Persistent Test-time Adaptation in Recurring Testing Scenarios

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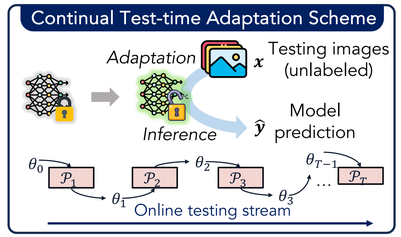
NEURAL INFORMATION PROCESSING SYSTEMS

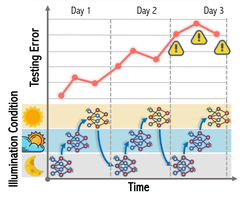
INTRODUCTION

Continual Test-time Adaptation (TTA) operates on an ML classifier $f_t: \mathcal{X} \to \mathcal{Y}$, parameterized by $\theta_t \in \Theta$ gradually changing over time. The model explores an online stream of testing data $X_t \sim P_t$ for adapting itself $f_{t-1} \to f_t$ (self-supervised learning) before predicting $\widehat{Y}_t = f_t(X_t)$.



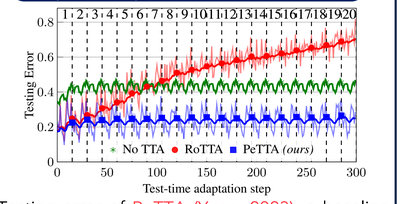
Does the model adaptability persist after a long time adapting to multiple data shifts?

Hypothetical Setting



- In practice, testing environments may *change recurringly*.
- Preserving adaptability when visiting *the same* testing condition is *not guaranteed*.

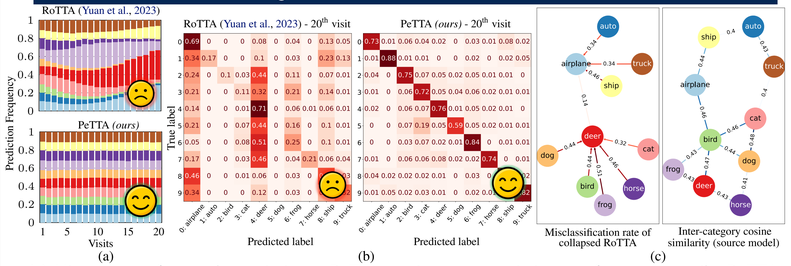
Empirical Experiment on CIFAR-10-C



- Testing error of RoTTA (Yuan, 2023), a baseline TTA algorithm raises - *performance degradation*.
- Quickly exceeding the error of the source model (without TTA, accepting domain shift as-it-is).
- PeTTA *(ours)* demonstrates its stability.

Recurring Test-time Scenario: $\mathcal{P}_1 \to \mathcal{P}_2 \to \cdots \to \mathcal{P}_D \to \cdots \to \mathcal{P}_1 \to \mathcal{P}_2 \to \cdots \to \mathcal{P}_D$

TTA Under Recurring TTA on CIFAR-10 → CIFAR-10-C Task for 20 Visits



(a) (b) (c)

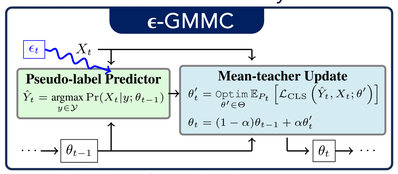
(a) Histogram of model predictions: PeTTA achieves a persisting performance while RoTTA degrades. (b) Confusion matrix at the last visit (c) Force-directed graph showing (left) the most prone to misclassification; (right) similar categories tend to be easily collapsed.

ϵ-PERTURBED GAUSSIAN MIXTURE MODEL CLASSIFIER (ϵ-GMMC)

*ϵ-GMMC - a simple yet representative **failure case** of TTA for **theoretical analysis***

Setting: A simplified continual TTA process
- Let $p_{y,t} = \Pr(Y_t = y)$; $\hat{p}_{y,t} = \Pr(\hat{Y}_t = y)$.
- Binary classification $\mathcal{X} \times \mathcal{Y} = \mathbb{R} \times \{0,1\}$.
- Underlying distribution follows a mixture of 2 Gaussian: $P_t(x, y) = p_{y,t}\mathcal{N}(x; \mu_y, \sigma_y^2)$.

Main Task: predicting X_t was sampled from cluster 0 or 1 (negative or positive).



ϵ−GMMC performs 2 main steps:
- *Predicting pseudo-labels ($\hat{Y}_t$).*
- *Updating with mean teacher model.*

Key Idea: The *predictor* is **perturbed** for retaining a **false negative rate (FNR)** of $\boldsymbol{\varepsilon_t = \Pr\{Y_t = 1 | \hat{Y}_t = 0\}}$ to simulate undesirable effects of the testing stream in TTA, making model prone to collapse.

A Mathematical Definition of Model Collapse

Definition 1 (Model Collapse). *A model is said to be collapsed from step $\tau \in \mathcal{T}, \tau < \infty$ if there exists a non-empty subset of categories $\hat{\mathcal{Y}} \subset \mathcal{Y}$ such that $\Pr\{Y_t \in \hat{\mathcal{Y}}\} > 0$ but the marginal $\Pr\{\hat{Y}_t \in \hat{\mathcal{Y}}\}$ converges to zero in probability:*

$$\lim_{t \to \tau} \Pr\{\hat{Y}_t \in \hat{\mathcal{Y}}\} = 0.$$

Factors contributing to the model collapse:
- *(i) **Data-dependent factors**:* the prior data distribution (p_0), the nature difference between two categories ($|\mu_0 - \mu_1|$) from the dataset.
- *(ii) **Algorithm-dependent factors**:* update rate (α), the false negative rate at each step (ε_t).

Assumption 1 (Static Data Stream). *The marginal distribution of the true label follows the same Bernoulli distribution* $\mathrm{Ber}(p_0)$*:* $p_{0,t} = p_0$, $(p_{1,t} = p_1 = 1 - p_0), \forall t \in \mathcal{T}$.

Lemma 2 (ϵ-GMMC After Collapsing). *For a binary ϵ-GMMC model, with Assumption 1, if $\lim_{t\to\tau} \hat{p}_{1,t} = 0$ (collapsing), the cluster 0 in GMMC converges in distribution to a single-cluster GMMC with parameters:*

$$\mathcal{N}(\hat{\mu}_{0,t}, \hat{\sigma}_{0,t}^2) \xrightarrow{d} \mathcal{N}(p_0\mu_0 + p_1\mu_1,\ p_0\sigma_0^2 + p_1\sigma_1^2 + p_0p_1(\mu_0 - \mu_1)^2).$$

Corollary 1 (A Condition for ϵ−GMMC Collapse). *With fixed p_0, α, μ_0, μ_1, ϵ−GMMC is collapsed if there exists a sequence of $\{\epsilon_t\}_{\tau-\Delta_\tau}^{\tau}$ ($\tau \geq \Delta_\tau > 0$) such that:*

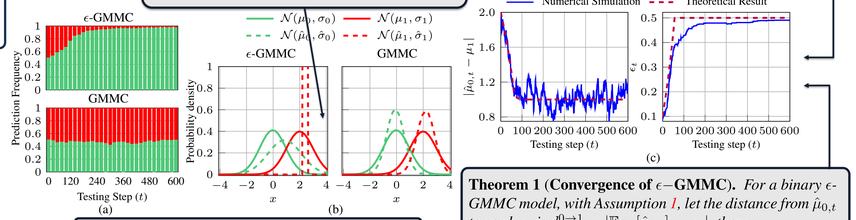
$$p_1 \geq \epsilon_t > 1 - \frac{d_{t-1}^{0\to1}}{|\mu_0 - \mu_1|}, \quad t \in [\tau - \Delta_\tau, \tau].$$

Theorem 1 (Convergence of ϵ−GMMC). *For a binary ϵ-GMMC model, with Assumption 1, let the distance from $\hat{\mu}_{0,t}$ toward μ_1 is $d_t^{0\to1} = |\mathbb{E}_{P_t}[\hat{\mu}_{0,t}] - \mu_1|$, then:*

$$d_t^{0\to1} - d_{t-1}^{0\to1} \leq \alpha \cdot p_0 \cdot \left(|\mu_0 - \mu_1| - \frac{d_{t-1}^{0\to1}}{1 - \epsilon_t}\right).$$

Lemma 1 (Increasing FNR). *Under Assumption 1, a binary ϵ-GMMC would collapsed (Def. 1) with $\lim_{t\to\tau} \hat{p}_{1,t} = 0$ (or $\lim_{t\to\tau} \hat{p}_{0,t} = 1$, equivalently) if and only if $\lim_{t\to\tau} \epsilon_t = p_1$.*

ε−GMMC Simulation Result



(a) Histogram of model predictions. (b) The probability density function of the two clusters after convergence (*dashed line*) versus the true data distribution. (c) Distance toward μ_1 and false-negative rate (ε_t) coincides with the theoretical analysis.

PERSISTENT TEST-TIME ADAPTATION (PeTTA)

Key Idea: *Striking a balance between **adaptation and preventing model collapse***

With ϕ_{θ_t} is the deep feature extractor of f_t, let $\boldsymbol{z} = \phi_{\theta_t}(\boldsymbol{x})$. Keeping track of a collection of the running mean of feature vector $\boldsymbol{z}$: $\{\hat{\mu}_t^y\}_{y \in \mathcal{Y}}$ in which $\hat{\boldsymbol{\mu}}_t^y$ is exponential moving average updated with vector $\boldsymbol{z}$ if $f_t(\boldsymbol{x}) = y$.

Persistent TTA

(1) Sensing the divergence from $\boldsymbol{\theta_0}$

$$\gamma_t^y = 1 - \exp\left(-(\hat{\boldsymbol{\mu}}_t^y - \boldsymbol{\mu}_0^y)^T (\boldsymbol{\Sigma}_0^y)^{-1} (\hat{\boldsymbol{\mu}}_t^y - \boldsymbol{\mu}_0^y)\right)$$

$\boldsymbol{\mu}_0^t, \boldsymbol{\Sigma}_0^t$ are pre-computed on the source distribution

(2) Adaptive Learning Rate $\boldsymbol{\alpha_t}$ and Regularization $\boldsymbol{\lambda_t}$

$$\bar{\gamma}_t = \frac{1}{|\hat{\mathcal{Y}}_t|} \sum_{y \in \hat{\mathcal{Y}}_t} \gamma_t^y, \quad \hat{\mathcal{Y}}_t = \left\{\hat{Y}_t^{(i)} | i = 1, \cdots, N_t\right\}$$

$$\lambda_t = \bar{\gamma}_t \cdot \lambda_0, \qquad \alpha_t = (1 - \bar{\gamma}_t) \cdot \alpha_0,$$

PeTTA

$$\theta_t' = \underset{\theta' \in \Theta}{\mathrm{Optim}}\, \mathbb{E}_{P_t}\left[\mathcal{L}_{\mathrm{CLS}}\left(\hat{Y}_t, X_t; \theta'\right) + \mathcal{L}_{\mathrm{AL}}\left(X_t; \theta'\right)\right] + \lambda_t \mathcal{R}(\theta')$$

$$\theta_t = (1 - \alpha_t)\theta_{t-1} + \alpha_t \theta_t'.$$

(3) Anchor Loss

$$\mathcal{L}_{\mathrm{AL}}(X_t; \theta) = -\sum_{y \in \mathcal{Y}} \Pr(y | X_t; \theta_0) \log \Pr(y | X_t; \theta)$$

EXPERIMENTAL RESULTS

Average classification error on the task *ImageNet* → *ImageNet-C* for 20 recurring TTA visits.

Method	Recurring TTA visit 1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	Avg
Source	82.0																				82.0
LAME (Boudiaf et al., 2022)	80.9																				80.9
CoTTA (Wang et al., 2022)	98.6	99.1	99.4	99.4	99.5	99.5	99.5	99.5	99.6	99.7	99.6	99.6	99.6	99.6	99.6	99.6	99.6	99.6	99.7	99.7	99.5
EATA (Niu et al., 2022)	60.4	59.3	65.4	72.6	79.1	84.2	88.7	92.7	95.2	96.9	97.7	98.1	98.4	98.6	98.7	98.8	98.8	98.9	98.9	99.0	89.0
RMT (Döbler et al., 2023)	72.3	71.0	69.9	69.1	68.8	68.5	68.4	68.3	70.0	70.2	70.1	70.2	72.8	76.8	75.6	75.1	75.1	75.2	74.8	74.7	71.8
MECTA (Hong et al., 2023)	77.2	82.8	86.1	87.9	88.9	89.4	89.8	89.9	90.0	90.4	90.6	90.7	90.7	90.8	90.8	90.9	90.8	90.8	90.7	90.8	89.0
RoTTA (Yuan et al., 2023)	68.3	62.1	61.8	64.5	68.4	75.4	82.7	95.1	95.8	96.6	97.1	97.9	98.3	98.7	99.0	99.1	99.3	99.4	99.5	99.6	87.9
RDumb (Press et al., 2023)	72.2	73.0	73.2	72.8	72.2	72.8	73.3	72.7	71.9	73.0	73.2	73.1	72.0	72.7	73.3	73.1	72.1	72.6	73.3	73.1	72.8
ROID (Marsden et al., 2024)	62.7	62.3	62.3	62.3	62.5	62.3	62.4	62.4	62.3	62.6	62.5	62.3	62.5	62.4	62.5	62.4	62.4	62.5	62.4	62.5	62.4
TRIBE (Su et al., 2024)	**63.6**	64.0	64.9	67.8	69.6	71.7	73.5	75.5	77.4	79.8	85.0	96.5	99.4	99.8	99.9	99.8	99.8	99.9	99.9	99.9	84.4
PeTTA *(ours)*[*]	65.3	**61.7**	**59.8**	**59.1**	**59.4**	**59.6**	**59.8**	**59.3**	**59.4**	**60.0**	**60.3**	**61.0**	**60.7**	**60.4**	**60.6**	**60.7**	**60.8**	**60.7**	**60.4**	**60.2**	**60.5**

Does model reset help? A comparison with a *reset-based approach* at different frequencies.

Reset Every	Recurring TTA visit 1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	Avg
$T = 1000$	72.2	73.0	73.2	72.8	72.2	72.8	73.3	72.7	71.9	73.0	73.2	73.1	72.0	72.7	73.3	73.1	72.1	72.6	73.3	73.1	72.8
$T = 5000$	70.2	70.8	71.6	72.1	72.4	72.6	72.9	73.1	73.2	73.6	73.7	73.9	74.0	74.0	74.3	74.1	74.1	73.8	73.5	71.9	73.0
$T = 75000$	67.0	67.1	67.2	67.5	67.5	67.6	67.8	67.6	67.6	67.6	67.5	67.7	67.6	67.9	68.1	67.9	67.4	67.5	67.7	67.5	67.6
PeTTA *(ours)*[*]	**65.3**	**61.7**	**59.8**	**59.1**	**59.4**	**59.6**	**59.8**	**59.3**	**59.4**	**60.0**	**60.3**	**61.0**	**60.7**	**60.4**	**60.6**	**60.7**	**60.8**	**60.7**	**60.4**	**60.2**	**60.5**

CONTRIBUTIONS

- ✓ A new testing scenario – **recurring TTA**.
- ✓ Theoretical analysis on performance degradation of TTA on $\boldsymbol{\epsilon}$ –perturbed Gaussian Mixture Model Classifier.
- ✓ A new baseline – **persistent TTA (PeTTA)**.

AUTHOR PAPER PROJECT