Практическая работа №3. Алгоритмы на графах

Дана матрица смежности неориентированного взвешенного графа (таблица 3.1, 0 означает отсутствие ребра).

- 1. Необходимо построить минимальное остовное дерево.
- 2. Запустите функцию, реализующую алгоритм поиска в глубину, для перечисления всех вершин в минимальном остовном дереве. Результат должен быть представлен с помощью одного из контейнеров STL.
- 3. Напишите функцию для поиска минимального пути (в смысле суммарного веса пройденных рёбер) между і-м и всеми остальными пунктами, куда можно построить маршрут. Результат должен быть представлен с помощью одного из контейнеров STL.
- 4. Реализовать функцию подсчета степени (количества инцидентных ребер) вершин в полученном дереве (обход дерева сделать на основе поиска в ширину). Реализовать функцию подсчета средней степени по всему дереву.

Таблина 3.1

Вариант	Матрица смежности
1.	{
	{ 0, 9, 5, 4, 8, 5, 1, 6, 1, 9, 5, 0 },
	{ 9, 0, 1, 7, 7, 8, 2, 8, 2, 0, 7, 3 },
	{ 5, 1, 0, 4, 0, 9, 4, 4, 5, 2, 3, 1 },
	{ 4, 7, 4, 0, 5, 3, 8, 2, 3, 4, 5, 9 },
	{ 8, 7, 0, 5, 0, 5, 4, 7, 7, 5, 4, 4 },
	{ 5, 8, 9, 3, 5, 0, 5, 9, 4, 8, 1, 1 },
	{ 1, 2, 4, 8, 4, 5, 0, 1, 6, 4, 2, 0 },
	{ 6, 8, 4, 2, 7, 9, 1, 0, 8, 9, 4, 4 },
	{ 1, 2, 5, 3, 7, 4, 6, 8, 0, 2, 0, 7 },
	{ 9, 0, 2, 4, 5, 8, 4, 9, 2, 0, 3, 4 },
	{ 5, 7, 3, 5, 4, 1, 2, 4, 0, 3, 0, 2 },
	{ 0, 3, 1, 9, 4, 1, 0, 4, 7, 4, 2, 0 },
	}
2.	{
	{ 0, 5, 3, 6, 8, 9, 7, 8, 1, 7, 0, 0, 4, 8 },

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                 \{6, 3, 2, 0, 4, 6, 6, 4, 6, 8, 8, 6, 9, 4\},\
                 \{8, 6, 8, 4, 0, 2, 8, 0, 9, 0, 8, 2, 0, 5\},\
                 \{9, 9, 1, 6, 2, 0, 8, 5, 5, 9, 8, 8, 9, 8\},\
                 \{7, 6, 3, 6, 8, 8, 0, 3, 6, 6, 8, 1, 5, 6\},\
                 \{8, 5, 0, 4, 0, 5, 3, 0, 7, 1, 4, 7, 8, 5\},\
                 \{1, 0, 8, 6, 9, 5, 6, 7, 0, 1, 2, 5, 2, 2\},\
                 { 7, 8, 8, 8, 0, 9, 6, 1, 1, 0, 6, 2, 4, 8 },
                 \{0, 0, 5, 8, 8, 8, 8, 4, 2, 6, 0, 8, 4, 3\},\
                 \{0, 0, 5, 6, 2, 8, 1, 7, 5, 2, 8, 0, 5, 5\},\
                 \{4, 5, 8, 9, 0, 9, 5, 8, 2, 4, 4, 5, 0, 3\},\
                 \{8, 6, 4, 4, 5, 8, 6, 5, 2, 8, 3, 5, 3, 0\},\
         }
3.
                 \{0, 1, 7, 0, 9, 2, 4, 9, 3, 1, 4, 7, 3\},\
                 \{1, 0, 8, 6, 0, 0, 4, 8, 5, 7, 6, 7, 4\},\
                 \{7, 8, 0, 9, 6, 0, 6, 1, 3, 0, 4, 4, 9\},\
                 \{0, 6, 9, 0, 4, 5, 1, 1, 5, 6, 4, 9, 3\},\
                 \{9, 0, 6, 4, 0, 7, 0, 0, 9, 0, 4, 7, 6\},\
                 \{2, 0, 0, 5, 7, 0, 4, 5, 3, 8, 5, 1, 8\},\
                 \{4, 4, 6, 1, 0, 4, 0, 3, 4, 3, 4, 8, 0\},\
                 \{9, 8, 1, 1, 0, 5, 3, 0, 3, 5, 7, 5, 6\},\
                 \{3, 5, 3, 5, 9, 3, 4, 3, 0, 2, 3, 0, 4\},\
                 \{1, 7, 0, 6, 0, 8, 3, 5, 2, 0, 7, 9, 4\},\
                 { 4, 6, 4, 4, 4, 5, 4, 7, 3, 7, 0, 9, 8 },
                 \{7, 7, 4, 9, 7, 1, 8, 5, 0, 9, 9, 0, 6\},\
                 \{3, 4, 9, 3, 6, 8, 0, 6, 4, 4, 8, 6, 0\},\
         }
4.
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                 \{2, 7, 0, 9, 3, 5, 1, 9, 1, 0, 8, 0\},\
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                 \{5, 7, 3, 8, 0, 1, 7, 3, 0, 6, 8, 9\},\
                 \{1, 1, 5, 8, 1, 0, 7, 0, 0, 8, 6, 9\},\
                 { 7, 9, 1, 4, 7, 7, 0, 0, 7, 2, 5, 8 },
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         }
5.
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                 \{1, 0, 1, 8, 6, 0, 0, 0, 8, 8\},\
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                 \{0, 8, 6, 0, 1, 3, 0, 3, 4, 3\},\
                 \{1, 6, 6, 1, 0, 4, 6, 8, 5, 7\},\
                 \{3, 0, 4, 3, 4, 0, 1, 3, 6, 1\},\
                 \{6, 0, 5, 0, 6, 1, 0, 4, 7, 1\},\
                 \{6, 0, 7, 3, 8, 3, 4, 0, 1, 8\},\
                 { 7, 8, 6, 4, 5, 6, 7, 1, 0, 1 },
                 \{1, 8, 2, 3, 7, 1, 1, 8, 1, 0\},\
         }
6.
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                 { 5, 0, 8, 0, 3, 8, 4, 8, 6, 6, 6, 3, 4 },
                 \{6, 8, 0, 2, 0, 0, 0, 9, 3, 5, 3, 8, 1\},\
                 \{6, 0, 2, 0, 2, 4, 7, 7, 7, 9, 5, 5, 5\},\
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                 \{5, 4, 0, 7, 5, 8, 0, 6, 9, 0, 1, 2, 0\},\
                 \{0, 8, 9, 7, 5, 1, 6, 0, 4, 6, 7, 3, 3\},\
                 \{0, 6, 3, 7, 4, 5, 9, 4, 0, 4, 4, 1, 1\},\
                 \{8, 6, 5, 9, 4, 4, 0, 6, 4, 0, 9, 2, 7\},\
                 \{8, 6, 3, 5, 1, 5, 1, 7, 4, 9, 0, 6, 9\},\
                 \{4, 3, 8, 5, 4, 8, 2, 3, 1, 2, 6, 0, 3\},\
                 \{4, 4, 1, 5, 2, 6, 0, 3, 1, 7, 9, 3, 0\},\
7.
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                 \{2, 2, 2, 4, 5, 0, 5, 7, 0\},\
         }
8.
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9.
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         }
11.
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                 \{1, 7, 0, 8, 3, 0, 1, 1, 4, 7\},\
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                 \{9, 0, 6, 1, 0, 1, 2, 0, 7, 8\},\
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12.
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                 { 2, 6, 7, 0, 9, 7, 2, 8, 0, 8, 1 },
                 \{5, 5, 0, 9, 0, 7, 7, 5, 0, 1, 8\},\
                 \{6, 2, 9, 7, 7, 0, 1, 8, 5, 9, 0\},\
                 \{4, 9, 0, 2, 7, 1, 0, 6, 4, 9, 4\},\
                 \{0, 5, 8, 8, 5, 8, 6, 0, 9, 6, 6\},\
                 \{2, 9, 2, 0, 0, 5, 4, 9, 0, 8, 8\},\
                 \{1, 8, 0, 8, 1, 9, 9, 6, 8, 0, 7\},\
                 \{1, 3, 8, 1, 8, 0, 4, 6, 8, 7, 0\},\
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13.
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                 \{6, 0, 1, 9, 0, 3, 1, 9, 1\},\
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                 \{9, 8, 1, 4, 1, 8, 0, 7, 7\},\
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                 \{3, 5, 4, 2, 1, 3, 7, 4, 0\},\
14.
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                 \{2, 2, 0, 4, 2, 2, 5, 3, 4, 6, 0, 3, 0\},\
                 \{1, 5, 4, 0, 1, 2, 4, 9, 4, 8, 8, 0, 9\},\
                 \{9, 1, 2, 1, 0, 3, 5, 4, 4, 4, 5, 4, 8\},\
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         }
15.
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16.
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                 \{0, 9, 5, 5, 0, 3, 8, 2, 6, 4, 3\},\
                 { 3, 4, 1, 5, 3, 0, 3, 2, 2, 2, 8 },
                 \{4, 3, 9, 2, 8, 3, 0, 7, 6, 7, 6\},\
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                 \{6, 6, 3, 2, 6, 2, 6, 4, 0, 7, 3\},\
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         }
17.
                 \{0, 9, 7, 9, 6, 9, 5, 5, 6, 3, 6\},\
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18.
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                 \{0, 6, 0, 8, 8, 4, 3, 6, 5, 3, 6, 6, 5\},\
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                 \{6, 1, 6, 3, 7, 4, 2, 2, 5, 5, 0, 9, 6\},\
                 \{6, 4, 6, 6, 2, 2, 9, 3, 8, 9, 9, 0, 5\},\
                 \{7, 2, 5, 8, 0, 6, 8, 2, 1, 7, 6, 5, 0\},\
         }
19.
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                 \{4, 0, 5, 3, 5, 3, 2, 3, 9, 6, 2\},\
                 \{0, 5, 0, 4, 9, 9, 9, 6, 2, 7, 2\},\
                 { 7, 3, 4, 0, 5, 7, 8, 4, 1, 8, 1 },
                \{1, 5, 9, 5, 0, 4, 8, 2, 3, 4, 2\},\
                 \{8, 3, 9, 7, 4, 0, 6, 1, 5, 4, 6\},\
                 \{9, 2, 9, 8, 8, 6, 0, 0, 7, 7, 6\},\
                 \{7, 3, 6, 4, 2, 1, 0, 0, 9, 2, 7\},\
                 \{6, 9, 2, 1, 3, 5, 7, 9, 0, 1, 1\},\
                 \{8, 6, 7, 8, 4, 4, 7, 2, 1, 0, 5\},\
                 \{3, 2, 2, 1, 2, 6, 6, 7, 1, 5, 0\},\
         }
20.
                 \{0, 5, 2, 7, 4, 8, 8, 8, 0, 6, 8, 4\},\
                 { 5, 0, 7, 2, 0, 8, 9, 6, 4, 2, 5, 4 },
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                 { 7, 2, 1, 0, 6, 8, 0, 6, 3, 9, 4, 3 },
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                 \{6, 2, 6, 9, 9, 6, 5, 7, 6, 0, 8, 1\},\
                 \{8, 5, 3, 4, 6, 9, 5, 6, 5, 8, 0, 9\},\
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21.
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                 \{6, 0, 1, 1, 7, 7, 4, 7, 4, 8, 3\},\
```

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                 \{9, 7, 5, 6, 9, 0, 9, 2, 0, 8, 1\},\
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                 { 7, 8, 9, 3, 9, 8, 8, 4, 7, 0, 4 },
                 \{1, 3, 0, 6, 7, 1, 5, 0, 1, 4, 0\},\
22.
                 \{0, 7, 7, 9, 0, 4, 7, 6, 4, 4, 1, 4\},\
                 \{7, 0, 7, 5, 5, 2, 1, 1, 8, 5, 9, 0\},\
                 \{7, 7, 0, 8, 9, 0, 9, 8, 9, 7, 4, 1\},\
                 \{9, 5, 8, 0, 7, 3, 9, 6, 5, 5, 5, 2\},\
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                 \{6, 1, 8, 6, 3, 2, 2, 0, 3, 3, 6, 9\},\
                 \{4, 8, 9, 5, 5, 3, 7, 3, 0, 5, 6, 2\},\
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                 \{1, 9, 4, 5, 0, 9, 4, 6, 6, 6, 6, 0, 7\},\
                 \{4, 0, 1, 2, 2, 3, 7, 9, 2, 4, 7, 0\},\
23.
                 \{0, 8, 2, 8, 9, 3, 7, 1, 5, 6\},\
                 \{8, 0, 2, 9, 4, 7, 7, 1, 3, 5\},\
                 \{2, 2, 0, 9, 5, 2, 9, 5, 9, 9\},\
                 \{8, 9, 9, 0, 0, 9, 7, 7, 2, 8\},\
                 \{9, 4, 5, 0, 0, 3, 2, 0, 3, 1\},\
                 \{3, 7, 2, 9, 3, 0, 3, 0, 5, 9\},\
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                 \{1, 1, 5, 7, 0, 0, 8, 0, 2, 6\},\
                 { 5, 3, 9, 2, 3, 5, 7, 2, 0, 7 },
                 \{6, 5, 9, 8, 1, 9, 0, 6, 7, 0\},\
         }
24.
                 {
```

```
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                 \{7, 0, 0, 7, 1, 3, 0, 5, 0, 4, 6\},\
                 \{7, 0, 0, 4, 6, 7, 0, 3, 9, 4, 1\},\
                 \{7, 7, 4, 0, 4, 8, 4, 8, 5, 3, 5\},\
                 \{0, 1, 6, 4, 0, 5, 5, 2, 2, 9, 6\},\
                 \{2, 3, 7, 8, 5, 0, 7, 1, 5, 9, 5\},\
                 \{4, 0, 0, 4, 5, 7, 0, 8, 6, 5, 2\},\
                 \{4, 5, 3, 8, 2, 1, 8, 0, 2, 2, 8\},\
                 \{3, 0, 9, 5, 2, 5, 6, 2, 0, 9, 4\},\
                 \{2, 4, 4, 3, 9, 9, 5, 2, 9, 0, 2\},\
                 \{3, 6, 1, 5, 6, 5, 2, 8, 4, 2, 0\},\
25.
                 \{0, 1, 4, 4, 8, 5, 6, 7, 5, 2, 4, 2\},\
                 \{1, 0, 6, 9, 1, 2, 3, 1, 2, 8, 9, 5\},\
                 \{4, 6, 0, 7, 4, 8, 9, 6, 2, 6, 7, 6\},\
                 \{4, 9, 7, 0, 2, 0, 0, 8, 8, 8, 7, 8\},\
                 { 8, 1, 4, 2, 0, 3, 9, 2, 7, 7, 3, 1 },
                 { 5, 2, 8, 0, 3, 0, 0, 6, 4, 4, 5, 3 },
                 \{6, 3, 9, 0, 9, 0, 0, 2, 2, 9, 2, 3\},\
                 \{7, 1, 6, 8, 2, 6, 2, 0, 7, 4, 2, 6\},\
                 \{5, 2, 2, 8, 7, 4, 2, 7, 0, 3, 4, 6\},\
                 \{2, 8, 6, 8, 7, 4, 9, 4, 3, 0, 3, 4\},\
                 \{4, 9, 7, 7, 3, 5, 2, 2, 4, 3, 0, 7\},\
                 \{2, 5, 6, 8, 1, 3, 3, 6, 6, 4, 7, 0\},\
26.
                 \{0, 3, 8, 7, 6, 6, 0, 2, 0, 0\},\
                 \{3, 0, 9, 6, 3, 9, 9, 5, 1, 4\},\
                 \{8, 9, 0, 4, 2, 4, 9, 8, 8, 0\},\
                 \{7, 6, 4, 0, 5, 8, 5, 0, 3, 7\},\
                 \{6, 3, 2, 5, 0, 2, 8, 8, 9, 4\},\
                 \{6, 9, 4, 8, 2, 0, 6, 9, 7, 6\},\
                 \{0, 9, 9, 5, 8, 6, 0, 1, 8, 4\},\
                 \{2, 5, 8, 0, 8, 9, 1, 0, 6, 7\},\
                 \{0, 1, 8, 3, 9, 7, 8, 6, 0, 6\},\
                 \{0, 4, 0, 7, 4, 6, 4, 7, 6, 0\},\
```

```
27.
                 \{0, 9, 4, 3, 8, 7, 8, 2, 1\},\
                 \{9, 0, 8, 2, 1, 0, 7, 9, 5\},\
                 \{4, 8, 0, 8, 4, 4, 7, 5, 5\},\
                 \{3, 2, 8, 0, 3, 4, 6, 2, 6\},\
                 \{8, 1, 4, 3, 0, 5, 3, 2, 2\},\
                 \{7, 0, 4, 4, 5, 0, 5, 2, 6\},\
                 \{8, 7, 7, 6, 3, 5, 0, 0, 0, 0\},\
                 \{2, 9, 5, 2, 2, 2, 0, 0, 6\},\
                 \{1, 5, 5, 6, 2, 6, 0, 6, 0\},\
28.
                 \{0, 7, 6, 4, 7, 0, 9, 2, 7\},\
                 \{7, 0, 7, 6, 8, 5, 7, 4, 6\},\
                 \{6, 7, 0, 6, 2, 1, 8, 6, 0\},\
                 \{4, 6, 6, 0, 5, 8, 4, 7, 1\},\
                 \{7, 8, 2, 5, 0, 0, 0, 2, 5\},\
                 \{0, 5, 1, 8, 0, 0, 2, 2, 3\},\
                 \{9, 7, 8, 4, 0, 2, 0, 6, 1\},\
                 \{2, 4, 6, 7, 2, 2, 6, 0, 3\},\
                 \{7, 6, 0, 1, 5, 3, 1, 3, 0\},\
29.
                 \{0, 9, 9, 3, 9, 6, 2, 9, 1, 5, 7\},\
                 \{9, 0, 4, 3, 1, 3, 3, 3, 2, 6, 0\},\
                 \{9, 4, 0, 4, 6, 1, 7, 5, 6, 7, 6\},\
                 \{3, 3, 4, 0, 7, 0, 6, 6, 9, 5, 9\},\
                 \{9, 1, 6, 7, 0, 8, 2, 3, 7, 3, 8\},\
                 \{6, 3, 1, 0, 8, 0, 6, 9, 3, 7, 2\},\
                 \{2, 3, 7, 6, 2, 6, 0, 8, 3, 6, 6\},\
                 \{9, 3, 5, 6, 3, 9, 8, 0, 3, 0, 3\},\
                 \{1, 2, 6, 9, 7, 3, 3, 3, 0, 4, 0\},\
                 { 5, 6, 7, 5, 3, 7, 6, 0, 4, 0, 8 },
                 \{7, 0, 6, 9, 8, 2, 6, 3, 0, 8, 0\},\
30.
```

```
{ 0, 9, 9, 8, 5, 9, 5, 1, 0, 5, 3, 6 },

{ 9, 0, 7, 4, 7, 5, 6, 6, 5, 8, 4, 3 },

{ 9, 7, 0, 2, 7, 7, 6, 5, 8, 0, 8, 1 },

{ 8, 4, 2, 0, 0, 9, 0, 9, 4, 0, 4, 8 },

{ 5, 7, 7, 0, 0, 0, 1, 1, 8, 9, 7, 5 },

{ 9, 5, 7, 9, 0, 0, 6, 5, 3, 2, 3, 7 },

{ 5, 6, 6, 0, 1, 6, 0, 5, 7, 5, 4, 4 },

{ 1, 6, 5, 9, 1, 5, 5, 0, 2, 2, 6, 2 },

{ 0, 5, 8, 4, 8, 3, 7, 2, 0, 3, 8, 1 },

{ 5, 8, 0, 0, 9, 2, 5, 2, 3, 0, 4, 7 },

{ 3, 4, 8, 4, 7, 3, 4, 6, 8, 4, 0, 6 },

{ 6, 3, 1, 8, 5, 7, 4, 2, 1, 7, 6, 0 },
```

Код 3.1. Обход в глубину и ширину графа, заданного с помощью матрицы смежности

```
#include <iostream>
using namespace std;
int main()
{
      // матрица смежности
      vector<vector<int> > mat =
      {
              \{0, 1, 2, 0, 0, 0, 0\},\
              \{1, 0, 2, 0, 0, 0, 0\},\
              {2, 2, 0, 4, 0, 0, 1},
              \{0, 0, 4, 0, 1, 2, 2\},\
              \{0, 0, 0, 1, 0, 1, 0\},\
              \{0, 0, 0, 2, 1, 0, 0\},\
              {0, 0, 1, 2, 0, 0, 0}
      };
      vector <int> used(7, 0);
      //0 - вершина не посещена при поиске, 1 - помещена в структуру данных для вершин,
      //но не обработана, 2 - обработана, смежные вершины помещены в структуру данных
      //DFS - поиск в глубину
      stack<int> Stack;
      int iter = 0;
      Stack.push(0); // помещаем в очередь первую вершину
      while (!Stack.empty())
```

```
{ // пока стек не пуст
       int node = Stack.top(); // извлекаем вершину
       Stack.pop();
       std::cout << "\nDFS at vertex " << node<< endl;</pre>
       if (used[node] == 2) continue;
       used[node] = 2; // отмечаем ее как посещенную
       iter++;
       for (int j = 0; j < 7; j++)
       { // проверяем для нее все смежные вершины
              if (mat[node][j] > 0 && used[j] != 2)
              { // если вершина смежная и не обнаружена
                     Stack.push(j); // добавляем ее в стек
                     used[j] = 1; // отмечаем вершину как обнаруженную
              }
       std::cout << node << endl; // выводим номер вершины
}
std::cout << "\nVisited vertices";</pre>
for (int i = 0; i < 7; i++) std::cout << used[i] << " ";
for (int i = 0; i < 7; i++)
       used[i] = 0;
queue<int> Queue;
//BFS - поиск в ширину
Queue.push(0);
                            //в качестве начальной вершины используем 0.
used[0] = 2;
vector <int> dist(7, 10000); //расстояния до вершин от 0-й в числе ребер
dist[0] = 0;
 iter = 0;
while (!Queue.empty())
       int node = Queue.front(); //извлекаем из очереди текущую вершину
       Queue.pop();
      //Здесь должна быть обработка текущей вершины.
       std::cout << "\nBFS at vertex " << node<< endl;</pre>
       if (used[node] == 2) continue;
             used[node] = 2;
       iter++;
       for (int j = 0; j < 7; j++)
       { // проверяем для нее все смежные вершины
              if (mat[node][j] > 0 && used[j] != 2)
              { // если вершина смежная и не обнаружена
                     Queue.push(j); // добавляем ее в очередь
                     used[j] = 1; // отмечаем вершину как обнаруженную
                     if (dist[j] > dist[node] + 1)
                            dist[j] = dist[node] + 1;
              }
      }
}
std::cout << "\nVisited vertices";</pre>
```

```
for (int i = 0; i < 7; i++) std::cout << used[i] << " ";
    std::cout << "\nDistances";
    for (int i = 0; i < 7; i++) std::cout << dist[i] << " ";

    char c; cin >> c;
    return 0;
}
```