WCET Analysis Lab: Assignment 1

Markus Klein Johannes Kasberger

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Problem 1

Recommended (3): As a warm-up exercise, follow the instruction in Timing Analysis Lab: First Steps

Q: How long does it take to execute simple once, according to measurements, and according to the static analysis?

Answer

• Measurements: 763 incl. function call - 70 overhead = 693 cycles

• Static analysis: 705 cycles

We used the compiler flag -O1.

The difference is 12 cycles so the measurement is not far away from the static analysis. After one run we measured 1018 cycles but after reflashing the target the result was 763 cycles again.

Problem 2

Recommended (3): Also extract the instruction trace as outlined in Timing Analysis Lab: First Steps. Then compare the number of cycles needed in one iteration of the loop, with the number of cycles aiT calculated.

Q: Do they coincide? What is the total number of cycles needed to execute simple according to the instruction trace buffer?

Answer

To number of cycles for one iteration we measured 77 cycles. The static analysis results in 77 cycles.

10162210	40001210	call = 0x400011a0	[40001210]
10162233	40001214	st %g1, [%l1]	$[40000000 \ 07735935]$
10162243	$400011\mathrm{a}0$	mov 42, %g3	$[0000002\mathrm{a}]$
10162253	$400011\mathrm{a}4$	mov = 0, $%g2$	[00000000]
1+2+1+1 =	5		

```
\%g3.
                                     1, \%g1
                                                             [0000002b]
10162263
            400011a8
                         add
10162273
            400011ac
                         add
                               \%g1,
                                     1, \%g1
                                                             [0000002\,\mathrm{c}]
10162283
            400011b0
                         add
                               \%g1,
                                     1, \%g1
                                                             [0000002d]
10162293
            400011b4
                         add
                               \%g1,
                                     1, \%g1
                                                             [0000002\,\mathrm{e}\,]
10162303
                               \%g1,
                                     1, \%g1
            400011b8
                         add
                                                             [0000002 f]
                                     1,
10162313
            400011 \,\mathrm{bc}
                         add
                               \%g1,
                                         \%g1
                                                             [00000030]
                               \%g1,
                                     1, \%g1
10162323
            400011c0
                         add
                                                             [00000031]
10162333
                         add
                               \%g1, 1, \%g3
                                                             [00000032]
            400011c4
                               \%g2, 1, \%g2
10162343
                         add
                                                             [00000001]
            400011c8
10162353
                               \%g2,
                                                             fffffff9]
            400011 \,\mathrm{cc}
                         cmp
                                     8
10162363
            400011d0
                         bne
                               0x400011a8
                                                             [4000125c]
10162373
            400011d4
                                                            [00000000]
                         nop
14
                               \%g3,
                                     1, \%g1
                                                            [00000033]
10162383
            400011a8
                         add
10162393
            400011ac
                         add
                               \%g1,
                                     1, \%g1
                                                             [00000034]
                               \%g1,
10162404
            400011b0
                         add
                                     1, \%g1
                                                             [00000035]
10162414
                               \%g1,
                                     1, \%g1
                                                             [00000036]
            400011b4
                         add
10162424
            400011b8
                         add
                               \%g1,
                                     1, \%g1
                                                             [00000037]
10162434
            400011 \, \mathrm{bc}
                               \%g1,
                                     1,
                                         \%g1
                                                             [00000038]
                         add
                               \%g1,
                                     1, \%g1
10162444
            400011c0
                                                             [00000039]
                         add
10162454
                               \%g1, 1, \%g3
            400011c4
                         add
                                                             [0000003a]
10162464
            400011c8
                         add
                               \%g2, 1, \%g2
                                                             [00000002]
10162474
            400011 \,\mathrm{cc}
                         cmp
                               \%g2,
                                     8
                                                             fffffffa
10162484
            400011d0
                               0x400011a8
                                                             [4000125c]
                         bne
10162494
            400011d4
                                                             [00000000]
                         nop
10162504
                               \%g3, 1, \%g1
                                                             [0000003b]
            400011a8
                         add
10162514
                               \%g1,
                                     1, \%g1
                                                             [0000003\,{
m c}\,]
            400011 ac
                         add
10162524
            400011b0
                         add
                               \%g1, 1, \%g1
                                                             [0000003d]
10162534
            400011b4
                         add
                               \%g1,
                                     1, \%g1
                                                             [0000003\,\mathrm{e}\,]
10162544
            400011b8
                         add
                               \%g1,
                                     1, \%g1
                                                             [0000003 f]
10162554
                               \%g1,
                                     1, \%g1
                                                             [00000040]
            400011 \, \mathrm{bc}
                         add
                                     1, \%g1
10162564
            400011c0
                         add
                               \%g1,
                                                             [00000041]
                                                             [00000042]
10162574
                               \%g1,
                                     1, \%g3
            400011c4
                         add
10162584
                               \%g2, 1, \%g2
                                                             [00000003]
            400011c8
                         add
10162594
            400011 \,\mathrm{cc}
                               \%g2, 8
                                                             fffffffb
                         cmp
10162604
            400011d0
                         bne
                               0x400011a8
                                                            [4000125c]
10162614
            400011d4
                                                             [00000000]
                         nop
                               \%g3, 1, \%g1
10162624
            400011a8
                         add
                                                             [00000043]
10162634
            400011ac
                               \%g1, 1, \%g1
                                                             [00000044]
                         add
10162644
                               \%g1,
                                     1, \%g1
            400011b0
                         add
                                                             [00000045]
                               \%g1.
                                     1, \%g1
                                                             [00000046]
10162654
            400011b4
                         add
10162664
            400011b8
                         add
                               \%g1,
                                     1, \%g1
                                                             [00000047]
                               \%g1,
10162674
            400011\,\mathrm{bc}
                         add
                                     1, \%g1
                                                             [00000048]
10162684
            400011c0
                         add
                               \%g1,
                                     1, \%g1
                                                            [00000049]
```

```
[0000004a]
            400011\,\mathrm{c}4
                              \%g1, 1, \%g3
10162694
                         add
10162704
            400011c8
                         add
                               \%g2, 1, \%g2
                                                             [00000004]
10162714
                              \%g2, 8
                                                             fffffffc
            400011 cc
                        cmp
10162724
            400011d0
                         bne
                               0x400011a8
                                                             [4000125c]
10162734
            400011d4
                                                            [00000000]
                         nop
10162744
                              \%g3, 1, \%g1
                                                            [0000004b]
            400011a8
                         add
                                     1,
                                        \%g1
10162754
            400011ac
                              \%g1,
                                                            [0000004\,\mathrm{c}]
                         add
10162764
                              \%g1,
                                     1, \%g1
            400011b0
                         add
                                                            [0000004d]
                                        \%g1
10162774
            400011b4
                         add
                               \%g1,
                                     1,
                                                            [0000004\,\mathrm{e}\,]
10162784
            400011b8
                         add
                              \%g1,
                                     1, \%g1
                                                            [0000004 f]
10162795
                              \%g1,
                                     1,
            400011 \,\mathrm{bc}
                         add
                                        \%g1
                                                             [00000050]
                               \%g1, 1, \%g1
10162805
            400011c0
                                                            [00000051]
                         add
10162815
                               \%g1, 1, \%g3
                                                            [00000052]
            400011c4
                         add
10162825
            400011\,\mathrm{c}8
                              \%g2, 1, \%g2
                                                            [00000005]
                         add
                               \%g2,
10162835
            400011 \,\mathrm{cc}
                                     8
                                                            [fffffffd]
                        cmp
10162845
                               0x400011a8
                                                             4000125c]
            400011d0
                         bne
10162855
            400011d4
                                                             [00000000]
                         nop
                              \%g3, 1, \%g1
10162865
            400011a8
                         add
                                                             [00000053]
                              \%g1,
10162875
                                     1, \%g1
                                                            [00000054]
            400011ac
                         add
10162885
            400011b0
                         add
                              \%g1,
                                     1, \%g1
                                                            [00000055]
10162895
            400011b4
                              \%g1,
                                     1,
                                        \%g1
                                                            [00000056]
                         add
                              \%g1,
                                     1, \%g1
10162905
            400011b8
                                                            [00000057]
                         add
                               \%g1,
                                     1,
                                        \%g1
10162915
            400011bc
                         add
                                                            [00000058]
10162925
            400011c0
                         add
                               \%g1,
                                     1, \%g1
                                                            [00000059]
                              \%g1, 1, \%g3
10162935
            400011c4
                         add
                                                             [0000005a]
10162945
            400011\,\mathrm{c}8
                              \%g2, 1, \%g2
                                                            [00000006]
                         add
10162955
            400011 \,\mathrm{cc}
                              \%g2, 8
                                                             fffffffe
                        cmp
10162965
                               0x400011a8
            400011d0
                         bne
                                                             [4000125\,\mathrm{c}\,]
10162975
            400011d4
                                                            [00000000]
                         nop
10162985
            400011a8
                         add
                               \%g3,
                                     1, \%g1
                                                            [0000005b]
10162995
            400011ac
                         add
                              \%g1, 1, \%g1
                                                            [0000005\,{
m c}\,]
10163005
            400011b0
                         add
                              \%g1,
                                     1, \%g1
                                                            [0000005d]
10163015
            400011b4
                               \%g1,
                                     1, \%g1
                         add
                                                            [0000005e]
                                     1, \%g1
10163025
            400011b8
                         add
                               \%g1,
                                                            [0000005 f]
10163035
                               \%g1,
                                     1,
                                        \%g1
                                                            [00000060]
            400011bc
                         add
10163045
                              \%g1.
                                     1. \%g1
                                                            [00000061]
            400011c0
                         add
10163055
            400011c4
                         add
                               \%g1, 1, \%g3
                                                             [00000062]
10163065
            400011c8
                         add
                              \%g2, 1, \%g2
                                                            [00000007]
10163075
            400011 \,\mathrm{cc}
                              \%g2,
                                     8
                                                             ffffffff]
                        cmp
                               0x400011a8
10163085
            400011d0
                         bne
                                                            [4000125c]
10163095
            400011d4
                                                            [00000000]
                         nop
                              \%g3, 1, \%g1
                                                            [00000063]
10163105
            400011a8
                         add
                              \%g1,
                                     1, \%g1
                                                            [00000064]
10163115
            400011ac
                         add
10163125
            400011b0
                         add
                              \%g1,
                                    1, \%g1
                                                             [00000065]
                              \%g1,
10163135
            400011b4
                         add
                                     1, \%g1
                                                            [00000066]
10163145
            400011b8
                         add
                              \%g1,
                                     1, \%g1
                                                            [00000067]
```

10163155	$400011\mathrm{bc}$	add	%g1, 1, %g1	[00000068]
10163165	$400011\mathrm{c}0$	add	%g1, 1, %g1	[00000069]
10163175	$400011\mathrm{c}4$	add	%g1, 1, %g3	[0000006a]
10163186	$400011\mathrm{c8}$	add	%g2, 1, $%g2$	[800000008]
10163196	$400011\mathrm{cc}$	cmp	%g2, 8	[00000000]
10163206	$400011\mathrm{d}0$	bne	0x400011a8	$[4000125\mathrm{c}]$
10163216	$400011\mathrm{d}4$	nop		[00000000]
8*14				-
10163228	$400011\mathrm{d}8$	retl		[400011d8]
1				

5 + 8 * 14 + 1

Just based on the number of instructions we calculated the number of cycles needed = 118 cycles. This is much shorter than the result of the static analysis. The reason for this is that we don't know the exact memory timing and the instruction decode takes more time.

Problem 3

Mandatory (4): First, create a project containing the files contained in the insertion sort folder of the task specification. Now complete the function main.c:run(), executing insertion sort a few times, with array size 32 and different input data. Measure the minimum and maximum time needed to execute the sort function.

Q: What were the results of the measurement? How many test sets would do you need to cover all possible execution path?

Answer

We used the compiler flag -Os.

Case	$oxed{measurement} [cycles]$
Best-case (pre sorted)	3659
Worst-case (upside down sorted)	44267
Average-case (unsorted)	24875

Problem 4

Mandatory (5): Add loop bounds and additional flow facts for insertion sort.c:insertion sort(), using the symbolic name @size for the size of the array to be sorted. Next, analyze the WCET of insertion sort, assuming an array size of 32. Keep the array size as a symbolic name (user register @size). Finally, write a test function which calls insertion sort more than once, with different array sizes (e.g., 16,32 and 64). Also repeat the static analysis with different array sizes.

Q: How many cycles do you need to execute insertion sort according to the static analysis?

Answer

The static analysis resulted in 74694 cycles.

Q: What results do you get for an array size of 8,16 or 64, using measurements and static analysis?

Answer

method	size 16[cycles]	size 32[cycles]	size 64[cycles]
measurement	11527	34579	132899
static	18232	77224	318088

Q: In addition to the size of the array, what other aspects of the input data might influence the WCET?

Answer

The structure of the data. For instance: The worst-case occurs when the input data is sorted upside down. The best-case occurs if the input data is already sorted.

Problem 5

Recommended (8 Points): Assume that your goal was to find out the WCET of task.c:task(). Before analyzing the execution time, you should answer a few basic questions about the input data for the monitoring task, and analyze the control flow on the source code level.

Q: What is the set of input data which might influence the execution time of the task at the software side?

Answer

If many samples are missing the interpolation of the data has big influence on the runtime. Most of the other loops just depend on the amount of samples used for calculation but this does not depend on the input data and is determined at compile time.

Q: Is it tractable to enumerate every possible input?

Answer

No it's not traceable. The result of the interpolation is dependent on the history of the last samples so enumerating the history and the inputs would require many differnt testcases.

Q: Which loops need to be bounded?

Answer

The loops we found are in the merge samples function.

Q: Add all loop bounds and flow facts you can find to the file task.c (as source code annotations).

Answer

```
\begin{array}{ll} \text{if} \; (! \; \text{IS\_VALUE\_MISSING}(x)) \\ \{ \end{array}
```

```
/* Only interpolate if we interpolate at most MAX_CONSECUTIVE_MISSING samples
int missing_samples = i - valid - 1;
if (missing_samples > 0 && missing_samples <= MAX_CONSECUTIVE_MISSING)
{
   /* TODO: loop bound */
   for (j = i-1; j > valid; --j)
        {
        /* At most once for each invalid input sample */
            /* TODO: flow fact */
            sample_value_t y = sample_buffer_get(sbuf,j);
            if (! IS_VALUE_MISSING(y)) break;
            y = iinterpolate16(valid, sample_buffer_get(sbuf, valid), i, x, j);
            sample_buffer_set(sbuf,j, y);
        }
}
valid = i;
```

Problem 6

Recommended (8 Points): Analyze the fft() function called in task.c. Try to find loop bounds for the Fast Fourier Transform implementation (fixedpoint.c:fp radix2fft with-scaling) first. If you have difficulties finding them, add a debug statement and run the transform with different input data sizes. Add flow constraints relating the execution frequency of the inner loops with the functions execution frequency. Finally, try to analyze the execution time using aiT. There is already a timing measurement for the fft in the executable, so it is easy to compare the number of cycles estimated to execute the function.

Q: Compare the worst-case number of iterations for the inner loop with and without using these flow constraints. Finally, think about the complexity of calculating loop bounds for FFT.

Answer

Comparison static analysis with measurement:

type	cycles
measurement	178807
static with flow constraints	160344

 $Comparison \ of inner \ loop \ in \ fp \ radix 2 fft \ with scaling \ with/without \ flow \ constraints:$

	type
	static without flow
Ì	static with flow c

Q: Does the FFT loop bound depend on the input data?

Answer

It just depends on the ammount of the input data and not the data itself.

Problem 7

Optional Challenge (5 Bonus Points): Try to analyze the WCET of task.c:task() using

aiT. If you attempt to solve this challenge, use the control flow graph and disassembling capabilities of aiT, and be sure to understand the source code you are analyzing.

Problem 8

Mandatory (4): Answer the following questions

Q: How much time did you spend writing annotations and analyzing the code? Was it less or more than you expected? How much time did you spend on this first assignment?

Answer

- Mandatory Part: 6 hours
- Recommended Part:

Q: What is the ratio between observed and actual execution time? Discuss the causes of the overestimation.

Answer

Q: As you learned, sometimes it is necessary to annotate the assembler code. Why? What problems can you see because of this?

Answer