

Data Mining

Combining Learners

2003.10.06



Agenda

- Methods
- Bagging
- Arcing
- Bumping
- etc.

Combining learners to improve prediction

- Stacking (David Wolpert)
- Bagging (Leo Breiman)
- Arcing (Yoav Freund and Robert Shapire)
- Bumping (Robert Tibshirani)

Bagging

- Bagging (Bootstrap AGGregatING) averages a given procedure over many samples, to reduce its variance.
- Suppose $C(\mathbf{x}, t)$ is a classifier, producing a K -vector output with 1 one and $K - 1$ zeros, at input point t
- To bag C , we draw bootstrap samples

$$\mathbf{X}^{*1}, \dots, \mathbf{X}^{*B}$$

each of size N with replacement from the training data. Then

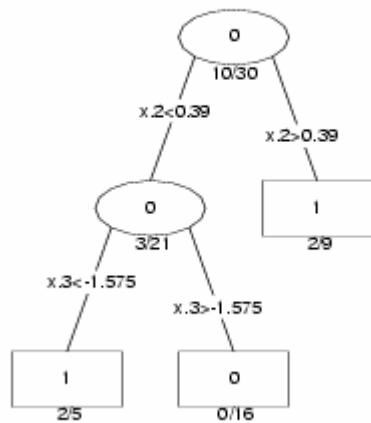
$$\hat{C}_{bag}(t) = \frac{1}{B} \sum C(\mathbf{x}^{*b}, t)$$

and we classify to the class with largest “vote” in \hat{C}_{bag} .

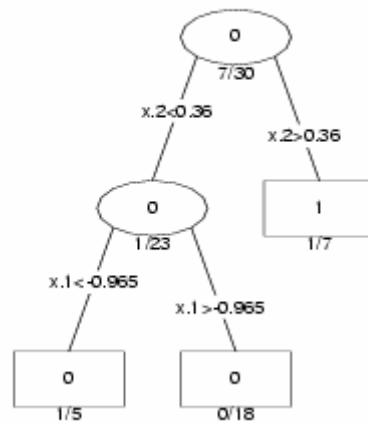
- Bagging can dramatically reduce the variance of unstable procedure (like trees), leading to improved prediction. However any simple structure in C (e.g a tree) is lost.

Discussions on Trees

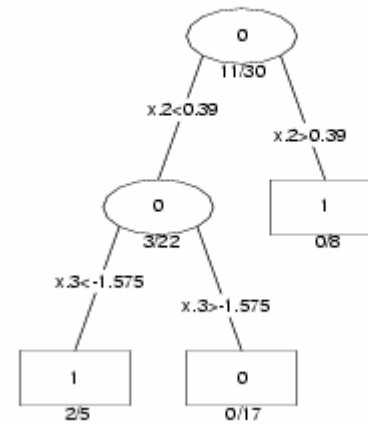
Original Tree



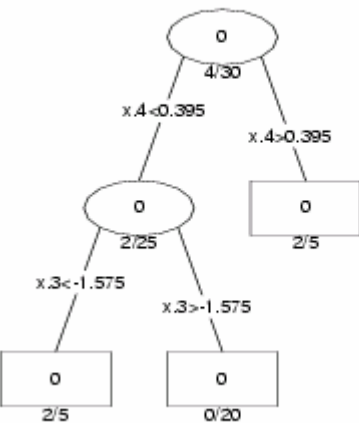
Bootstrap Tree 1



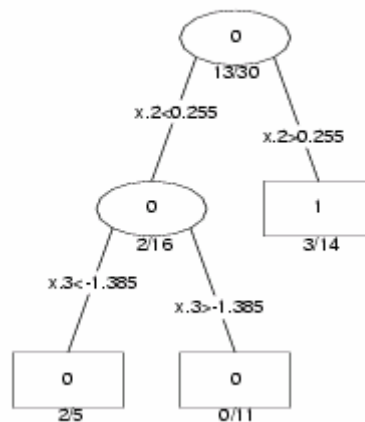
Bootstrap Tree 2



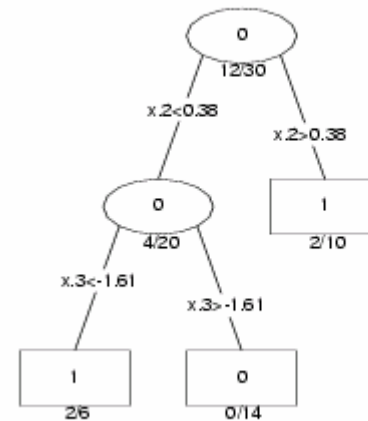
Bootstrap Tree 3



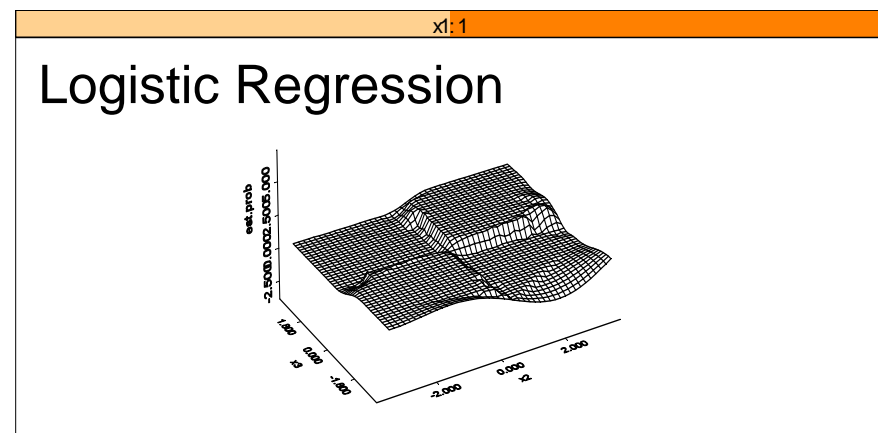
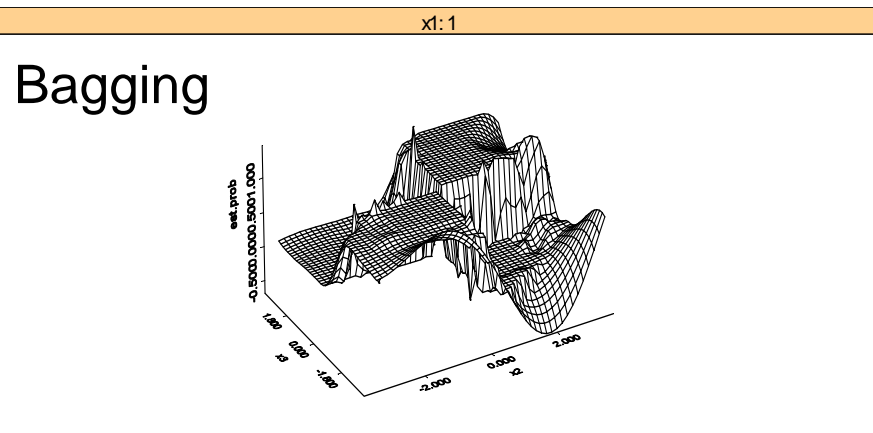
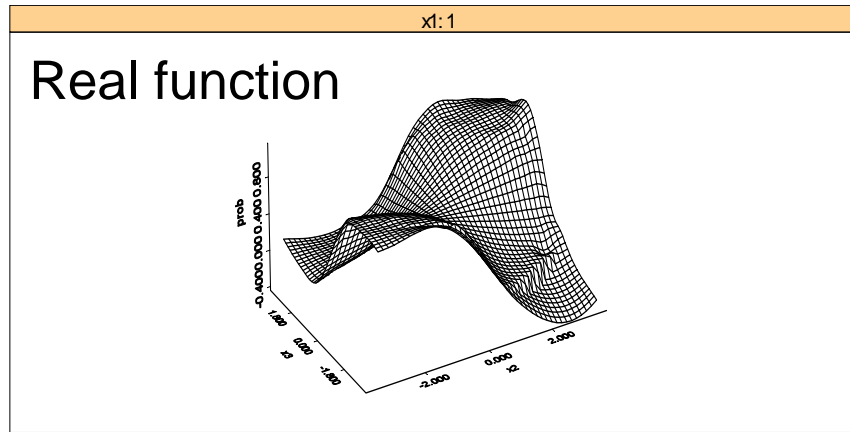
Bootstrap Tree 4



Bootstrap Tree 5

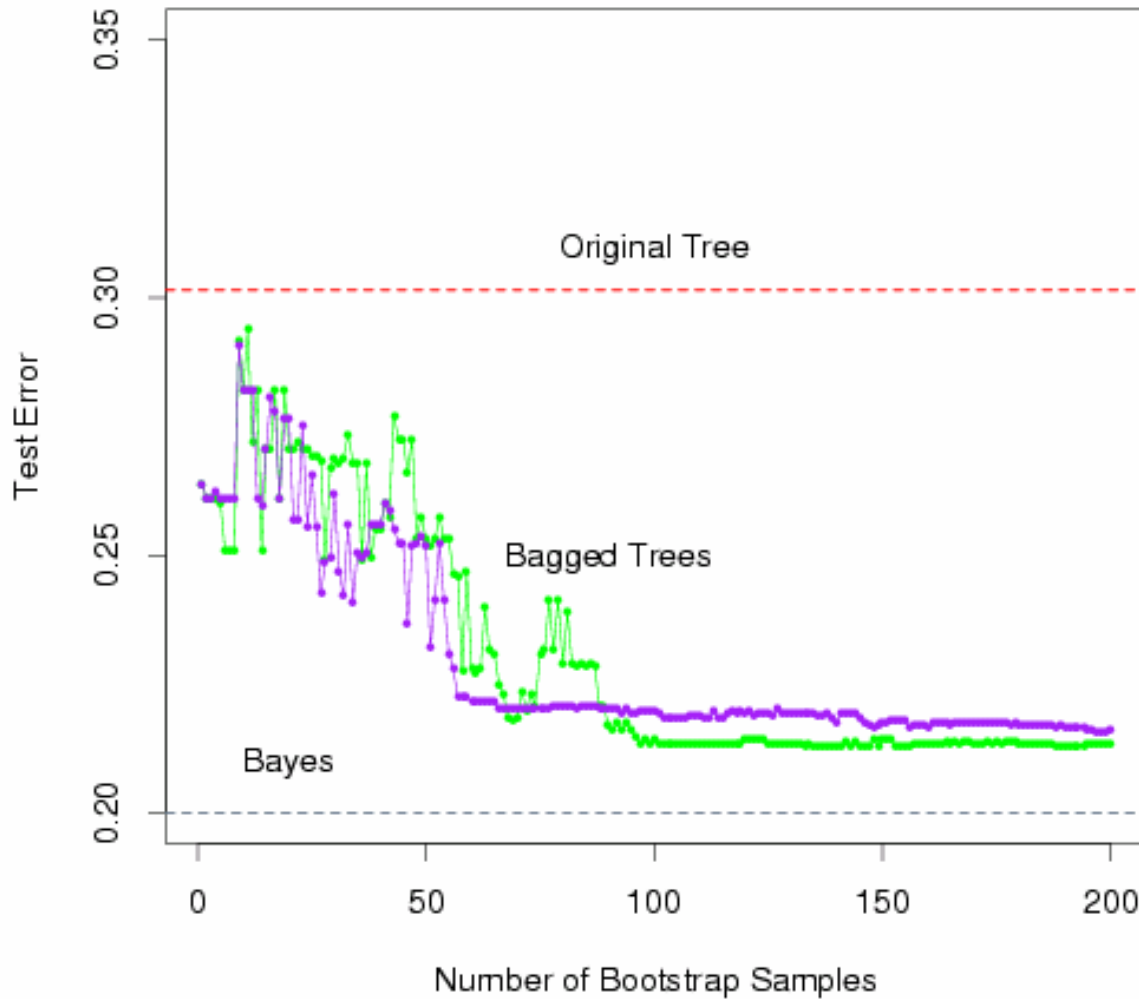


Decision boundary : Bagging



- Bagging averages many trees, and produces *smoother* decision boundary.

Discussions on bagging



Arcing

- Arcing (Adaptive Resampling and Combining) designed exclusively for classification problem.
- Developed by Yoav Freund and Robert Shapire (1995), in the name of “boosting”, but Breiman renamed it as “arcing”.
- Idea: Like bagging, but take unequal probability bootstrap samples. Put more weight on observations that are misclassified, to make the classifier work harder on those points
- Arcing can improve on bagging in many instances.

Arcing-fs algorithm-1

- **Step 0.** Start with equal observation weights $p(i) = 1/N$
- **Step 1.** At the k -th step, using $\{p(i), i = 1, \dots, N\}$, sample with replacement from the training set T to get the updated training set $T^{(k)}$ and construct classifier C_k using $T^{(k)}$.
- **Step 2.** Run T down the classifier C_k and let $d(i) = 1$ if the i th case is classified incorrectly, otherwise zero.

Arcing-fs algorithm-2

- Step 3. Define

$$\varepsilon_k = \sum_i p(i)d(i), \quad \beta_k = (1 - \varepsilon_k) / \varepsilon_k$$

and the updated $(k + 1)$ st step probabilities by

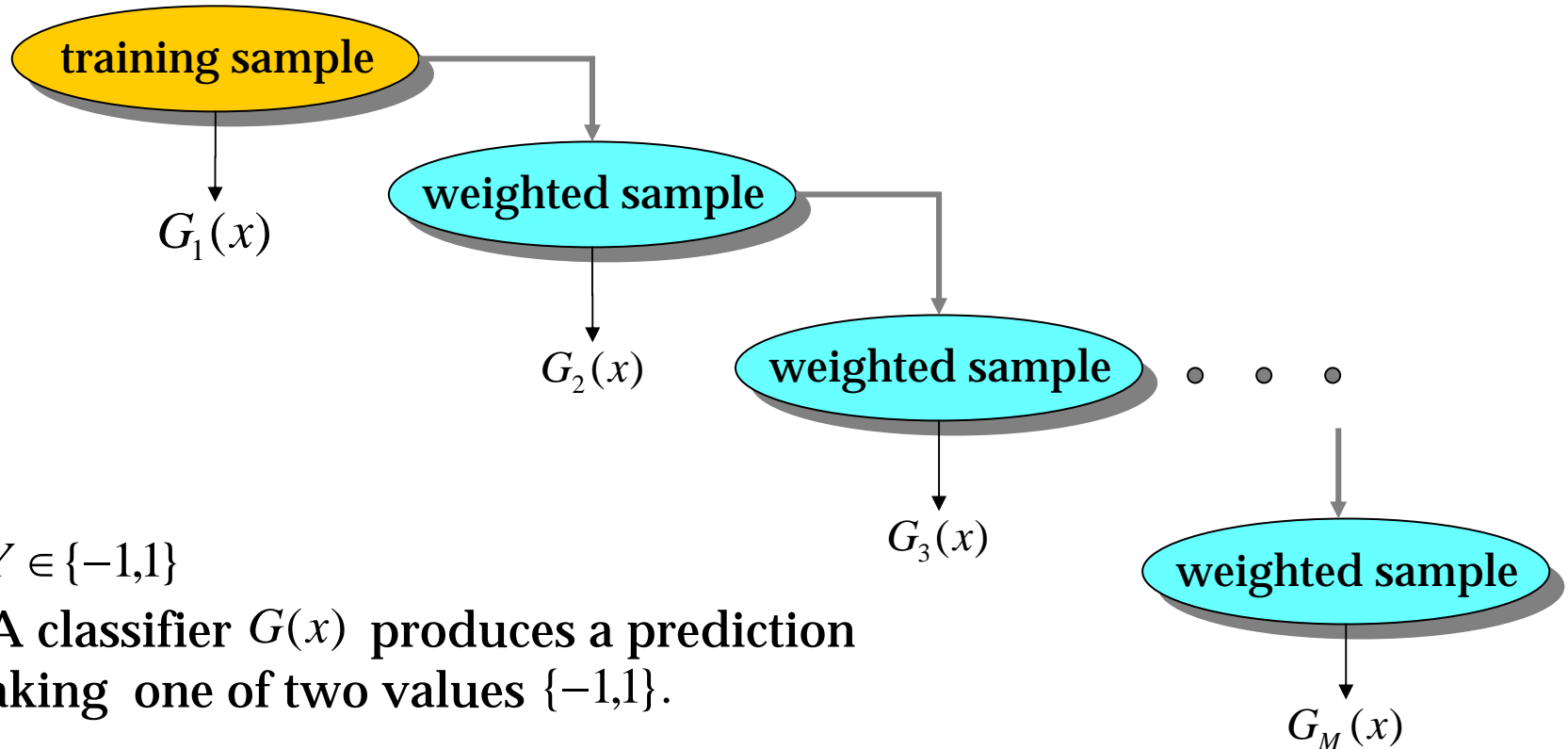
$$p(i) = \frac{p(i)\beta_k^{d(i)}}{\sum p(i)\beta_k^{d(i)}}$$

After K iterations, take a weighted vote of the classifications, with weights $\log(\beta_k)$.

Arcing-fs algorithm-3

- The smaller ε_k , the larger β_k
- $\varepsilon_k > 1/2$ means that the number of misclassification cases is greater than that of good ones.
- If ε_k becomes equal to or greater than $1/2$, then the original Freund and Schapire's algorithm exits from the construction loop.
- Breiman (1996) found that better results were gotten by setting all $\{p(i)\}$ equal and restarting.
- If $\varepsilon_k = 0$ again set the probabilities equal to restart.

Boosting



- $Y \in \{-1, 1\}$
- A classifier $G(x)$ produces a prediction taking one of two values $\{-1, 1\}$.

Final Classifier

$$G(x) = \text{sign}\left[\sum_{m=1}^M \alpha_m G_m(x)\right]$$

Stochastic Model search – Bumping

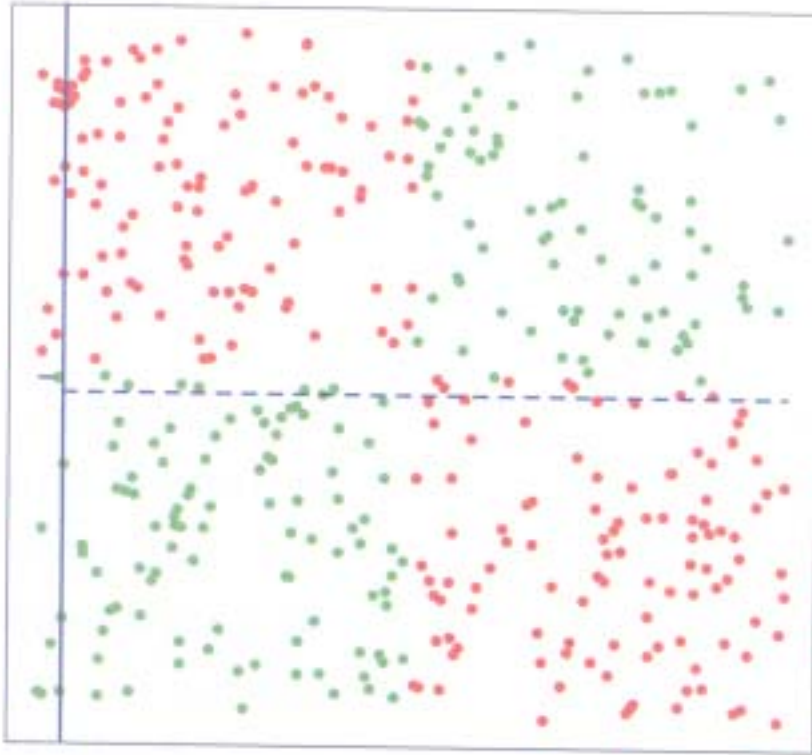
- Bumping stands for *Bootstrap Umbrella of Model Parameters*.
- As in bagging, we draw bootstrap samples and fit a model to each. Rather than average the predictions, we choose the bootstrap model that best fits the training data.
- In detail, we draw bootstrap samples $\mathbf{x}^{*1}, \dots, \mathbf{x}^{*B}$ and compute the classifiers

$$C_1 = C(\mathbf{x}^{*1}, t), \dots, C_B = C(\mathbf{x}^{*B}, t)$$

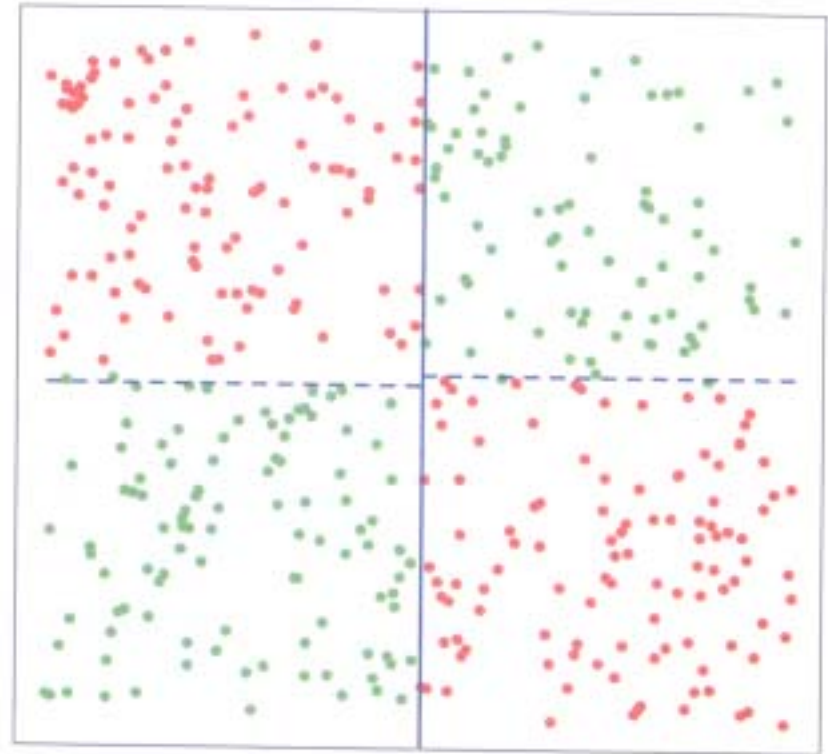
- Then we choose the classifier among C_1, \dots, C_B that has smallest misclassification error on the original training data.
- Bumping procedure applying to trees and neural nets can find a better local minimum, while still producing a model with the same structure.

Effect of Bumping

Regular 4-Node Tree



Bumped 4-Node Tree



Bumping search in NN

- Algorithm
 - STEP-1. Training data $\mathbf{z}^{*1}, \dots, \mathbf{z}^{*B}$. B bootstrap sample
 - STEP-2. bootstrap sample . neural net C_1, \dots, C_B $[-\delta, \delta]$
 - STEP-3. Training data C_1, \dots, C_B 가 C_{b_0} .
- - Random search $1/5$ computing time
 - bumping search

Features

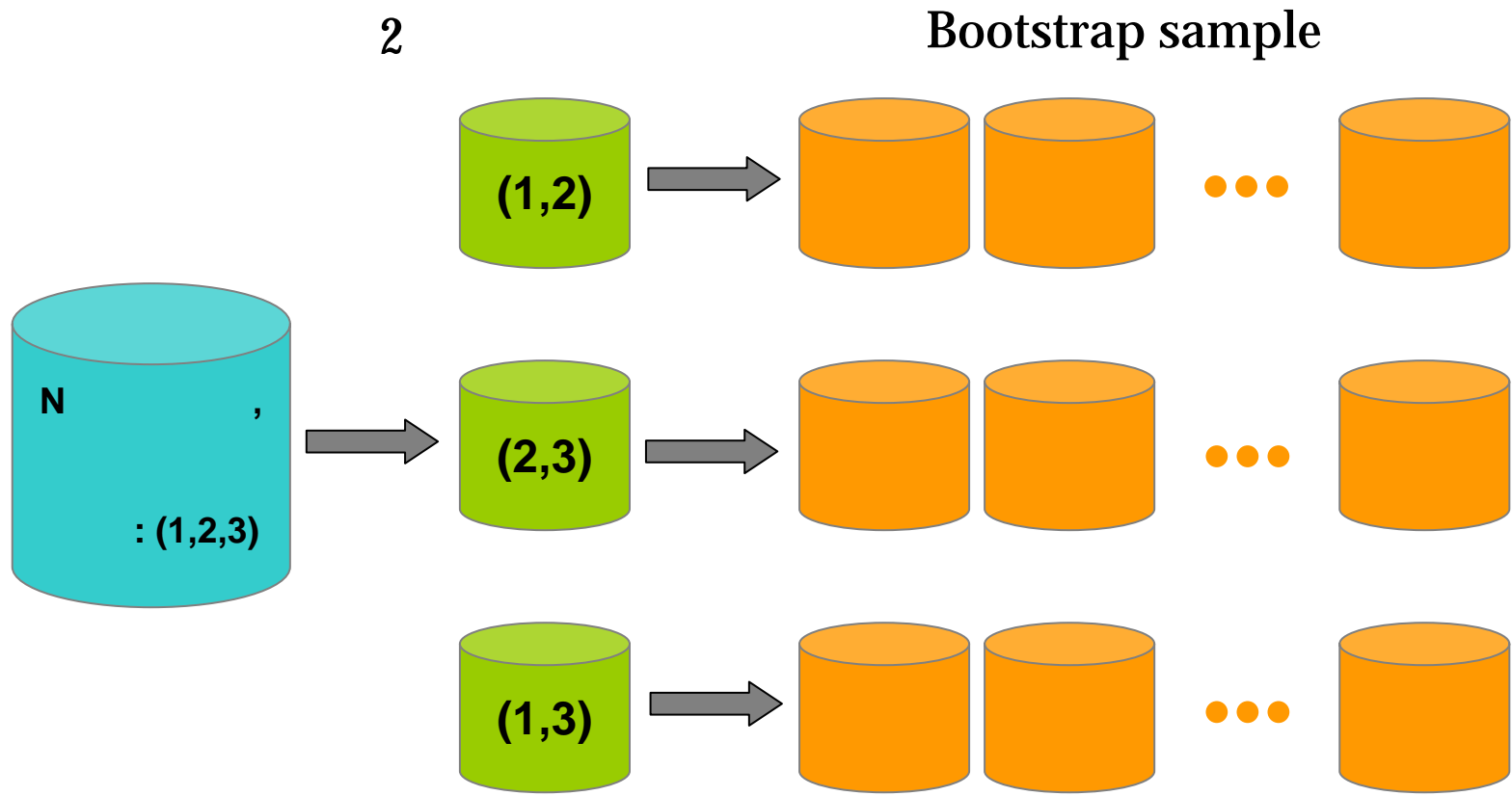
- Bagging improves the performance of classification in tree-based model upto 40% (considering 0-1 loss misclassification error measurement).
- Bagging reduces “variance”, not “bias”
- Bagging destroys tree structure.
- Bagging could not improve the performance of K-nearest neighbor method.
- Arcing is better than Bagging in the sense of misclassification error measurement.

Model Averaging

- Classification trees can be simple, but often produce noisy (bushy) or weak (stunted) classifiers.
 - Bagging (Breiman 1996): Fit many large trees to bootstrap-resampled versions of the training data, and classify by majority vote.
 - Boosting (Freund & Schapire 1996): Fit many large or small trees to reweighted versions of the training data. Classify by reweighted majority vote.
- In general Boosting > Bagging > Single Tree in stability and power.
- “AdaBoost ... best off-the-shell classifier in the world” (Leo Breiman, NIPS workshop 1996).

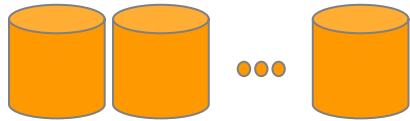
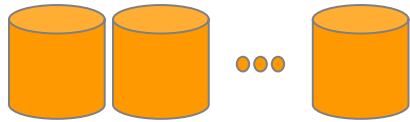
Applications – coupled with bagging

- Pairwise comparison



Applications – coupled with bagging (*cont.*)

Bootstrap sample



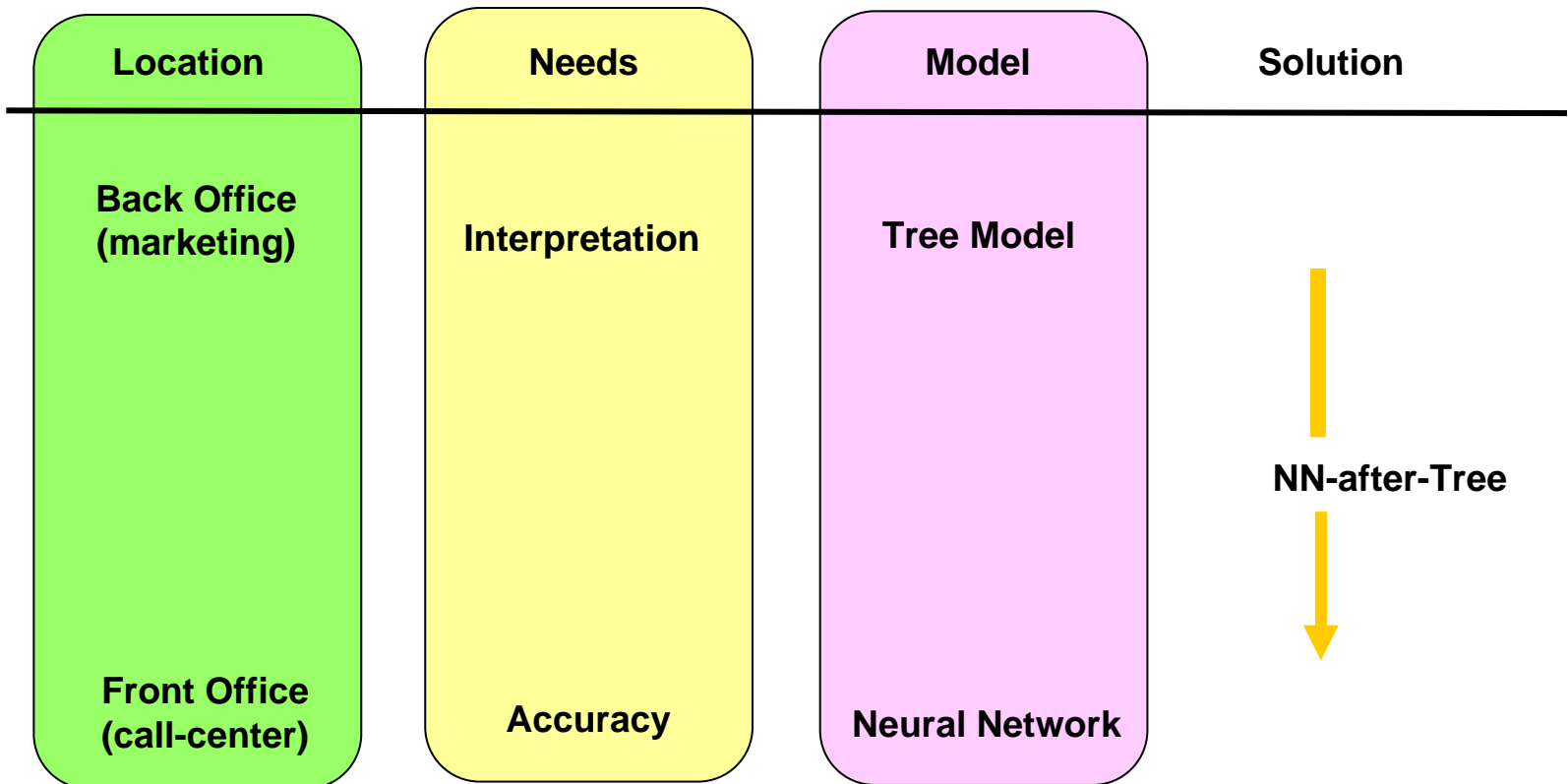
$(1,0,-) (1,0,-) \dots (0,1,-)$

$(-,0,1) (-,1,0) \dots (-,1,0)$

$(0,-,1) (0,-,1) \dots (1,-,0)$

Applications – hybrid model

- scoring , needs가
- scoring .
- tree model segmentation rule ,
- segmentation dummy , scoring .



The background is a light gray gradient. It features several abstract geometric elements: a dashed line with diagonal segments running from the top left towards the right; a large, faint, light gray circle in the top right corner; and various thin, light gray lines and smaller circles scattered across the bottom and right sides, creating a technical or architectural feel.

Q&A