

**Math 302 , Problem Set 2** Due January 30,2025 6 P.M.

Draw a Venn diagram corresponding to the following logical conditions.

1.

$$A \implies B.$$

2.

$$A \iff B.$$

3.

$$\neg A \wedge \neg B.$$

Give formal proofs of the following (with  $A, B, C$  sets).

4. If  $A \subset B$  then  $A \cup B = B$ .

5. If  $A \subset B$  then  $B^c \subset A^c$ .

6. If  $A \subset B$  then  $B \setminus (B \setminus A) = A$ .

7.  $A \subset B \cap C$  if and only if  $A \subset B$  and  $A \subset C$ .

8.

$$A \cap (B \cup C) = (A \cap B) \cup (A \cap C).$$

9.

$$A \cup (B \cap C) = (A \cup B) \cap (A \cup C).$$

10.

$$A = (A \cap B) \cup (A \setminus B).$$