1 Interpreting Regular Expressions

1. Interpreting a Regular Expression

Find the shortest string $\omega \in \{a, b\}^*$ that is not in the language represented by the regular expression $a^*(ab)^*b^*$. Give reasons for your answer.

- 2. Interpreting a Regular Expression Consider the regular expression $(a(cd)^*b)^*$.
 - (a) Find a string of length 2 over $\{a, b, c, d\}$ which matches the expression.
 - (b) Find a string of length 1 over $\{a, b, c, d\}$ which does not match the expression.

Finden Sie für den oben angegebenen regulären Ausdruck

- (a) einen String der Länge 2 mit den Symbolen $\{a, b, c, d\}$, welcher als gültig erkannt wird
- (b) einen String der Länge 1 mit den Symbolen $\{a, b, c, d\}$, welcher als ungültig erkannt wird

3. Interpreting a Regular Expression

Describe in an English sentence (as simple as possible) the language corresponding to the regular expression:

$$(b+ab)^*(a+ab)^*.$$

Beschreiben Sie in einem möglichst einfachen deutschen Satz die Sprache des oben gegebenen regulären Ausdrucks.

2 C, C#, Java Comments

4. Comments In C, C#, or Java comments can be given in the form /* This is the comment */. This means that comments start with the string /* and end with the string */. The comment itself can be an arbitrary string with the exception that the string */ must not occur.

More precisely we could say that the language of a comment is now the string starting with "/" followed by a "*" followed by an arbitrary long sequence of characters except the sequence "*/" and ending with the sequence "*/". You may write $\alpha - \{\text{``x''}\}$ to denote a set of characters excluding one specific character "x".

- (a) Give a state diagram of a DFA which can parse this language.
- (b) Give a regular grammar which describes the language of C comments.
- (c) Describe this language by a regular set.
- (d) Is it possible to describe nested comments, e.g., /* This is a /* nested */ comment */, by a regular expression? Give arguments for your decision.

In C, C# oder Java gibt es die Blockkommentare, welche in /* und */ eingeschlossen sind. Der Kommentar selbst kann eine beliebige Zeichenkette sein, welche nur dadurch eingeschränkt ist, dass sie die Sequenz */ nicht beinhalten darf.

- (a) Geben Sie das Zustandsdiagramm eines DFA an, der diese Sprache erkennt.
- (b) Geben Sie die dazugehörige reguläre Grammatik an.
- (c) Geben Sie den dazugehörigen regulären Ausdruck an.
- (d) Ist es möglich, geschachtelte Kommentare in Form eines regulären Ausdrucks zu beschreiben? Begründen Sie Ihre Antwort.

3 as and bs sometimes cs

5. aabs and bbs

Given a language L defined over the alphabet $\{a,b\}$ defined recursively as follows:

- 1. $\varepsilon \in L$.
- 2. If $x \in L$ then $aabx \in L$ and $xbb \in L$.
- 3. Nothing else is in L.

Please answer the following questions concerning L:

- (a) Draw the state diagram of the DFA parsing strings of this language.
- (b) Give the regular grammar for L.
- (c) Give the regular expression which describes L.
- 6. 4i + 1b's Given the following regular language:

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L(G(S)) = \{ \omega \in (a \mid b \mid c)^* \mid \omega \text{ has } 4i + 1b\text{'s } (i \ge 0) \}
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- (a) Give the state diagram of a DFA which parses this language.
- (b) Give a regular grammar G(S) which describes this language.
- (c) Give a regular expression which describes this language.
- 7. **No** bbb Given the following regular language:

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L(G(S)) = \{\omega \in (a \mid b)^* \mid \omega \text{ does } not \text{ contain the substring } bbb\}
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- (a) Give the state diagram of a DFA which parses this language.
- (b) Give a regular grammar G(S) which describes this language.

Gegeben sei oben genannte reguläre Sprache.

- (a) Zeichnen Sie das Zustandsdiagramm eines DFA, der diese Sprache erkennt.
- (b) Geben Sie die reguläre Grammatik G(S) für diese Sprache an.

4 With 0s and 1s

8. Starts with two 0s

Given the following regular language:

$$L(G(S)) = \{\omega \in (0 \mid 1)^* \mid \omega \text{ starts with two 0s} \}$$

- (a) Give the state diagram of a DFA which parses this language.
- (b) Give a regular grammar G(S) which describes this language.
- (c) Give a regular expression which describes this language.

9. Ends with 00 or 01

Given the following regular language: $L(G(S)) = \{\omega \in (0 \mid 1)^* \mid \omega \text{ ends with } 00 \text{ or } 01\}$

- (a) Give the state diagram of a DFA which parses this language.
- (b) Give a regular grammar G(S) which describes this language.
- (c) Give a regular expression which describes this language.

Geben sei obige reguläre Sprache L(G(S)).

- (a) Zeichnen Sie das Zustandsdiagramm eines DFA, der diese Sprache erkennt.
- (b) Geben Sie die reguläre Grammatik G(S) für diese Sprache an.
- (c) Geben Sie den regulären Ausdruck für diese Sprache an.