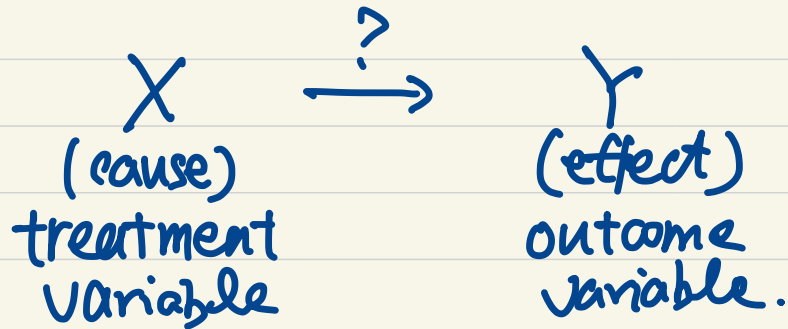


Causal Inference

- Causal questions .

Does X cause Y ?

How large is the effect of X on Y ?



| | | |
|------------|--------------|------------|
| Examples : | treatment | effect |
| | minimum wage | employment |
| | education | income |

Treatment : an action with binary values.

$$A = \begin{cases} 1 & \text{the action is taken (treated)} \\ 0 & \text{" not taken (untreated/control)} \end{cases}$$

Outcome $Y = \begin{cases} Y_1 & \text{if treated} \\ Y_0 & \text{if not treated.} \end{cases}$

$$\begin{aligned}\text{Causal effect} &= Y^1 - Y^0 \quad \leftarrow \text{potential outcomes.} \\ &= (\text{the outcome if treated}) \\ &\quad - (\text{the outcome if not treated}).\end{aligned}$$

Individual causal effect:

$$Y_i^1 - Y_i^0 \quad \text{we can only observe one of } Y_i^1 \text{ and } Y_i^0.$$

Average causal effect: (ATE)

$$\text{ATE} = E[Y_i^1 - Y_i^0] = E[Y_i^1] - E[Y_i^0].$$