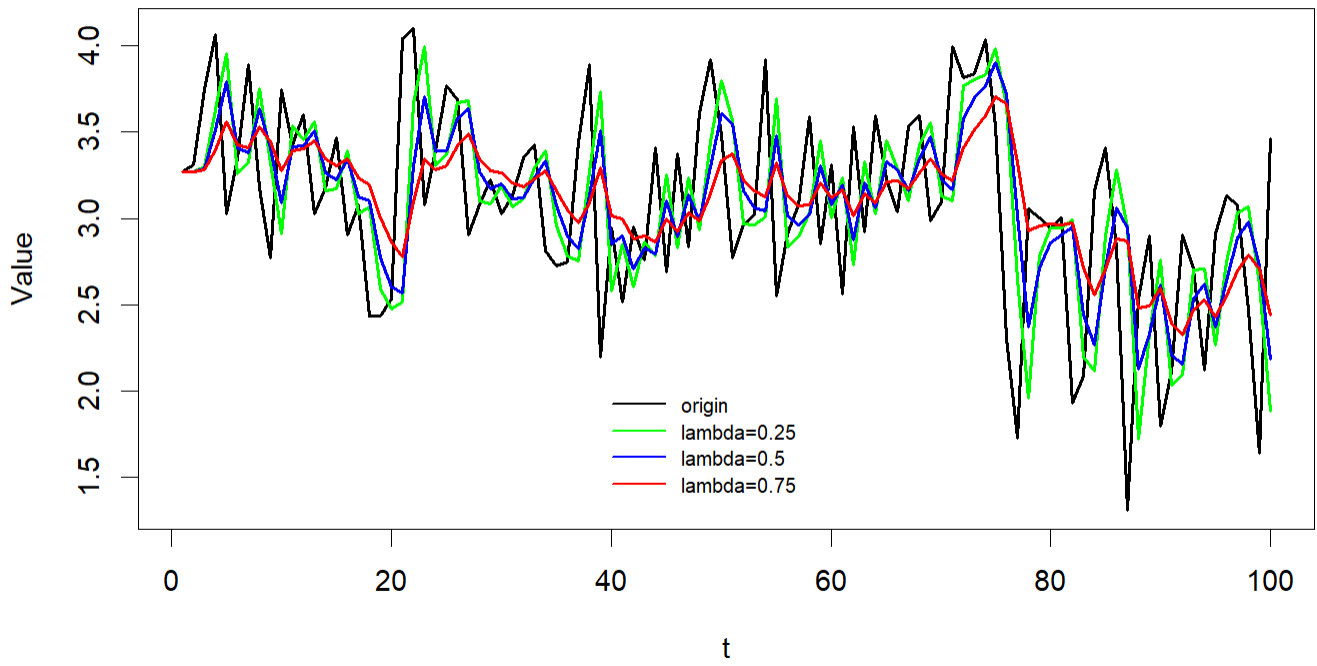


## Pb 3.30

**3.30** For the logarithm of the glacial varve data, say,  $x_t$ , presented in [Example 3.33](#), use the first 100 observations and calculate the EWMA,  $\tilde{x}_{t+1}^t$ , given in (3.151) for  $t = 1, \dots, 100$ , using  $\lambda = .25, .50$ , and  $.75$ , and plot the EWMA's and the data superimposed on each other. Comment on the results.

```
1  library(astsa)
2  n <- 100
3  x <- c(log(varve[1:n]))
4  # 预测
5  EWMA <- function(x, lambda) {
6    xhat=x[1]
7    for(i in 2:n) {xhat=c(xhat, lambda*tail(xhat, 1)+(1-lambda)*x[i-1])}
8    return(xhat)
9  }
10 lambda <- c(.25, .5, .75)
11 xhat1 <- EWMA(x, lambda[1])
12 xhat2 <- EWMA(x, lambda[2])
13 xhat3 <- EWMA(x, lambda[3])
14 # 画图
15 plot.ts(x, col='black', lwd=2, ylab='Value', xlab='t', main='各水平曲线对比')
16 lines(xhat1, col='green', lwd=2)
17 lines(xhat2, col='blue', lwd=2)
18 lines(xhat3, col='red', lwd=2)
19 legend('bottom', inset=.01, bty='n',
        legend=c("origin", "lambda=0.25", "lambda=0.5", "lambda=0.75"), cex=0.7, col=c('black', 'green',
        'blue', 'red'), lwd=c(1.5, 1.5, 1.5, 1.5), x.intersp = 0.6, y.intersp = 0.5)
```

各水平曲线对比



观察发现， $\lambda$  越大则过去的预测值所占的权重就越高，预测值受最近样本的影响就越小，曲线也就越平滑。