

Driving Directions: "8- Connected Neighbors"

NW N NE  
W ■ E  
SW S SE

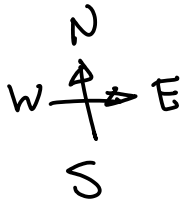
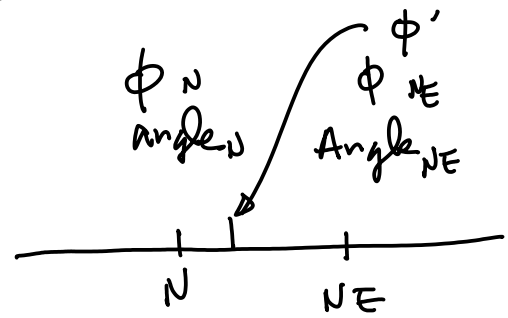


Fig. 4

Find the Direction of Driving at Each Step that in the end will Minimize the Objective Function in Eqn (9).

$$\text{Policy } \pi(\underset{\substack{\uparrow \\ \text{Action} \\ (\text{8 Directions})}}{\alpha_{k+1}}, S_{k+1} | S_k) \rightarrow \underset{\substack{\uparrow \\ \text{Reward}}}{\delta_{k+1}}$$

Action	Reward
N	$\delta_N = ?$
NW	$\delta_{NW} = ?$
W	$\delta_W = ?$
SW	$\vdots$
S	$\vdots$



NW N NE  
W ■ E  
SW S SE

Determine Reward Function Based On Moving Direction of Shortest Path.

List of Possible moving Directions

1. From Fig. 4. Only 5 possible Directions

NW N NE  
W ■ E  
SW S SE

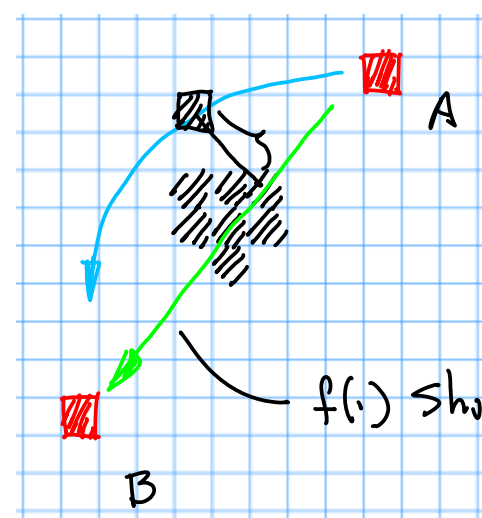
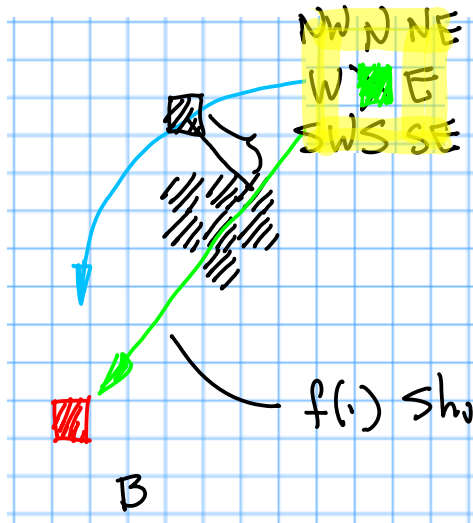


Fig. 5

Example 1. 1. plane 8-Directional Template (N, S, ...) on top of Point A.  
Use shortest path, green line,

as a reference to Define A set of Reward function Based on the direction Matching Reward (DMR) Policy



$f(\cdot)$  Shortest Path

Fig. 6

$$\pi_{DMR} : \Delta = 0.5$$

X-SW +1.0 Best Matching X-SW Overlap

X-W +0.6 Next Best X-W Angle  $< \pi/2$

X-S +0.6 " " X-S "  $< \pi/2$

X-SE +0.1 " " X-SE "  $< \pi/2$

X-E -0.1 Opposite X-E "  $> \pi/2$

X-NW -0.1

Angle  $> \pi/2$

X-N -0.6

Angle  $> 3\pi/4$

X-NE -1.0

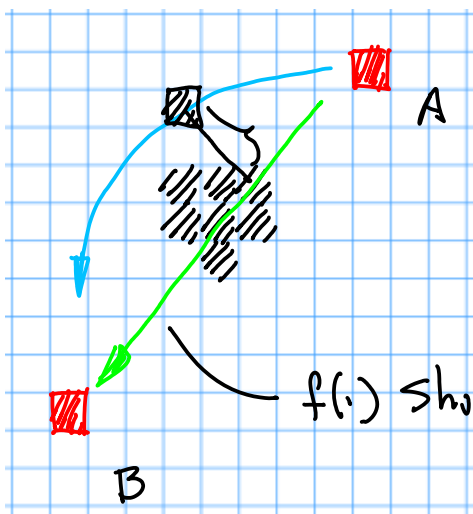
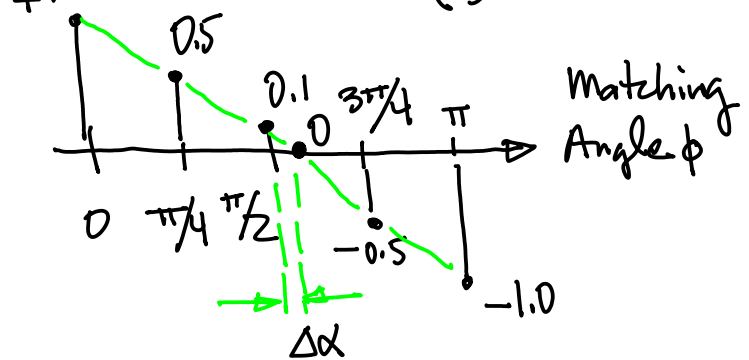
Angle  $\approx \pi$

Algorithm: Best Matching Direction. Highest "+" Reward

Worst matching Direction

Smallest "-" Reward

$$r = a\phi + b \dots (1)$$



$f(\cdot)$  Shortest Path

Fig. 7

Program Implementation:

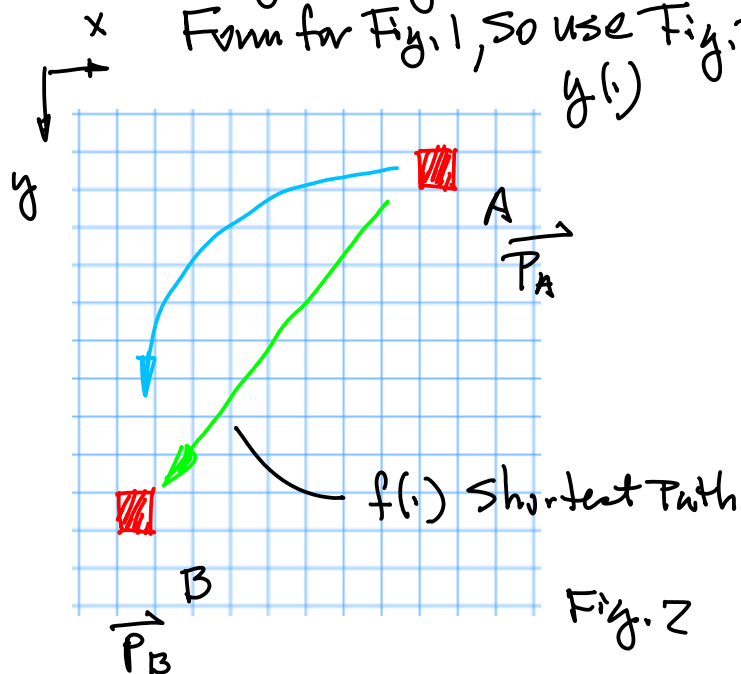
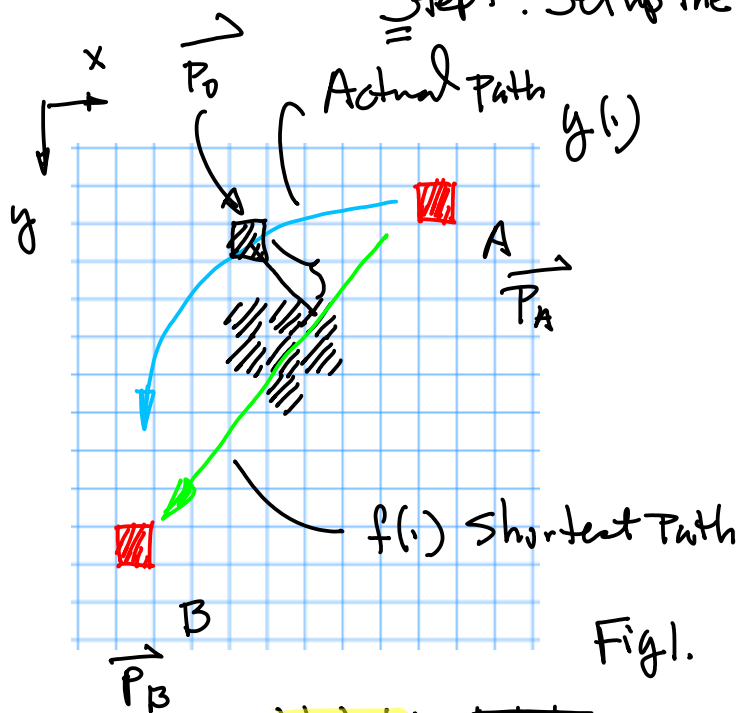
1° Implement Reward Function (1).

Note: Angle  $\phi$  is formed Between Blue line and green Line.

Compute Reward.

March 12 (Sat), 22

Step 1. Setup the System  $AS$  in Fig. 1, Fig. 2 is the Abstract Form for Fig. 1, So use Fig. 2.



Step 2.

NW N NE  
W X E  
SW S SE

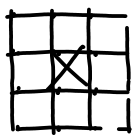
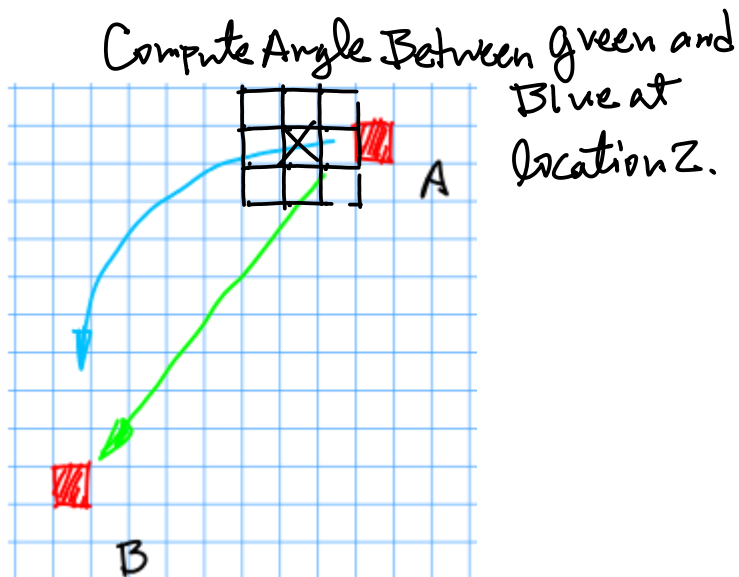
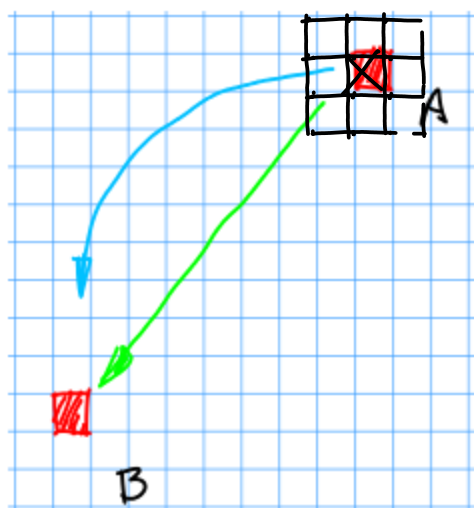


Fig. 2b. 8-Connected Neighbour.

Define Python module for the Angle Computation for 8-Connected Neighbours in Fig. 2b.

Step 3. Compute Angle Between Green and Blue at Location 1.



March 12 (Sat) 22

4

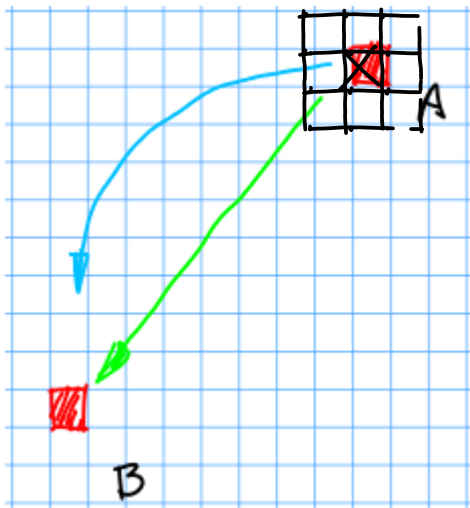


Fig. 3

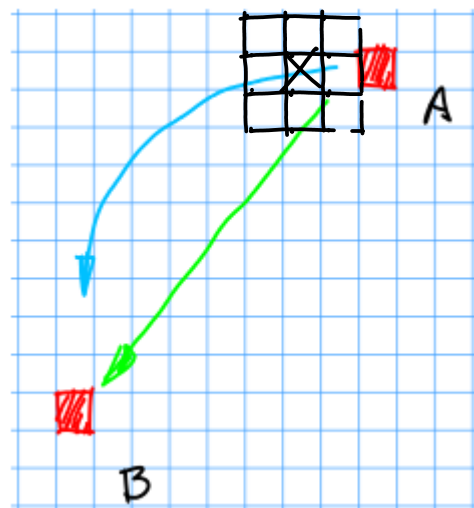


Fig. 4

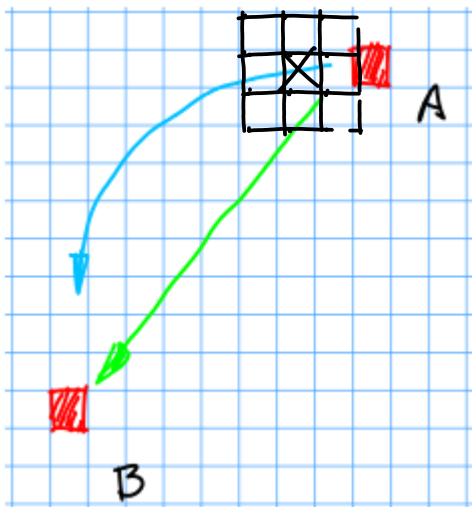


Fig. 5

Compute Angle Between green and Blue at Location 3.

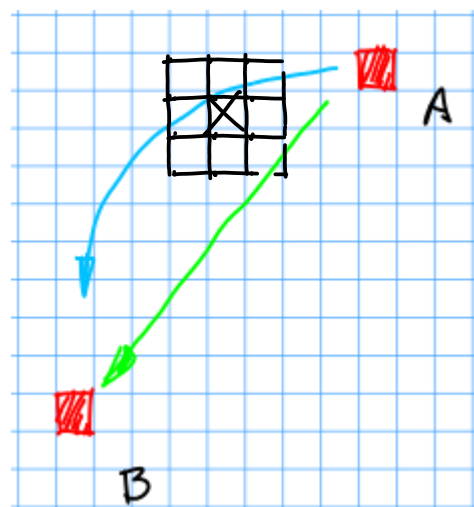


Fig. 6

Compute Angle Between green and Blue at Location 4.

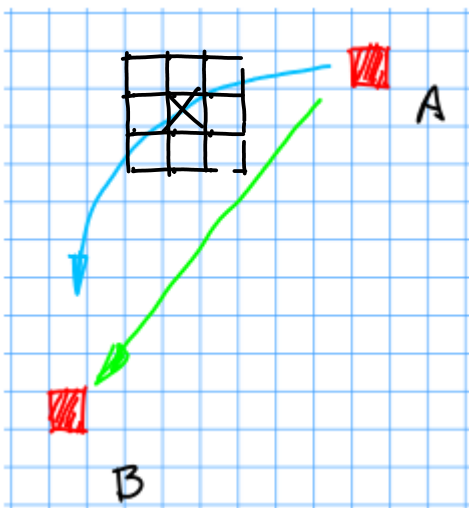


Fig. 7

Compute Angle Between green and Blue at Location 5.

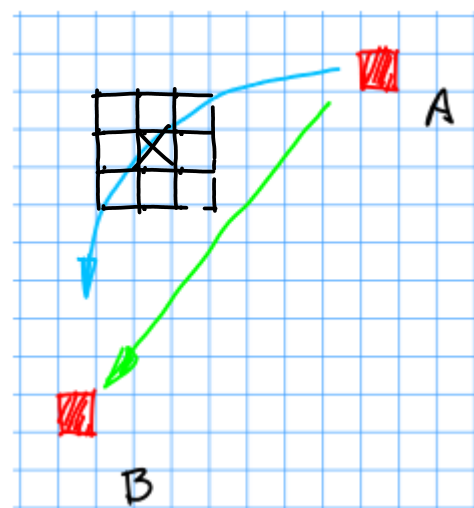


Fig. 8

Compute Angle Between green and Blue at Location 6.

March 12 (Sat), 22

5

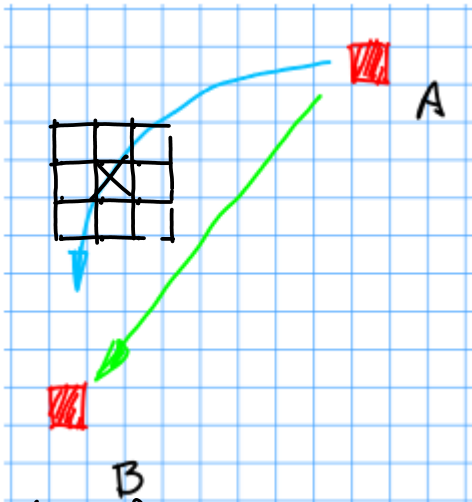


Fig 9

Compute Angle Between green and Blue at location 7.

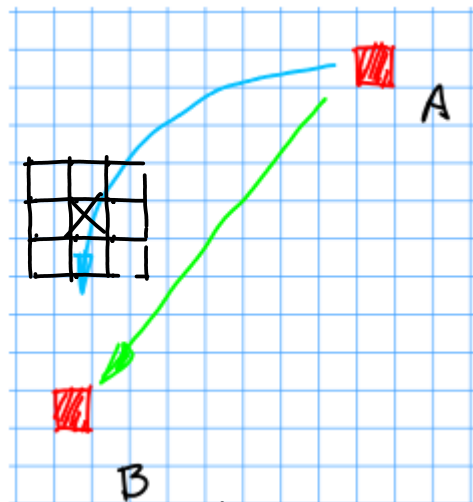


Fig 10

Compute Angle Between green and Blue at location 8.

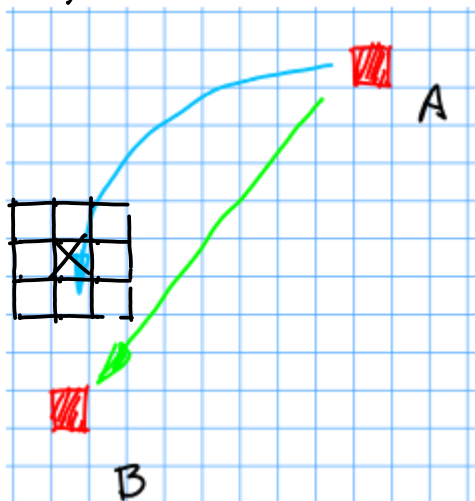


Fig 11

Compute Angle Between green and Blue at location 9.

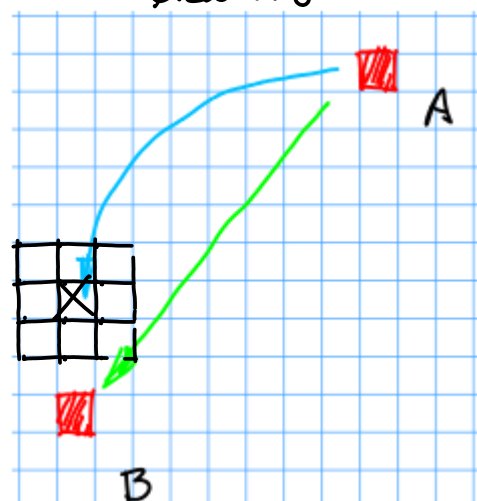


Fig 12

Compute Angle Between green and Blue at location 10.

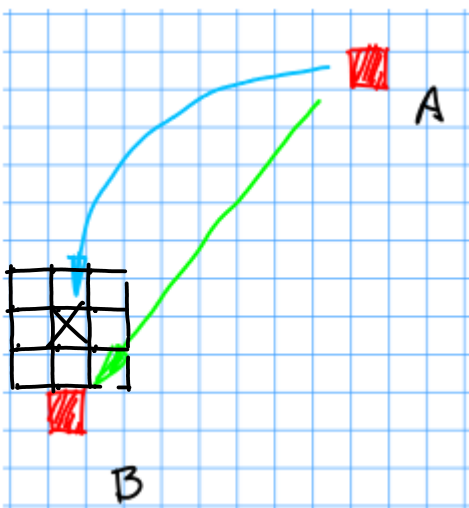


Fig 13

Compute Angle at location 11.

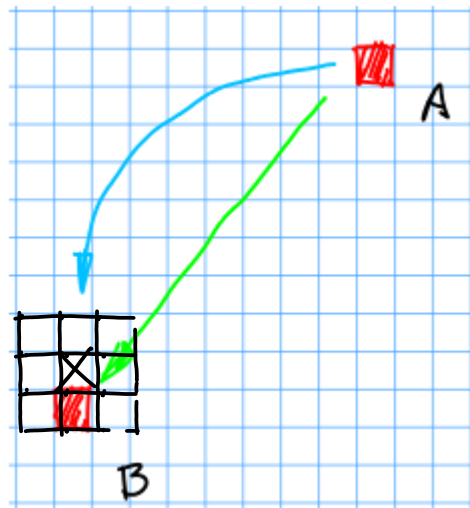


Fig 14

Compute Angle at location 12.

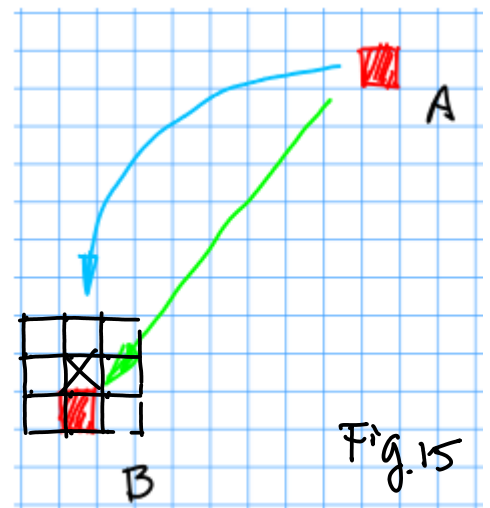


Fig 15

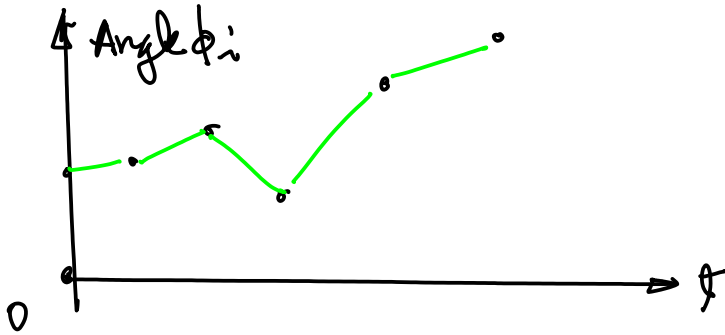
Compute Angle at location 13.

March 12 (Sat), 22

6

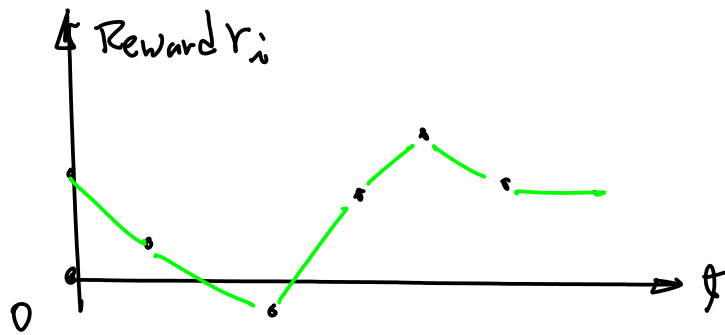
Step 4

Plot All the Angles  $\phi_1, \phi_2, \dots, \phi_i \dots$  in the plot below, plot All Reward Function values  $r_1, r_2, \dots, r_i \dots$  in the plot below.



Then find Sum of all Rewards.

$$R_{\Sigma} = \sum_{i=1}^{N-1} r_i \quad \dots (1)$$



(End)