## fig\_toc

## April 5, 2022

```
import numpy as np
import pandas as pd
import scipy.stats as stats
import scipy.optimize as optimize
import pymc3 as pm
import arviz as az
import theano.tensor as tt

import networkx as nx

import matplotlib.pyplot as plt
import matplotlib.gridspec as gridspec
import seaborn as sns; sns.set_theme(style='ticks', context='paper', u

ofont_scale=0.8);

%reload_ext watermark
%watermark -a "Mathieu Baltussen" -d -t -u -v -iv
```

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Python implementation: CPython Python version : 3.9.5 IPython version : 7.28.0

arviz : 0.11.4 numpy : 1.20.3 networkx : 2.6.3

sys : 3.9.5 | packaged by conda-forge | (default, Jun 19 2021, 00:32:32)

[GCC 9.3.0]

theano : 1.1.2 scipy : 1.6.2 matplotlib: 3.4.2 pandas : 1.2.4 seaborn : 0.11.1 pymc3 : 3.11.4

```
[2]: data = pd.read_csv("../data/CEKS33.csv")
kf = 0.125  # minute^-1
E = 0.012
data = data.assign(kf=kf, Tr=E)
data_1 = data[data.AAA == 0]
data_2 = data[data.AAA != 0]
```

```
[3]: with pm.Model() as model_1:
         k_cat = pm.Uniform("k_cat", 0, 500)
         K_M = pm.Uniform("K_M", 0, 500)
         K_I = pm.Uniform("K_I", 1000, 10000)
         sigma = pm.Exponential("sigma", 10)
         S_in = data_1["R"].values
         I_in = data_1["AAA"].values
         P_obs = data_1["AMC"].values
         S_{obs} = (
             S_in - P_obs
         ) # Substrate concentration inside reactor determined via stoichiometricu
      \rightarrow conservation at steady-state
         E = data_1["Tr"].values
         kf = data_1["kf"].values
         # Inference of probabilistic model at steady-state conditions
         P = pm.Normal(
             "obs",
             mu=k_cat * E * S_obs / (kf * (K_M + S_obs * (1 + I_in / K_I))),
             sigma=sigma,
             observed=P_obs,
         )
         idata_1 = pm.sample(
             1000,
             tune=1000,
             cores=4,
             step=pm.NUTS(target_accept=0.95),
             return_inferencedata=True,
         )
     with pm.Model() as model_2:
         k_cat = pm.Uniform("k_cat", 0, 500)
         K_M = pm.Uniform("K_M", 0, 500)
         K_I = pm.Uniform("K_I", 1000, 10000)
         sigma = pm.Exponential("sigma", 10)
         S in = data 2["R"].values
         I_in = data_2["AAA"].values
         P obs = data 2["AMC"].values
```

```
S obs = (
        S_{in} - P_{obs}
    ) # Substrate concentration inside reactor determined via stoichiometric⊔
\rightarrow conservation at steady-state
    E = data_2["Tr"].values
    kf = data 2["kf"].values
    # Inference of probabilistic model at steady-state conditions
    P = pm.Normal(
        "obs",
        mu=k_cat * E * S_obs / (kf * (K_M + S_obs * (1 + I_in / K_I))),
        sigma=sigma,
        observed=P_obs,
    idata_2 = pm.sample(
        1000,
        tune=1000,
        cores=4,
        step=pm.NUTS(target_accept=0.95),
        return_inferencedata=True,
    )
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    K_I = pm.Uniform("K_I", 1000, 10000)
    sigma = pm.Exponential("sigma", 10)
    S_in = data["R"].values
    I_in = data["AAA"].values
    P_obs = data["AMC"].values
    S obs = (
        S_in - P_obs
    ) # Substrate concentration inside reactor determined via stoichiometric,
\rightarrow conservation at steady-state
    E = data["Tr"].values
    kf = data["kf"].values
    # Inference of probabilistic model at steady-state conditions
    P = pm.Normal(
        "obs",
        mu=k_cat * E * S_obs / (kf * (K_M + S_obs * (1 + I_in / K_I))),
        sigma=sigma,
        observed=P_obs,
    idata = pm.sample(
        1000,
```

```
cores=4,
             step=pm.NUTS(target_accept=0.95),
             return_inferencedata=True,
         )
    Multiprocess sampling (4 chains in 4 jobs)
    NUTS: [sigma, K_I, K_M, k_cat]
    <IPython.core.display.HTML object>
    Sampling 4 chains for 1_000 tune and 1_000 draw iterations (4_000 + 4_000 draws
    total) took 6 seconds.
    Multiprocess sampling (4 chains in 4 jobs)
    NUTS: [sigma, K_I, K_M, k_cat]
    <IPython.core.display.HTML object>
    Sampling 4 chains for 1_000 tune and 1_000 draw iterations (4_000 + 4_000 draws
    total) took 13 seconds.
    There were 2 divergences after tuning. Increase `target_accept` or
    reparameterize.
    There were 2 divergences after tuning. Increase `target_accept` or
    reparameterize.
    There was 1 divergence after tuning. Increase `target_accept` or reparameterize.
    The number of effective samples is smaller than 25% for some parameters.
    Multiprocess sampling (4 chains in 4 jobs)
    NUTS: [sigma, K_I, K_M, k_cat]
    <IPython.core.display.HTML object>
    Sampling 4 chains for 1_000 tune and 1_000 draw iterations (4_000 + 4_000 draws
    total) took 4 seconds.
[4]: posterior df 1 = idata 1.to dataframe(["posterior"])
     posterior_df_2 = idata_2.to_dataframe(["posterior"])
     posterior_df = idata.to_dataframe(["posterior"])
     with model_1:
         post_pred_1 = pm.sample_posterior_predictive(
             idata_1, var_names=["obs", "k_cat", "K_M", "K_I", "sigma"]
     posterior_df_1 = pd.DataFrame(
         {
             "k_cat": post_pred_1["k_cat"],
             "K_M": post_pred_1["K_M"],
             "K_I": post_pred_1["K_I"],
```

tune=1000,

"sigma": post\_pred\_1["sigma"],

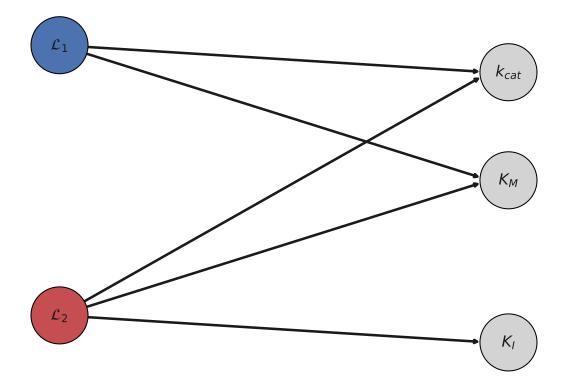
}

)

```
with model_2:
          post_pred_2 = pm.sample_posterior_predictive(
              idata_2, var_names=["obs", "k_cat", "K_M", "K_I", "sigma"]
      posterior_df_2 = pd.DataFrame(
          {
              "k_cat": post_pred_2["k_cat"],
              "K_M": post_pred_2["K_M"],
              "K I": post pred 2["K I"],
              "sigma": post_pred_2["sigma"],
          }
      )
      with model:
          post_pred = pm.sample_posterior_predictive(
              idata, var_names=["obs", "k_cat", "K_M", "K_I", "sigma"]
          )
      posterior_df = pd.DataFrame(
          {
              "k_cat": post_pred["k_cat"],
              "K_M": post_pred["K_M"],
              "K_I": post_pred["K_I"],
              "sigma": post_pred["sigma"],
          }
      )
     <IPython.core.display.HTML object>
     <IPython.core.display.HTML object>
     <IPython.core.display.HTML object>
[25]: left = nx.bipartite.sets(model graph)[0]
      pos = nx.bipartite_layout(model_graph, list(left)[::-1], scale=0.8)
      print(pos)
      pos = {
          "\mathcal{L}_{2}\\": np.array([0.25, 0.25]),
          "\mathcal{L}_{1}\\": np.array([0.25, 0.75]),
          "$k_{cat}$": np.array([0.75, 0.7]),
          "$K_M$": np.array([0.75, 0.5]),
          "$K_I$": np.array([0.75, 0.2]),
      }
      fig, ax = plt.subplots(constrained_layout=True)
      with sns.color_palette("deep"):
          nx.draw(
              model_graph,
```

```
pos=pos,
   ax=ax,
   with_labels=True,
   node_size=2000,
   node_color=["CO", "lightgrey", "lightgrey", "C3", "lightgrey"],
   width=2,
   edgecolors="black",
   arrowstyle="-|>",
   arrowsize=6,
   connectionstyle="arc,armB=-15",
)
```

```
{'$\\mathcal{L}_{2}$': array([-0.8, -0.5]), '$\\mathcal{L}_{1}$': array([-0.8, 0.5]), '$k_{cat}$': array([ 0.53333333, -0.5 ]), '$K_M$': array([0.533333333, 0.5 ])}
```

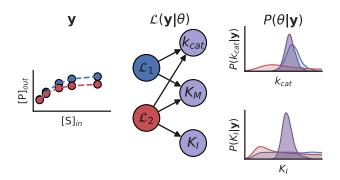


```
sns.kdeplot(data[i], ax=axes[i], fill=True, clip_on=True, alpha=0.6,_
        →color=pal[i])
               sns.kdeplot(data[i], ax=axes[i], fill=False, clip_on=True,_
       \# y_max = max(max(ax.qet_yticks())) for ax in axes)*1.1
          x_min, x_max = min(axes[-1].get_xticks()), max(axes[-1].get_xticks())
          for i, ax in enumerate(axes):
               \# ax.set_ylim(0, y_max)
              ymax = max(ax.get_yticks())*(n_plots - i)
              ax.set_ylim(0)
              ax.set xlim(x min, x max)
              ax.patch.set_alpha(0)
          for ax in axes[:-1]:
              ax.axis("off")
              sns.despine(ax=ax, left=True, bottom=True)
          axes[-1].set_yticks([])
          axes[-1].set_ylabel("")
           sns.despine(ax=axes[-1], left=True)
          return axes, pal
[114]: palette = sns.cubehelix palette(3, start=0.4, rot=-.2, dark=0.4, light=0.9)
      palette
[114]: [[0.8785578419340125, 0.9014144832192498, 0.9687173115546507],
        [0.6406706030956623, 0.622799643084166, 0.8302502287527784],
        [0.4428111826648146, 0.3448837880001888, 0.5788669999260483]]
[218]: model graph = nx.DiGraph()
      model_graph.add_edge(r"$\mathcal{L}_{1}$", r"$k_{cat}$")
      model graph.add edge(r"$\mathcal{L} {1}$", r"$K M$")
      model_graph.add_edge(r"$\mathcal{L}_{2}$", r"$k_{cat}$")
      model graph.add edge(r"$\mathcal{L} {2}$", r"$K M$")
      model_graph.add_edge(r"$\mathcal{L}_{2}$", r"$K_I$")
      pos = {
           "\mathcal{L}_{2}\\": np.array([0.33, 0.425]),
          "\mathcal{L}_{1}\\": np.array([0.33, 0.575]),
          "$k_{cat}$": np.array([0.66, 0.65]),
           "$K_M$": np.array([0.66, 0.5]),
          "$K_I$": np.array([0.66, 0.35]),
      fig = plt.figure(figsize=(3.25, 1.75), constrained_layout=True)
```

```
gs = fig.add_gridspec(4, 3, wspace=0.2, hspace=0.0)
# gs.subplots()
ax_1 = fig.add_subplot(gs[1:3, 0])
ax_1.scatter(data_1.R, data_1.AMC, ec="black", fc="C0", label=r"[I]=0 $\mu M$",__
⇒s=32)
ax_1.scatter(data_2.R, data_2.AMC, ec="black", fc="C3", label=r"[I]=1500 $\mu_L
\hookrightarrow M$", s=32)
ax 1.plot(data 1.R, data 1.AMC, "--", c="CO")
ax_1.plot(data_2.R, data_2.AMC, "--", c="C3")
# ax_1.legend()
ax_1.set_xlim(0, 600)
ax_1.set_ylim(0, 9)
\# ax_1.text(-0.18, 0.95, 'A', transform=ax_1.transAxes, weight="bold", size=10)
ax_1.set_xlabel(r"$[$S$]_{in}$")
ax_1.set_ylabel(r"$[$P$]_{out}$")
ax_1.set_xticks([])
ax_1.set_yticks([])
sns.despine(ax=ax_1)
ax_1.margins(y=-0.3)
ax_2 = fig.add_subplot(gs[:, 1])
with sns.color_palette("deep"):
    nx.draw(
        model_graph,
        pos=pos,
        ax=ax_2,
        with_labels=True,
        node_size=400,
        node_color=["CO", palette[1], palette[1], "C3", palette[1]],
        width=1,
        edgecolors="black",
        arrowstyle="-|>",
        arrowsize=9,
        connectionstyle="arc",
        font_size=10
    ax_2.margins(x=0.25, y=0.1)
    ax_3 = fig.add_subplot(gs[0:2, 2:])
    sns.kdeplot(posterior_df_1["k_cat"], ax=ax_3, fill=True, color="CO")
    sns.kdeplot(posterior_df_2["k_cat"], ax=ax_3, fill=True, color="C3")
```

```
sns.kdeplot(posterior_df["k_cat"], ax=ax_3, fill=True, color=palette[2],__
 \rightarrowalpha=0.5)
    sns.despine(ax=ax_3)
    ax 3.set xlim(75, 120)
    ax_3.set_ylabel(r"$P(k_{cat}|\mathbb{y})$")
    ax 3.set xlabel(r"$k {cat}$")
    ax 3.set xticks([])
    ax_3.set_yticks([])
    \# qs_rp = qs[2:, 2].subgridspec(3,1, hspace=-0.1)
    # axes, pal = plot_ridgeplots(fig, gs_rp, 3, [
                                                   posterior_df_1['K_I'],
                                                   posterior_df_2['K_I'],
                                                   posterior_df['K_I']],
                                   start_color=0.4
    ax_4 = fig.add_subplot(gs[2:, 2])
    sns.kdeplot(posterior df 1["K I"], ax=ax 4, fill=True, color="CO")
    sns.kdeplot(posterior_df_2["K_I"], ax=ax_4, fill=True, color="C3")
    sns.kdeplot(posterior_df["K_I"], ax=ax_4, fill=True, color=palette[2],__
 \rightarrowalpha=0.5)
    sns.despine(ax=ax_4)
    ax_4.set_xlim(0, 8000)
    ax 4.set vlabel(r"P(K {I}|\mathbb{Y}))")
    ax_4.set_xlabel(r"$K_{I}$")
    ax_4.set_xticks([])
    ax_4.set_yticks([])
\# ax 0 = fiq.add subplot(qs[0, 0])
# sns.despine(ax=ax_0, left=True, bottom=True)
ax 1.text(0.5, 2.25, r"$\mathbf{y}$\", transform=ax 1.transAxes, ha='center', |
→fontsize=10, va='center', weight='bold', in_layout=False)
ax 2.text(0.5, 1.05, r"\text{mathcal}(L)(\mathcal{y}|\lambda )", transform=ax 2.
→transAxes, fontsize=10, ha='center', va='center', weight='bold',
→in_layout=False)
ax_3.margins(y=0.2)
ax_3.text(0.5, 1.13, r"$P(\theta|\mathbf{y})$", transform=ax_3.transAxes,__
→ha='center', fontsize=10, va='center', weight='bold', in_layout=True)
plt.savefig("../figures/fig_toc.svg", dpi=300)
plt.show()
```

/home/mathieu/anaconda3/envs/phd/lib/python3.9/sitepackages/numpy/core/\_asarray.py:171: VisibleDeprecationWarning: Creating an ndarray from ragged nested sequences (which is a list-or-tuple of lists-or-tuples-or ndarrays with different lengths or shapes) is deprecated. If you meant to do this, you must specify 'dtype=object' when creating the ndarray. return array(a, dtype, copy=False, order=order, subok=True)



[]: