

March 23rd (T) YY, ZHL.

1. Demo {  
 a Photo/Image  
 b Video

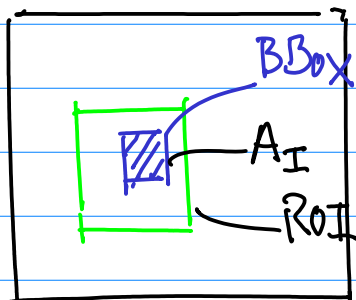
~ ravity — main Program

~ Box.py —  
 Bounding

Testing Program: Rectangle\_intersection.py.

Todo: Send readme.txt,

Threshold  $T = 0.25$



Area (Intersection)  
 Blue

$A_I$  v.s.  $T$

$A_I \geq T \rightarrow$  Alarm  
 $A_I < T$  No Action

To Learn Policy

$$\pi(\vec{a}_t | \vec{s}_t) \quad \dots (2)$$

to maximize Eqn (1).

Augment Eqn (1) with  
 Entropy to maximize  
 Entropy at each visited  
 State.

Define 2 Thresholds {  
 Upper Threshold  $T_u$   
 Lower Threshold  $T_L$

$A_I$   
 $T_u \approx 50\%$

$A_I$  Interested

$T_L \approx 10\%$

Discarded

$A_I$  is not to be considered

Discard  
 $A_I$  if it is Bigger than  $T_u$

$$\propto \gamma / (\pi(a_t | s_t)) \quad \dots (3)$$

Weight  
 ("Temperature" parameter  
 determines the relative  
 importance of Entropy term)  
 Entropy  
 Function  
 Independent  
 Variable  $\pi$   
 Policy

PART II

CTI

March 24 (Wed)

DRL-SAC

Soft Actor Critic Algorithm & Apps.

UC Berkeley & Google PP. 4

Standard RL Objective to maximize  
 Reward

$$\max \left\{ \sum_{\tau} E_{(s_t, a_t) \sim p_{\pi}} [r(\vec{s}_t, \vec{a}_t)] \right\} \quad \dots (1)$$

# Lecture Note on SAC

CTI  
PART II

14L March 25

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Hence Reward in Eqn(1) becomes

$$\max \left\{ \sum_{\tau} E_{(s_t, a_t) \sim p_{\pi}} [r(\vec{s}_t, \vec{a}_t)] + \alpha \gamma I(\pi(a_t | s_t)) \right\}$$

Soft Policy Iteration

Q-value (Reward)

$$Q: S \times A \rightarrow \mathbb{R}$$

... (1) Discount factor

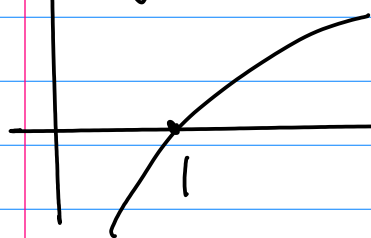
$$T^{\pi} Q(\vec{s}_t, \vec{a}_t) \triangleq r(\vec{s}_t, \vec{a}_t) + \gamma E_{\vec{s}_{t+1} \sim p} [V(\vec{s}_{t+1})] \dots (1^*)$$

Bellman operator  
for each action  
leads to Reward

where

$$V(\vec{s}_{t+1}) = E_{\vec{a}_t \sim \pi} [Q(\vec{s}_t, \vec{a}_t) - \alpha \log \pi(\vec{a}_t | \vec{s}_t)] \dots (2)$$

$\log \pi(\cdot)$



Note: Based on (2)

$\pi(\cdot) \propto \log \pi(\vec{a}_t | \vec{s}_t)$ , so  $\pi(\vec{a}_t | \vec{s}_t)$  is

Reward Based Function

Policy introduced Q-Value (Reward)

Lemma 1. Bellman Operator  $T$  "0" initial time  $t=0$ .

Given initial Condition  $\vec{Q}^0: S \times A \rightarrow \mathbb{R}$  with  $|A| < \infty$

Define Bellman Operator  $T$  as

$$Q^{k+1} = T^{\pi} Q^k \dots (3)$$

"All" total Number of finite Actions

## Part II

CTI

3

$$Q^{k+1} = T^{\pi} Q^k$$

Time Index

Q-Value

(Reward) Function Bellman Operator under Policy  $\pi$

Note: 1° "Argmin" find minimum from a collection of elements, functions, etc.

Example Argmin  $\{1, -1.2, -110, 212\}$   
 $= -110$

For  $k=0$ , we have

$$Q^1 = T^{\pi} Q^0$$

$$k=1, Q^2 = T^{\pi} Q^1 = T^{\pi} (T^{\pi} Q^0) = (T^{\pi})^2 Q^0 \dots (4)$$

...

$$k=i, Q^{i+1} = (T^{\pi})^{i+1} Q^0 \dots (5)$$

Update Q-Value (Reward)  
 Update Policy  $\pi$

$$Z^0 \pi(\vec{a}_t | \vec{s}_t) \text{ Policy}$$

$\pi(\cdot | \vec{s}_t)$  All policies for each/every  $\vec{a}_t$  from  $\vec{a}_t$ .

$\pi'(\cdot | \vec{s}_t)$  one selected from the All policies (all action, e.g. "o" for  $\vec{a}_t$ )

$$\pi_{\text{new}} = \underset{\pi' \in \Pi}{\text{Argmin}} D_{KL} \left( \pi'(\cdot | \vec{s}_t) \parallel \frac{e^{\frac{1}{2} Q^{\pi_{old}}(\vec{s}_t | \cdot)}}{Z^{\pi_{old}}(\vec{s}_t)} \right) \dots (6)$$

Note: 1°  $\pi \in \Pi$  Policy from (belongs to) all collections of the Policies

2°  $D_{KL}$  KL: Kull Back - Leibler Divergence

3°  $\pi'$  One  $\pi$  realization from the collection of All Policies, A particular Policy

Generalize Eqn(b), we have

Lemma 2.

$$\pi_{\text{New}} = f(\pi_{\text{old}} \text{ from one of } | \text{ Conditions } | \text{ the all possible Policies } \dots (bb))$$

$$Q^{\pi^*}(\vec{s}_t, \vec{a}_t) \geq Q^{\pi}(\vec{s}_t, \vec{a}_t)$$

where  $\pi^*$  is from Eqn(b)

f to be minimization problem, so

$$\pi_{\text{New}} = \underset{\pi}{\operatorname{argmin}} D_{\text{KL}}(\pi_{\text{old}} \text{ from one of } | \text{ Condition } | \text{ the all policies } \dots (bc))$$

Policy  $\pi \in \Pi$ , under Eqn(b) converges to

Probability or likelihood

Note: Eqn(b) needs Better Explanation, as why it is formulated as

Note: Parameterized Policy as Gaussian Distribution

$$\frac{e^{-\frac{1}{2} Q^{\pi_{\text{old}}}(\vec{s}_t, \cdot)}}{Z^{\pi_{\text{old}}}(\vec{s}_t)} \dots (b)$$

$D_{\text{KL}}$  minimization Problem.

Now, introduce parameterized Q function, and Policy  $\pi$ .

Note: In NN Softmax Activation Function

We map Neuron Output in  $(-\infty, +\infty)$  to probabilistic distribution  $[0, 1]$ , e.g.

$$f: z \in (-\infty, +\infty) \rightarrow f(z) \in [0, 1]$$

where

$$f(z_i) = \frac{e^{z_i}}{\sum_{j=1}^N e^{z_j}} \dots (8)$$

$Q_{\theta}, \pi_{\phi}, \theta(\text{Theta}), \phi(\text{phi})$  are  
Theta phi

$\phi$ : Policy parameters

$$J_Q(\theta) = E_{(\vec{s}_t, \vec{a}_t) \sim \theta} \left[ \frac{1}{2} \left( Q_\theta(\vec{s}_t, \vec{a}_t) - \left( r(\vec{s}_t, \vec{a}_t) + \gamma E_{\vec{s}_{t+1} \sim p} [V_\theta(\vec{s}_{t+1})] \right) \right)^2 \right] \quad \dots (9)$$

Objective Function

Eqn (1\*) Bellman Iteration

$Q(\theta)$  Q-value (Reward) Function with Parameter  $\theta$  (Theta)

$$\nabla J_Q(\theta) = E_{(\vec{s}_t, \vec{a}_t) \sim \theta} \left\{ \left[ Q_\theta(\vec{s}_t, \vec{a}_t) - \left( r(\vec{s}_t, \vec{a}_t) + \gamma E_{\vec{s}_{t+1} \sim p} [V_\theta(\vec{s}_{t+1})] \right) \right] \cdot \nabla Q_\theta(\vec{s}_t, \vec{a}_t) \right\} \quad \dots (10)$$

$$J_\pi(\phi) = E_{\vec{s}_t \sim D} \left[ E_{\vec{a}_t \sim \pi_\phi} [\alpha \log(\pi_\phi(\vec{a}_t | \vec{s}_t)) - Q_\theta(\vec{s}_t, \vec{a}_t)] \right] \quad \dots (11)$$

$$J_\pi(\phi) = E_{\vec{s}_t \sim D} \left[ E_{\vec{a}_t \sim \pi_\phi} [\cdot] \right]$$

For all states  $\vec{s}_t$  For all actions  $\vec{a}_t$

Note:

$$\frac{d}{dx} \ln(x) = \frac{1}{x}, \quad \frac{d}{dx} \log_a(x) = \frac{1}{x} \frac{1}{\ln(a)} \quad \dots (12)$$

$$\pi(\vec{a}_t, \vec{s}_t) \quad \text{Eqn (1), PP. 2}$$

$$\vec{a}_t = f_\phi(\epsilon_t; \vec{s}_t) \quad \dots (13) \quad \text{Parameterized Policy?}$$

Action

Action Vector

Multi-dimensional

$$\vec{a}_t = (a_{t1}, a_{t2}, \dots, a_{tn})$$

$$J_\pi(\phi) = E_{\vec{s}_t \sim D, \epsilon_t \sim N} [\alpha \log \pi_\phi(f_\phi(\epsilon_t; \vec{s}_t) | \vec{s}_t) - Q_\theta(\vec{s}_t, f_\phi(\epsilon_t; \vec{s}_t))] \quad \dots (14)$$

Parameter for  $\pi$

$\pi_\phi(f_\phi(\epsilon_t | \vec{s}_t) | \vec{s}_t)$  is from

$\pi_\phi(\vec{a}_{\phi t} | \vec{s}_t)$ , or is from

$\pi_\phi(\vec{a}_t | \vec{s}_t)$  is from Eqn(2) PP, 2.

$$\hat{\nabla}_\phi J_\pi(\phi) = \nabla_\phi \alpha \log(\pi_\phi(\vec{a}_t | \vec{s}_t)) + \nabla_{\vec{a}_t} \alpha \log(\pi_\phi(\vec{a}_t | \vec{s}_t)) -$$

Note: Jacobian

Suppose  $\vec{f}: \mathbb{R}^n \rightarrow \mathbb{R}^m$

$$\vec{x} \in \mathbb{R}^n, \vec{f}(\vec{x}) \in \mathbb{R}^m \quad \dots (16a)$$

$$\nabla f_1(\vec{x}) = \begin{bmatrix} \frac{\partial f_1}{\partial x_1} \\ \vdots \\ \frac{\partial f_1}{\partial x_n} \end{bmatrix} \quad \dots (16e)$$

Example:  $f(x_1, x_2) = f(\vec{x}), \vec{x} \in \mathbb{R}^2$

$$\text{Then } \vec{f}(\vec{x}) = [f_1(\vec{x}), f_2(\vec{x})], \quad \vec{x} = (x_1, x_2) \quad \dots (16b)$$

$$\vec{f}(\vec{x}) \in \mathbb{R}^2. \quad \dots (16c)$$

$$\nabla^T f_1(\vec{x}) = \left( \frac{\partial f_1}{\partial x_1} \quad \dots \quad \frac{\partial f_1}{\partial x_n} \right) \quad \dots (16f)$$

Jacobian: Matrix of All its 1st order

Partial Derivatives.

Hence, Jacobian

$$\vec{J} \triangleq \left[ \frac{\partial \vec{f}}{\partial x_1}, \dots, \frac{\partial \vec{f}}{\partial x_n} \right] = \begin{bmatrix} \frac{\partial f_1}{\partial x_1} & \dots & \frac{\partial f_1}{\partial x_n} \\ \vdots & & \vdots \\ \frac{\partial f_m}{\partial x_1} & & \frac{\partial f_m}{\partial x_n} \end{bmatrix} \quad \dots (16d)$$

$$\vec{J} = \begin{bmatrix} \nabla^T f_1 \\ \vdots \\ \nabla^T f_m \end{bmatrix} \quad \dots (16g)$$

gradient of  $f_1(\vec{x})$

$$\nabla f_1 =$$

Note:  $\nabla f_1(\vec{x})$ , if  $f(\vec{x})$  changed to  $f(\vec{x}; \theta)$

$\nabla_{\phi} f_1(\vec{x}; \phi)$ , so we are taking Partial derivative wrt  $\phi$ .

$\phi = (\phi_1, \phi_2, \dots, \phi_n)$ ,  $\vec{\phi}$  is written

Simplified as  $\phi$ .

## Automating Entropy Adjustment

$$\max_{\pi_{0:T}} E_{P_{\pi}} \left[ \sum_{t=0}^T r(\vec{s}_t, \vec{a}_t) \right] \quad \text{s.t.} \quad E_{(\vec{s}_t, \vec{a}_t) \sim P_{\pi}} [-\log(\pi_t(\vec{a}_t | \vec{s}_t))] \geq H, \forall t \dots (17)$$

... (18)

$r(\vec{s}_t, \vec{a}_t)$ : reward function

$\sum_{t=0}^T r(\vec{s}_t, \vec{a}_t)$ : Summation of reward function from  $t=0$  to  $t=T$ ;

$$\max \left[ \sum_{t=0}^T r(\vec{s}_t, \vec{a}_t) \right]$$

maximize the reward function from  $t \in [0, T]$  period.

$$\max E \left[ \sum_{t=0}^T r(\vec{s}_t, \vec{a}_t) \right]$$

maximize expected reward function from  $[0, T]$

Now Add Notation to detail it up

$$\max_{\pi_{0:T}} E \left[ \sum_{t=0}^T r(\vec{s}_t, \vec{a}_t) \right]$$

$\pi_{0:T}$  Policy  $\pi$  from time 0 to T.  $P_{\pi}$  under Policy, Policy  $\pi$

So, we have Eqn (17).

$$-\log(\pi_t(\vec{a}_t | \vec{s}_t)) = \log \frac{1}{\pi_t(\vec{a}_t | \vec{s}_t)}$$

Dynamic Programming, Solving for the policy backward through time

See Ref. pp. 7  
"SAC" Paper

Rewrite Objective Function, Eqn (17)

$$\max_{\pi_0} \{ E[r(\vec{s}_0, \vec{a}_0)] + \max_{\pi_1} \{ E[\dots] + \max_{\pi_T} E[r(\vec{s}_T, \vec{a}_T)] \} \} \dots (18)$$

$$\max_{\pi_0} \{ E[r(\vec{s}_0, \vec{a}_0)] + \max_{\pi_1} \{ E[r(\vec{s}_1, \vec{a}_1)] + \max_{\pi_2} \{ E[r(\vec{s}_2, \vec{a}_2)] \} \} \} \text{ for } t=2$$

$$\max_{\pi_2} \{ E[r(\vec{s}_2, \vec{a}_2)] + \max_{\pi_3} \{ E[r(\vec{s}_3, \vec{a}_3)] \} \} \text{ for } t=3$$

$$\max_{\pi_3} \{ E[r(\vec{s}_3, \vec{a}_3)] + \max_{\pi_4} \{ E[r(\vec{s}_4, \vec{a}_4)] \} \} \text{ for } t=4$$

...

Note :

1<sup>o</sup> Stochastic Gradient

$$\hat{\nabla}_{\theta} J_Q(\theta)$$

from Eqn (6)

Ref. SAC.

Ref. Fujimoto, 2018

2<sup>o</sup> Policy Gradient

$$\hat{\nabla}_{\phi} J_{\pi}(\phi)$$

from Eqn (10), Ref

21-Dimensional Humanoid

3<sup>o</sup> Single Q function  $\rightarrow$  2 soft Q-function  
Speed up training.



SAC<sub>ref.</sub>  
Algorithm 1. (pp. 8)

Input:  $\theta_1, \theta_2, \phi$        $\theta_1, \theta_2$  for Reward  
    $\phi$  for Policy  $\pi$   
 $\bar{\theta}_1 \leftarrow \theta_1, \bar{\theta}_2 \leftarrow \theta_2$

$\mathcal{D} \leftarrow \emptyset$       Replay Pool

for each iteration do

for environment Step do  
     $\vec{a}_t \sim \pi_\phi(\vec{a}_t | \vec{s}_t)$       Sample action from policy  
     $\vec{s}_{t+1} \sim p(\vec{s}_{t+1} | \vec{s}_t, \vec{a}_t)$       Sample Transition from Enviro.  
     $\mathcal{D} \leftarrow \mathcal{D} \cup \{(\vec{s}_t, \vec{a}_t, r(\vec{s}_t, \vec{a}_t), \vec{s}_{t+1})\}$       Store transition in Replay pool  
end for

for each gradient step do

$\theta_i \leftarrow \theta_i - \lambda_Q \hat{\nabla}_{\theta_i} J_Q(\theta_i)$  for  $i \in \{1, 2\}$       update Q-func Parameter  
 $\phi \leftarrow \phi - \lambda_\pi \hat{\nabla}_\phi J_\pi(\phi)$       update policy weights  
 $\alpha \leftarrow \alpha - \lambda \hat{\nabla}_\alpha J(\alpha)$       update temperature  
 $\bar{\theta}_i \leftarrow \tau \theta_i + (1 - \tau) \bar{\theta}_i$  for  $i \in \{1, 2\}$       Update network Weights  
end for

end for

Output:  $\theta_1, \theta_2, \phi$

Note: 4 Dual Objectives  $\rightarrow$  Dual Gradient Descent  
   Alternating Between  
   Lagrangian.

$$\alpha^* = \underset{\alpha}{\operatorname{argmin}} E_{\vec{a}_t \sim \pi_t^*}[\cdot] \quad \dots (17)$$

5. "Off-Policy" Data? Ref.

# Path Planning with Reward Function

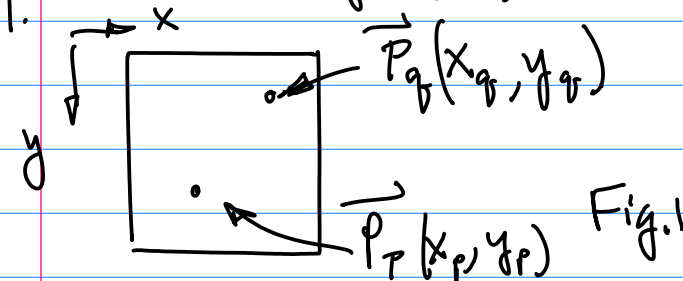
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April 2nd, 2021

Reward Functions Based On Difference For Autonomous Driving

- micro-Scale:  $\vec{P}_p$  to  $\vec{P}_q$  within One Image ( $x_w - y_w - z_w$ )
- medium Scale: Within One Room. ( $I(x, y)$ )
- Global Scale: One Environment Multiple Rooms.

Micro-Scale  
Within One Image  $I(x, y)$



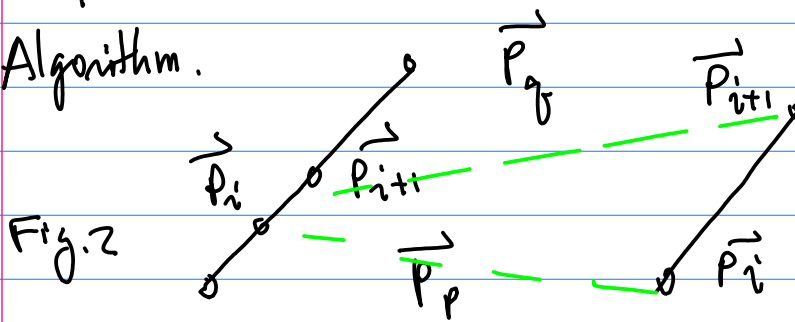
2. the Path from  $\vec{P}_p$  to  $\vec{P}_q$  is accomplished step by step starting from  $\vec{P}_p$ , then update each Step  $\vec{P}_i$  to  $\vec{P}_{i+1}$ , ...,  $i=1, 2, \dots, N$

$\vec{P}_1 = \vec{P}_p$  (starting point)

$\vec{P}_N = \vec{P}_q$  (ending point)

3.  $\vec{P}_i$  for  $i=1, 2, \dots, N$  is Computed Based on DDA

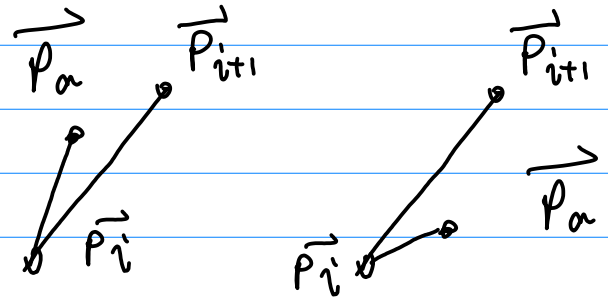
Algorithm.



$\vec{P}_i$  to  $\vec{P}_{i+1}$  is one pixel equivalent distance in the world coordinate

$\vec{P}_{act}$  or  $\vec{P}_a(x_a, y_a)$   
Actual AUV Travels during that Step  $i$  to  $i+1$ , e.g. time  $t_i$  to  $t_{i+1}$ , is

Case I Actual Displacement within  $\vec{P}_{i+1}$



Case II Actual Displacement outside  $\vec{P}_{i+1}$

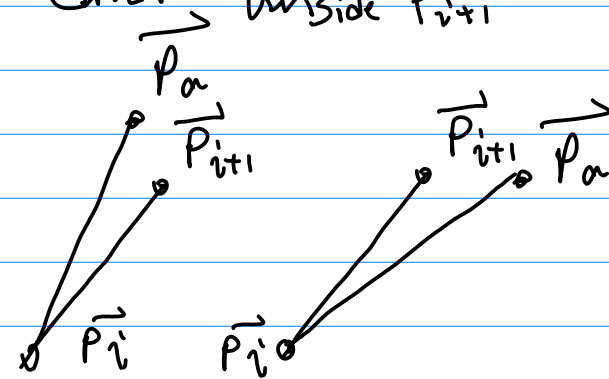


Fig. 4.

Case III Opposite Directions as in Case I & II.

# Path Planning with Reward Function HL

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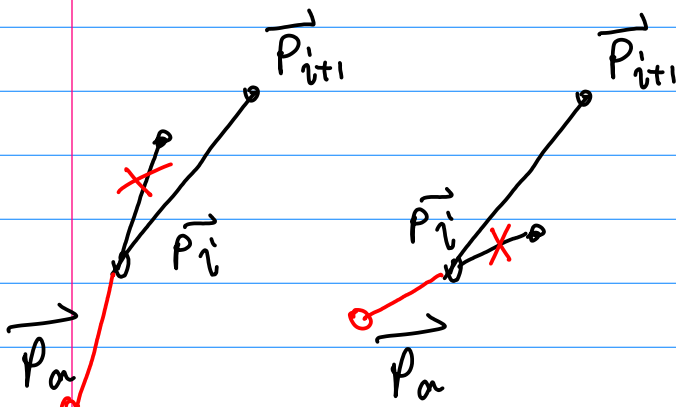


Fig 5a

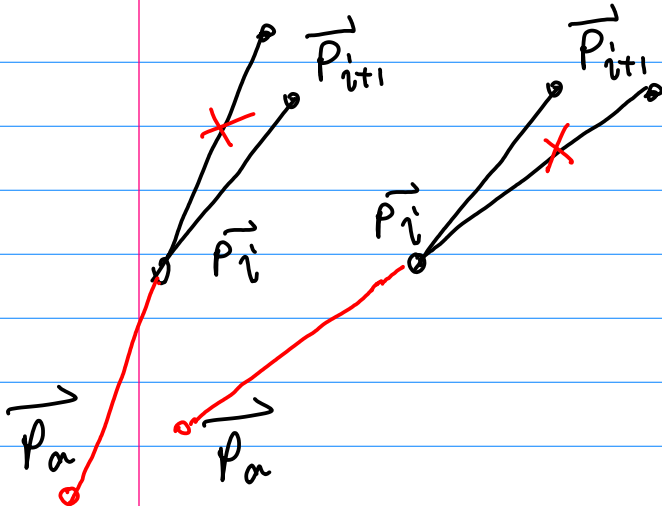


Fig 5b

Actual Displacement Direction Vector

$$\vec{d}_a \triangleq \vec{P}_a - \vec{P}_i = (x_a - x_i, y_a - y_i) \quad \dots (3)$$

5. Define Deviation Index Based on

$\begin{cases} a & \text{Distance Difference} \\ b & \text{Directional Difference} \end{cases}$

Note:

$$\vec{d}_d \cdot \vec{d}_a = \|\vec{d}_d\| \|\vec{d}_a\| \cos \alpha \quad \dots (4)$$

Normalize it to make it an index

$$\frac{\vec{d}_d \cdot \vec{d}_a}{\|\vec{d}_d\| \|\vec{d}_a\|} = \cos \alpha \quad \dots (4-1)$$

4. Path Deviation  $\vec{P}_a$  calculation By Dot Product

$$(\vec{P}_a - \vec{P}_i) \cdot (\vec{P}_{i+1} - \vec{P}_i) \quad \dots (1)$$

where

Desired Direction Vector

$$\vec{d}_d \triangleq \vec{P}_{i+1} - \vec{P}_i = (x_{i+1} - x_i, y_{i+1} - y_i) \quad \dots (2)$$

Property 1: Displacement if  $\vec{d}_a = \vec{d}_d$  and distance

$$\|\vec{P}_a - \vec{P}_i\| = \|\vec{P}_{i+1} - \vec{P}_i\|$$

then, the AGV is on the right path direction and has the exact desired displacement distance to make  $\vec{P}_a = \vec{P}_{i+1}$

~~Define~~  
Definition 1. Direction Index  $I_{dir}$ , a  
Scalar is defined as  
the angle  $\alpha$  Between  
 $(\vec{P}_a - \vec{P}_i)$  and  $(\vec{P}_{i+1} - \vec{P}_i)$ ;

e.g.

$$I_{dir} = \cos \alpha = \frac{\vec{d}_a \cdot \vec{d}_d}{\|\vec{d}_a\| \|\vec{d}_d\|} \dots (5)$$

Define Distance index  $I_{dis}$ , as  
Scalar as

$$I_{dis} = \begin{cases} \frac{\|\vec{P}_a - \vec{P}_i\|}{\|\vec{P}_{i+1} - \vec{P}_i\|}, & \dots (6a) \\ \frac{\|\vec{P}_a - \vec{P}_i\| - \|\vec{P}_{i+1} - \vec{P}_i\|}{\|\vec{P}_{i+1} - \vec{P}_i\|} & \text{if } \|\vec{P}_a - \vec{P}_i\| \leq \|\vec{P}_{i+1} - \vec{P}_i\| \end{cases}$$

$$\text{if } \|\vec{P}_a - \vec{P}_i\| > \|\vec{P}_{i+1} - \vec{P}_i\| \dots (6b)$$

Note  $I_{dis} \in [0, 1]$ ; and  $I_{dir} \in [0, 1]$   
( $\cos \alpha$ )

Definition 2. Define Combo Index  $I_\Sigma$   
for AUV as

$$I_\Sigma = \beta I_{dir} + (1 - \beta) I_{dis} \dots (7)$$

$$I_\Sigma = \beta I_{dir} + (1 - \beta) I_{dis}$$

where  $\beta \in [0, 1]$

for Equal weights on  
direction and distance  
we have  $\beta = \frac{1}{2}$ . So

$$I_\Sigma = \frac{1}{2} (I_{dir} + I_{dis}) \dots (7a)$$

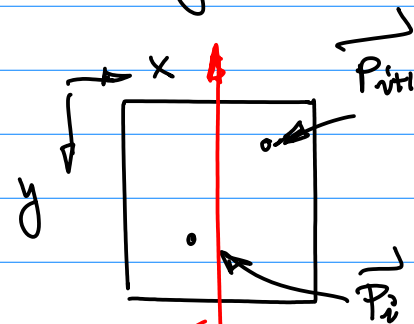
PART II. Consider Actuation.

Note 1. How to find  $\vec{d}_a$ ?

magnetometer find  $\vec{d}_a$

Note 2. How to find  $\vec{d}_d$

See Eqn (2), Computer Vision  
Technique plus  $X_w - Y_w - Z_w$   
mapping.

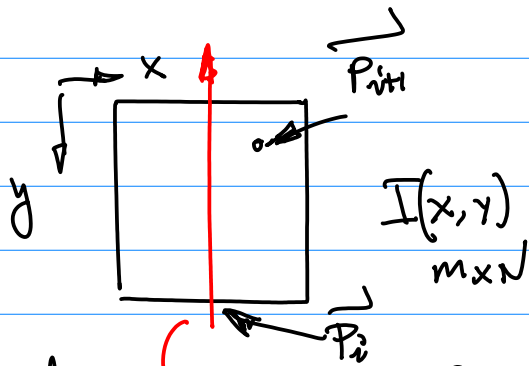


Vehicle Forward Looking  
Direction LSMSEN  
= Physical world Calibration  
in  $X_w - Y_w - Z_w$

LSMSEN Sensor Input

# Path Planning with Reward Function HL

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- i' Angle  $\theta = 132.615^\circ$  for Example (Theta), Vehicle forward direction
- ii' Red Line on  $I(x,y)$ : Vehicle forward Looking Direction
- iii'  $P_i$  Current time  $i$  position

For  $M \times N$  Image,  $\vec{P}_i(x,y) = \text{Im}(\frac{M}{2}, N-1)$   
 $m$ : Col.  $\dots (8)$   
 $N$ : Row

iv' Mapping from  $I(x,y)$  to  $x_w - y_w - z_w$

$$f: (x,y) \in \mathbb{I}^2 \rightarrow (x_w, y_w, z_w) \in \mathbb{R}^3 \dots (9)$$

Definition 4. Define AGV forward Looking Direction By LSMSEN Sensor Input. e.g., Equal to the Angle from LSMSEN.

Definition 5. Define AGV  $\vec{P}_i$  Position as the  $(x,y) = (\frac{M}{2}, N-1)$ , for  $M \times N$   $I(x,y)$ .

Property 2. A feature Point  $\vec{P}_{i+1}$  on Image  $I(x,y)$ 's location  $(x_{i+1}, y_{i+1})$  is mapped to the  $x_w - y_w - z_w$  By the mapping function  $f$  as follows

$$f: (x,y) \in \mathbb{I}^2 \rightarrow (x_w, y_w, z_w) \in \mathbb{R}^3 \text{ such that}$$

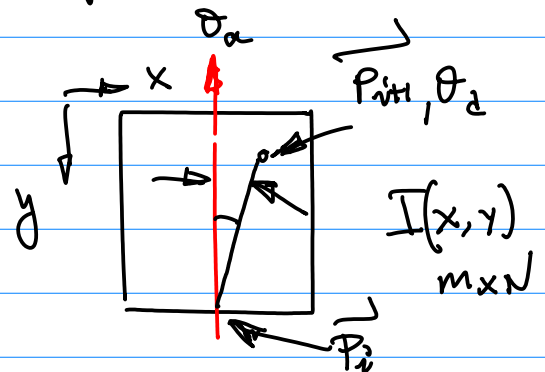
$$(x_{i+1}, y_{i+1}) \rightarrow (x_{i+1}, y_{i+1}, z_i) \Big|_{z_i=c}$$

e.g., for  $\text{Emh}(x_{i+1}, y_{i+1})$  we have  $(x_{i+1}, y_{i+1}, c)_w$

5. Driving objectives:  
To align the Red line with  $\vec{d}_{dir} = (\vec{P}_{i+1} - \vec{P}_i)$

How much to Drive?

$\alpha$  Angle  $\theta_d - \theta_a = \Delta\theta$  to be zero'd



distance to  $\vec{P}_{i+1}$  to be zero'd.

	map to $X_w Y_w Z_w$	Result
$\theta_a$	LSMSEN	—
$\theta_d$	$f(\cdot)$	$X_{i+1,w}, Y_{i+1,w}$

from  $X_{i,w}, Y_{i,w}$  to  $X_{i+1,w}, Y_{i+1,w}$

{ Left wheel } Displacement, dis  
                   { Angle  
 { Right wheel } Displacement, dis  
                   { Angle

6 DoF Robot Arm Reward function.

1. 3 Types Movement

Linear  $\vec{P}_i$  to  $\vec{P}_{i+1}$   
 Angular (Joint Angle)  
 Arc,  $\vec{P}_i$  to  $\vec{P}_{i+1}$  via Control Pt.  
 $\vec{P}_c$