

# QUIZ 3

Due Jun 8 at 12:30pm

Points 40

Questions 20

Available Jun 8 at 11am - Jun 8 at 12:30pm about 2 hours

Time Limit 90 Minutes

## Instructions

MULTIPLE CHOICE. Choose the best answer.

## Attempt History

	Attempt	Time	Score
LATEST	<a href="#">Attempt 1</a>	50 minutes	40 out of 40

⚠️ Correct answers will be available Jun 15 at 12am - Jun 16 at 12am.

Score for this quiz: **40** out of 40  
Submitted Jun 8 at 11:56am  
This attempt took 50 minutes.

Question 1

2 / 2 pts

What is the slope of the normal line to the curve  $y = 2x^3$  at the point  $(2, 16)$ ?

☐ 6

☒ -1/24

☐ -1/6

☐ 24

**Question 2**

Which of the following is the second derivative of  $y = \cos(2x + 3)$ ?

- ☐  $-\cos(2x + 3)$
- ☐  $-\cos(2)$
- ☐  $\cos 0$
- ☒  $-4\cos(2x + 3)$



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**Question 3**

2 / 2 pts

The derivative of  $y = \frac{x}{x-1}$  is \_\_\_\_\_?

- ☐ 1
- ☐  $\frac{1}{(x-1)^2}$
- ☒  $\frac{-1}{(x-1)^2}$
- ☐  $\frac{2x-1}{(x-1)^2}$

**Question 4**

If  $f(x) = (4x^3 + 2x - 1)^4$ , then  $f'(x)$  \_\_\_\_\_?

- ☐  $48x(12x^2 + 2)^3$
- ☐  $4(4x^3 + 2x - 1)^3$
- ☒  $8(6x^2 + 1)(4x^3 + 2x - 1)^3$
- ☐  $4(12x^2 + 2)^3$



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**Question 5**

2 / 2 pts

Suppose  $f(x) = \tan(x^2) + \cot^2 x$ . What is  $f'(x)$ ?

- ☐  $\sec^2(x^2) - 2 \cot x$
- ☐  $\sec^2(2x) - 2 \csc x \cot x$
- ☒  $2x \sec^2(x^2) - 2 \csc^2 x \cot x$
- ☐  $\sec^2(x^2) - 2 \csc x \cot x$

**Question 6**

2 / 2 pts

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Let  $A(x) = 3x^2$ . The instantaneous rate of change in  $A$  with respect to  $x$  at  $x = -2$  is equal to

☐ 3

☒ -12

☐ 12

☐ -3

### Question 7



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$$\frac{d}{dx}(\sec^2 x - \tan^2 x) = \underline{\hspace{2cm}}?$$

☒ 0

☐  $4 \sec x \tan x$

☐  $2 \sec x - 2 \tan x$

☐  $2 \sec x + 2 \tan x$

### Question 8

2 / 2 pts

Given  $x^2 - 3xy^3 = 10$ . Find  $\frac{dy}{dx}$ .

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☐  $\frac{2x}{9y^2}$

☐  $-\frac{2x}{9y^2}$

☐  $\frac{3y^2 - 2x}{9xy^2}$

☒  $\frac{2x - 3y^2}{9xy^2}$

### Question 9

Given the function defined by:

$$f(x) = \begin{cases} 2x, & \text{if } x > 2 \\ x^2, & \text{if } x \leq 2 \end{cases}$$

What is  $f'_+(2)$ ?

☐ 4

☐ DNE

☒ 2

☐  $+\infty$



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### Question 10

2 / 2 pts

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Given the function defined by:

$$f(x) = \begin{cases} 2x, & \text{if } x > 2 \\ x^2, & \text{if } x \leq 2 \end{cases}$$

Does  $f'(2)$  exist? Why?

- ☐ Yes;  $f'_+(2) = f'_-(2)$
- ☐ No;  $\lim_{x \rightarrow 2^+} f(x) \neq \lim_{x \rightarrow 2^-} f(x)$
- ☒ No;  $f'_+(2) \neq f'_-(2)$
- ☐ Yes;  $f$  is continuous at  $x = 2$ .



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### Question 11

2 / 2 pts

Let  $f(x) = \cos^2(4x^3)$ , then  $f'(x)$  is

- ☐  $-24x^2 \cos(4x^3)$
- ☒  $-24x^2 \cos(4x^3) \sin(4x^3)$
- ☐  $-2 \cos(4x^3) \sin(4x^3)$
- ☐  $-12x^2 \sin^2(4x^3)$

**Question 12**

Given  $f(x) = \sin\left(\frac{x-1}{x+2}\right)$ . Then,  $f'(x)$  is

- ☐  $\cos\left(\frac{x-1}{x+2}\right)$
- ☐  $\cos\left(\frac{3(x-1)}{(x+2)^3}\right)$
- ☐  $\cos\left(\frac{3}{(x+2)^2}\right)$
- ☒  $\frac{3}{(x+2)^2} \cos\left(\frac{x-1}{x+2}\right)$



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**Question 13**

2 / 2 pts

Which of the following statements is NOT ALWAYS TRUE?

- ☐ If  $f$  is differentiable at  $x = a$ , then  $f$  is continuous at  $x = a$ .
- ☐ If  $f'_+(a) = f'_-(a) = k$ , then  $f'(a) = k$ .
- ☐ If  $f'_+(a) \neq f'_-(a)$ , then  $f'(a)$  do not exists.
- ☒ If  $f$  is continuous at  $x = a$ , then then  $f$  is differentiable at  $x = a$ .

## Question 14

The derivative of  $f(x) = \frac{x^2}{6} + \frac{6}{\sqrt{x}}$  is

☐  $\frac{x}{12} - \frac{3}{\sqrt[3]{x^2}}$

☐  $\frac{x}{3} - \frac{3}{\sqrt[3]{x^2}}$

☐  $\frac{x}{12} - \frac{3}{\sqrt{x^3}}$

☒  $\frac{x}{3} - \frac{3}{\sqrt{x^3}}$



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## Question 15

2 / 2 pts

The 4th derivative of  $y = \frac{2}{x}$  is?

☐  $-\frac{2}{x^2}$

☐  $\frac{4}{x^3}$

☒  $\frac{48}{x^5}$

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☐  $\frac{12}{x^4}$

### Question 16

Let

$$f(x) = \begin{cases} x^2 & x \leq 1 \\ 2x & x > 1 \end{cases}$$

Which of the following statements is FALSE?



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$f'(1)$  does not exist because  $f(x)$  is NOT continuous at  $x = 1$



$f'(1) = 2$



$f'_-(1) = 2$



$f'_+(1) = 2$

### Question 17

2 / 2 pts

Given that:

$$\cos(x + y) - \sin(x + y) = 2.$$

Then  $\frac{dy}{dx}$  is equal to ?

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☐ 1☐ undefined☒ -1☐ 0**Question 18**

Suppose that the tumor in a person's body is spherical in shape. The average rate of change of the volume with respect to the radius, as the radius increases from 1.0 cm to 1.1 cm, is 1.0 cm is?

Recall that the volume of the sphere is given by

$V(r) = \frac{4}{3}\pi r^3$ , where  $r$  is the radius

☐  $\frac{19}{12}\pi$ ☐  $\pi$ ☒  $\frac{7}{3}\pi$ ☐  $4\pi$ 

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**Question 19****2 / 2 pts**

Suppose that the tumor in a person's body is spherical in shape. The instantaneous rate of change of the volume with respect to the radius, as the radius increases from 1.0 cm to 1.1 cm, is 1.0 cm is?

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tumor with respect to the radius, when  $t$

Recall that the volume of the sphere is given by

$V(r) = \frac{4}{3}\pi r^3$ , where  $r$  is the radius

☐  $\frac{19}{12}\pi$

☒  $4\pi$

☐  $\pi$

☐  $\frac{7}{3}\pi$

### Question 20



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Find the equation of the line tangent to the curve

$x^2 + 4y^2 = 13$  at the point  $(3, -1)$ .

☐  $4x - 3y - 15 = 0$

☒  $3x - 4y - 13 = 0$

☐  $4x + 3y - 9 = 0$

☐  $3x + 4y - 5 = 0$

Quiz Score: **40** out of 40