

## Sintaxe abstrata:

$$\begin{aligned}
 e &\in \text{Expr} \\
 e &::= n \mid b \mid e_1 \text{ op } e_2 \mid \text{if } e_1 \text{ then } e_2 \text{ else } e_3 \\
 &\quad \mid x \mid \text{let } x:T = e_1 \text{ in } e_2 \\
 &\quad \mid e_1 := e_2 \mid !e \mid \text{new } e \mid () \mid \text{while } e_1 \text{ do } e_2 \mid e_1; e_2 \mid \boxed{1} \\
 &\quad \mid \text{read } () \mid \text{print } e \\
 \\
 v &\in \text{Values} \\
 v &::= n \mid b \mid () \mid \boxed{1} \\
 \\
 T &\in \text{Types} \\
 T &::= \text{int} \mid \text{bool} \mid \text{ref } T \mid \text{unit}
 \end{aligned}$$

 Semântica operacional *small-step*:

$$\begin{aligned}
 &\frac{||[n]|| = ||[n_1+n_2]||}{n_1+n_2, \sigma, \text{in}, \text{out} \longrightarrow n, \sigma, \text{in}, \text{out}} \quad (\text{OP}+) & \frac{e_2, \sigma, \text{in}, \text{out} \longrightarrow e'_2, \sigma', \text{in}', \text{out}'}{v \text{ op } e_2, \sigma, \text{in}, \text{out} \longrightarrow v \text{ op } e'_2, \sigma', \text{in}', \text{out}'} \quad (\text{OP2}) \\
 & & \frac{e_1, \sigma, \text{in}, \text{out} \longrightarrow e'_1, \sigma', \text{in}', \text{out}'}{e_1 \text{ op } e_2, \sigma, \text{in}, \text{out} \longrightarrow e'_1 \text{ op } e_2, \sigma', \text{in}', \text{out}'} \quad (\text{OP1}) \\
 \\
 &\text{if true then } e_2 \text{ else } e_3, \sigma, \text{in}, \text{out} \longrightarrow e_2, \sigma, \text{in}, \text{out} \quad (\text{IF1}) & \text{if false then } e_2 \text{ else } e_3, \sigma, \text{in}, \text{out} \longrightarrow e_3, \sigma, \text{in}, \text{out} \quad (\text{IF2}) \\
 & & \frac{e_1, \sigma, \text{in}, \text{out} \longrightarrow e'_1, \sigma', \text{in}', \text{out}'}{\text{if } e_1 \text{ then } e_2 \text{ else } e_3, \sigma, \text{in}, \text{out} \longrightarrow \text{if } e'_1 \text{ then } e_2 \text{ else } e_3, \sigma', \text{in}', \text{out}'} \quad (\text{IF3}) \\
 \\
 & & \frac{e_1, \sigma, \text{in}, \text{out} \longrightarrow e'_1, \sigma', \text{in}', \text{out}'}{\text{let } x:T = e_1 \text{ in } e_2, \sigma, \text{in}, \text{out} \longrightarrow \text{let } x:T = e'_1 \text{ in } e_2, \sigma', \text{in}', \text{out}'} \quad (\text{E-LET1}) \\
 & & \frac{}{\text{let } x:T = v \text{ in } e_2, \sigma, \text{in}, \text{out} \longrightarrow \{v/x\} e_2, \sigma, \text{in}, \text{out}} \quad (\text{E-LET2}) \\
 \\
 &\frac{l \in \text{Dom}(\sigma)}{l := v, \sigma, \text{in}, \text{out} \longrightarrow (), \sigma[l \mapsto v], \text{in}, \text{out}} \quad (\text{ATR1}) & \frac{e, \sigma, \text{in}, \text{out} \longrightarrow e', \sigma', \text{in}', \text{out}'}{l := e, \sigma, \text{in}, \text{out} \longrightarrow l := e', \sigma', \text{in}', \text{out}'} \quad (\text{ATR2}) \\
 & & \frac{e_1, \sigma, \text{in}, \text{out} \longrightarrow e'_1, \sigma', \text{in}', \text{out}'}{e_1 := e_2, \sigma, \text{in}, \text{out} \longrightarrow e'_1 := e_2, \sigma', \text{in}', \text{out}'} \quad (\text{ATR}) \\
 \\
 &\frac{l \in \text{Dom}(\sigma) \quad \sigma(l) = v}{!l, \sigma, \text{in}, \text{out} \longrightarrow v, \sigma, \text{in}, \text{out}} \quad (\text{DEREF1}) & \frac{e, \sigma, \text{in}, \text{out} \longrightarrow e', \sigma', \text{in}', \text{out}'}{!e, \sigma, \text{in}, \text{out} \longrightarrow !e', \sigma', \text{in}', \text{out}'} \quad (\text{DEREF}) \\
 & & \frac{e, \sigma, \text{in}, \text{out} \longrightarrow e', \sigma', \text{in}', \text{out}'}{\text{new } e, \sigma, \text{in}, \text{out} \longrightarrow \text{new } e', \sigma', \text{in}', \text{out}'} \quad (\text{NEW}) \\
 &\frac{l \notin \text{Dom}(\sigma)}{\text{new } v, \sigma, \text{in}, \text{out} \longrightarrow l, \sigma[l \mapsto v], \text{in}, \text{out}} \quad (\text{NEW1}) \\
 \\
 &\frac{}{(); e_2, \sigma, \text{in}, \text{out} \longrightarrow e_2, \sigma, \text{in}, \text{out}} \quad (\text{SEQ1}) & \frac{e_1, \sigma, \text{in}, \text{out} \longrightarrow e'_1, \sigma', \text{in}', \text{out}'}{e_1; e_2, \sigma, \text{in}, \text{out} \longrightarrow e'_1; e_2, \sigma', \text{in}', \text{out}'} \quad (\text{SEQ}) \\
 \\
 &\text{while } e_1 \text{ do } e_2, \sigma, \text{in}, \text{out} \longrightarrow \text{if } e_1 \text{ then } (e_2; \text{while } e_1 \text{ do } e_2) \text{ else } (), \sigma, \text{in}, \text{out} \quad (\text{E-WHILE}) \\
 \\
 &\text{print } n, \sigma, \text{in}, \text{out} \longrightarrow (), \sigma, \text{in}, \text{out}.n \quad (\text{PRINT}) & \frac{e, \sigma, \text{in}, \text{out} \longrightarrow e', \sigma', \text{in}', \text{out}'}{\text{print } e, \sigma, \text{in}, \text{out} \longrightarrow \text{print } e', \sigma', \text{in}', \text{out}'} \quad (\text{PRINT}) \\
 \\
 &\text{read } (), \sigma, n, \text{in}, \text{out} \longrightarrow n, \sigma, \text{in}, \text{out} \quad (\text{READ})
 \end{aligned}$$

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**Sistema de Tipos:**

$\frac{}{\Gamma \vdash n : \text{int}}$	(T-INT)	$\frac{\Gamma \vdash e_1 : \text{bool} \quad \Gamma \vdash e_2 : T \quad \Gamma \vdash e_3 : T}{\Gamma \vdash \text{if } e_1 \text{ then } e_2 \text{ else } e_3 : T}$	(T-IF)
$\frac{}{\Gamma \vdash b : \text{bool}}$	(T-BOOL)	$\frac{\Gamma(x) = T}{\Gamma \vdash x : T}$	(T-VAR)
$\frac{\Gamma \vdash e_1 : \text{int} \quad \Gamma \vdash e_2 : \text{int}}{\Gamma \vdash e_1 + e_2 : \text{int}}$	(T-OP+)	$\frac{\Gamma \vdash e_1 : T \quad \Gamma, x \mapsto T \vdash e_2 : T'}{\Gamma \vdash \text{let } x : T = e_1 \text{ in } e_2 : T'}$	(T-LET)
$\frac{\Gamma \vdash e_1 : \text{ref } T \quad \Gamma \vdash e_2 : T}{\Gamma \vdash e_1 := e_2 : \text{unit}}$	(T-ATR)	$\frac{\Gamma \vdash e_1 : \text{bool} \quad \Gamma \vdash e_2 : \text{unit}}{\Gamma \vdash \text{while } e_1 \text{ do } e_2 : \text{unit}}$	(T-WHILE)
$\frac{\Gamma \vdash e : \text{ref } T}{\Gamma \vdash ! e : T}$	(T-DEREF)	$\frac{\Gamma \vdash e_1 : \text{unit} \quad \Gamma \vdash e_2 : T}{\Gamma \vdash e_1; e_2 : T}$	(T-SEQ)
$\frac{\Gamma \vdash e : T}{\Gamma \vdash \text{new } e : \text{ref } T}$	(T-NEW)	$\frac{}{\Gamma \vdash \text{read } () : \text{int}}$	(T-READ)
$\frac{}{\Gamma \vdash () : \text{unit}}$	(T-UNIT)	$\frac{\Gamma \vdash e : \text{int}}{\Gamma \vdash \text{print } e : \text{unit}}$	(T-PRINT)

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**Trabalho**

O trabalho consiste em implementar em OCaml um interpretador para a linguagem L2 da especificação acima e com variações definidas abaixo que serão deixadas propositalmente subespecificadas.

O trabalho será avaliado da seguinte forma:

- nota máxima 9,0 para os trabalhos que implementarem somente L2 conforme a especificação dada acima
- nota máxima 10,0 para os trabalhos que implementarem também uma dentre as seguintes opções:
  - arrays
  - mecanismo de exceções
  - expressão *for* para repetições

Arquivo com as definições dos datatypes necessários e com alguns casos de teste referentes a L2 da especificação dada será disponibilizado no moodle.

**O trabalho deve ser realizado em grupo.**