

# On the Art of Establishing Correspondence

**Jiri Matas**



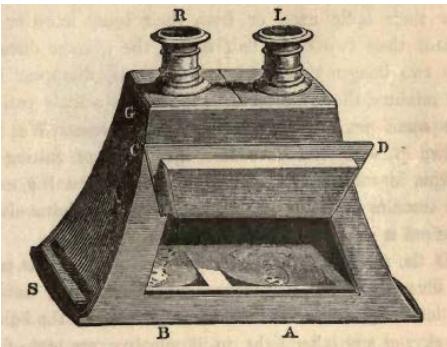
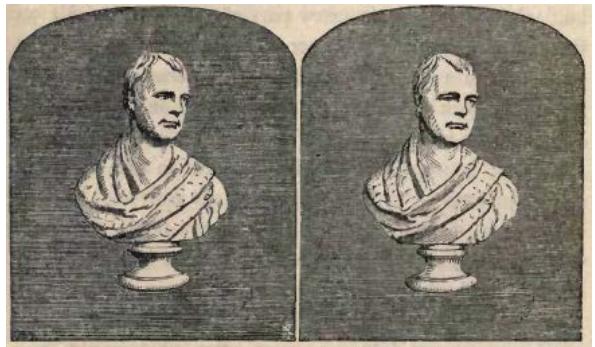
Presentation prepared with  
**Dmytro Mishkin**



Visual Recognition Group  
Center for Machine Perception  
Czech Technical University in Prague  
<http://cmp.felk.cvut.cz>



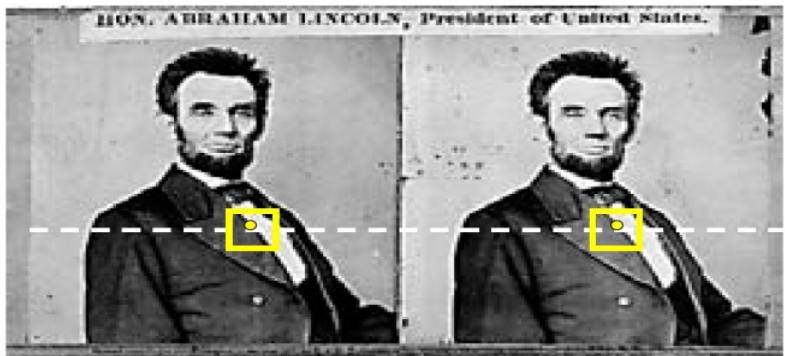
# Correspondence in Stereoscopic Images



Brewster  
Stereoscope, 1856

A “photo” for  
each eyes

Correspondence established by the human visual system.



Correspondence by classical narrow-baseline stereo methods,  
e.g. Cox 1996

# Correspondence Problems



Given images A and B, find a geometric model linking them and a set of features consistent with the model.

# Correspondence Problems



Given images A and B, find a geometric model linking them.

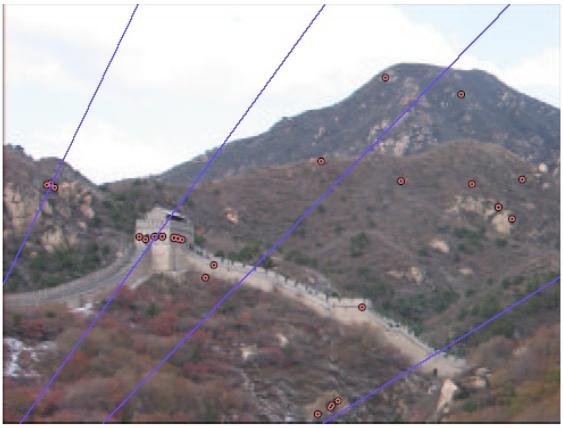
Given images A and B, and a geometric model linking them ( $F, E, H$ ), estimate reliably the confidence that the model is correct.

If images A and B are geometrically unrelated, establish fast and with high confidence this fact.

Given a set of  $n$  images  $A_i$ , select a subset of pairs that are geometrically related much faster than in time proportional to  $n^2$ .

(Registration) Given images A and B and an approximation of the geometric model linking them ( $F, E, H$ ), find the highest precision model.

## Widening of the baseline, zooming in/out, rotation



Standard approach:

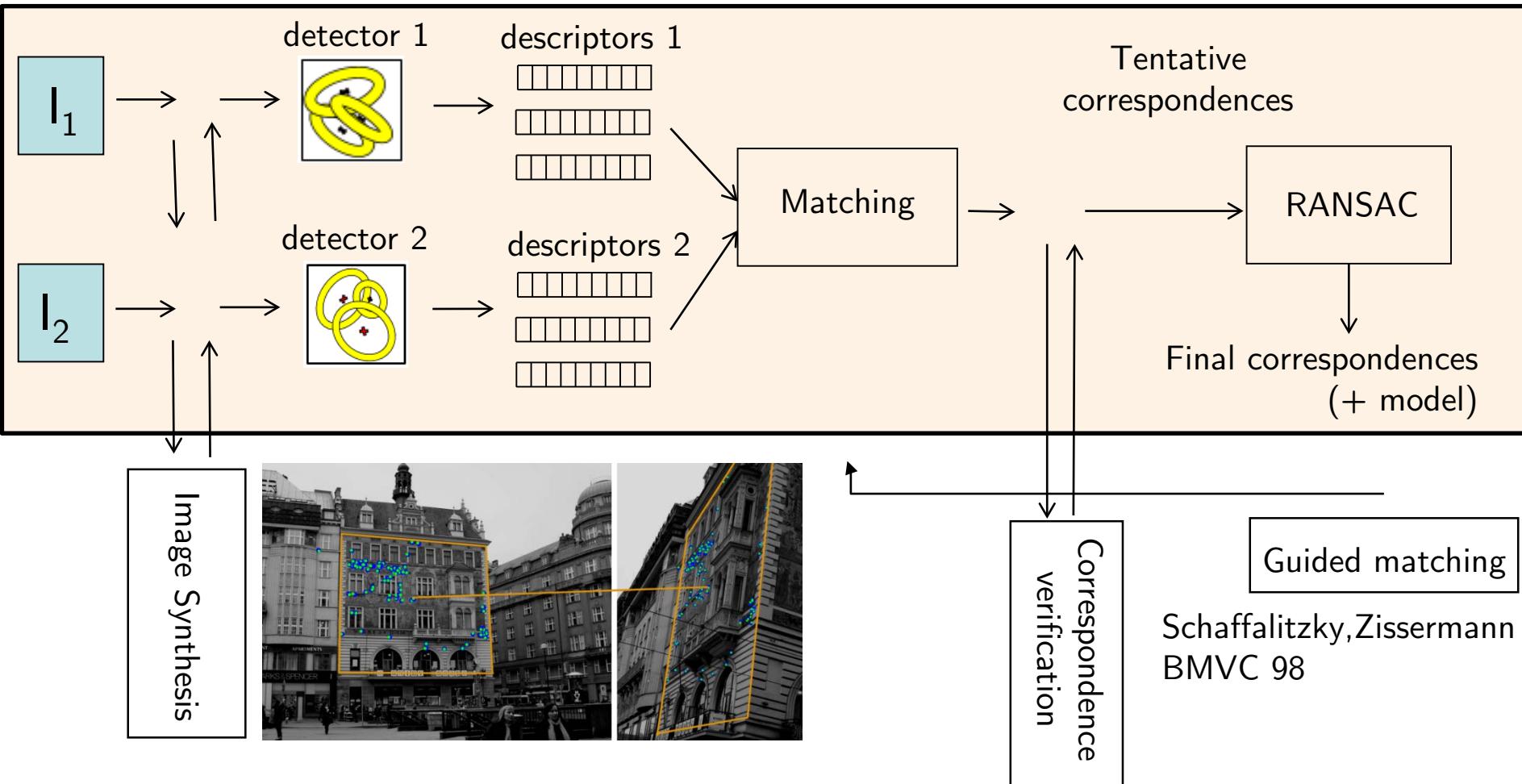
D. Lowe, 2000, SIFT



Also:

Mikolajczyk & Schmid,  
Tuytelaars & van Gool,  
Matas et al. and many  
other

# Classical Two-view Correspondence Pipeline

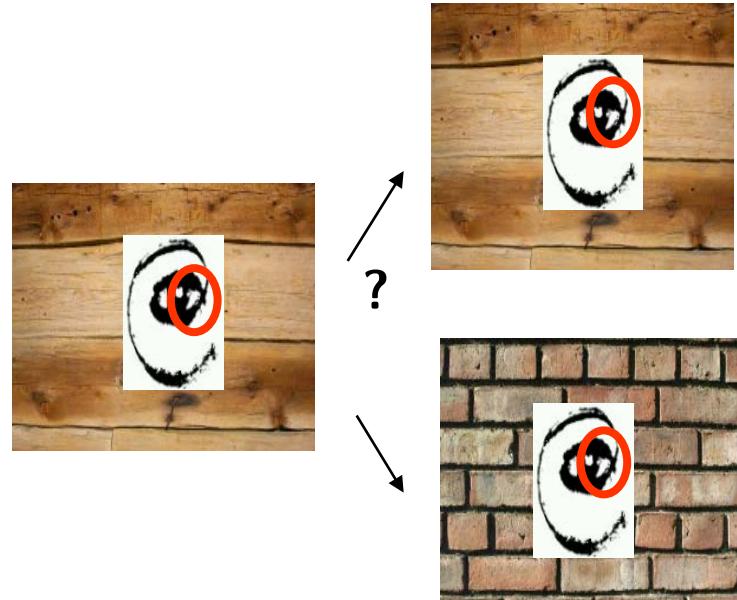


Morel, Yu: ASIFT: A New Framework for Fully Affine Invariant Image Comparison. SIAM JIS 2009  
Mishkin, MODS: Fast and robust method for two-view matching. CVIU 2015

- Difficult matching problems:
  - Rich 3D structure with many occlusions
  - Small overlap
  - Image quality and noise
  - (Repetitive patterns)



measurement region too large

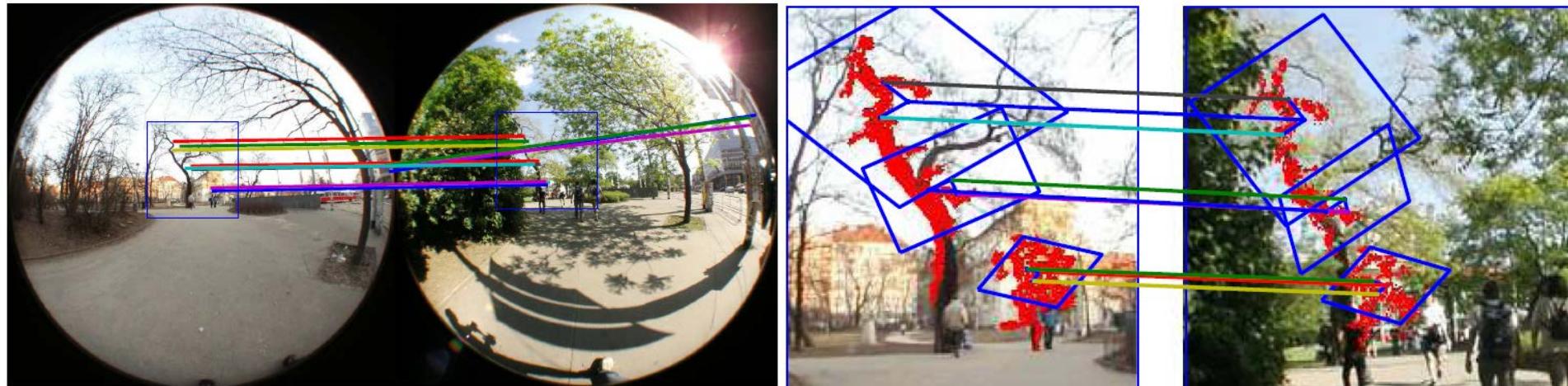


measurement region too small

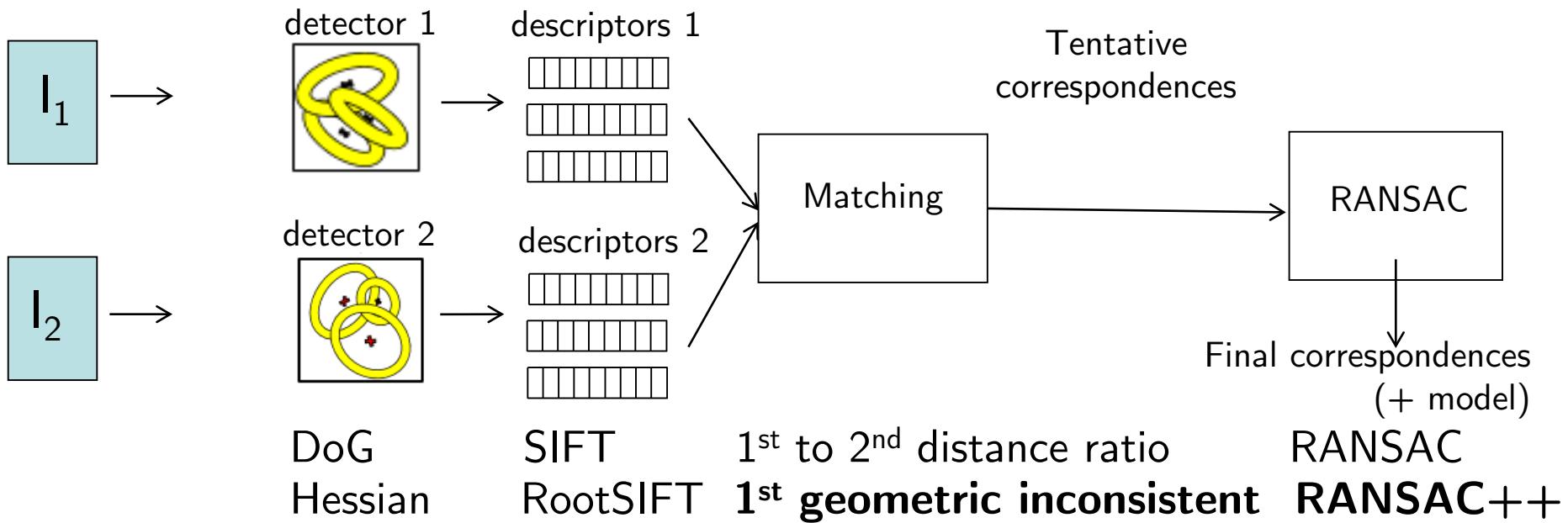
# Correspondence Verification by Co-segmentation



- high discriminability
  - significantly outperforms a standard selection process based SIFT-ratio
- very fast (0.5 sec / 1000 correspondences)
- always applicable before RANSAC
- the process generating tentative correspondences can be much more permissive
  - 99% of outliers not a problem, correct correspondences recovered
  - higher number of correct correspondences



# Classical Two-view Correspondence Pipeline



1<sup>st</sup> Geometrically Inconsistent Constraint  
[Mishkin et al., Two-View Matching with View Synthesis Revisited. IVCNZ 2013]  
(rediscovered: in [Sarlin et.al, CVPR 2019])

similar constraints used for training descriptors:  
SuperPoint (CVPRW 2018), D2Net (CVPR 2019), RFNet (arXiv 2019, called “neighbor mask”)

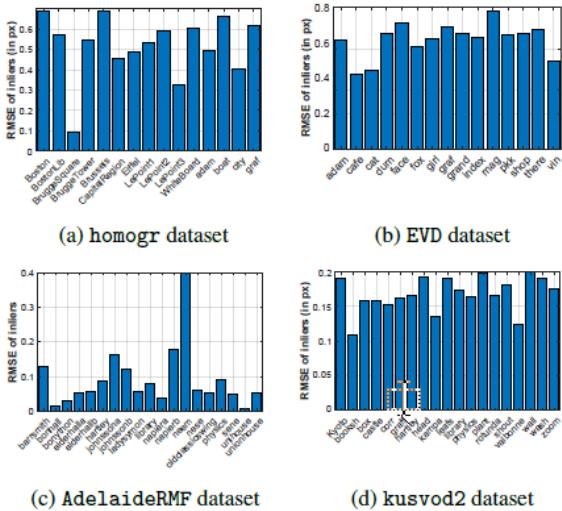


Idea: do not require the user to provide the scale.

The optimal one is different for every problem.

**Marginalize:** the result is a weighted average over a range of  $\sigma$ , weighted by the log-likelihood for the mode.

		[1] a	$+ \sigma$	[1] b	$+ \sigma$	[2]	[3]	MAGSAC
H – homography, F – fundamental m., E – essential m.	(1) F	0.56	0.52	0.58	0.50	1.01	0.63	<b>0.38</b>
	(2) F	0.28	<b>0.27</b>	0.31	0.31	0.33	0.46	0.30
	(4) F	0.53	0.52	0.50	0.50	0.58	0.72	<b>0.47</b>
	(5) H	3.39	2.13	3.53	2.19	2.95	1.83	<b>1.37</b>
	(6) H	5.42	4.07	4.78	3.55	4.55	5.05	<b>1.76</b>
	(3) E	9.61	9.48	10.62	10.23	10.17	15.56	<b>6.51</b>
	(all)	3.30	2.83	3.39	2.88	3.27	4.04	<b>1.80</b>
	(1) F	25	25	<b>17</b>	<b>17</b>	<b>17</b>	55	31
	(2) F	393	394	<b>380</b>	<b>380</b>	<b>380</b>	447	939
	(3) F	132	140	119	128	126	<b>46</b>	467
	(4) H	71	72	64	65	65	<b>37</b>	131
	(5) H	367	369	353	356	355	291	<b>162</b>
	(6) E	2 548	2 549	2 535	2 537	2 536	4 637	<b>2 398</b>
	(all)	589	592	<b>578</b>	581	580	921	688
	(1) F	0.06	0.06	0.06	0.06	0.06	0.06	<b>0.00</b>
	(2) F	<b>0.00</b>						
	(3) F	<b>0.00</b>						
	(4) H	0.12	0.12	0.12	0.12	0.12	<b>0.00</b>	0.06
	(5) H	0.57	0.50	0.57	0.43	0.53	0.33	<b>0.29</b>
	(6) E	0.27	0.22	0.26	0.22	0.24	0.23	<b>0.00</b>
	(all)	0.18	0.15	0.16	0.14	0.16	0.10	<b>0.03</b>



[1]a – LO-RANSAC

[1]b – LO-MSAC

[2] – LO-RANSAAC

[3] – AC-RANSAC

## Distribution assumptions:

- Outliers are uniformly distributed ( $\sim \mathcal{U}(0, l)$ )

Typically, the inlier residuals are calculated as the Euclidian-distance from the model in a  $\rho$ -dimensional space. Thus,

- the inliers residuals have chi-square distribution

Likelihood of model  $\theta$  given  $\sigma$ :

$$L(\theta | \sigma) = \frac{1}{l^{|x|-|I(\sigma)|}} \prod_{x \in I(\sigma)} \left[ 2C(p)\sigma^{-p} D^{p-1}(\theta, x) \exp \frac{-D^2(\theta, x)}{2\sigma^2} \right]$$

Distance function

Comes from the outlier distribution      Set of inliers which  $\sigma$  implies      Comes from the inliers' distribution

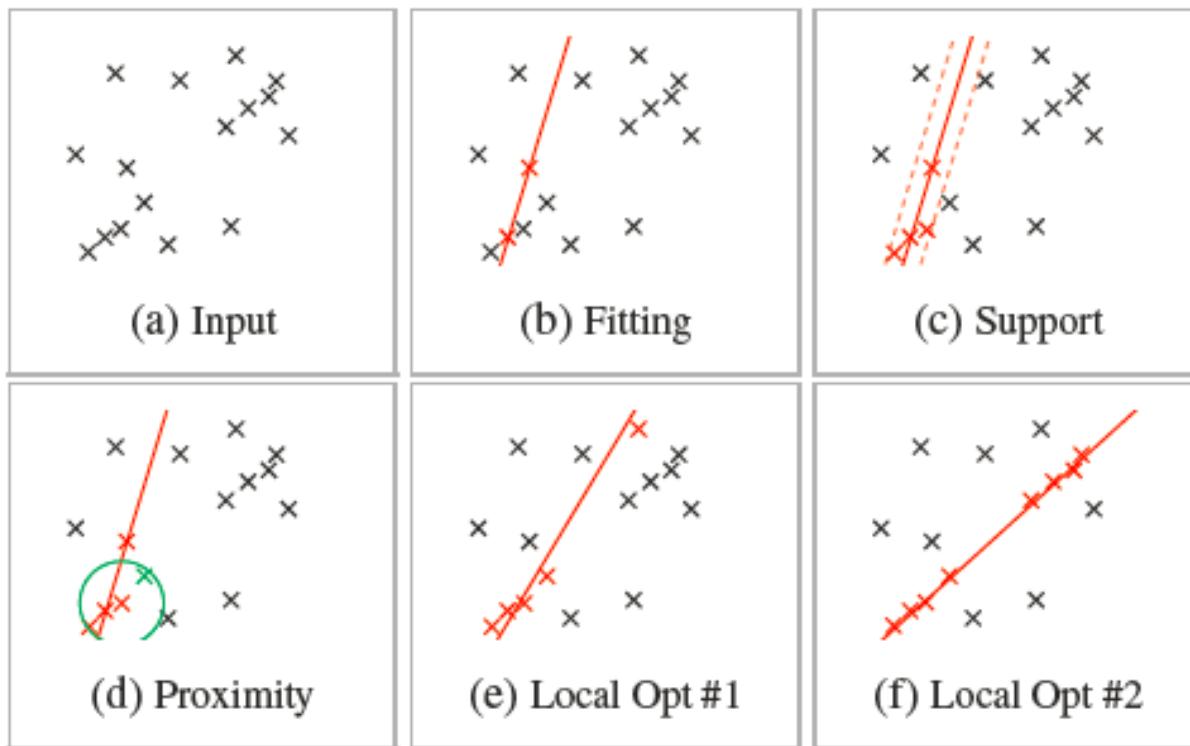


Figure 1: The proposed graph-cut based local optimization converging from a “not-all-inlier” sample, i.e. it is contaminated by an outlier, to the desired model. (a) The input data points, (b) RANSAC-like sampling and model fitting, (c) computation of model support, e.g. counting the inliers, (d) considering spatial proximity by graph-cut, (e-f) iterated local optimization using least-squares fitting and graph-cut.

# GC RANSAC - Performance

		Confidence 95%						
		RSC	PSC	PSCd	FLO	SPRT	GC	P-NSC
	$\mathcal{E}$	1.3 ± 0.0	1.4 ± 0.4	1.6 ± 0.2	0.88 ± 0.3	1.2 ± 0.3	0.8 ± 0.4	0.8 ± 0.2
	$\mathcal{T}$	0.9 ± 0.2	0.5 ± 0.1	0.8 ± 0.2	1.6 ± 0.5	1.1 ± 0.15	2.8 ± 0.7	3.1 ± 0.3
	$\mathcal{S}$	34.2 ± 1.0	14.8 ± 1.1	23.2 ± 6.2	30.3 ± 5.2	69.9 ± 5.7	29.9 ± 9.5	19.1 ± 6.1
	$\mathcal{E}$	2.5 ± 2.1	7.9 ± 5.1	9.8 ± 6.7	1.8 ± 1.7	6.5 ± 6.3	0.7 ± 0.2	4.2 ± 2.3
	$\mathcal{T}$	7.1 ± 3.9	0.8 ± 0.2	0.9 ± 0.4	6.2 ± 1.6	5.1 ± 1.7	7.8 ± 1.7	8.1 ± 3.3
	$\mathcal{S}$	113.7 ± 65.2	5.6 ± 2.7	4.6 ± 2.9	59.6 ± 46.3	229 ± 123	37.8 ± 26.8	69.7 ± 39.6
	$\mathcal{E}$	2.3 ± 0.6	4.3 ± 0.9	3.1 ± 0.9	1.3 ± 1.1	2.4 ± 0.6	0.35 ± 0	2.4 ± 0.6
	$\mathcal{T}$	17.8 ± 7.9	4.9 ± 2.1	4.6 ± 1.1	16.7 ± 5.9	13.2 ± 5.2	18.3 ± 5.5	13.7 ± 5.2
	$\mathcal{S}$	39.7 ± 17.2	12.1 ± 5.33	10 ± 2.2	33.5 ± 13	36.6 ± 19.8	33.3 ± 29.5	26.4 ± 13.5

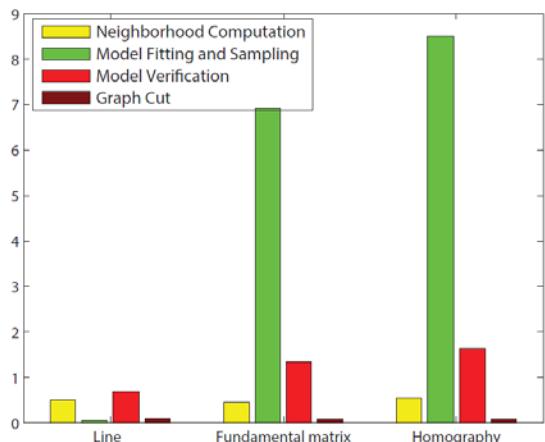
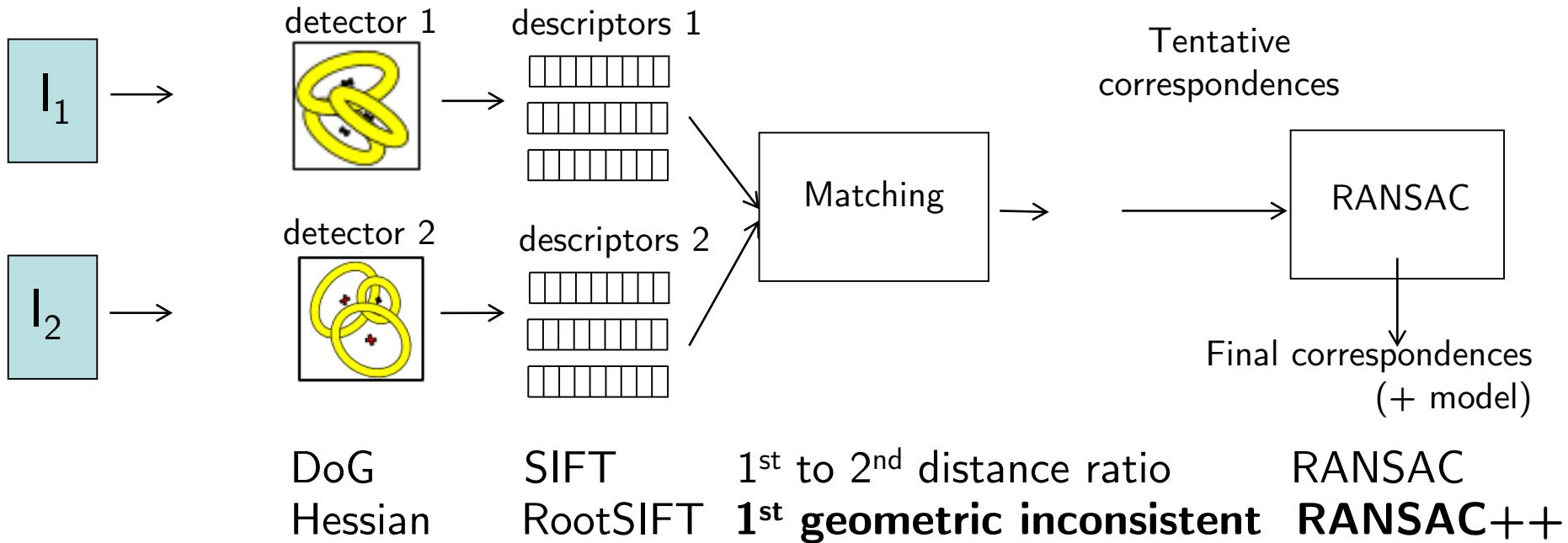


Figure 7: The breakdown of the processing times in milliseconds. Computed as the mean of all tests. *Best viewed in color.*

# Is Classical Two-view Pipeline Dead? Dying?



- Learnt descriptors superior: HardNet, ContextDesc; but that does not change the pipeline
- Detection and description learnt together, possibly also the metric for matching: SuperPoint, D2Net have superior results
- RANSAC-like differential methods for end-to-end pipelines:
  - Ranftl and Koltun, Deep Fundamental Matrix Estimation, ECCV 2018
  - Brachmann, PhD thesis, 2018

D. DeTone, T. Malisiewicz, A. Rabinovich:  
SuperPoint: Self-Supervised Interest Point Detection and  
Description. CoRR abs/1712.07629 (2017):

*Convolutional neural networks have been shown to be  
superior to hand-engineered representations on almost all  
tasks requiring images as input.*

# The Classical Pipeline: what is the verdict of the Image Matching: Local Features & Beyond CVPR 2019 Workshop Challenge?

We appreciate the collaboration of the organizers.

Big thank you goes to:

Eduard Trulls [trulls@google.com](mailto:trulls@google.com)

Kwang Moo Yi [kyi@uvic.ca](mailto:kyi@uvic.ca)

Thanks to the authors of:

- COLMAP who made this type of challenge possible
  - Johannes Schönberger, Jan-Michael Frahm
- Challenge Contributors that provided their results to us
  - Mihai Dusmanu (D2Net)
  - Zixin LUO (ContextDesc)
  - Daniel DeTone (SuperPoint)

Stereo best mAP15: 8%

SfM best mAP15: 73%

Why? Seems that something is wrong? Plus SfM seems simpler!

## [P1] Phototourism dataset – Stereo task

Performance in stereo matching, averaged over all the test sequences.

- [Click here for a breakdown by sequence](#)

Stereo – averaged over all sequences									
Method	Date	Type	#kp	MS	mAP <sup>5°</sup>	mAP <sup>10°</sup>	mAP <sup>15°</sup>	mAP <sup>20°</sup>	mAP <sup>25°</sup>
(+) SIFT + ContextDesc + Inlier Classification V2 kp:8000, match:custom	19-05-28	F/M	7515.2	0.3633	0.0016	0.0217	0.0823	0.1818	0.2963

## [P2] Phototourism dataset – Multi-view task

Performance in SfM reconstruction, averaged over all the test sequences.

- [Click here for a breakdown by sequence](#)
- [Click here for a breakdown by subset size](#)

MVS – averaged over all sequences												
Method	Date	Type	lms (%)	#Pts	SR	TL	mAP <sup>5°</sup>	mAP <sup>10°</sup>	mAP <sup>15°</sup>	mAP <sup>20°</sup>	mAP <sup>25°</sup>	ATE
(+) SIFT + ContextDesc + Inlier Classification V2 kp:8000, match:custom	19-05-28	F/M	98.6	6126.0	97.5	3.44	0.5755	0.6830	0.7389	0.7750	0.8006	—

## Examples of image pairs – nothing super difficult

Q



map5



map10



map15



map 25



# Examples of image pairs

Q



map5



map10



map15



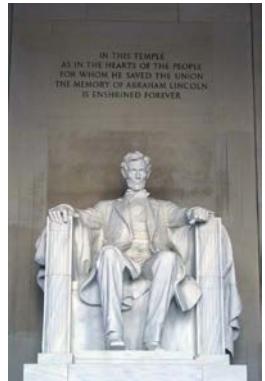
map 25



# Examples of image pairs

Q

map5



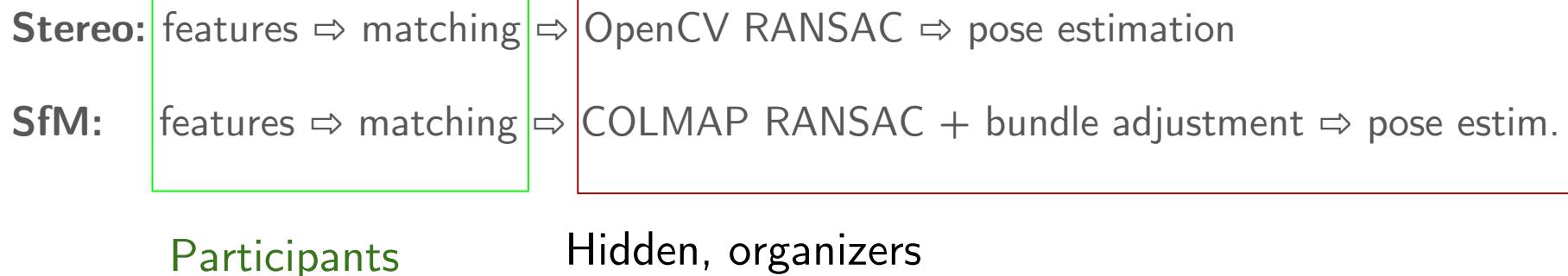
map10



map 35



# What are the differences in Stereo vs. SfM evaluation?



Seems that there is a problem with RANSAC or its parameters.  
(not visible nor tunable by participants)

# Our changes in camera pose estimation in evaluation

**Before:** normalize keypoints by K  
and run

RansacE (threshold hard to interpret)

```
def normalize_keypoints(keypoints, image_shape, K):
    C_x = (image_shape[1] - 1.0) * 0.5
    C_y = (image_shape[0] - 1.0) * 0.5
    # Correct coordinates using K
    C_x += K[0, 2]
    C_y += K[1, 2]
    f_x = K[0, 0]
    f_y = K[1, 1]
    keypoints = (keypoints - np.array([[C_x, C_y]])) / np.array([[f_x, f_y]])

    return keypoints
```

```
def eval_decompose():
    ...
    kp1 = normalize_keypoints(kp1, img1_shp, calc1["K"])
    kp2 = normalize_keypoints(kp2, img2_shp, calc2["K"])
    E, mask_new = cv2.findEssentialMat(
        kp1, kp2, method=method, threshold=0.01)
    ...

```

**After:** run RansacF (threshold in pixels)  
get E from F by formula  $E = K' F K$

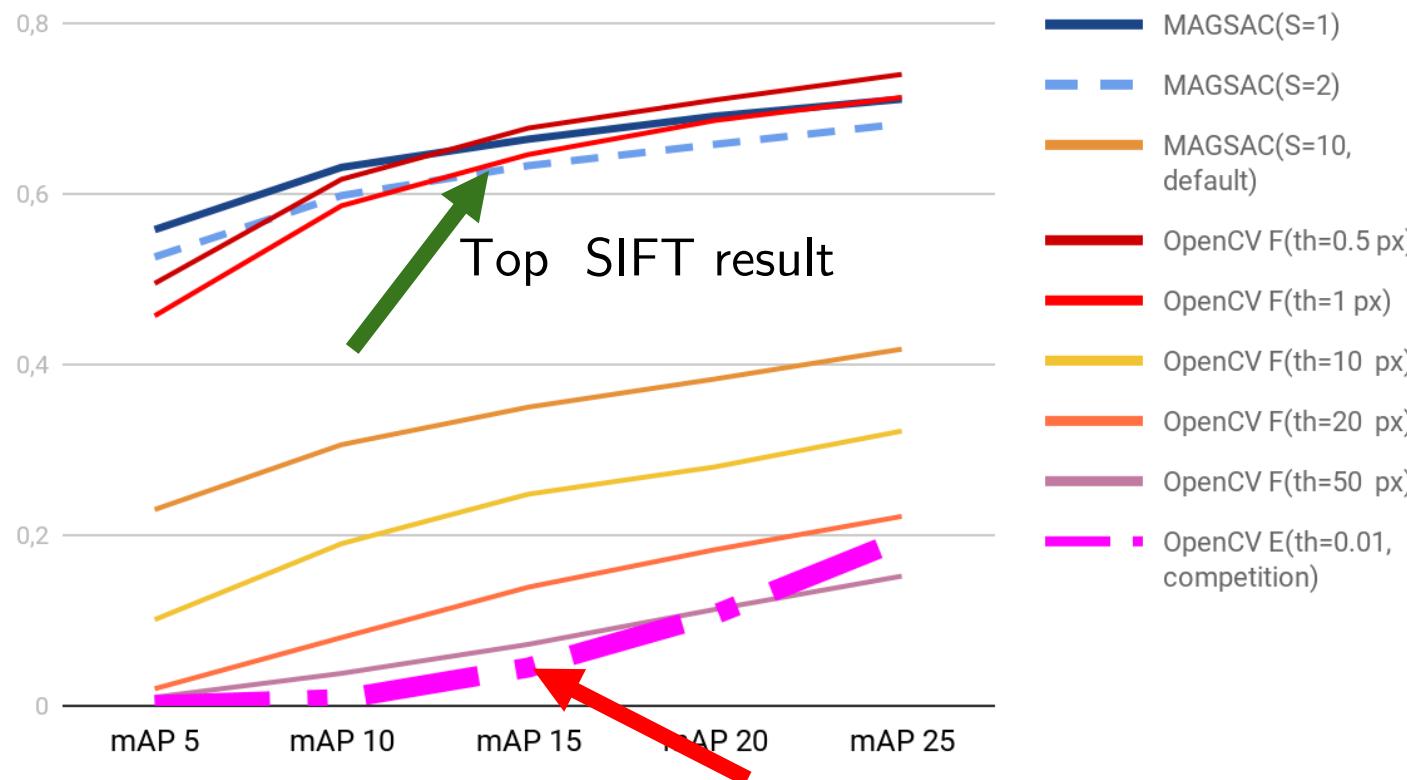
```
def eval_decompose_F():
    ...
    F, mask_new = cv2.findFundamentalMat(
        kp1, kp2, method, 1.0, 0.99)
    E = np.matmul(np.matmul(K2.T, F), K1)
```

$$K = [[866, 0, 505.5], [0, 866, 379], [0, 0, 1]]$$

$$\det(K)^{1/3} = 58$$

# Pose precision, recovered by the competition procedure for SIFTs – The OpenCV detector and descriptor

stereo mAP, reichstag seq, OpenCV SIFT feats, SNN = 0.8

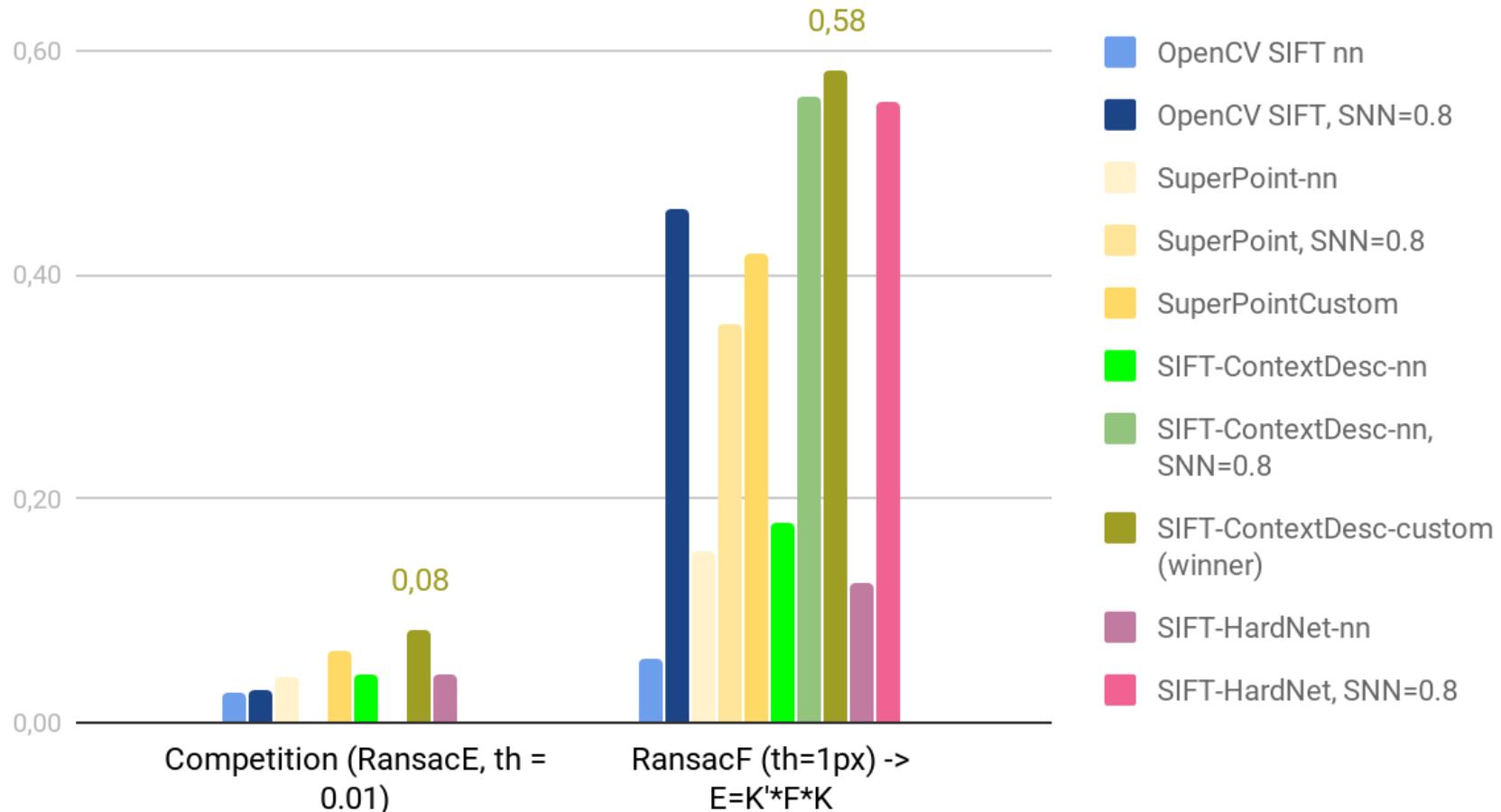


# Re-evaluated results: everyone benefits

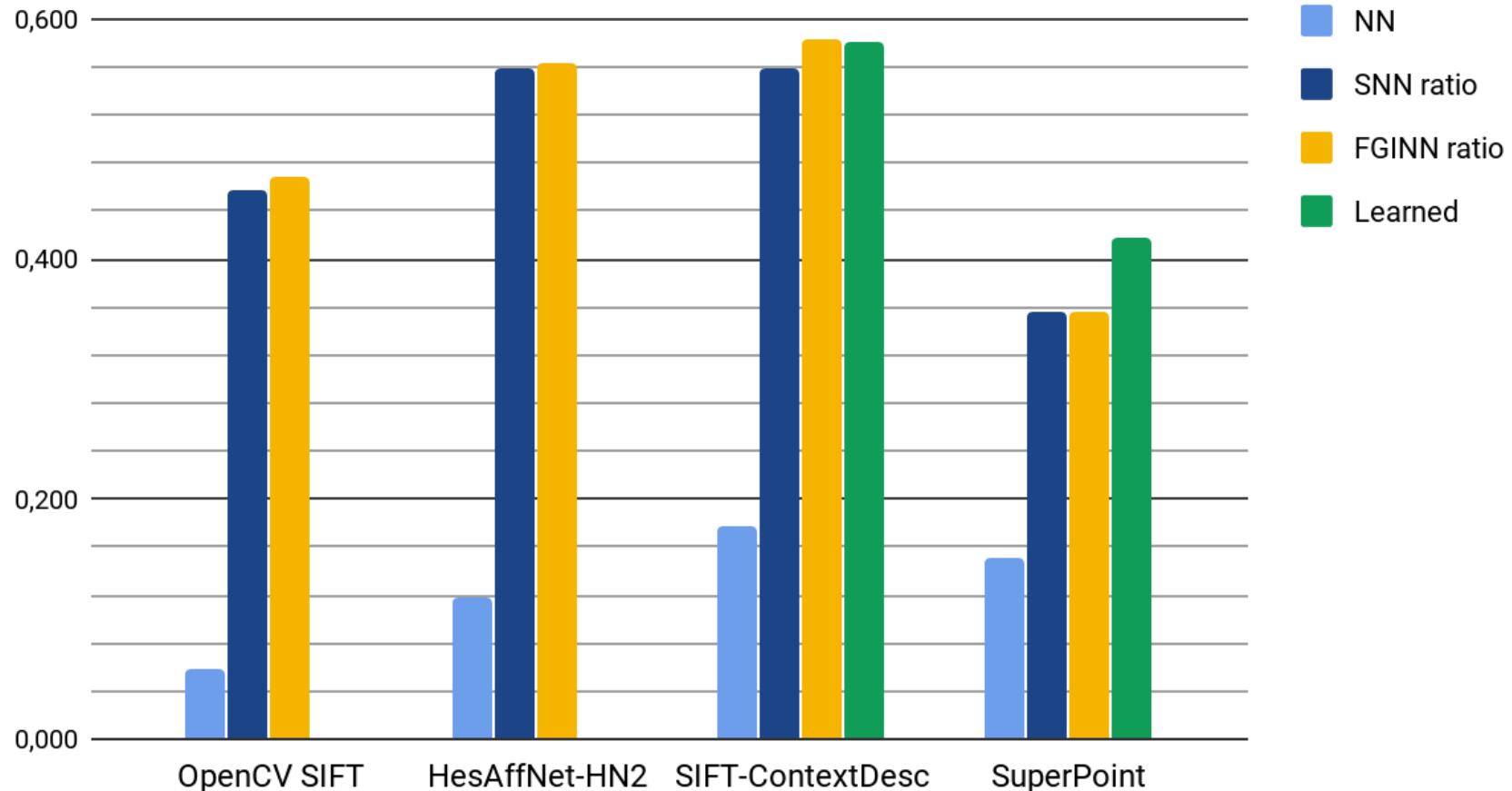


- Winner is the same,
- Ratio test is super important
- SIFT > SuperPoint now.
- HardNet is a strong baseline

mAP 15°, stereo, all seq



## stereo mAP 15, all seqs, RansacF (th=1px)

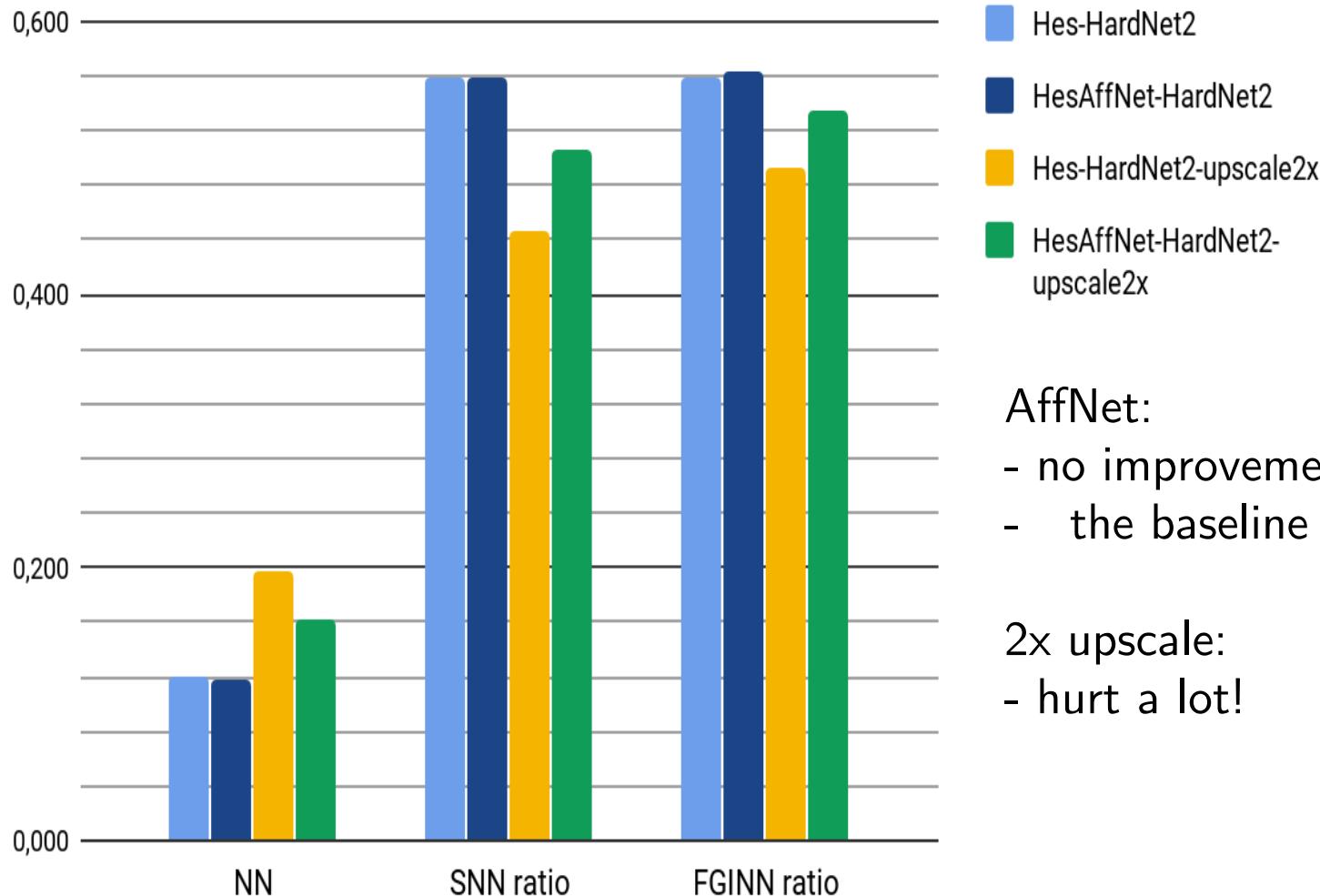


### Learned

Moo Yi, Trulls, Ono, Lepetit, Salzmann, Fua:  
Learning to Find Good Correspondences, CVPR 2018

# CMP Lessons: Does AffNet help?

stereo mAP 15, all seqs, RansacF (th=1px)



AffNet:

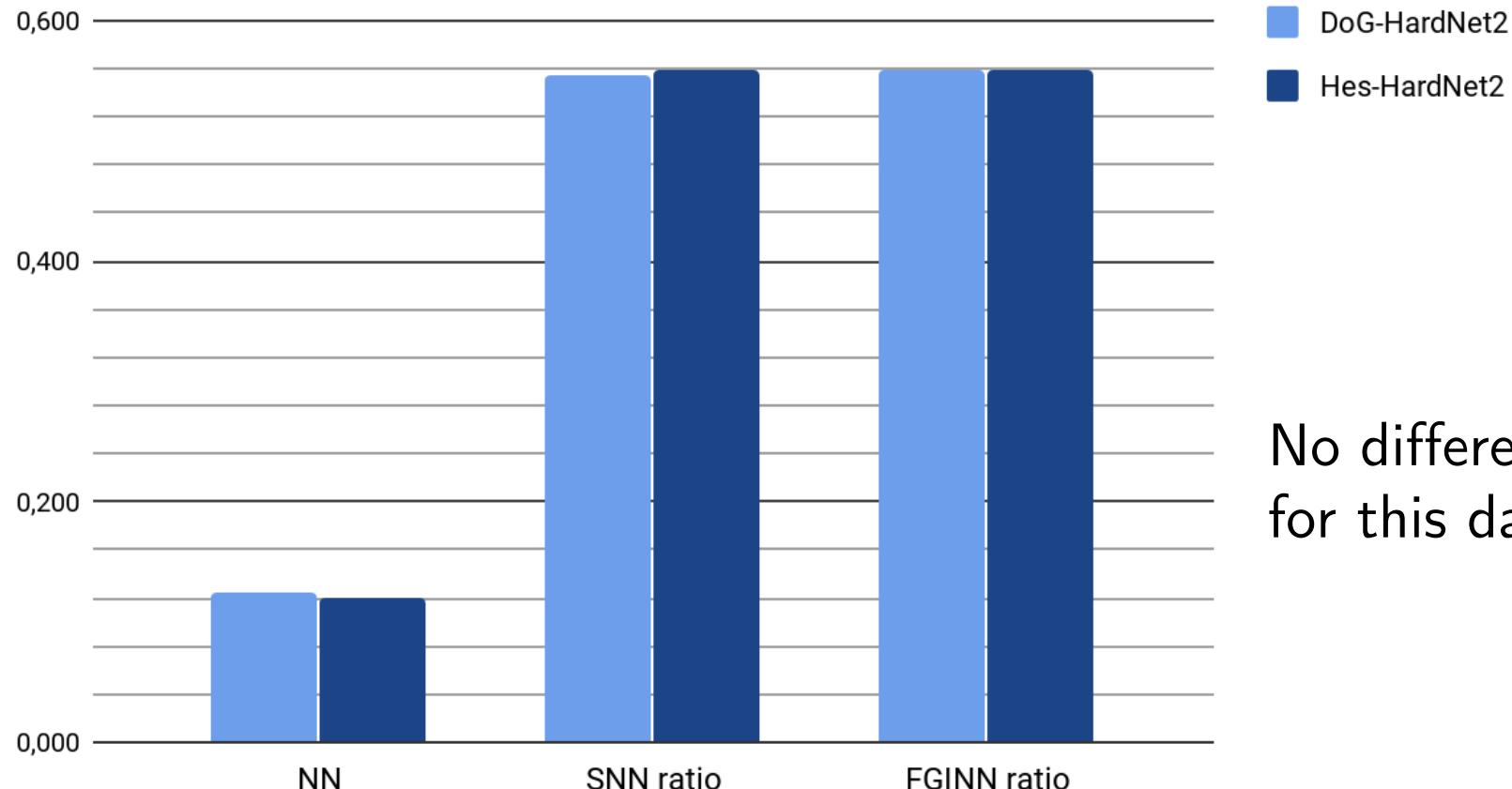
- no improvement, no loss
- the baseline is narrow here

2x upscale:

- hurt a lot!

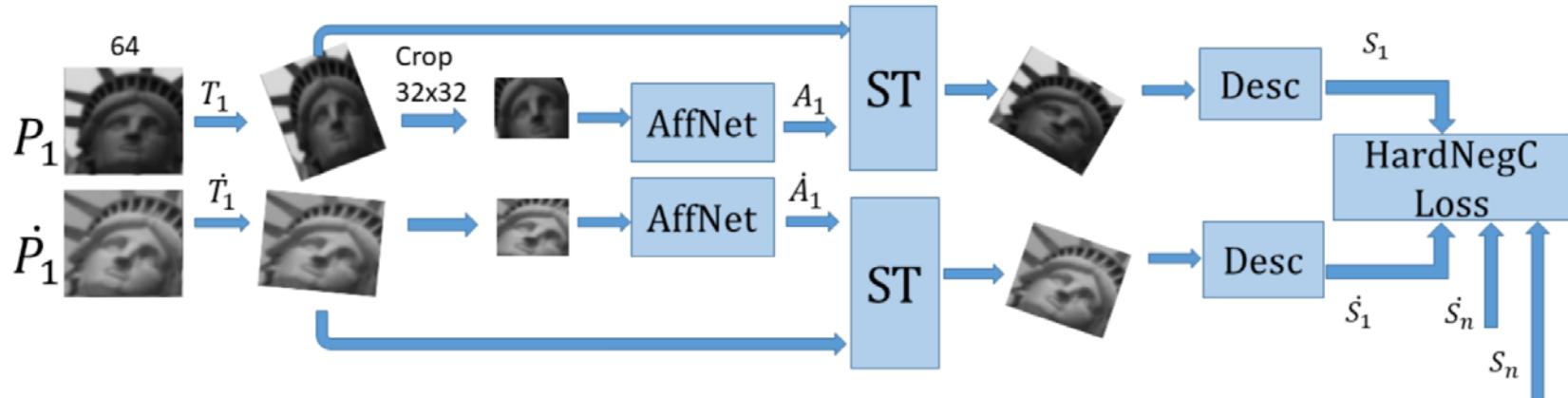
# CMP Lessons: Does Hessian vs DoG (SIFT) help?

stereo mAP 15, all seqs, RansacF (th=1px)



No difference  
for this dataset

# AffNet: learning measurement region

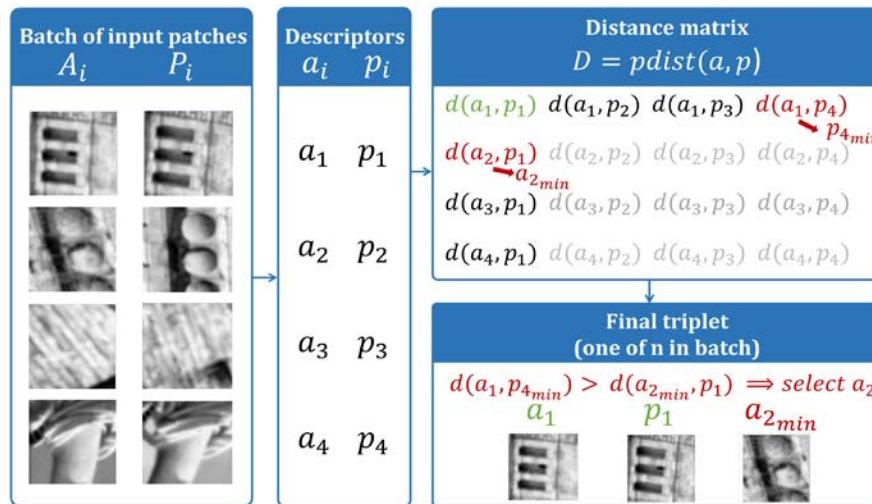


**Fig. 5.** AffNet training. Corresponding patches undergo random affine transformation  $T_i, \dot{T}_i$ , are cropped and fed into AffNet, which outputs affine transformation  $A_i, \dot{A}_i$  to an unknown canonical shape. ST – the spatial transformer warps the patch into an estimated canonical shape. The patch is described by a differentiable CNN descriptor.  $n \times n$  descriptor distance matrix is calculated and used to form triplets, according to the HardNegC loss.

$$L = \frac{1}{n} \sum_{i=1,n} \max (0, 1 + d(s_i, \dot{s}_i) - d(s_i, N)), \quad \boxed{\frac{\partial L}{\partial N} := 0,}$$

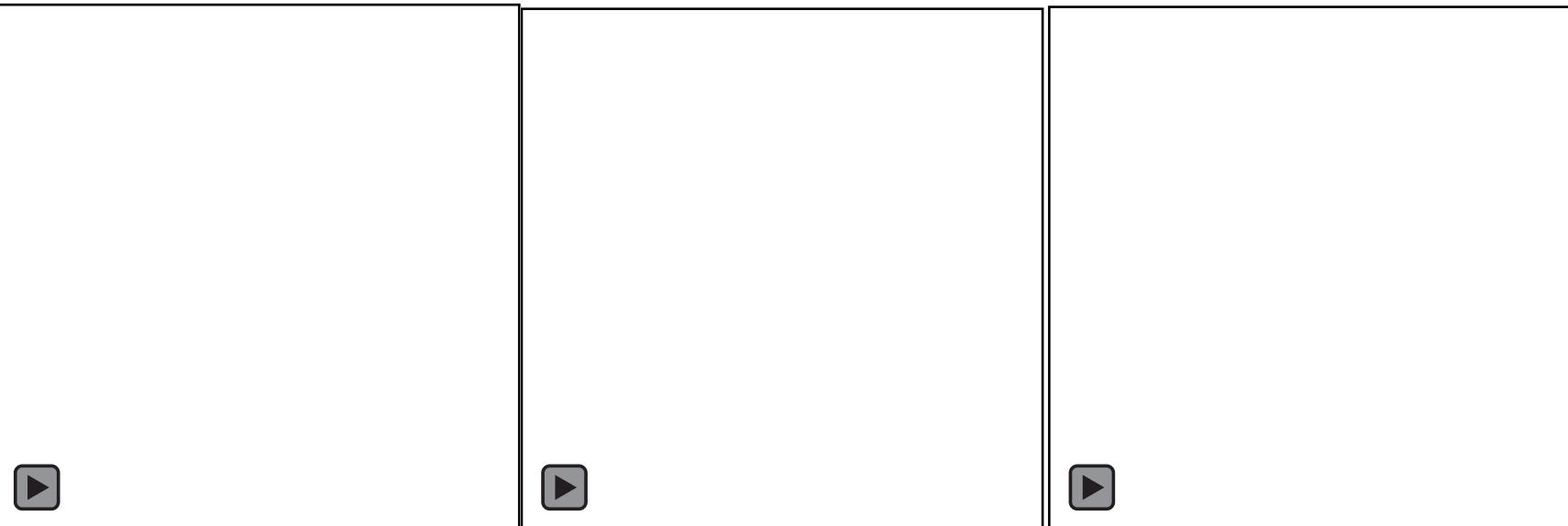
Mishkin et.al. Repeatability Is Not Enough: Learning Affine Regions via Discriminability.  
ECCV 2018

# HardNegC loss: treat negative example as constant



$$L = \frac{1}{n} \sum_{i=1,n} \max(0, 1 + d(s_i, \dot{s}_i) - d(s_i, N)), \quad \frac{\partial L}{\partial N} := 0,$$

# Why HardNegC loss is needed?

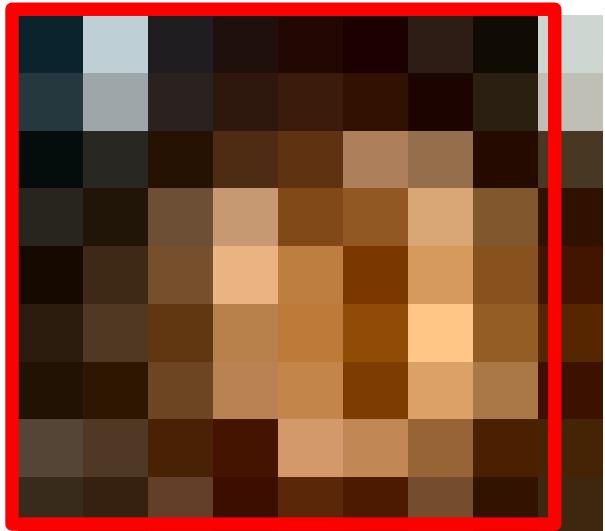


# Lessons Learned from the CMP IMW Submission:

- Good and properly set RANSAC is extremely important
- Neither SNN ratio test, nor good RANSAC working on its own
- SNN + good RANSAC is a powerful combination
- FGINN > SNN, use it
- Learning to match gives a moderate boost over SNN
- DoG/Hessian + HardNet + FGINN is very competitive and simple baseline
- AffNet doesn't harm, potentially helps for difficult to connect image

# The Correspondence Problem - Challenges

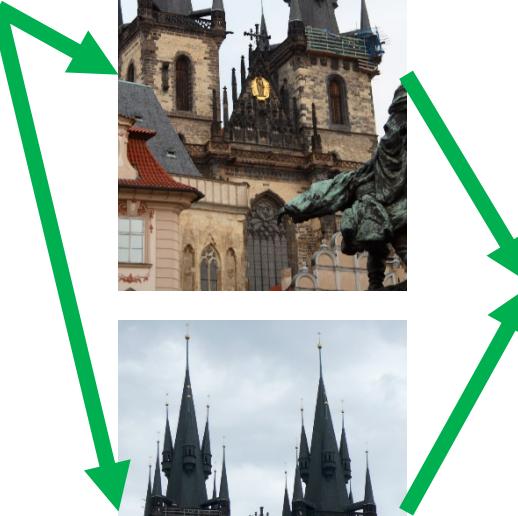
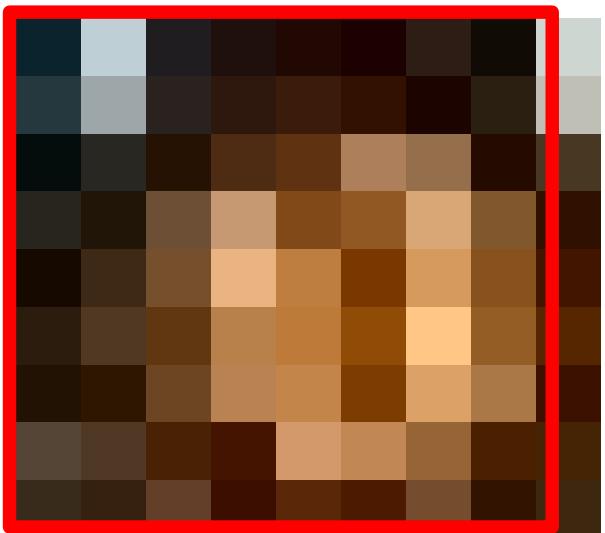
# Matching in the context of other images



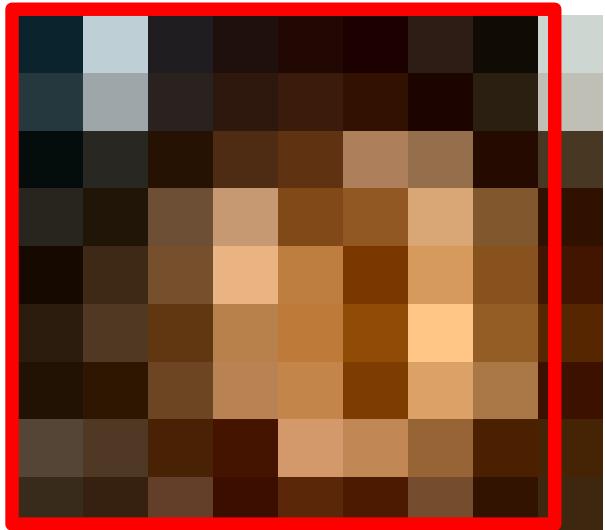
?



# Matching in the context of other images



# Matching in the context of other images



# Finding correspondences



For a large viewpoint  
change (including scale)

=>

**the wide-baseline  
stereo problem**



## Applications:

- pose estimation
- 3D reconstruction
- location recognition

# Finding correspondences



for large viewpoint change  
(including scale)

=>

**the wide-baseline (WBS)  
stereo problem**



# Finding correspondences



for large  
**illumination change**

=>

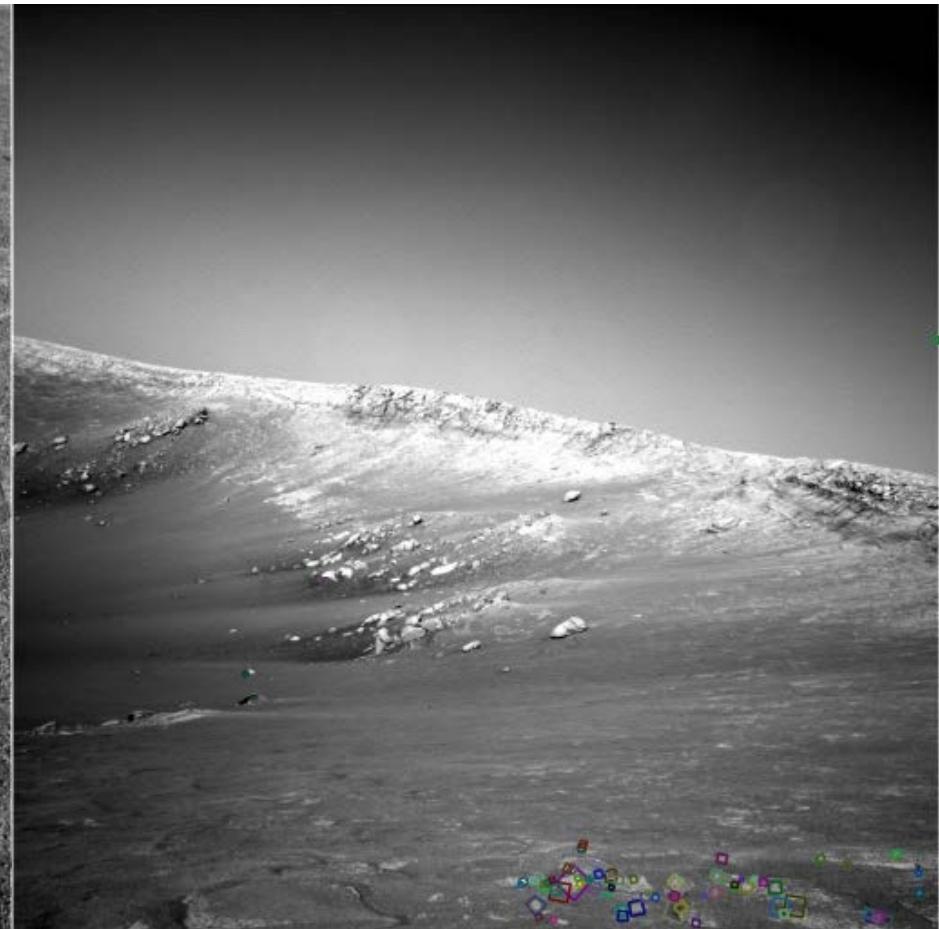
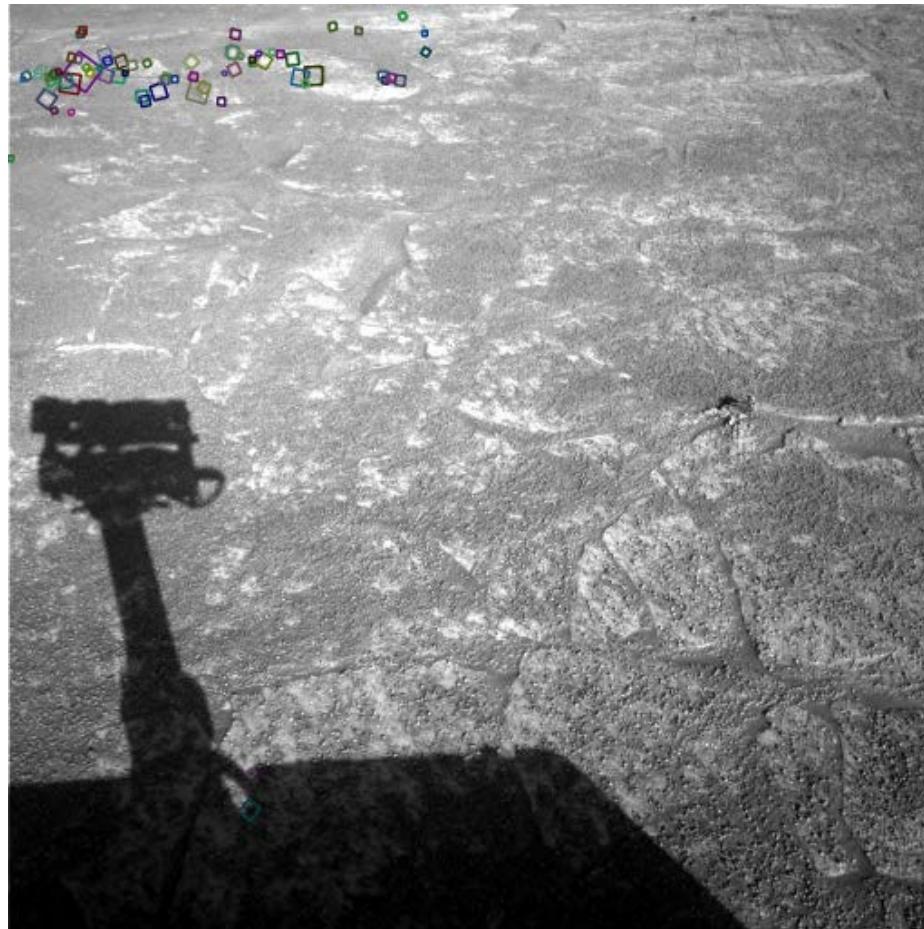
wide “illumination-baseline”  
stereo problem



## Applications:

- location recognition
- summarization of image collections

Find the matches (look for tiny colored squares...)



NASA Mars Rover images  
with SIFT feature matches  
Figure by Noah Snavely

# Finding correspondences



For large  
time difference

=>

wide temporal-baseline  
stereo problem



## Applications:

- historical reconstruction
- location recognition
- photographer recognition
- camera type recognition

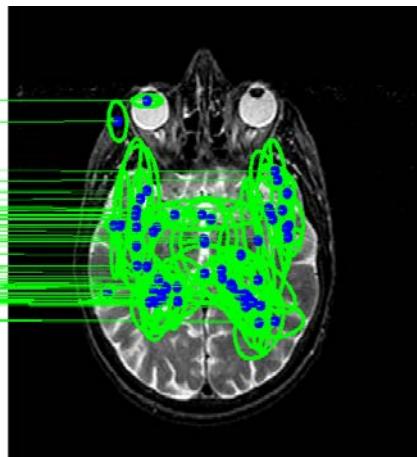
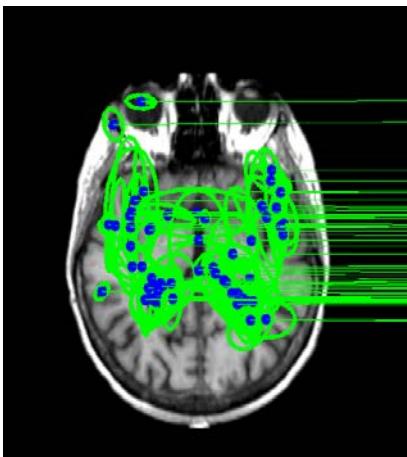
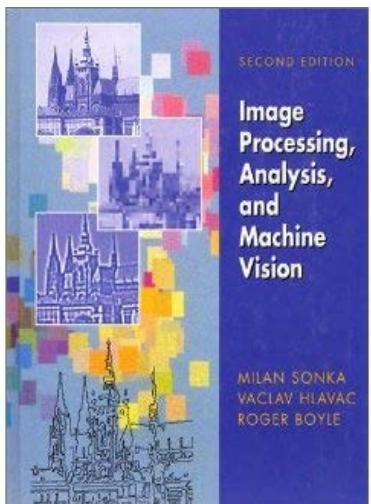
# Finding Correspondences



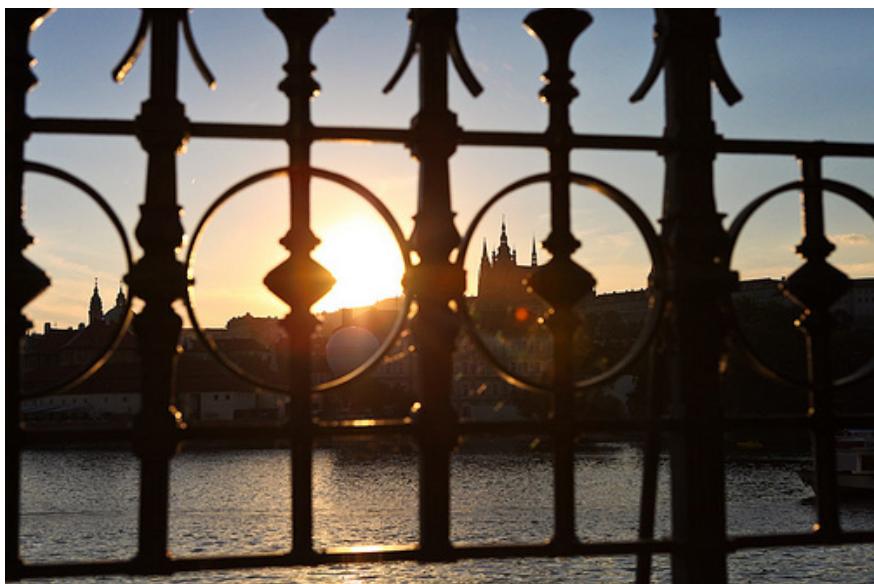
change of modality

Applications:

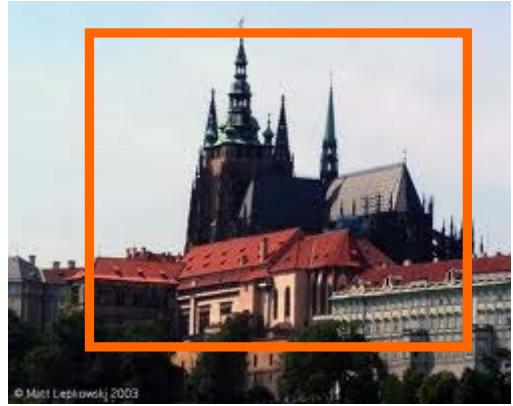
- medical imaging
- remote sensing



# with occlusion “almost everywhere”



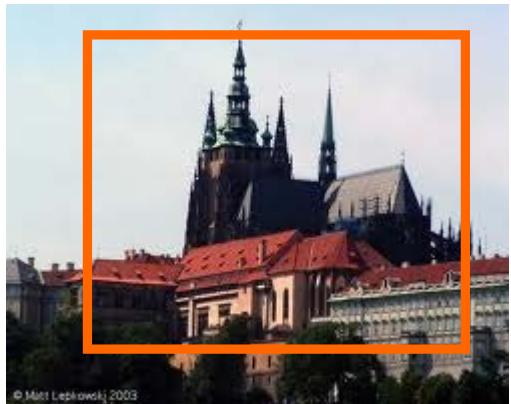
# “Inprecise” Geometry ☺



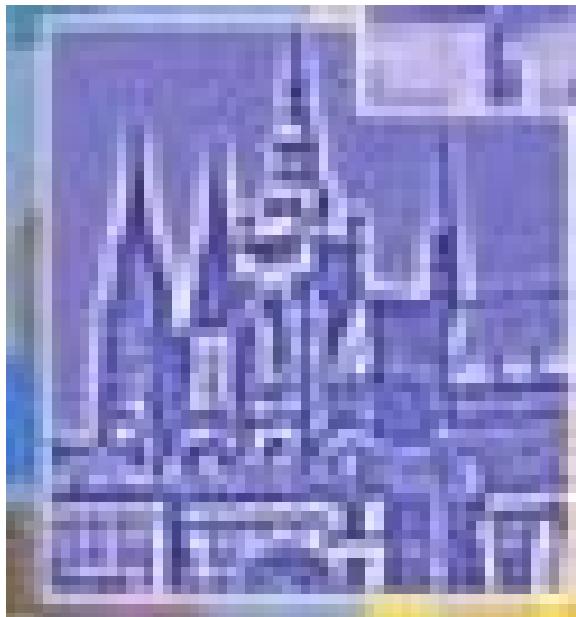
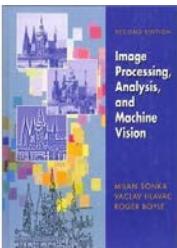
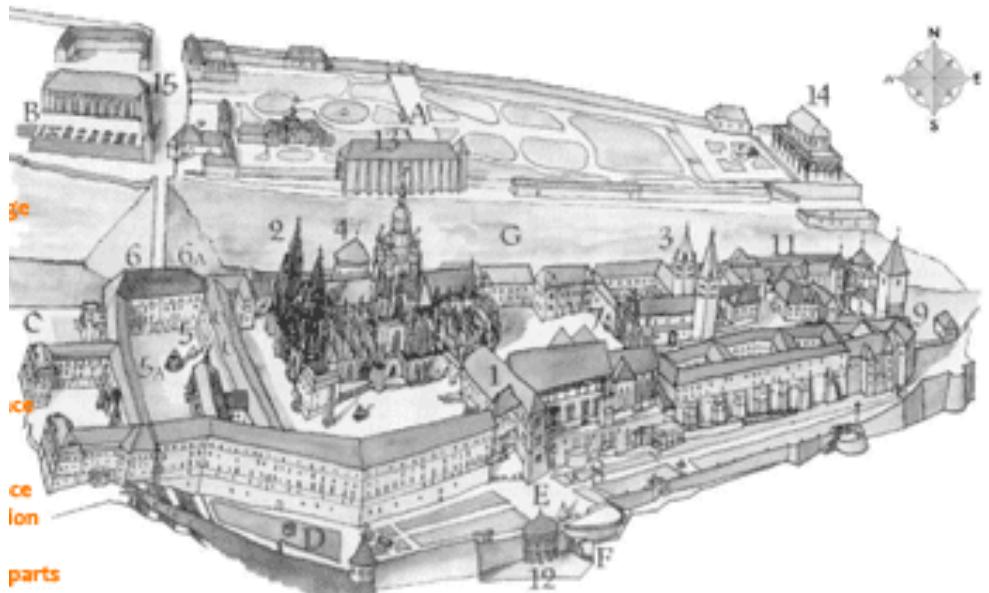
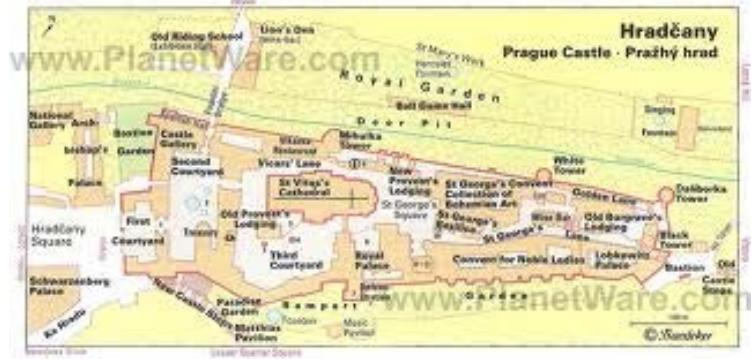
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# Retrieving different modalities



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# Thank you!