

EART119 – In Class Assignment – Week 1 – First Calculations and Functions-

1. Consider two satellites at different velocities but the same orbit around earth. Let's assume their positions as a function of time can be described by two discrete functions $f(t)$ and $g(t)$ with:

$$f(t) = c \cdot (t - t_0)^2, \text{ with } t_0 = 2.5, c = 1.1$$

$$g(t) = A \cdot t + t_0 \text{ with } A = 5, \text{ and } -10 \leq t \leq 10$$

Write a program that finds the approximate crossover point at which $f(t) \sim g(t)$ (remember we are dealing with discrete functions). Evaluate the function values of $g(t)$ and $f(t)$ for $N = 1000$, equally spaced point within the given interval (use: `np.linspace`).

The criteria for the detection of the crossover point is:

$$|f(t) - g(t)| < \varepsilon, \text{ for } -10 \leq t \leq 10, \text{ and } \varepsilon = 0.1$$

- a. What are t , $g(t)$ and $f(t)$ at the crossover point?
- b. Solve this using a "for loop" structure and then vectorize the problem to eliminate the loop for faster processing.
- c. Do the same problem for $g(t) = A \cdot t + t_0$ using the vectorized solution. Return all cross-over points!
- d. Find the minimum of the difference between the two discrete functions:
 - i. $\min |f(t) - g(t)|$

Look at [matlab_to_python.pdf](#) reference sheet before starting the following assignment.

2. Compute the average and standard deviation of a matrix of downhole well pressures using matrix operations. Specifically, you can use the following:

$$mean = \frac{1}{n} \sum_{i=1}^n D_i$$

In matrix notation:

$$\overline{mean} = \mathbf{D}^{m \times n} \cdot \overline{\mathbf{1}}^{n \times 1} / n$$

m – are the number of wells,

n – are the number of pressure measurements in each well

Where \mathbf{D} is the data matrix with dimensions $m \times n$, $\overline{\mathbf{1}}$ is the unity vector of dimension $1 \times n$ and n is the total number of measurements. And the standard deviation is given by:

$$std = \left(\sum_{i=1}^n (D_i - mean)^2 / n \right)^{1/2}$$

In matrix notation:

$$\overline{std} = \left\{ [(\mathbf{D}^{m \times n} - \overline{mean}^{m \times 1} \cdot \overline{\mathbf{1}}^{1 \times n})] ** 2 \cdot \overline{\mathbf{1}}^{n \times 1} / m \right\}^{1/2}$$

3. Solve the following linear system of equations:

$$\begin{bmatrix} 1 \\ 2 \end{bmatrix} \begin{bmatrix} x_0 + x_1 = 9 \end{bmatrix}$$

$$\begin{bmatrix} 1 \\ 2 \end{bmatrix} \begin{bmatrix} x_0 + 2x_1 = 8, \end{bmatrix} \text{ Use np.linalg.solve!}$$