Lab 15 - Multivariate Regression & Interpretation

Your name here November 30, 2017

Complete the following exercises below and include all code used to find the answers. Knit together the PDF document and commit both the Lab 15 RMD file and the PDF document to Git. Push the changes to GitHub so both documents are visible in your public GitHub repository.

1. Select a second explanatory variable from your dataset that you think has implications for the theoretical association of your focal relationship.

a. Describe the theoretical reasoning for selecting this variable.

The reason why I think the type of the crime also has a theoretical relationship with the total prison length is the amount of stereotyping in policing. Meaning that LE is more likely to police blacks.

b. What type of relationship do you think this variable has with your focal variables? Given that, what do you expect to happen to your focal relationship when it is added to the model?

I think this variable has a confounding relationship with my race variable is because while this variable may increase minority in the CJS, certain types of crimes may also increase the sentence severity more than others.

c. Is it a continuous or categorical variable? What implications does this have for a multivariate regression equation?

This is a categorical variable. This affects the multivariate regression by having many different parameters, instead of just one for each variable.

d. Conduct a multivariate linear regression with this additional explanatory variable and save the model object. Print out the full results by calling summary() on your model object.

```
library(tidyverse)
## -- Attaching packages ----
## √ ggplot2 2.2.1
                        √ purrr
                                  0.2.4
## \sqrt{\text{tibble }} 1.3.4
                        √ dplyr
                                  0.7.4
## √ tidyr
             0.7.2
                        √ stringr 1.2.0
## √ readr
             1.1.1
                        √ forcats 0.2.0
## -- Conflicts -----
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                      masks stats::lag()
# importing data
data <- read.csv("~/monitoring-federal-criminal-sentences/clean_data/merged_data/96-15.csv")
# only comparing blacks and whites and prison length less than 700 (dp and lwp above that so excluding
data2 <- data %>%
  filter(MONRACE <= 2) %>%
  filter(TOTPRISN <= 700)</pre>
race <- lm(TOTPRISN ~ factor(MONRACE), data2)</pre>
summary(race)
##
## Call:
```

lm(formula = TOTPRISN ~ factor(MONRACE), data = data2)

```
##
## Residuals:
##
      Min
              1Q Median
  -74.34 -36.16 -17.16 15.84 654.84
##
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    41.15506
                                0.06697
                                          614.6
                                                   <2e-16 ***
## factor(MONRACE)2 33.18971
                                0.13133
                                          252.7
                                                   <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 60.81 on 1114262 degrees of freedom
## Multiple R-squared: 0.05421,
                                    Adjusted R-squared: 0.05421
## F-statistic: 6.386e+04 on 1 and 1114262 DF, p-value: < 2.2e-16
crime_race <- lm(TOTPRISN ~ factor(MONRACE) + factor(TYPE), data2)</pre>
summary(crime_race)
##
## Call:
## lm(formula = TOTPRISN ~ factor(MONRACE) + factor(TYPE), data = data2)
##
## Residuals:
##
              1Q Median
                            3Q
                                  Max
  -96.70 -29.28 -11.96
##
                        13.96 672.96
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                     23.0370
                                 0.1192
                                         193.34
                                                   <2e-16 ***
## factor(MONRACE)2
                     20.9567
                                 0.1303
                                         160.79
                                                   <2e-16 ***
                                         295.77
## factor(TYPE)1
                     42.2451
                                 0.1428
                                                   <2e-16 ***
## factor(TYPE)2
                     39.9636
                                 0.2051
                                         194.81
                                                   <2e-16 ***
## factor(TYPE)3
                     -3.0225
                                 0.1592
                                         -18.99
                                                   <2e-16 ***
## factor(TYPE)4
                     52.7113
                                 0.3186
                                         165.47
                                                   <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 56.89 on 1114229 degrees of freedom
     (29 observations deleted due to missingness)
## Multiple R-squared: 0.1721, Adjusted R-squared: 0.1721
## F-statistic: 4.632e+04 on 5 and 1114229 DF, p-value: < 2.2e-16
```

- e. Describe the results of the multivariate analysis, highlighting:
- the apparent association between the control variable and the focal response variable
- how the focal association changed when you incorporated the control variable
- the implications of these results for your focal association

The association between race (the main variable) and the tpe of the crime is quite significant. Blacks in general receive harsher sentences (20+ compared to whites), and drug crimes (type 1) receives an additional 41 months worth of imprisonment on average!

When I included the control - the correlation between blacks and sentence length became slightly weeker, and went to drug crimes. Blacks are still very significant.

This tells me that crime type is important to account for in future models, and lumping data is not a good idea in case of crime types.

f. How well does this model fit the data? Is it an improvement over the bivariate model? Why or why not?

This is not a improvement over my bivariate data because it has a weak r-squared, and lots of bad residuals at the tail end.

2. Select any additional variables you want to incorporate into your final model. For each additional variable added to the model answer the following questions:

```
library(tidyverse)
race_type_interaction <- lm(TOTPRISN ~ factor(MONRACE) + factor(TYPE) + XCRHISSR + XFOLSOR, data2)
summary(race_type_interaction)
##
## Call:
## lm(formula = TOTPRISN ~ factor(MONRACE) + factor(TYPE) + XCRHISSR +
##
       XFOLSOR, data = data2)
##
## Residuals:
       Min
##
                1Q
                    Median
                                 3Q
                                        Max
##
  -216.07
           -18.68
                     -3.97
                              11.61
                                     635.99
##
## Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                    -67.783349
                                  0.114664 -591.15
                                                      <2e-16 ***
## factor(MONRACE)2
                      7.767409
                                  0.091235
                                             85.14
                                                      <2e-16 ***
## factor(TYPE)1
                     -5.068605
                                  0.107050
                                            -47.35
                                                      <2e-16 ***
                      6.895167
                                             47.21
## factor(TYPE)2
                                  0.146055
                                                      <2e-16 ***
## factor(TYPE)3
                     -2.769758
                                  0.112885
                                            -24.54
                                                      <2e-16 ***
## factor(TYPE)4
                      6.573262
                                  0.221508
                                             29.68
                                                      <2e-16 ***
## XCRHISSR
                      7.605865
                                  0.023304 326.37
                                                      <2e-16 ***
## XFOLSOR
                      5.156278
                                  0.005112 1008.67
                                                      <2e-16 ***
## ---
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 38.83 on 1106975 degrees of freedom
     (7281 observations deleted due to missingness)
## Multiple R-squared: 0.6144, Adjusted R-squared: 0.6143
```

a. Describe the theoretical reasoning for selecting this variable.

F-statistic: 2.519e+05 on 7 and 1106975 DF, p-value: < 2.2e-16

Selecting both the criminal history and severity of the crime will help us dig deeper into the granularity of the type of the crime and the outcome of the punishment.

b. What type of relationship do you think this variable has with your focal variables? Given that, what do you expect to happen to your focal relationship when it is added to the model?

These variables have a intervening relationship with my focal variable. I expect it to make the race and type variables weaker.

c. Is it a continuous or categorical variable? What implications does this have for a multivariate regression equation?

These are continuous variables. This just means that we have really granular data and it only counts for 1 linear paramter!

d. Conduct a multivariate linear regression by adding one explanatory variable at a time and save the model objects. Print out the full results by calling summary() on each model object.

```
library(tidyverse)
# only comparing blacks and whites and prison length less than 700 (dp and lwp above that so excluding
data2 <- data %>%
  filter(MONRACE <= 2) %>%
  filter(TOTPRISN <= 700) %>%
  filter(EDUCATN < 3)</pre>
race type interaction <- lm(TOTPRISN ~ factor(MONRACE):YEAR + factor(MONRACE) + factor(TYPE) + XCRHISSR
summary(race_type_interaction)
##
## Call:
## lm(formula = TOTPRISN ~ factor(MONRACE):YEAR + factor(MONRACE) +
       factor(TYPE) + XCRHISSR + XFOLSOR, data = data2)
##
##
## Residuals:
##
       Min
                1Q
                    Median
                                3Q
                                       Max
##
  -223.90
           -18.58
                     -4.01
                             12.36
                                    616.56
##
## Coefficients:
##
                           Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                          44.920828
                                     17.835170
                                                 2.519
                                                          0.0118 *
## factor(MONRACE)2
                         876.459994 33.244600
                                               26.364
                                                        < 2e-16 ***
## factor(TYPE)1
                          -7.710244
                                      0.119498 -64.522
                                                        < 2e-16 ***
## factor(TYPE)2
                           5.239015
                                                33.748
                                      0.155241
                                                        < 2e-16 ***
## factor(TYPE)3
                          -3.131153
                                      0.124942 -25.061
                                                        < 2e-16 ***
## factor(TYPE)4
                           3.485879
                                      0.237234
                                               14.694
                                                        < 2e-16 ***
## XCRHISSR
                           7.835824
                                      0.024632 318.121
                                                        < 2e-16 ***
## XFOLSOR
                           5.347210
                                      0.005566 960.751
                                                        < 2e-16 ***
## factor(MONRACE)1:YEAR
                          -0.057448
                                      0.008888 -6.463 1.03e-10 ***
## factor(MONRACE)2:YEAR
                          -0.490620
                                      0.014051 -34.917 < 2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 39.09 on 982589 degrees of freedom
     (4715 observations deleted due to missingness)
## Multiple R-squared: 0.6213, Adjusted R-squared:
## F-statistic: 1.791e+05 on 9 and 982589 DF, p-value: < 2.2e-16
library(ggplot2)
```

- e. Describe the results of the multivariate analysis, highlighting:
- the apparent association between each additional control variable and the focal response variable
- how the focal association changed when you incorporated each control variable
- the implications of these results for your focal association

This is weird - accounting for XCRHISSR and XFOLSOR - drug crimes actually receive less prison time. The focal (race) did become weaker after including these two variables. This also means that the severity of the crime and the history of the individual plays a larger role in sentencing.

f. How well does the full (all explanatory variables included) model fit? Are any of the other models you ran a better fit? Explain how you came to the conclusion you did.

I think no matter what I add - they will be significant and relatively strong. Perhaps I should consider keeping this data, and subsetting data to more disadvantaged individuals and go from there.

g. Select the model that you think best fits the data. Provide a brief synopsis of the analysis of your data using this model and describe the implications for the theoretical arguments you set out to test.

```
final <- glm(TOTPRISN + XFOLSOR ~ factor(MONRACE) +</pre>
                                  factor(TYPE) +
                                  factor(EDUCATN)+
                                  AGE:factor(MONRACE) +
                                  YEAR +
                                  XCRHISSR,
                                  data = data2,
                                  family = "poisson")
summary(final)
##
## Call:
##
  glm(formula = TOTPRISN + XFOLSOR ~ factor(MONRACE) + factor(TYPE) +
       factor(EDUCATN) + AGE:factor(MONRACE) + YEAR + XCRHISSR,
##
##
       family = "poisson", data = data2)
##
##
  Deviance Residuals:
##
       Min
                 1Q
                      Median
                                    3Q
                                            Max
  -18.608
             -4.622
                      -1.837
                                 2.305
##
                                         55.173
##
## Coefficients:
##
                          Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                                160.579
                         7.292e+00
                                     4.541e-02
                                                         < 2e-16 ***
## factor(MONRACE)2
                         4.670e-01
                                     9.156e-04
                                                510.116
                                                         < 2e-16 ***
## factor(TYPE)1
                         7.737e-01
                                     3.848e-04 2010.824
                                                         < 2e-16 ***
## factor(TYPE)2
                         5.130e-01
                                     4.843e-04 1059.238
                                                         < 2e-16 ***
## factor(TYPE)3
                         -2.806e-01
                                     5.179e-04 -541.784
                                                         < 2e-16 ***
## factor(TYPE)4
                                     6.360e-04 1124.755
                         7.153e-01
                                                         < 2e-16 ***
## factor(EDUCATN)1
                         7.425e-03
                                     1.321e-03
                                                  5.619 1.92e-08 ***
## factor(EDUCATN)2
                         1.862e-02
                                     1.327e-03
                                                 14.027
                                                         < 2e-16 ***
## YEAR
                         -2.095e-03
                                     2.263e-05
                                                -92.591
                                                         < 2e-16 ***
## XCRHISSR
                         1.535e-01
                                     6.710e-05 2286.978
                                                         < 2e-16 ***
                                                         < 2e-16 ***
## factor(MONRACE)1:AGE 7.606e-03
                                     1.437e-05
                                                529.380
## factor(MONRACE)2:AGE -2.034e-03
                                     2.212e-05
                                                -91.922
                                                         < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
##
   (Dispersion parameter for poisson family taken to be 1)
##
##
                                on 981652
       Null deviance: 54340807
                                            degrees of freedom
## Residual deviance: 35072453
                                on 981641
                                            degrees of freedom
##
     (5661 observations deleted due to missingness)
## AIC: 40631498
##
## Number of Fisher Scoring iterations: 5
```

Blacks receive on average of 0.47 additional months compared to whites. Drug, gun, and violent crime all receive higher sentences (by .5-.7 months) than other and immigration crimes. Education has a weak correlation with the outcome of the sentencing below college graduate level (Beta is small). There is a slight downward trend in crime severity in the recent 2 decades. And white people are more likely than blacks to commit more crime as they get older.