {j+1}/{len(dv)}")

      a_test = np.zeros((len(s), len(dv)))

      for i in range(len(s)):
```

```

for j in range(len(dv)):
    weights = np.exp(-(DV[:50] - dv[j]) ** 2 + (S[:50] - s[i]) ** 2) / (2 *
↪ sigma ** 2))
    a_test[i, j] = np.sum(weights * A[:50]) / np.sum(weights)

```

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The following code will plot the data for you. Does it make sense when considering:

Negative (slower than leader) and positive (faster than leader) speed differences?

Small and large headways?

```
[7]: X, Y = np.meshgrid(dv, s)
      axs = plt.axes()
      p = axs.pcolor(X, Y, a, shading='nearest')
      axs.set_title('Acceleration [m/s/s]')
      axs.set_xlabel('Speed difference [m/s]')
      axs.set_ylabel('Headway [m]')
      axs.figure.colorbar(p)
      axs.figure.set_size_inches(10, 7)
```

