

CS181 HW4

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1. Asd

1. (a) $\underbrace{2^{1088}}_n \text{ inputs} \rightarrow \underbrace{2^{256}}_1 \text{ output}$

$$\Rightarrow n = \frac{2^{1088}}{2^{256}} = 2^{1088-256} = \boxed{2^{832}}$$

$$(b) p(\text{find}) = \frac{2^{832}}{2^{1088}} = \boxed{2^{-256}} \approx \boxed{8.63 \cdot 10^{-78}}$$

2.

2. to show if f has weakly collision resistant property,
then f has one way property.

proof by contrapositive:

Assume f is not a one way function.

then given $y \in Y$, we are able to find some
 $x \in X$ such that $f(x) = y$.

which means if we know $y = f(x)$, $x \in X$, $y \in Y$

we can find $x' \in X$ such that $f(x') = y$.

Also notice that $|X|/|Y|$ is large, set that
to be n , that means that

$p(x' = x) = \frac{1}{n}$, which is super small

since f is n to 1, and we will hit on x
with $\frac{1}{n}$ chance.

so $p(x' \neq x) = 1 - \frac{1}{n} \approx 1$

so it's highly likely to find an $x' \in X$ and
 $f(x') = y = f(x)$ with almost 100%
chance that $x' \neq x$
i.e. f is not weakly collision resistant.

Hence, by contrapositive, if f has weakly collision
property, then it also has the one-way
property

inputSHA3() is in 345.cpp

outputSHA3() is in 345.cpp

```
00110001001100100011001100110100001101010011011000110111001110000011100100110000001100010011
00100011001100110100001101010011011000110111001110000011100100110000001100010011001000110011
00110100001101010011011000110111001110000011100100110000001100010011001000110011001101000011
010100110110001101110011100000111001001100000011000100110010001100110011010000110100110110
0010111001110000011100100110000001100010011001000110011001000001101001101100011011000110110011
10000011100100110000001100010011001000110011001101000011010100110110001101110011100000111001
00110000001100010011001000110011001101000011010100110110001101110011100000111001001100000011
00010011001000110011001101000011010100110110001101110011100000111001001100000011000100110010
00110011001101000011010100110110001101110011100000111001001100000011000100110010001100110011
01000011010100110110001101110011100000111001001100000011000100110010001100110011010000110101
00110110001100111001110000011100100110000001100010011001000110011001101000011010100111000011
011100111000001110010011000000110001001100100110010011010000110101001101100011011100111000
00111001001100000011000100110010001100110011010000110101001101100011011100111000001110010011
00000011000100110010001100110011010000110101001101100011011100111000001110010011000000110001
00110010001100110011010000110101001101100011011100111000001110010011000000110001001100100011
00110011010000110101001101100011100111000001110010011000000110001001100100011001100110100
0011010100110110001101110011100000111001001100000011000100110010001100110011010001101010011
01100011011100111000000110010011000001100100110000
```

5.

theta() is in 345.cpp

calculated value for a_out[4][3][9....18]: 0011011000

calculated value for a_out[3][1][15...24]: 0000101001