

Knowledge Representation

2023/2024

Exercise Sheet 2 - Description Logics and Non-Monotonic Reasoning

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Dr. Patrick Koopmann, Dr. Atefeh Keshavarzi Zafarghandi

Exercise 2.1 (\mathcal{EL} **Completion)** Use the completion algorithm to compute the materialization of the following ontology, that is, to compute all entailments of the form a:A, where A is a concept name.

Note: the concepts assigned to the interpretations of named individuals are *not marked* as initial concepts!

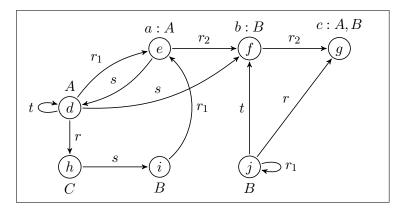
Exercise 2.2 (Tableaux Procedure) We want to use the tableaux procedure to decide concept subsumption. Assume we have the following TBox:

$$\mathcal{T} = \{ \forall r. \neg A \sqsubseteq \exists r. B, \quad \neg C \sqsubseteq D \}$$

We want to know whether $\mathcal{T} \models \forall r.A \sqsubseteq \exists r.C$

- (a) Reduce the subsumption problem to a concept unsatisfiability problem.
- (b) Normalize the TBox and the concept whose satisfiability you would check.
- (c) If possible, find a branch that leads to a clash.
- (d) If possible, find a complete branch without clash.
- (e) Does $\mathcal{T} \models \forall r.A \sqsubseteq \exists r.C$?

Exercise 2.3 ($\mathcal{SROIQ}(D)$) Consider the RBox $\mathcal{R} = \{ \operatorname{Fun}(t), \quad r_1 \circ r_2 \sqsubseteq r_1, \quad r \sqsubseteq s, \quad t \sqsubseteq s \}$ and the interpretation illustrated as follows:



- (a) Complete the interpretation to a model of \mathcal{R} .
- (b) Find the elements from the interpretation domain that belong to the following concepts:

$$\forall r_1.B \qquad \exists r_1.\{c\} \qquad \forall r_1^-.B \qquad \geq 2t.\top \qquad \geq 2s.(A \sqcup B)$$

(c) Which of the following axioms are entailed by \mathcal{R} ?

$$\mathsf{Fun}(s) \qquad \mathsf{Fun}(r) \qquad \mathsf{Fun}(t^{-}) \qquad \mathsf{Dom}(t) \sqsubseteq \leq 1t. \top$$

Exercise 2.4 Which of the following sentences contains a defeasible rule?

- (a) The meeting will be held in the conference room, unless there is a scheduling conflict.
- (b) Water boils at 100 degrees Celsius at standard atmospheric pressure.
- (c) The warranty covers all damages, unless it is deliberately.
- (d) A square has four equal sides and four right angles.
- (e) The bus departs at 9 AM.
- (f) She typically wake up early morning.
- (g) Al students usually like logics.

Exercise 2.5 How do you interpret the following default rules? Which of them are considered normal default rules?

- (a) Robot: Work
- (b) Robot: Work∧HandsnotBroken Work
- (c) $\frac{\text{Tomato:}\neg\text{Ripe}}{\text{Green}}$
- (d) $\frac{Suspect(x):\neg Guilty(x)}{Innocent(x)}$

Exercise 2.6 Given default theory T=(W,D) s.t $W=\{ \text{Dutch(bart), Logician(bart)} \}$, $\delta_1=\frac{\text{Dutch}(x):\text{Sporty}(x)}{\text{IceScater}(x)}$ $\delta_2:\frac{\text{Logician}(x):\text{Philosopher}(x)}{\text{Philosopher}(x)}$ $\delta_3:\frac{\text{Philosopher}(x):\neg\text{Sporty}(x)}{\neg\text{Sporty}(x)}$. Draw the associated process tree.

Exercise 2.7 Given default theory T=(W,D) with $W=\{a,d\}$, and $D=\{\delta_1,\delta_2,\delta_3\}$ such that $\delta_1=\frac{a:b}{b}$, $\delta_2=\frac{b:c}{c}$, $\delta_3=\frac{d:\neg c}{\neg c}$. Draw the process tree of T.

Exercise 2.8 Given AF $F=(\{a,b,c,d,e\},\{(a,b),(b,a),(b,c),(c,d),(d,e),(e,c)\})$. Draw the associated graph and indicate the sets of semantics for admissible, preferred, grounded, complete.

Exercise 2.9 Given AF $F = (\{a,b,c,d\},\{(a,b),(b,a),(a,c),(b,c),(c,d)\})$. An AF is called **relatively grounded** if the intersection of the preferred extensions is equal to the grounded extension. Check whether F is relatively grounded.