

# INTRO. TO LOGIC & FUNCT. PROG.

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In this assignment, you will write a type-checker for a simple functional language based on the lambda-calculus for simply-typed Propositional Natural Deduction proofs. You need to write a Prolog predicate *hastype*(*Gamma*, *E*, *T*), where

*Gamma* is a list of variable-type pairs, representing type assumptions on variables

*E* is an object language expression, where *E* ranges over  $\nu(X) \mid \backslash X.E \mid (E_1 E_2) \mid \langle E_1, E_2 \rangle \mid \text{proj } ^{(2)}_i E \mid \text{inl}(E) \mid \text{inr}(E) \mid \text{case } E \text{ of } \text{inl}(X) \Rightarrow E_1 \mid \text{inr}(Y) \Rightarrow E_2$

and

*T* is a type ranging over  $\text{TypeVar}(A) \mid T_1 \rightarrow T_2 \mid T_1 * T_2 \mid T_1 + T_2$

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You need to provide enough test examples to show your type checker works correctly.

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Note that this checker can work as a type inference engine. However it does not work for polymorphic type inference. Show with counter-examples that this is the case.

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For extra credit (50% extra)

-- extend the pairing and projection operation for arbitrary tuples. Hint: use lists and use check for projection operations being of the right kind.

-- generalise from just the two given constructors, to work with arbitrary sums that can have user-defined constructors and take tuples of arguments are arguments.

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