

# Domain Expansion: A Latent Space Construction Framework for Multi-Task Learning

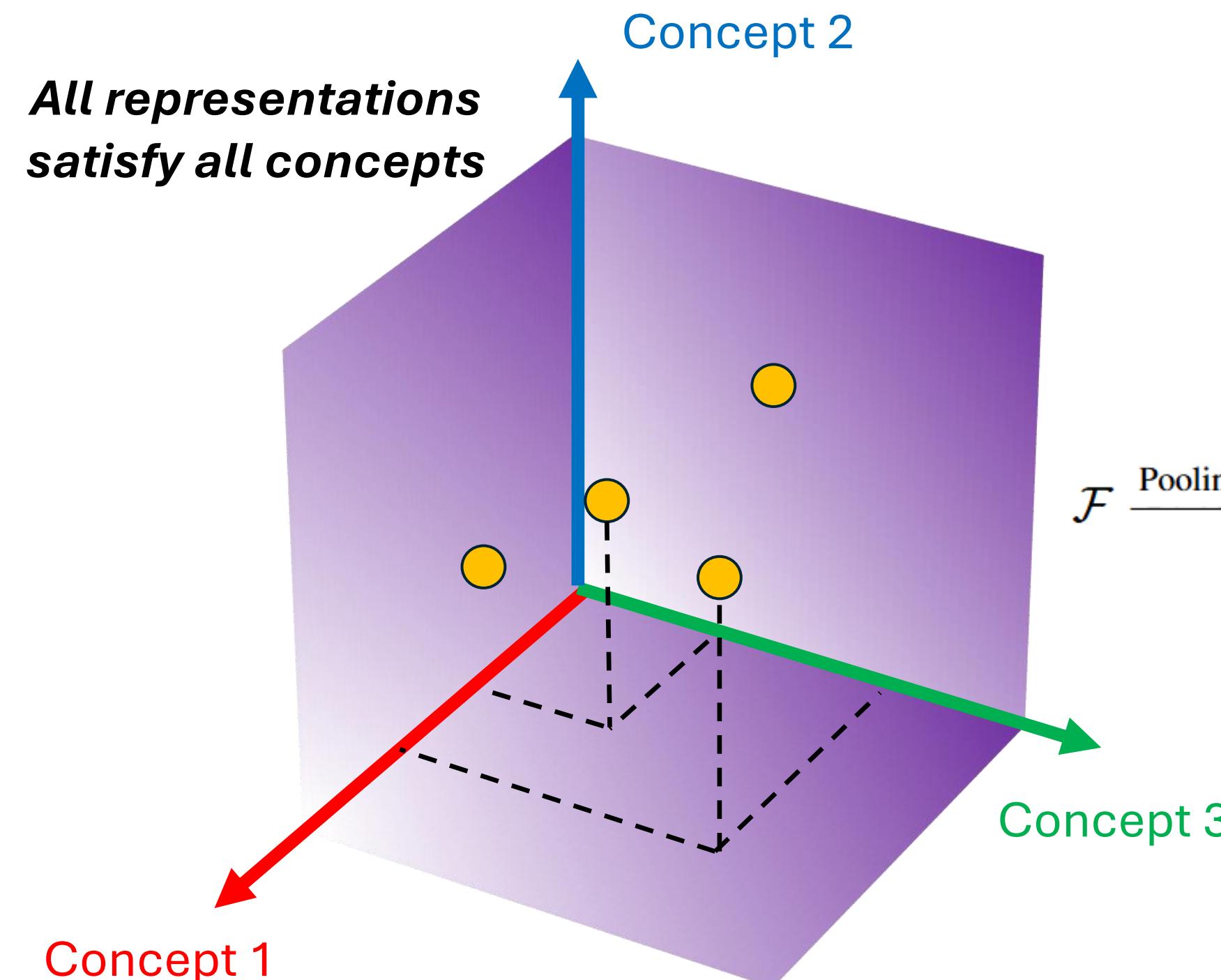
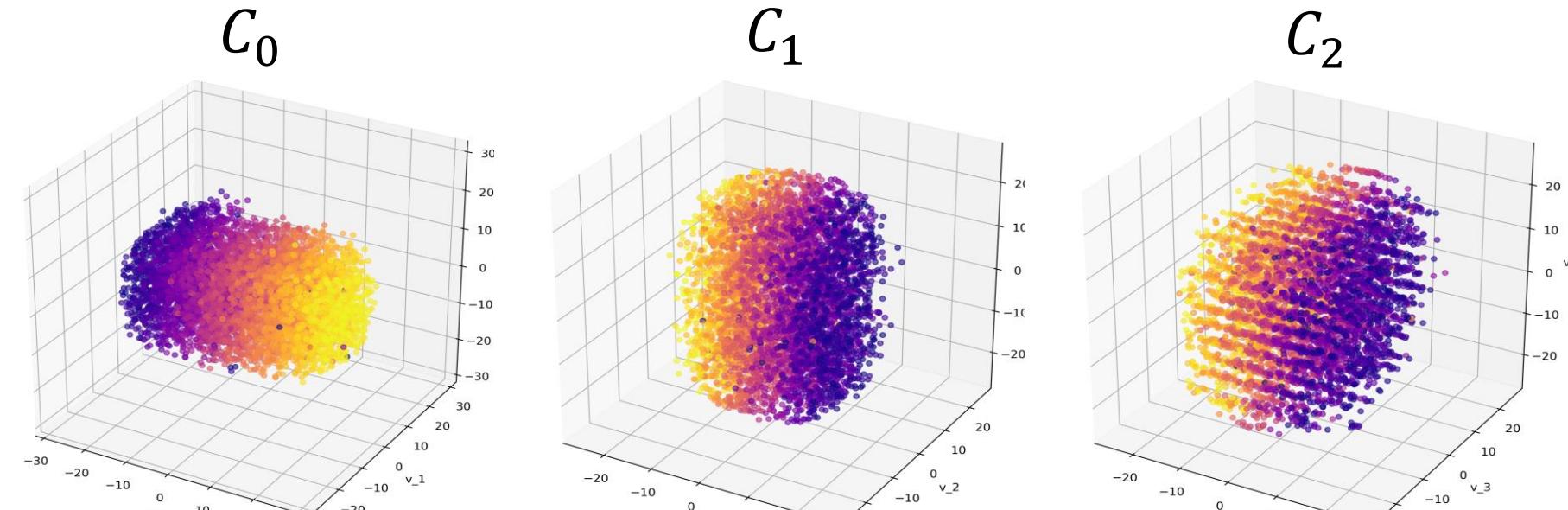
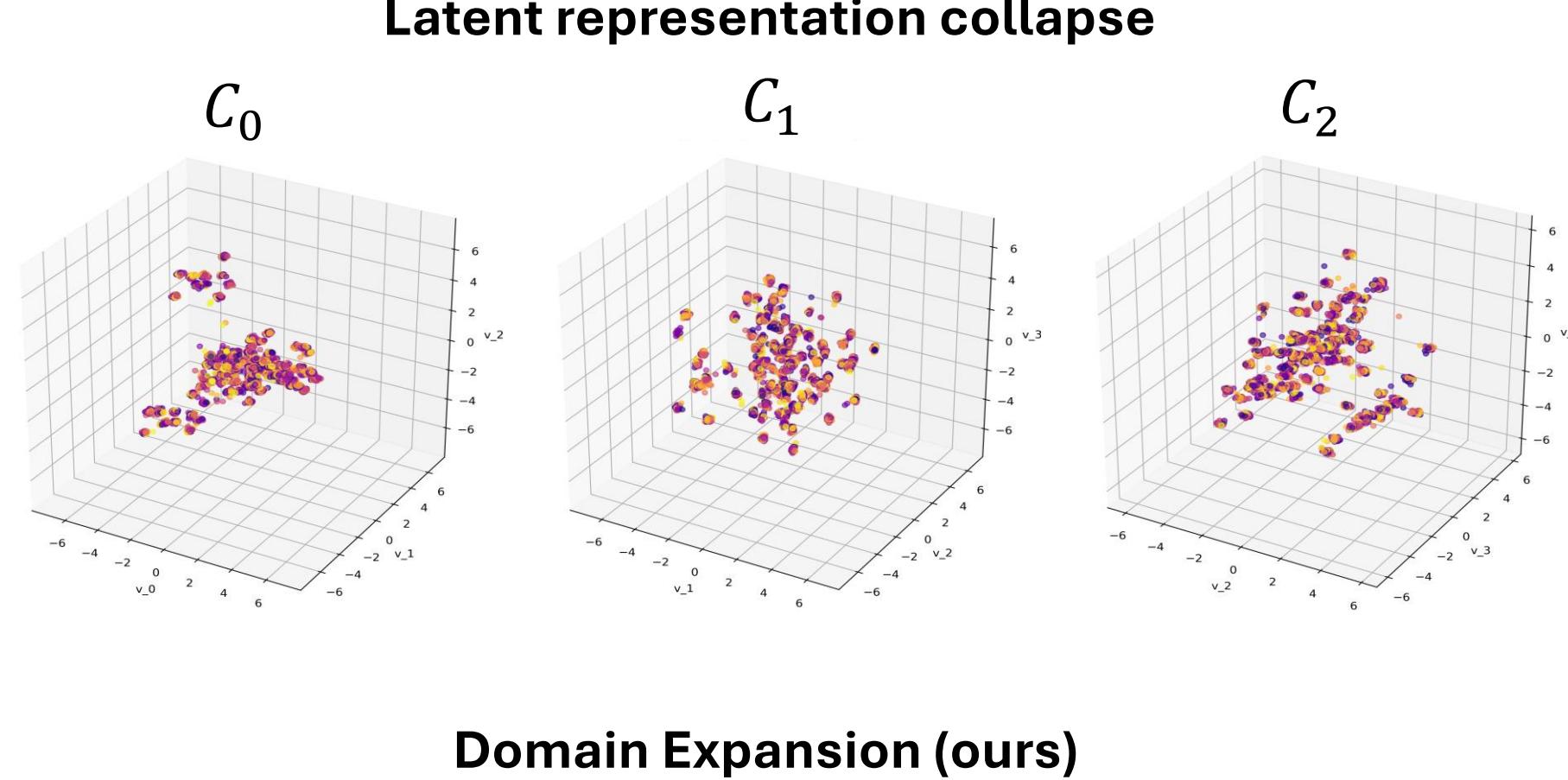
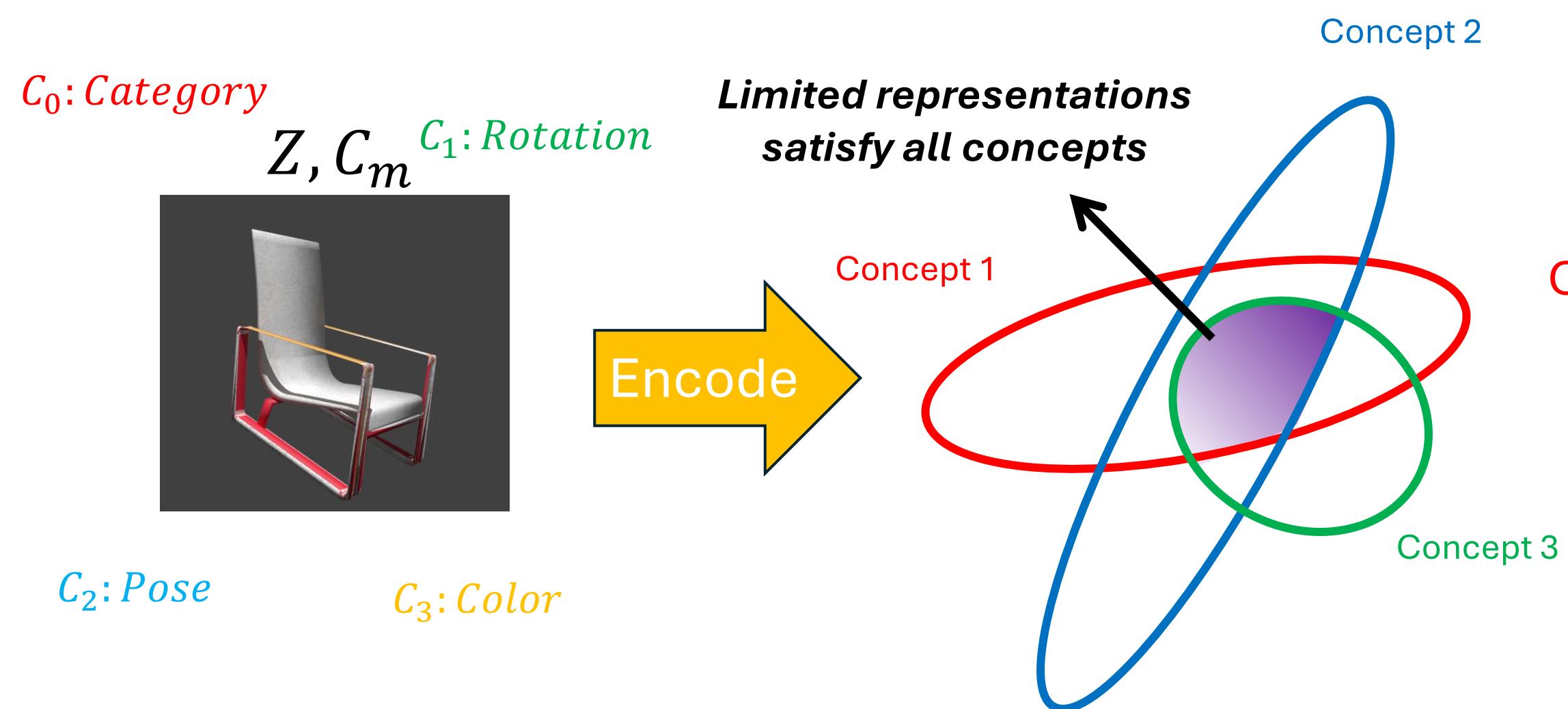


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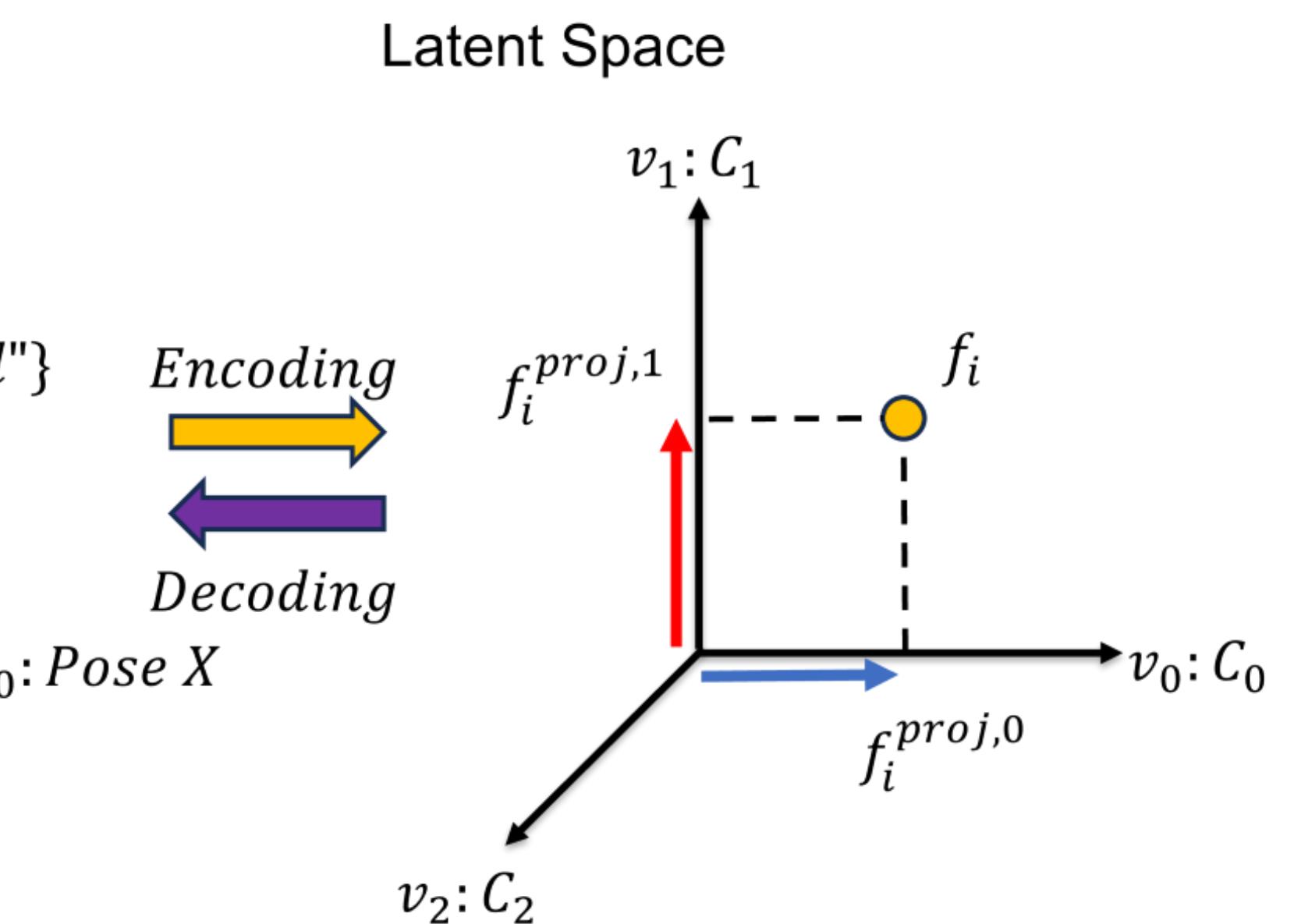
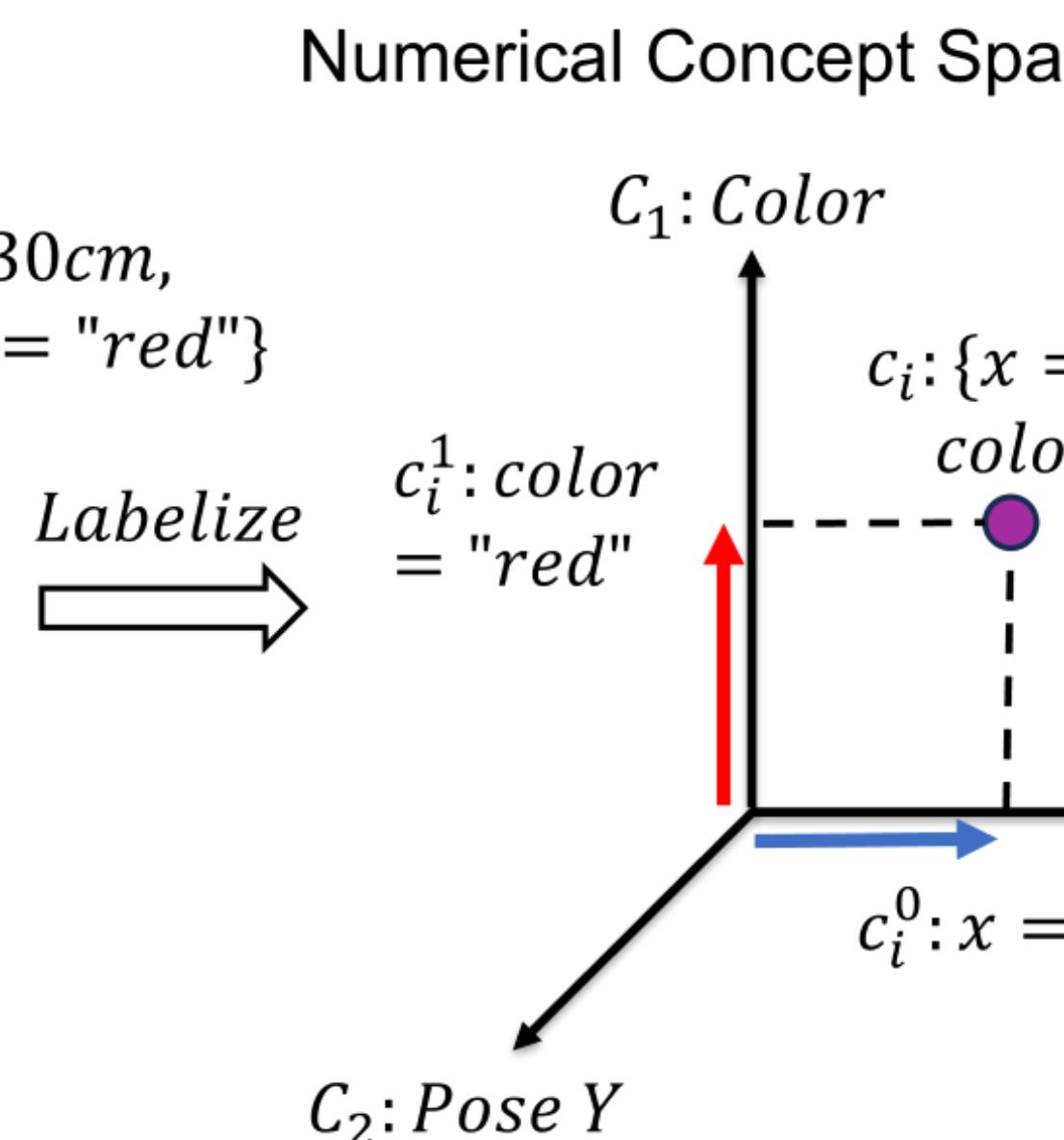
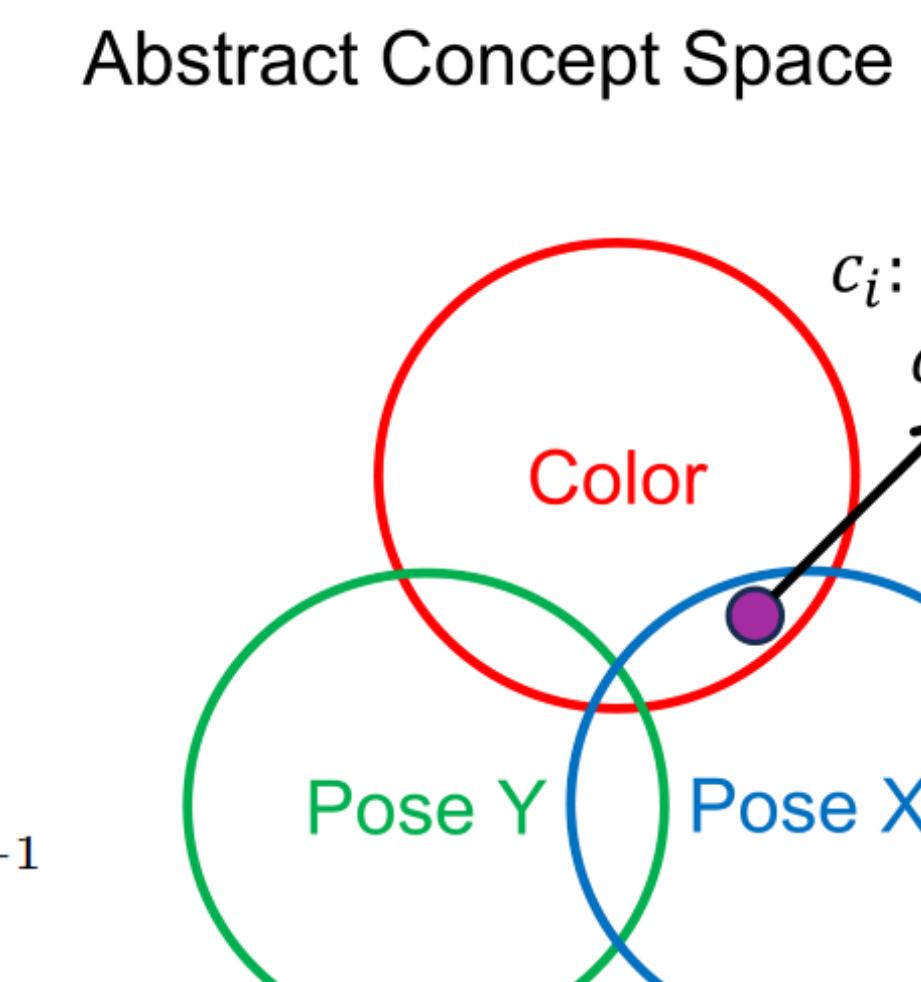
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## Latent Representation Collapse

A visual input often contains rich concepts. If we train a single model to handle all concepts at the same time, the features will be pulled in different directions, leading to a shrunken latent space. This shrunken latent space often degrades the model's performance. We call this phenomenon **latent representation collapse**.

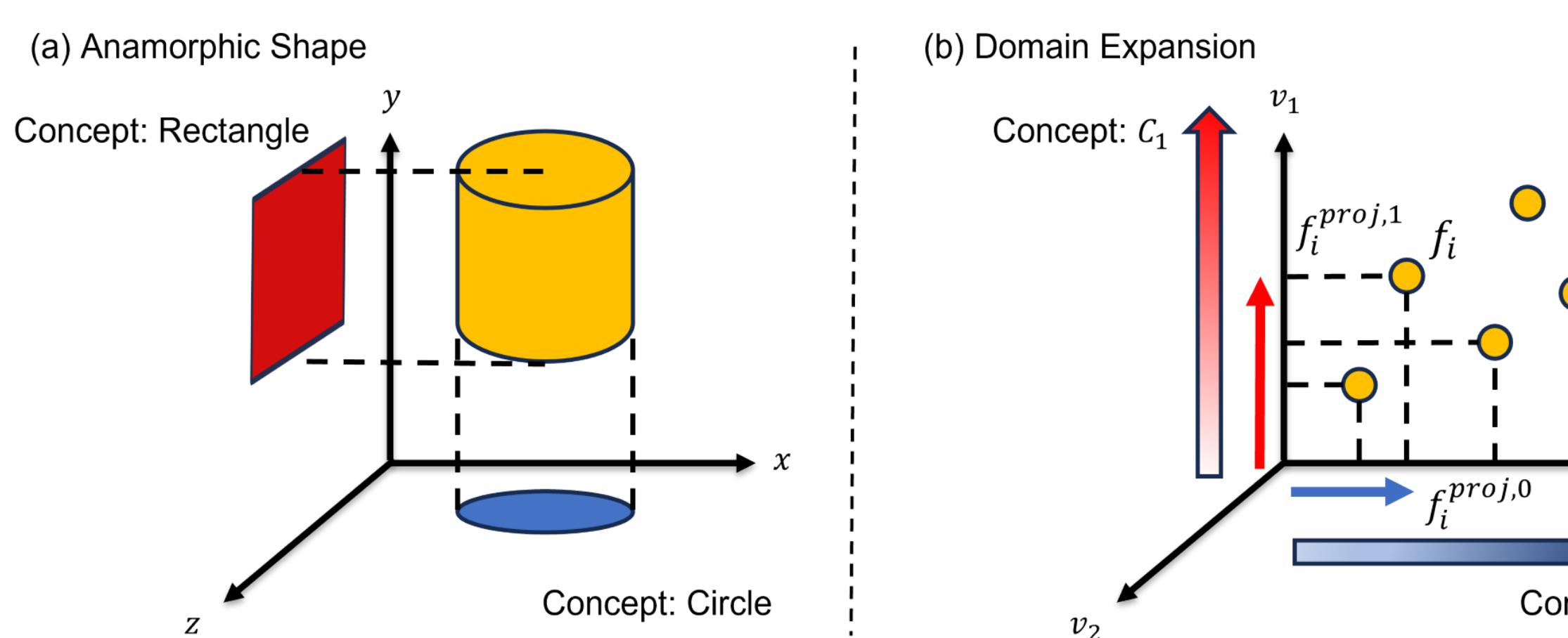


$$\mathcal{F} \xrightarrow{\text{Pooling}} \left\{ \begin{array}{l} \mathcal{F}_0^{\text{proj}} \xrightarrow{\text{Dec}_0} \mathcal{C}_0 \\ \mathcal{F}_1^{\text{proj}} \xrightarrow{\text{Dec}_1} \mathcal{C}_1 \\ \vdots \\ \mathcal{F}_{M-1}^{\text{proj}} \xrightarrow{\text{Dec}_{M-1}} \mathcal{C}_{M-1} \end{array} \right.$$



## Orthogonal Pooling

In the latent space, we use eigenvectors to represent concepts. Each eigenvector is assigned to a single target concept. This assignment ensures that the 1D subspace spanned by the **eigenvector is dedicated exclusively to each concept**."



## Properties and Operators

- Property 1: Multi-concept Encoding.

$$f_i \xrightarrow{\text{Pooling}} \{f_i^{\text{proj},0}, \dots, f_i^{\text{proj},M-1}\} \xrightarrow{\text{Dec}} \{c_i^0, \dots, c_i^{M-1}\} \rightarrow c_i.$$

- Property 2: Orthogonality of Target Concepts.

$$\mathcal{F}_0^{\text{proj}} \perp \mathcal{F}_1^{\text{proj}} \perp \dots \perp \mathcal{F}_{M-1}^{\text{proj}} \implies \mathcal{C}_0 \perp \mathcal{C}_1 \perp \dots \perp \mathcal{C}_{M-1}.$$

- Operator 1: Concept-Specific Adjustment ( $\oplus^m$ ) and ( $\ominus^m$ ).

$$c_i \oplus^m c_{\Delta}^m \rightarrow \{c_i^0, \dots, \{c_i^m \oplus^m c_{\Delta}^m\}, \dots, c_i^{M-1}\} \xrightarrow{\text{Dec}^{-1}} \{f_i^{\text{proj},0}, \dots, \{f_i^{\text{proj},m} + f_{\Delta}^{\text{proj},m}\}, \dots, f_i^{\text{proj},M-1}\} \xrightarrow{\text{Reconst}} f_i + f_{\Delta}^{\text{proj},m}.$$

- Operator 2: Concept Composition ( $\oplus$ ) and ( $\ominus$ ).

$$c_p \oplus c_q \rightarrow \{\{c_p^0 \oplus^0 c_q^0\}, \{c_p^1 \oplus^1 c_q^1\}, \dots, \{c_p^{M-1} \oplus^{M-1} c_q^{M-1}\}\} \xrightarrow{\text{Dec}^{-1}} \{\{f_p^{\text{proj},0} + f_q^{\text{proj},0}\}, \{f_p^{\text{proj},1} + f_q^{\text{proj},1}\}, \dots, \{f_p^{\text{proj},M-1} + f_q^{\text{proj},M-1}\}\} \xrightarrow{\text{Reconst}} f_p + f_q.$$

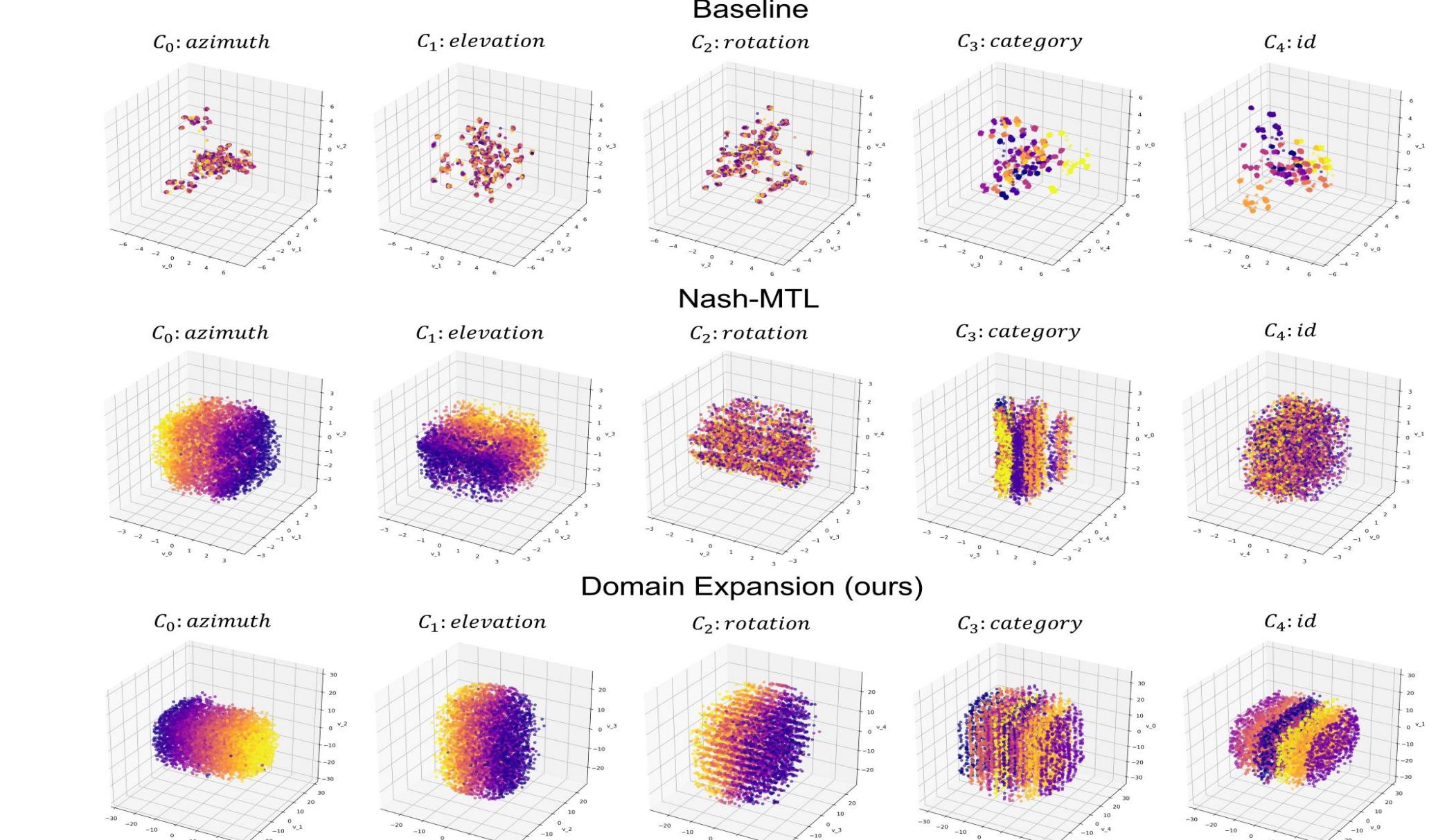


Table 1: Comprehensive comparison of representation quality, predictive performance, and concept composition. Arrows indicate whether higher ( $\uparrow$ ) or lower ( $\downarrow$ ) values are better.

Objective Set	Method	Representation & Predictive Performance						Concept Comp.				
		Spearman $\uparrow$			V-score $\uparrow$							
		az	el	rot	cat	id	az	el	rot	cat	id	Sim. $\uparrow$
Objective Set 1	baseline	0.41	0.34	0.35	0.16	0.14	0.12	0.09	0.09	0.28	0.37	0.22
	FAMO	0.49	0.41	0.42	0.00	0.00	0.12	0.09	0.09	0.19	0.18	0.28
	Nash-MTL	0.38	0.41	0.42	0.00	0.00	0.11	0.09	0.09	0.17	0.13	0.28
	<b>Ours</b>	<b>0.95</b>	<b>0.87</b>	<b>0.85</b>	<b>0.99</b>	<b>0.91</b>	<b>0.08</b>	<b>0.08</b>	<b>0.09</b>	<b>0.99</b>	<b>0.97</b>	<b>0.95</b>
Objective Set 2	baseline	0.01	0.01	0.01	0.99	0.00	0.77	0.38	0.38	0.99	0.99	0.42
	FAMO	0.28	0.23	0.22	0.99	0.00	0.19	0.14	0.13	0.99	0.99	0.28
	Nash-MTL	0.45	0.39	0.39	0.15	0.00	0.12	0.08	0.09	0.99	0.99	0.35
	<b>Ours</b>	<b>0.95</b>	<b>0.87</b>	<b>0.85</b>	<b>0.98</b>	<b>0.96</b>	<b>0.07</b>	<b>0.08</b>	<b>0.09</b>	<b>0.98</b>	<b>0.94</b>	<b>0.93</b>