

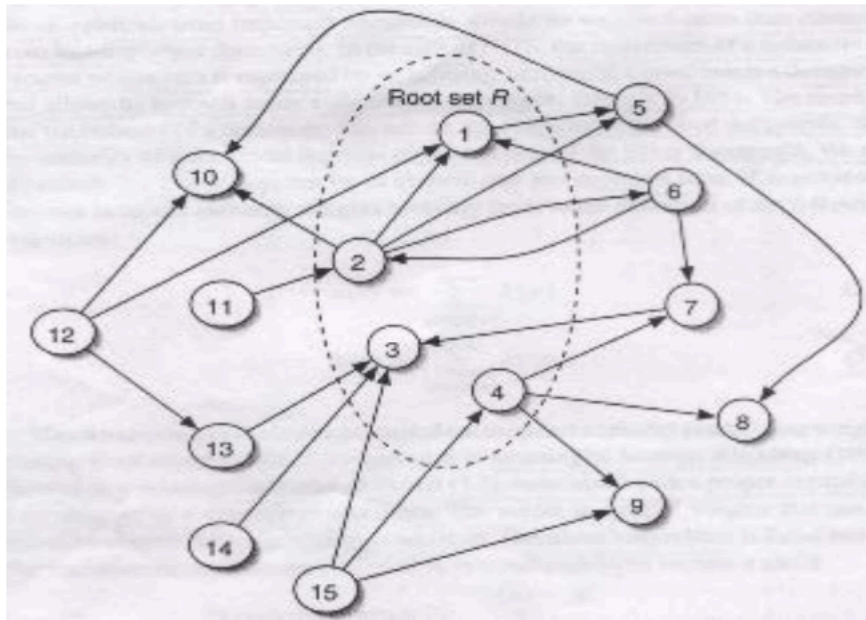
## Assignment 8 Social Network Analysis

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1. Apply the HITS algorithm to the following network (there is no one correct answer)



Root Set  $R = \{1, 2, 3, 4\}$  Extend it to form the base set  $S$

(1) Initialize  $S$  to  $R$ :  $S = R = \{1, 2, 3, 4\}$

(2) Add to  $S$  all pages pointed to by any page in  $R$

Add to  $S$  all pages that point to any page in  $R$ .

$S = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15\}$

(3) For each node initialize the  $a_p$  and  $h_p$  to  $1/n$

$a_1, a_2, a_3 \dots a_{15} = 1/15$

$h_1, h_2, h_3 \dots h_{15} = 1/15$

(4) In each iteration calculate the authority weight for each node in  $S$

$a_1 = h_2 + h_6 + h_{12} = 3/15$

$a_2 = h_6 + h_{11} = 2/15$

$a_3 = h_7 + h_{13} + h_{14} + h_{15} = 4/15$

$a_4 = h_{15} = 1/15$

$a_5 = h_1 + h_2 = 2/15$

$a_6 = h_2 = 1/15$

$a_7 = h_4 + h_6 = 2/15$

$a_8 = h_4 + h_5 = 2/15$

$a_9 = h_4 + h_{15} = 2/15$

$$a_{10}=h_2+h_5+h_{12}=3/15$$

$$a_{11}=0$$

$$a_{12}=0$$

$$a_{13}=h_{12}=1/15$$

$$a_{14}=0$$

$$a_{15}=0$$

$$\text{Normalize: } a_1=0.130, a_2=0.087, a_3=0.174, a_4=0.043, a_5=0.087, a_6=0.043, a_7=a_8=a_9=0.087, \\ a_{10}=0.130, a_{11}=a_{12}=a_{14}=a_{15}=0, a_{13}=0.043$$

$$h_1=a_5=0.087$$

$$h_2=a_1+a_5+a_6+a_{10}=0.391$$

$$h_3=0$$

$$h_4=a_7+a_8+a_9=0.261$$

$$h_5=a_8+a_{10}=0.217$$

$$h_6=a_1+a_2+a_7=0.304$$

$$h_7=a_3=0.174$$

$$h_8=0$$

$$h_9=0$$

$$h_{10}=0$$

$$h_{11}=a_2=0.087$$

$$h_{12}=a_1+a_{10}+a_{13}=0.304$$

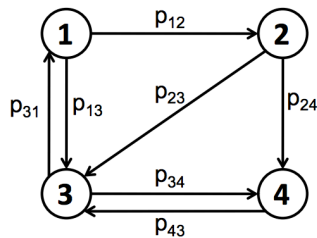
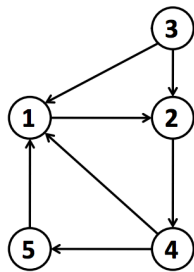
$$h_{13}=a_3=0.174$$

$$h_{14}=a_3=0.174$$

$$h_{15}=a_3+a_4+a_9=0.304$$

$$\text{Normalize: } h_1=0.035, h_2=0.158, h_3=0, h_4=0.105, h_5=0.088, h_6=0.123, h_7=0.070, h_8=h_9=h_{10}=0, \\ h_{11}=0.035, h_{12}=0.123, h_{13}=0.070, h_{14}=0.070, h_{15}=0.123$$

2. Find the Hubs and Authorities of the graphs below given by HITS. Are the results consistent with the notions of Hubs and Authorities?



$$(1) \text{Initialize: } a_1=a_2=a_3=a_4=a_5=1/5$$

$$h_1=h_2=h_3=h_4=h_5=1/5$$

Calculate

$$a1=h3+h4+h5=3/5$$

$$a2=h1+h3=2/5$$

$$a3=0$$

$$a4=h2=1/5$$

$$a5=h4=1/5$$

$$\text{Normalize: } a1=0.429, a2=0.286, a3=0, a4=0.143, a5=0.143$$

$$h1=a2=0.286$$

$$h2=a4=0.143$$

$$h3=a1+a2=0.725$$

$$h4=a1+a5=0.572$$

$$h5=a1=0.429$$

$$\text{Normalize: } h1=0.133, h2=0.066, h3=0.336, h4=0.265, h5=0.199$$

Hubs are 3 and 4

Authorities are 1 and 2.

$$(2)\text{Initialize: } a1=a2=a3=a4=1/4$$

$$h1=h2=h3=h4=1/4$$

Calculate

$$a1=h3=1/4$$

$$a2=h1=1/4$$

$$a3=h1+h2+h4=3/4$$

$$a4=h2+h3=2/4$$

$$\text{Normalize: } a1=0.143, a2=0.143, a3=0.429, a4=0.286$$

$$h1=a2+a3=0.572$$

$$h2=a3+a4=0.715$$

$$h3=a1+a4=0.429$$

$$h4=a3=0.429$$

$$\text{Normalize: } h1=0.267, h2=0.333, h3=0.2, h4=0.2$$

Hubs are 1 and 2

Authorities are 3 and 4.

The results are consistent with the notions of hubs and authorities.