Hugo

21. The quantum phase estimation circuit happens in 4 phases. SA Lou

· phase 1: imitialization

· phase 2: apply Fladomand gates H&m & 1

. phase 3: apply the combrolled Uk (10 m)

$$OD U^{k} | \Psi \rangle = (e^{2i\pi \theta})^{k} | \Psi \rangle$$

 $|0^{m}\rangle \otimes |\Psi\rangle$ $\left(\frac{1}{\sqrt{2^{m}}}\sum_{k=0}^{2^{m}-1}|k\rangle\right) \otimes |\varphi\rangle$

phase
$$h$$
: apply the inverse Quantum Flourier Transform QFT $\frac{1}{8}$ to the m first qubits)

$$\frac{1}{\sqrt{2^m}} \sum_{j=0}^{m-1} \frac{1}{\sqrt{2^m}} \sum_{k=0}^{2j\pi/2^m} e^{2j\pi/2^m}$$
where $\omega = e^{2j\pi/2^m}$

simplifications, we get, on the first on gulits,

$$|\psi\rangle:=\frac{1}{2^{m}}\sum_{j=0}^{2^{m}-1}\sum_{k=0}^{2^{m}-1}2^{2k\pi}k(\theta-j/2^{m})$$

Q2. $p_{\hat{g}} = |\langle \gamma | \hat{g} \rangle|^2 = \frac{1}{2^{m}} \left| \sum_{n=1}^{2^{m}-1} (e^{2i\pi(\Theta - \hat{g}/2^{m})^{n}})^{n} \right|$

$$\frac{1}{2^{2m}} = \frac{1}{2^{2m}} \left[\frac{1 - e^{2i\pi(2^{m}\theta - i)}}{1 - e^{2i\pi(\theta - i)2^{m}}} \right]^{2}$$

$$\pm 1 \text{ as } \theta \neq 1$$

 ± 1 as $\theta \pm i/2^m$

83. We have that, if $|\theta - \sqrt{3}/2^{m}| \ge 2^{-t-1}$, then $|\theta - \sqrt{3}/2^{m}| \ge 2^{-t-1} = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2m}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2m}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2m}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2m}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2m}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2m}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2m}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2m}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2m}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2m}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2m}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2m}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2m}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2m}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2m}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2m}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2m}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right) = 1/4 \cdot 2^{2m} \left(\frac{1}{2^{2m}} \frac{2^{2m}}{(4 \times (\theta - \sqrt{3}/2^{m}))^{2}} \right)$

So the probability of measuring an "invalid value" $|\theta - j(2^m)| \ge 2^{t-s}$ for any value is $\le 2^m \times 2^{t-2m} = 2^{t-m}$

Thus, the success probability is $= 1 - 2^{2t-m} \frac{1}{m-\infty}$ 1

END of Ussignment #5.