

The Final \mathcal{EL} -Completion Rules

\top -rule: Add \top to any individual.

\sqcap -rule 1: If d has $C \sqcap D$ assigned, assign also C and D to d .

\sqcap -rule 2: If d has C and D assigned, assign also $C \sqcap D$ to d .

\exists -rule 1: If d has $\exists r.C$ assigned:

1. If there is an element e with initial concept \underline{C} assigned, make e the r -successor of d .
2. Otherwise, add a new r -successor to d , and assign to it as initial concept \underline{C} .

\exists -rule 2: If d has an r -successor with C assigned, add $\exists r.C$ to d .

\sqsubseteq -rule: If d has C assigned and $C \sqsubseteq D \in \mathcal{T}$, then also assign D to d

The \mathcal{EL} -Completion Algorithm

Decide whether $\mathcal{O} \models C_0 \sqsubseteq D_0$

1. Start with initial element d_0 , assign to $\underline{C_0}$ to it as initial concept
2. Set **changed** := **true**
3. While **changed** = **true** :
 - 3.1 Set **changed** := **false**
 - 3.2 For every element d in the current interpretation:
 - 3.2.1 Apply all the rules on d in all possible ways so that only concepts from the input get assigned
 - 3.2.2 If a new element was added or a new concept assigned, set **changed** = **true**
4. If D_0 was assigned to d_0 , return **YES**, otherwise return **NO**

Concepts from the input: occur, possibly nested, explicitly in \mathcal{O} , C_0 or D_0