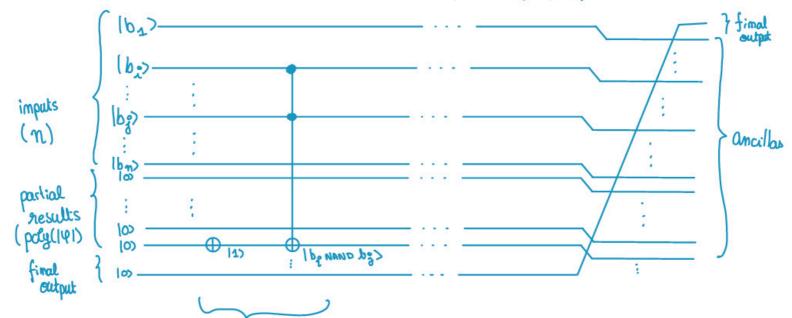
Consider a formula 9 with no variables. We can construct an oracle for 9 by using sweeps and NANDS (as any propositional formula can be transformed into an equivalent formula using with only variables and NANDS in poly-time). Using ancillar, we can evaluate 4 on some valuation  $b_1, ..., b_n$  with



Evaluate
a subformula
by NAND by

In the above circuit, we implicitely assumed that 223. This can be done as the NAND opera lien is symmetric (Same thing if  $\phi$ 's portial result is "higher" than  $\Psi$ 's).

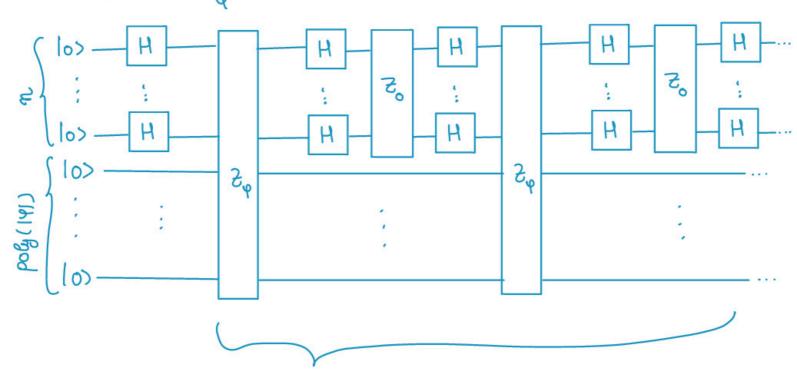
To evaluate a Sub formula of the form PNANDY, we use a very similar tactic but we place the Toffoli's controls on the two qubits responsible for \$\psi\$'s and \$\psi's partial result.

The only case that is some what ambiguous is i = j, but we can simply use a CNOT gate whose comtrol is on  $b_2 = b_3$ : |  $b_2$ :

Using tutorial #5's results, we can obtain a query oracle for evaluating 4:

Zu / b\_ ... b\_ > 10 pody (141)> = (-1) / | b\_ ... b\_ > 10 pody (141)>. (Q1, part II of Tutorial #5).

We can thus apply Grover's algorithm to the in first impuls of Zu:



Repeat & times

(As multiple valuations (b1, ..., bn) can satisfy 4, we can run

Groves's algorithm for de creasing values of k:  $k = 2^{n}/2^{it\sigma} = 2^{n-it\sigma}$  where iter is

the number of iterations of (not in) Grover's algorithm.

With high probability, we have  $k = G(\sqrt{2^n/e})$ , thus we have

a circuit of size

$$G(k \cdot (size(U_{\varphi}) + size(z_{o}))) = G(2^{n/2}poly(141))$$

$$\leq poly(141)$$

$$\leq poly(141)$$

END

of

Assignment #6