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$$(1) H_0: p_1 - p_2 \leq 0 \quad H_1: p_1 - p_2 > 0$$

$$(2) \alpha = 0.05$$

$$(3) \text{拒绝域 } C = \{Z > Z_{\alpha}\} = \{Z > 1.645\}$$

$$(4) n_1 = 200 \quad n_2 = 150 \quad X = 108 \quad Y = 78 \quad \hat{p}_1 = 0.54 \quad \hat{p}_2 = 0.52$$

$$\bar{p} = \frac{x+y}{n_1+n_2} = \frac{108+78}{200+150} = 0.531$$

$$Z = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{\bar{p}(1-\bar{p})\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}} = \frac{0.54 - 0.52}{\sqrt{0.531(1-0.531)\left(\frac{1}{200} + \frac{1}{150}\right)}} = 0.371$$