



# 110-2-one-shot-facial-2020-7-27.pptx

CTI One Corporation

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Project Lead: Harry Li, Ph.D.

Team Member:

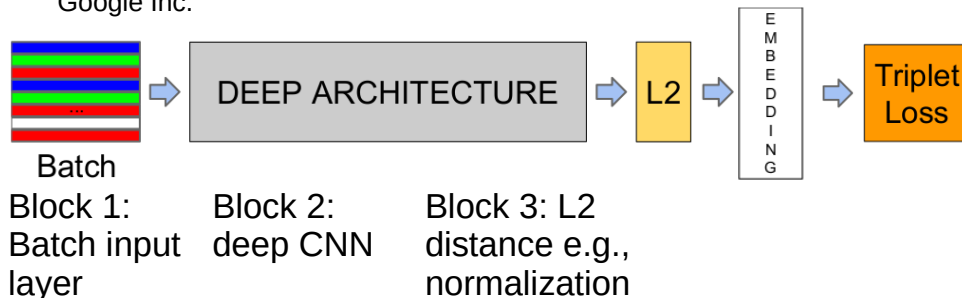


# FaceNet from Google

A Unified Embedding for Face Recognition and Clustering

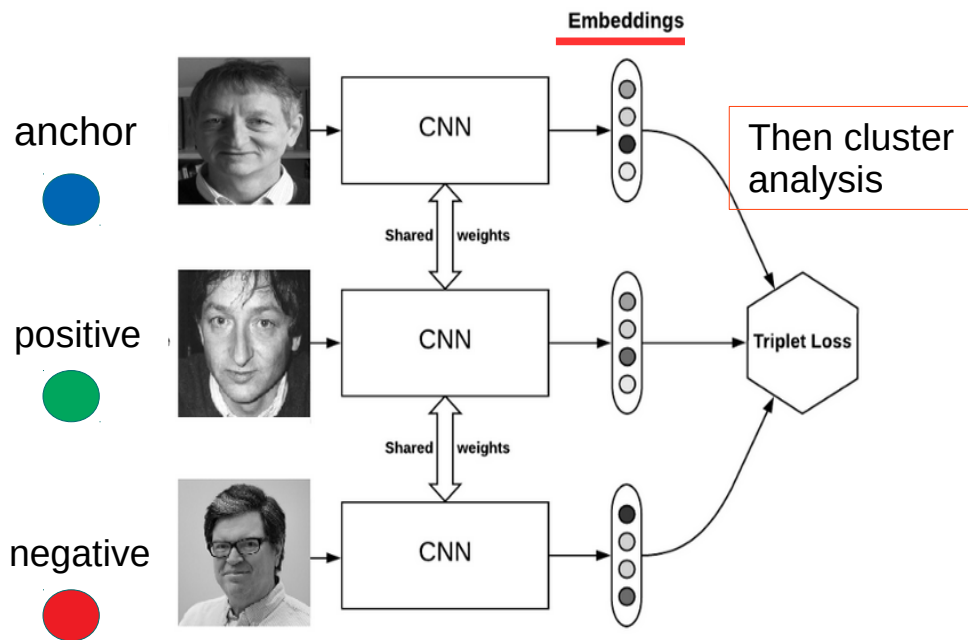
Florian Schroff Dmitry Kalenichenko James Philbin  
fschroff@google.com dkalenichenko@google.com  
jphilbin@google.com  
Google Inc.

FaceNet learns the mapping from the images and creates embeddings rather than using any output layer for recognition

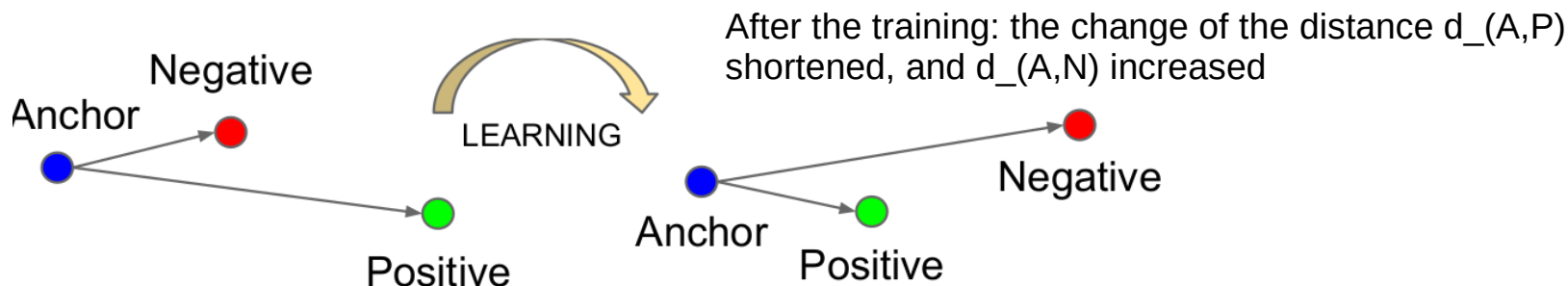


L2, e.g, the Euclidean norm, a positive distance, calculated as the square root of the sum of the squared vector values.

Namely, we strive for an embedding  $f(x)$ , from an image  $x$  into a feature space  $\mathbb{R}^d$ , such that the squared distance between *all* faces, independent of imaging conditions, of the same identity is small, whereas the squared distance between a pair of face images from different identities is large.



# Triplet Loss Function



The objective:

$$\|f(x_i^a) - f(x_i^p)\|_2^2 + \alpha < \|f(x_i^a) - f(x_i^n)\|_2^2 \quad \dots (1)$$

$$\forall (f(x_i^a), f(x_i^p), f(x_i^n)) \in \mathcal{T} \quad \dots (2)$$

The loss function to be minimized:

$$\sum_i^N \left[ \|f(x_i^a) - f(x_i^p)\|_2^2 - \|f(x_i^a) - f(x_i^n)\|_2^2 + \alpha \right]_+ \quad \dots (3)$$



# CNN1 Architecture

Table 1. NN1.

This table show the structure of our Zeiler&Fergus [22] based model with  $1 \times 1$  convolutions inspired by [9].

The input and output sizes are described in rows  $\times$  cols  $\times$  #f ilters.

The kernel is specified as rows  $\times$  cols, stride and the maxout [6] pooling size as  $p = 2$ .

One way to reduce the training time is to normalize the activities of the neurons.

<https://arxiv.org/abs/1607.06450>

layer	size-in	size-out	kernel	param	FLPS
conv1	$220 \times 220 \times 3$	$110 \times 110 \times 64$	$7 \times 7 \times 3, 2$	9K	115M
pool1	$110 \times 110 \times 64$	$55 \times 55 \times 64$	$3 \times 3 \times 64, 2$	0	
morm1	$55 \times 55 \times 64$	$55 \times 55 \times 64$		0	
conv2a	$55 \times 55 \times 64$	$55 \times 55 \times 64$	$1 \times 1 \times 64, 1$	4K	13M
conv2	$55 \times 55 \times 64$	$55 \times 55 \times 192$	$3 \times 3 \times 64, 1$	111K	335M
morm2	$55 \times 55 \times 192$	$55 \times 55 \times 192$		0	
pool2	$55 \times 55 \times 192$	$28 \times 28 \times 192$	$3 \times 3 \times 192, 2$	0	
conv3a	$28 \times 28 \times 192$	$28 \times 28 \times 192$	$1 \times 1 \times 192, 1$	37K	29M
conv3	$28 \times 28 \times 192$	$28 \times 28 \times 384$	$3 \times 3 \times 192, 1$	664K	521M
pool3	$28 \times 28 \times 384$	$14 \times 14 \times 384$	$3 \times 3 \times 384, 2$	0	
conv4a	$14 \times 14 \times 384$	$14 \times 14 \times 384$	$1 \times 1 \times 384, 1$	148K	29M
conv4	$14 \times 14 \times 384$	$14 \times 14 \times 256$	$3 \times 3 \times 384, 1$	885K	173M
conv5a	$14 \times 14 \times 256$	$14 \times 14 \times 256$	$1 \times 1 \times 256, 1$	66K	13M
conv5	$14 \times 14 \times 256$	$14 \times 14 \times 256$	$3 \times 3 \times 256, 1$	590K	116M
conv6a	$14 \times 14 \times 256$	$14 \times 14 \times 256$	$1 \times 1 \times 256, 1$	66K	13M
conv6	$14 \times 14 \times 256$	$14 \times 14 \times 256$	$3 \times 3 \times 256, 1$	590K	116M
pool4	$14 \times 14 \times 256$	$7 \times 7 \times 256$	$3 \times 3 \times 256, 2$	0	
concat	$7 \times 7 \times 256$	$7 \times 7 \times 256$		0	
fc1	$7 \times 7 \times 256$	$1 \times 32 \times 128$	maxout $p=2$	103M	103M
fc2	$1 \times 32 \times 128$	$1 \times 32 \times 128$	maxout $p=2$	34M	34M
fc7128	$1 \times 32 \times 128$	$1 \times 1 \times 128$		524K	0.5M
L2	$1 \times 1 \times 128$	$1 \times 1 \times 128$		0	
total				140M	1.6B



# CNN2 Architecture

type	output size	depth	#1×1	#3×3 reduce	#3×3	#5×5 reduce	#5×5	pool proj (p)	params	FLOPS
conv1 (7×7×3, 2)	112×112×64	1							9K	119M
max pool + norm	56×56×64	0						m 3×3, 2		
inception (2)	56×56×192	2		64	192				115K	360M
norm + max pool	28×28×192	0						m 3×3, 2		
inception (3a)	28×28×256	2	64	96	128	16	32	m, 32p	164K	128M
inception (3b)	28×28×320	2	64	96	128	32	64	$L_2$ , 64p	228K	179M
inception (3c)	14×14×640	2	0	128	256,2	32	64,2	m 3×3,2	398K	108M
inception (4a)	14×14×640	2	256	96	192	32	64	$L_2$ , 128p	545K	107M
inception (4b)	14×14×640	2	224	112	224	32	64	$L_2$ , 128p	595K	117M
inception (4c)	14×14×640	2	192	128	256	32	64	$L_2$ , 128p	654K	128M
inception (4d)	14×14×640	2	160	144	288	32	64	$L_2$ , 128p	722K	142M
inception (4e)	7×7×1024	2	0	160	256,2	64	128,2	m 3×3,2	717K	56M
inception (5a)	7×7×1024	2	384	192	384	48	128	$L_2$ , 128p	1.6M	78M
inception (5b)	7×7×1024	2	384	192	384	48	128	m, 128p	1.6M	78M
avg pool	1×1×1024	0								
fully conn	1×1×128	1							131K	0.1M
L2 normalization	1×1×128	0								
total									7.5M	1.6B

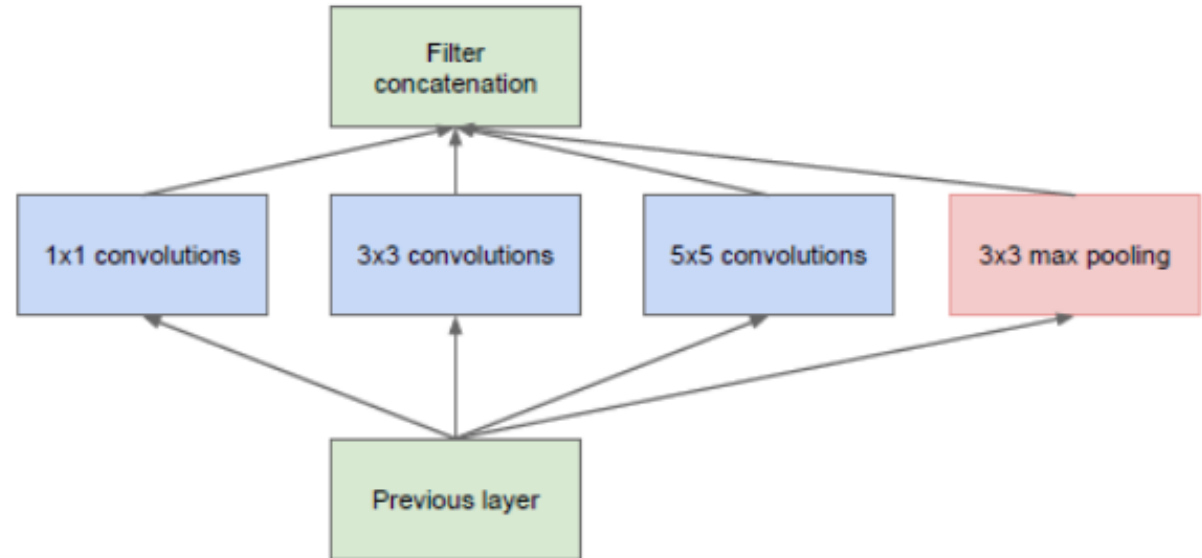


# CNN2 Architecture

Details of the NN2 Inception architecture. This model uses L 2 pooling instead of max pooling (m), where specified. The pooling is always 3×3 (aside from the final average pooling) and in parallel to the convolutional modules inside each Inception module. If there is a dimensionality reduction after the pooling it is denoted with p. 1×1, 3×3, and 5×5 pooling are then concatenated to get the final output.

“(Inception Layer) is a combination of all those layers (namely, 1×1 Convolutional layer, 3×3 Convolutional layer, 5×5 Convolutional layer) with their output filter banks concatenated into a single output vector forming the input of the next stage.”

<https://www.analyticsvidhya.com/blog/2018/10/understanding-inception-network-from-scratch/>



# Triple Lose Function for Learning/Training

FaceNet: A Unified Embedding for Face Recognition and Clustering

a

anchor



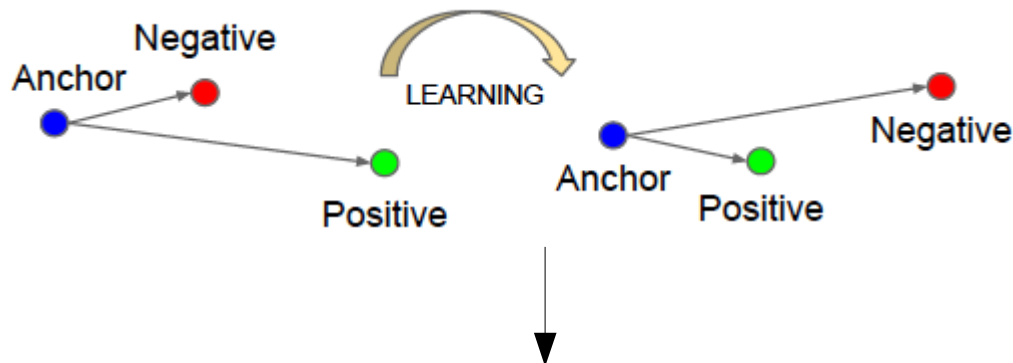
p

positive



n

negative



$$\sum_i^N \left[ \|f(x_i^a) - f(x_i^p)\|_2^2 - \|f(x_i^a) - f(x_i^n)\|_2^2 + \alpha \right]_+$$

$x_j^a$  image  $j$  from anchor group  $a$

$f(x_j^a)$  embedding, e.g., feature vectors



## Choose Extreme Triple Lose Function for Training

$$\text{Argmax } || f(x_i^a) - f(x_i^p) ||_2^2 \quad \dots (1)$$

$$\text{Argmin } || f(x_i^a) - f(x_i^n) ||_2^2 \quad \dots (2)$$

Use equations (1) and (2) to train CNN to make sure the worst positive matching is not so “far away”, and the worst negative matching is not so “close together”.

Choose around 1000–2000 samples (In most experiments the batch size was around 1800).

Use adaptive learning rate

$$W_t = W'_{t-1} - \eta * g_t \quad \dots (3)$$

Eqn (3) is the regular Stochastic Greatest Descent method, eta is a constant

$$W_t = W'_{t-1} - \eta'_t * g_t \quad \dots (4)$$

Changing eta prime leads to adaptive learning rate, where

$$\eta'_t = \eta / \sqrt{a_{t-1} + \epsilon} \quad \dots (5)$$

$$a_{t-1} = \sum_{i=1}^{t-1} g_i^2 \quad \text{and} \quad g_i = (\partial L / \partial W)$$





## Choose Extreme Triple Lose Function for Training

$$\text{Argmax } || f(x_i^a) - f(x_i^p) ||_2^2 \quad \dots (1)$$

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$$\eta'_t = \eta / \sqrt{a_{t-1} + \epsilon} \quad \dots (5)$$

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## TA (True Acceptance) and FA

Pair

$$TA(d) = \{(i, j) \in \mathcal{P}_{\text{same}}, \text{ with } D(x_i, x_j) \leq d\}$$

True accepts are the face pairs that were correctly classified as same at threshold 'd'.

$$FA(d) = \{(i, j) \in \mathcal{P}_{\text{diff}}, \text{ with } D(x_i, x_j) \leq d\}$$

False accepts are the face pairs that were incorrectly classified as same

$\mathcal{P}_{\text{same}}$  - It represents the pair of same identities

$\mathcal{P}_{\text{diff}}$  - It represents the pair of different identities

$D(x_i, x_j)$  - It is the square L2 distance between the pair of images

$d$  - It is the distance threshold

$$VAL(d) = \frac{|TA(d)|}{|\mathcal{P}_{\text{same}}|}, \quad FAR(d) = \frac{|FA(d)|}{|\mathcal{P}_{\text{diff}}|}$$

The validation rate (VAL) and false accept rate (FAR) for a given face distance 'd' is defined as

### References:

1. FaceNet: A Unified Embedding for Face Recognition and Clustering

<https://arxiv.org/abs/1503.03832> Cornell University



## Zeiler & Fergus Architecture in the FaceNet Research Paper

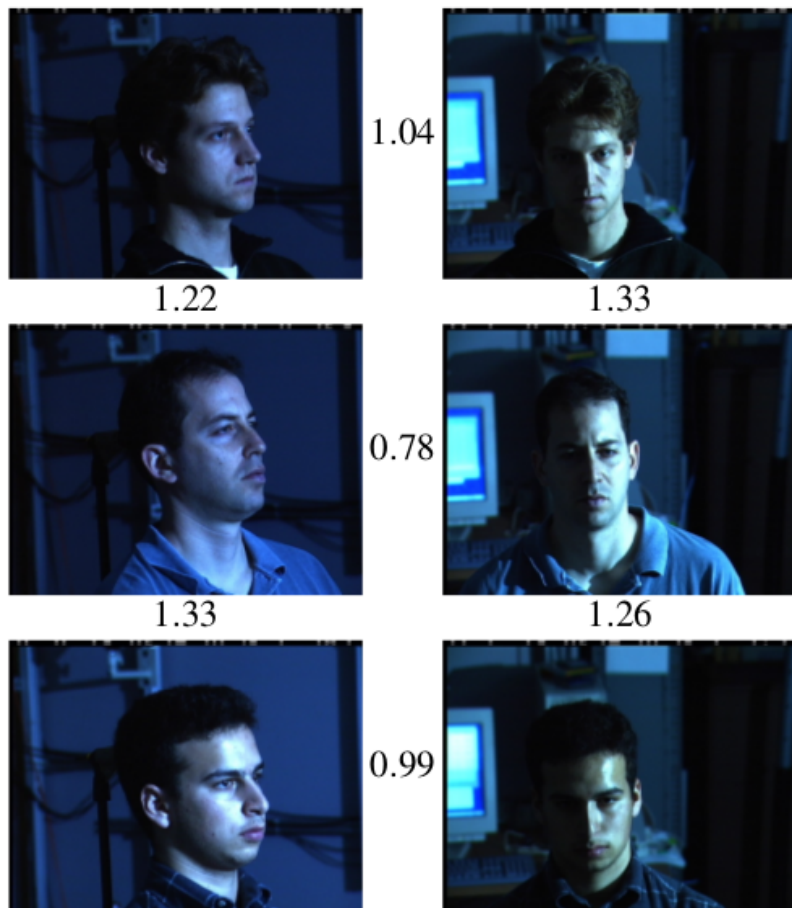
layer	size-in	size-out	kernel	param	FLPS
conv1	220×220×3	110×110×64	7×7×3, 2	9K	115M
pool1	110×110×64	55×55×64	3×3×64, 2	0	
rnorm1	55×55×64	55×55×64		0	
conv2a	55×55×64	55×55×64	1×1×64, 1	4K	13M
conv2	55×55×64	55×55×192	3×3×64, 1	111K	335M
rnorm2	55×55×192	55×55×192		0	
pool2	55×55×192	28×28×192	3×3×192, 2	0	
conv3a	28×28×192	28×28×192	1×1×192, 1	37K	29M
conv3	28×28×192	28×28×384	3×3×192, 1	664K	521M
pool3	28×28×384	14×14×384	3×3×384, 2	0	
conv4a	14×14×384	14×14×384	1×1×384, 1	148K	29M
conv4	14×14×384	14×14×256	3×3×384, 1	885K	173M
conv5a	14×14×256	14×14×256	1×1×256, 1	66K	13M
conv5	14×14×256	14×14×256	3×3×256, 1	590K	116M
conv6a	14×14×256	14×14×256	1×1×256, 1	66K	13M
conv6	14×14×256	14×14×256	3×3×256, 1	590K	116M
pool4	14×14×256	7×7×256	3×3×256, 2	0	
concat	7×7×256	7×7×256		0	
fc1	7×7×256	1×32×128	maxout p=2	103M	103M
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fc7128	1×32×128	1×1×128		524K	0.5M
L2	1×1×128	1×1×128		0	
total				140M	1.6B

<https://medium.com/analytics-vidhya/introduction-to-facenet-a-unified-embedding-for-face-recognition-and-clustering-dbdac8e6f02>

140 million parameters and 1.6 billion FLOPS (Floating point operations per second) per image.

Academic Datasets: Labeled Faces in the Wild (LFW) is the de-facto academic test set for face verification [7]

## Pose and Illumination Invariant



Illumination and Pose invariance. Pose and illumination have been a long standing problem in face recognition. This figure shows the output distances of FaceNet between pairs of faces of the same and a different person in different pose and illumination combinations. A distance of 0.0 means the faces are identical, 4.0 corresponds to the opposite spectrum, two different identities. You can see that a threshold of 1.1 would classify every pair correctly



# One Shot Facial Recognition

<https://machinelearningmastery.com/one-shot-learning-with-siamese-networks-contrastive-and-triplet-loss-for-face-recognition/>

One, or a few, examples are used

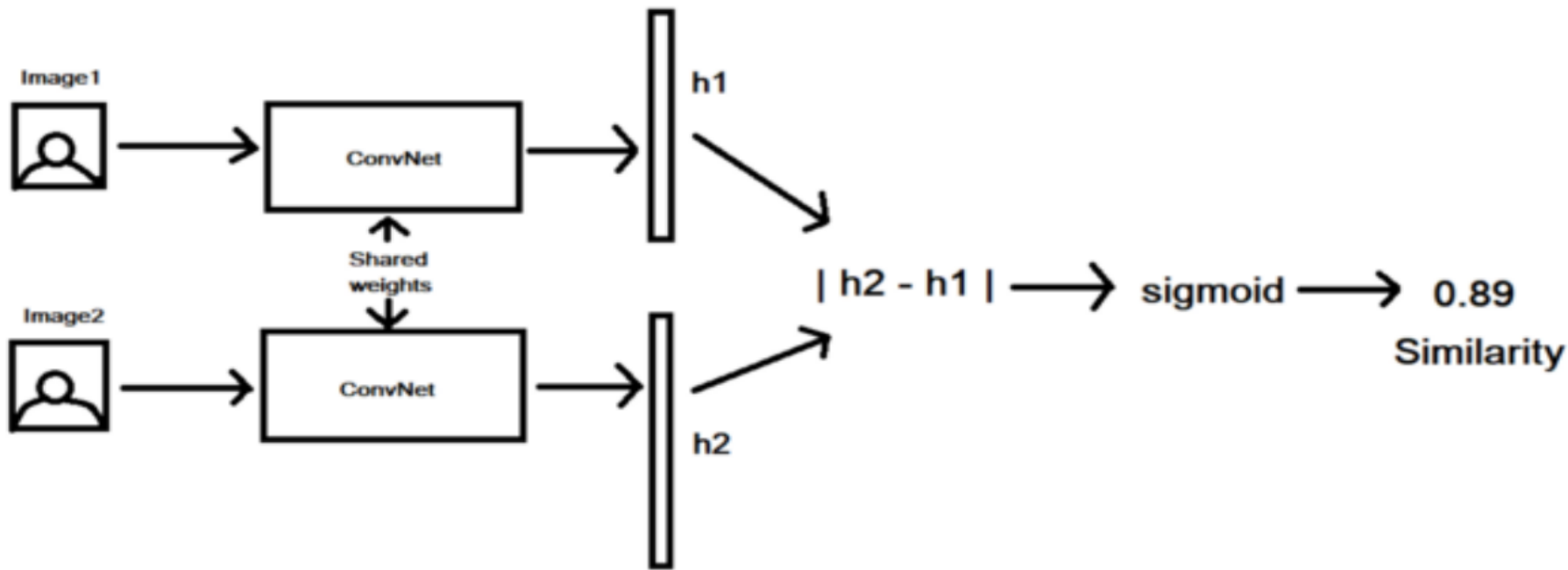
To classify many new examples in the future.

Low-dimensional feature representation, called a face embedding

Embeddings were learned using a Siamese network.



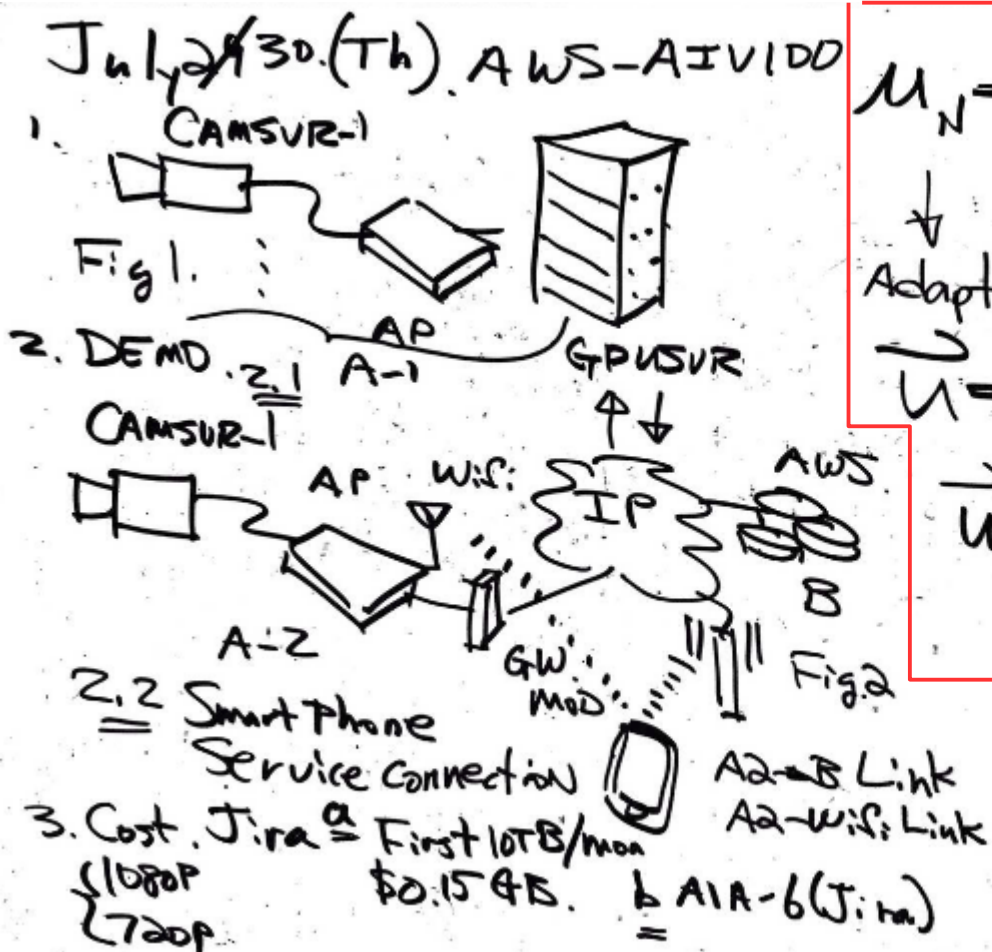
# Siamese For One Shot Facial Recognition



1. Siamese networks consist of two symmetrical neural networks sharing the same weights and architectures, then joined together at the end using an energy function,  $E$  which acts as a distance function.
2.  $E$  function's objective is to learn whether two input images are similar or different.



# July 31 Adaptive Facial Recognition



$$\mu_N = \frac{1}{N} \sum_{i=1}^N x_i \dots (1) \quad \begin{matrix} N-Add \\ 1-mult \end{matrix}$$

↓  $x_k$  Changed  $\Rightarrow \mu_N'$

Adaptive Facial Recognition

$\vec{U} = (u_1, u_2, \dots, u_N)$  vector

↓

$\vec{U}' = (u_1, u_2, \dots, u'_k, \dots, u_N)$

New Detection Algorithm

Given a feature vector  
 $U = (u_1, u_2, \dots, u_i, \dots, u_n) \dots (1)$

Then new feature vector  
 $U' = (u_1, u_2, \dots, u'_i, \dots, u_n) \dots (2)$   
 $u_i$  is not equal to  $u'_i$ , find new decision function





# July 31 Adaptive Facial Recognition Example

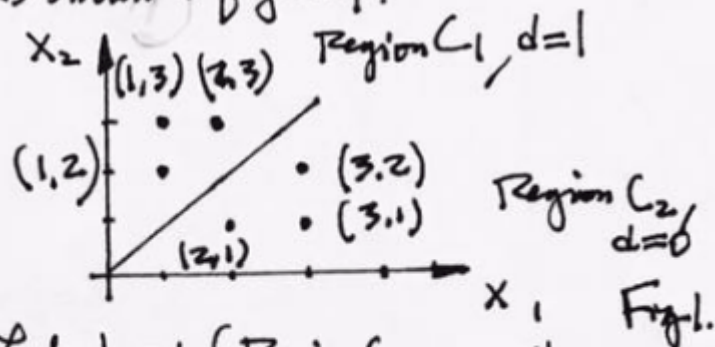
## Artificial Neural Networks (I)

Example: 1. Given 2 clusters  $C_1$  and  $C_2$  of Experimental Data,

$C_1: (1,2), (1,3), (2,3)$ ,

$C_2: (2,1), (3,1), (3,2)$

as shown in figure 1.



Let  $d_1 = 1$  (Region  $C_1$  as positive identification)  
 $d_2 = 0$  for Region  $C_2$

Step 1. train this neural networks with the given data, record the result  $\{w\}_{orig}$  and number of computation  $N$ .

Step 2. change one of the data set from any one of the classes, say,  $C_1$ , make  $(1,2)$  to  $(1,4)$ ; Retrain the network, and record the result  $\{w\}_{prim}$ , and record the number of computations  $N_{prim}$ ;

Step 3. now use new adaptive training approach by injecting  $\{w\}_{orig}$  to train the network to reach  $\{w\}_{prim}$ , record the number of computations  $N_{adpt}$ .

$N$  and  $P_{prim}$  should be about the same, while  $N_{adpt}$  should be ideally much smaller.





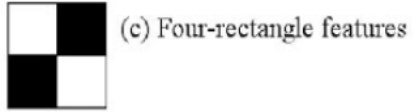
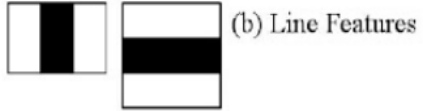
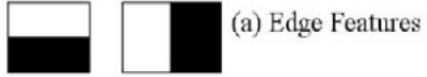
# Adaptive Training Example

<https://towardsdatascience.com/introduction-to-neural-networks-in-python-7e0b422e6c24>



# Haar Cascade for Facial Detection

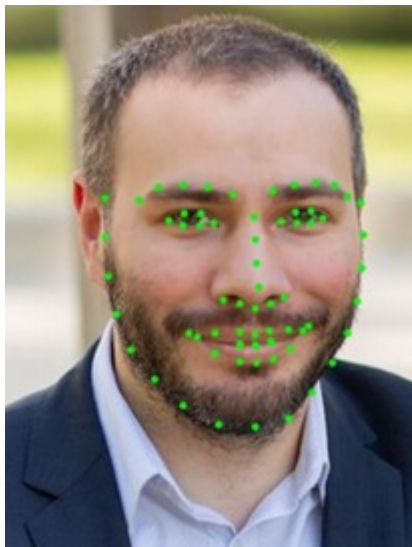
[https://opencv-python-tutroals.readthedocs.io/en/latest/py\\_tutorials/py\\_objdetect/py\\_face\\_detection/py\\_face\\_detection.html](https://opencv-python-tutroals.readthedocs.io/en/latest/py_tutorials/py_objdetect/py_face_detection/py_face_detection.html)





# Sample Detecting Facial Features

<https://towardsdatascience.com/detecting-face-features-with-python-30385aee4a8e>



Point map  
(67 points)

Jaw Points = 0–16

Right Brow Points = 17–21

Left Brow Points = 22–26

Nose Points = 27–35

Right Eye Points = 36–41

Left Eye Points = 42–47

Mouth Points = 48–60

Lips Points = 61–67

Note this model is  
simplified version with  
no upper face

## Feature Vectors

Jaw Points (17 pts)

Right Brow  
(5 pts)

Left Brow  
(5 pts)

Right Eye (6)

Left Eye (6)

Nose Points  
(9)

Lips (7)

Mouth (13)

\$pip -V (to check your pip version)



# Using <http://dlib.net/> For Feature Extraction

Dlib is a modern C++ toolkit containing machine learning algorithms and tools for creating complex software in C++ to solve real world problems. It is used in both industry and academia in a wide range of domains including robotics, embedded devices, mobile phones, and large high performance computing environments. Dlib's [open source licensing](#) allows you to use it in any application, free of charge.

## Sample code:

```
import cv2
import numpy as np
import dlib    #for facial feature extraction
```

1. Machine learning
2. Numerical algorithms
3. Graphical model inference algorithms

4. Image processing

5. Threading

6. Networking

7. GUI

8. Testing (Unit testing framework)

9. XML Parser etc.

```
# Load the predictor
predictor = dlib.shape_predictor("shape_predictor_68_face_landmarks.dat")
```

From dlib, additional features are possible



## Use Python3.7

\$python3.7 --version (to check your python 3.7 installation, if you have not installed python3.7, then install 3.7. To do so you will need to

\$sudo apt-get update

\$sudo apt install software-properties-common

\$sudo add-apt-repository ppa:deadsnakes/ppa

\$sudo apt-get update (I did this again, otherwise error message, python3.7 can not be found)

\$sudo apt install python3.7

```
final-py$ python3.7 --version  
Python 3.7.0
```

Make python3.7 your default

Locate .bashrc file (in your home directory)\_ and edit

\$vi ~/.bashrc (to add the following line)

alias python3=python3.7

Make modified .bashrc  
effective without login out and  
back again

\$source ~/.bashrc

Then check:  
\$python3

```
/0-video-image/final-py$ python3 --version  
Python 3.7.0
```



## OpenCV Python3.7

Make python3.7 your default, as described in the previous slide.



# Jupyter Notebook for iPython

<https://askubuntu.com/questions/847263/install-jupyter-notebook-for-python-2-7>

## To install jupyter notebook

```
sudo apt-get update
sudo apt-get -y install python3-pip python3-dev
sudo -H pip3 install --upgrade pip
sudo apt-get -y install ipython3 ipython3-notebook
pip3 install --user jupyter
```

Teaching Tool to tell a story

\$puypter --version

\$puypter notebook

It is possible to use Python 3 in Jupyter Notebook for Python 2 by adding the kernel for Python 2. If you're running Jupyter on Python 3, you can set up a Python 2 kernel like this:

```
python2 -m pip install ipykernel
python2 -m ipykernel install --user
```

## Tutorial

<https://www.youtube.com/watch?v=jZ952vChhul>



# Pycharm IDE for Python

PyCharm is probably the only Python dedicated IDE that supports the vast expanse of features Python has. Sublime, Atom and Sympy do exist, but they only exist! The integrated development environment experience that PyCharm provides is way better than the others.

To install pycharm:

<https://medium.com/@singh.shreya8/how-to-install-pycharm-in-ubuntu-16-04-ubuntu-14-04-ubuntu-18-04-linux-easiest-way-5ae19d052693>

To start pycharm:

`$sh pycharm.sh`

<https://www.youtube.com/watch?v=BPC-bGdBSM8&list=PLQ176FUIyIUZ1mwB-ulmQE-gmkwzjNLjP>

## Pycharm hello the world

<https://www.jetbrains.com/help/pycharm/creating-and-running-your-first-python-project.html#summary>

use Cmake to build and install OpenCV and Extra Modules from source and configure your Pycharm IDE

<https://towardsdatascience.com/how-to-install-opencv-and-extra-modules-from-source-using-cmake-and-then-set-it-up-in-your-pycharm-7e6ae25dbac5>







# OpenCV Build

[https://github.com/opencv/opencv\\_contrib](https://github.com/opencv/opencv_contrib)

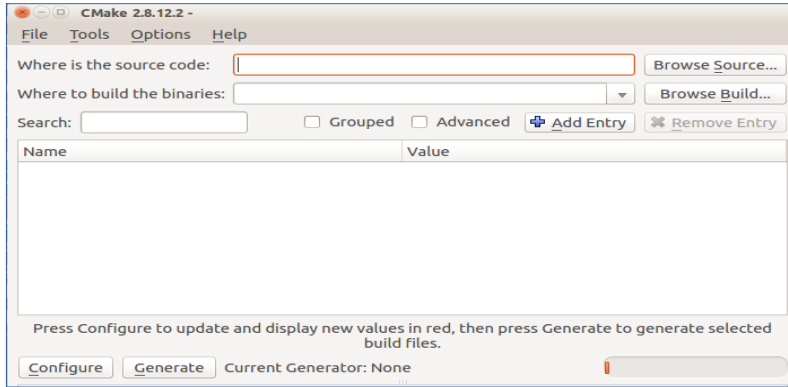
```
cmake -D CMAKE_BUILD_TYPE=RELEASE \  
-D CMAKE_INSTALL_PREFIX=/usr/local \  
-D INSTALL_C_EXAMPLES=ON \  
-D INSTALL_PYTHON_EXAMPLES=ON \  
-D WITH_TBB=ON \  
-D WITH_V4L=ON \  
-D WITH_QT=ON \  
-D WITH_OPENGL=ON \  
-D OPENCV_EXTRA_MODULES_PATH=../../opencv_contrib/modules \  
-D BUILD_EXAMPLES=ON ..
```



# Use cmake-gui to Build OpenCV Extra Modules

`$sudo apt-get Install cmake-qt-gui`

`$cmake-gui` (to start cmake gui)



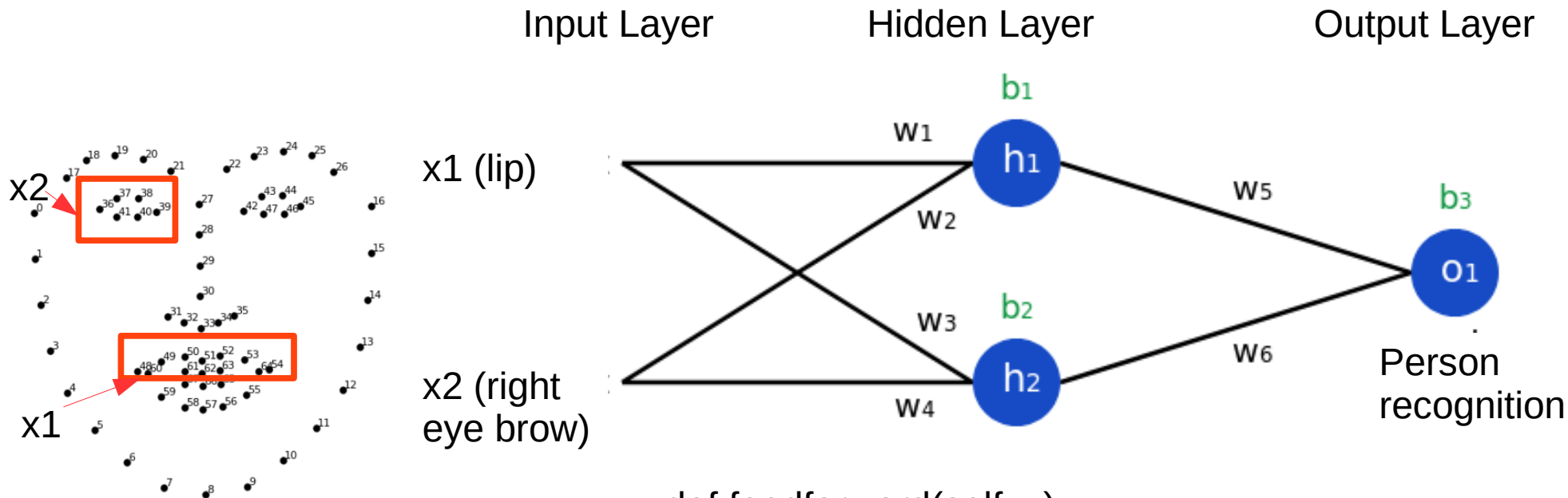
<https://www.pyimagesearch.com/2015/07/27/installing-opencv-3-0-for-both-python-2-7-and-python-3-on-your-raspberry-pi-2/>

Installing OpenCV 3.0 for both Python 2.7 and Python 3+ on your Raspberry Pi 2

1. `$ cd ~/.virtualenvs/cv3/lib/python2.7/site-packages/`
2. `$ ln -s /usr/local/lib/python2.7/site-packages/cv2.so cv2.so`



# Simple Feed Forward Neural Networks



To do: (1) add h3 hidden layer, (2) add o2 at output layer, modify the code

```
def feedforward(self, x):  
    # x is a numpy array with 2 elements.  
    h1 = sigmoid(self.w1 * x[0] + self.w2 * x[1] + self.b1)  
    h2 = sigmoid(self.w3 * x[0] + self.w4 * x[1] + self.b2)  
    o1 = sigmoid(self.w5 * h1 + self.w6 * h2 + self.b3)  
    return o1
```

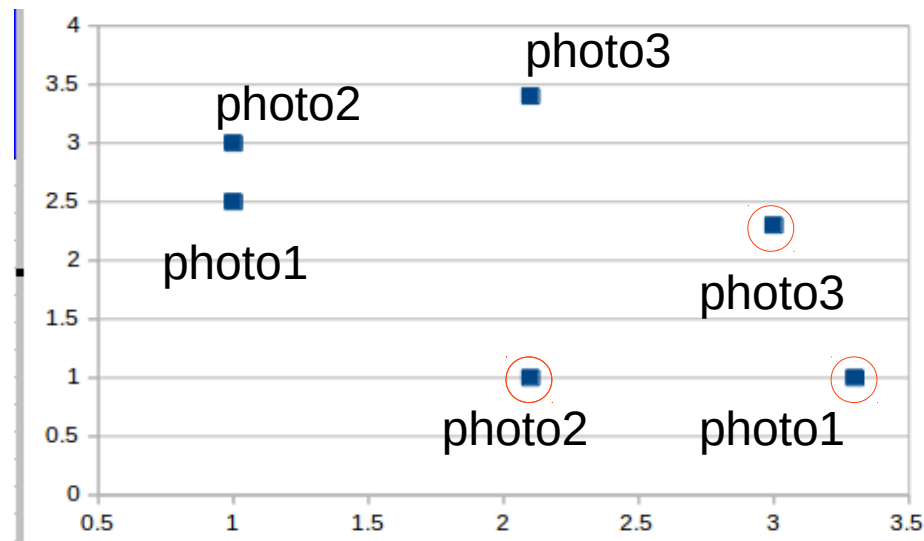
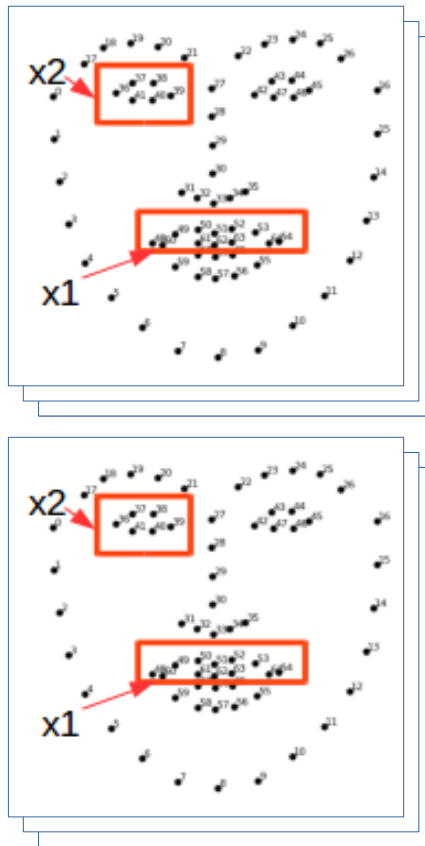


## Prepare the Data Set

For 2 persons

```
#-----  
# Define dataset and all_y_trues  
#-----  
data = np.array([  
    [1, 2.5], # person A  
    [1, 3],   # person A  
    [2.1, 3.4], # Person A  
    [2.1, 1], # person B  
    [3.3, 1], # person B  
    [3, 2.3], # person B  
])  
all_y_trues = np.array([  
    1, # person A  
    1, # person A  
    1, # person A  
    0, # person B  
    0, # person B  
    0, # person B  
])
```

For 2 persons





## Prepare the Output Layer

For 2 persons

```
#-----  
# Define dataset and all_y_trues  
#-----  
data = np.array([  
    [1, 2.5], # person A  
    [1, 3],   # person A  
    [2.1, 3.4], # Person A  
    [2.1, 1], # person B  
    [3.3, 1], # person B  
    [3, 2.3], # person B  
)  
all_y_trues = np.array([  
    1, # person A  
    1, # person A  
    1, # person A  
    0, # person B  
    0, # person B  
    0, # person B  
)
```

For 4 persons

(1) Output layer with 2 neurons,

o1 o2

0 0

0 1

1 0

1 1

(2) output layer with 4 neurons

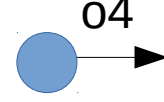
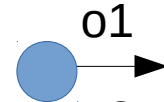
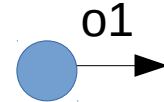
o1 o2 o3 o4

1 0 0 0

0 1 0 0

0 0 1 0

0 0 0 1 t





# Output Layer from ImageNet

<https://www2.eecs.berkeley.edu/Pubs/TechRpts/2020/EECS-2020-18.html>

## ImageNet Training in Minutes

Yang You, Zhao Zhang, Cho-Jui  
Hsieh, James Demmel and Kurt  
Keutzer

EECS Department

University of California, Berkeley

Technical Report No. UCB/EECS-  
2020-18

January 25, 2020

(1) Output layer with 2 neurons,

o1 o2

0 0

0 1

1 0

1 1



(2) output layer with 4 neurons

o1 o2 o3 o4

1 0 0 0

0 1 0 0

0 0 1 0

0 0 0 1 t



For 4 persons

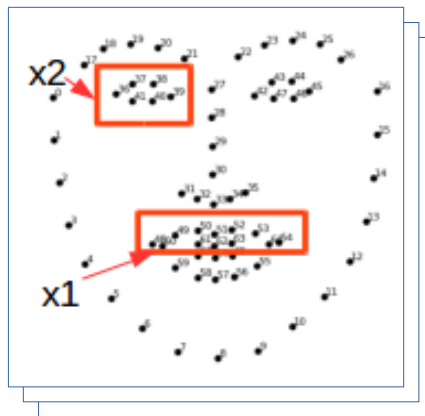
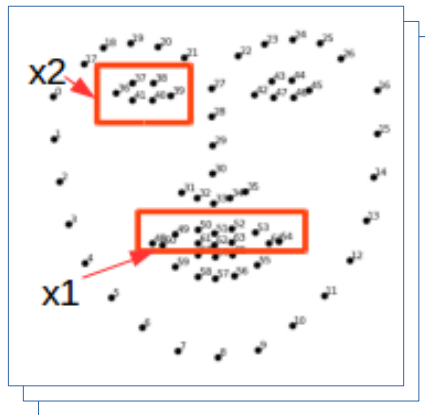


## Prepare the Data Set

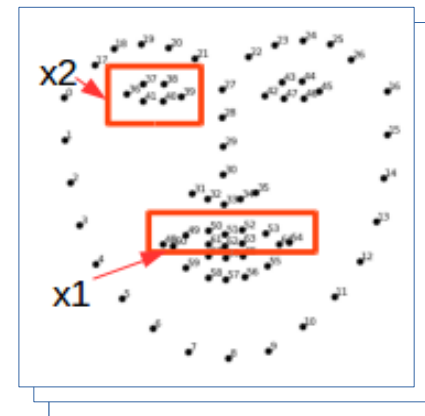
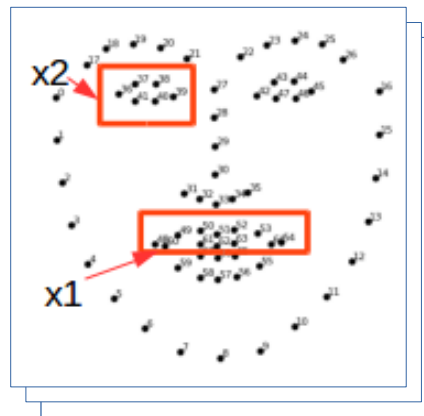
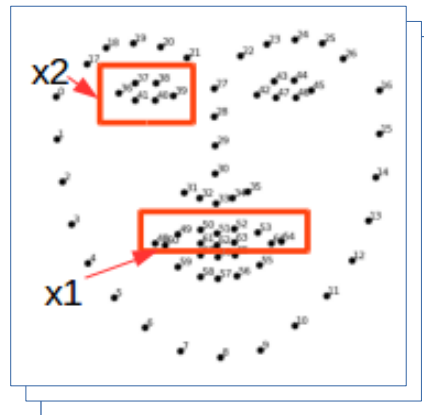
For 2 persons

```
#-----  
# Define dataset and all_y_trues  
#-----  
data = np.array([  
    [1, 2.5], # person A  
    [1, 3],   # person A  
    [2.1, 3.4], # Person A  
    [2.1, 1], # person B  
    [3.3, 1], # person B  
    [3, 2.3], # person B  
])  
all_y_trues = np.array([  
    1, # person A  
    1, # person A  
    1, # person A  
    0, # person B  
    0, # person B  
    0, # person B  
])
```

For 2 persons



For 4 persons





## 4 Person Data Set

For 4 persons

```
#-----  
# Define dataset and all_y_trues  
#-----  
data = np.array([  
    [1, 2.5],    # person A  
    [1, 3],      # person A  
    [2.1, 3.4],  # Person A  
    [2.1, 1],    # person B  
    [3.3, 1],    # person B  
    [3, 2.3],    # person B  
    [3, 2.5],    # person C  
    [3, 3.6],    # person C  
    [4.1, 5.4],  # Person C  
    [4.5, 3.1],  # person D  
    [3.3, 1.9],  # person D  
    [5.9, 2.3], # person D  
])
```

```
all_y_trues = np.array([  
    01, # person A  
    01, # person A  
    01, # person A  
    00, # person B  
    00, # person B  
    00, # person B  
    11, # person C  
    11, # person C  
    11, # person C  
    10, # person D  
    10, # person D  
    10, # person D  
])
```

For 4 persons

