

DBDM

Exercise 2.1.

(Natural) join \bowtie is associative and commutative.

Exercise 2.2.

It's the cartesian product.

Exercise 2.3.

1) We suppose $\{a_1, \dots, a_n\} \cap \{b_1, \dots, b_m\} = \emptyset$ and $\forall i \neq j, a_i \neq a_j, b_i \neq b_j$

$$R \bowtie_{\substack{a_1=b_1 \\ \vdots \\ a_n=b_n}} S = \sigma_{a_1=b_1} (\sigma_{a_2=b_2} (\dots \sigma_{a_n=b_n} (R \bowtie S) \dots))$$

$$\pi_{(A_R \cup A_S) \setminus \{a_1, \dots, a_n\}} (R \bowtie_{\substack{a_1=b_1 \\ \vdots \\ a_n=b_n}} S) = \rho_f(R) \bowtie S$$

$$f: A_R \rightarrow A_R'$$

$$a_i \mapsto b_i$$

$$\{a_1, \dots, a_n\} \ni a \mapsto a$$

2) Define $T = A_R \cap A_S$, and

$$f: A_S \rightarrow A \#$$

$$T \ni a \mapsto a$$

$$T \ni a \mapsto a' \leftarrow \text{fresh attribute}$$

$$R \bowtie S = \pi_{A_R \cup A_S} (R \bowtie_{a=a'} S)$$

Exercise 2.4.

$$\sigma_{\text{travel} \neq \text{travel}'} (\pi_{\text{travel}, \text{travel}'} (\text{usedFor} \bowtie \rho_f(\text{usedFor})))$$

$$f: \begin{array}{l} \text{train} \mapsto \text{train}' \\ \text{date} \mapsto \text{date}' \\ \text{travel} \mapsto \text{travel}' \end{array}$$

$$\sigma_{a \neq b}(q) = q \setminus \sigma_{a=b}(q)$$

Exercise 2.5.

$$\begin{aligned}\pi_{j=a}^i(R) &= R \bowtie S. \\ &= \left\{ u \in D^{A_R} \mid \underbrace{u(j)=a}_{u \in S} \right\}.\end{aligned}$$

Exercise 2.6.

1. R_1, \dots, R_m joins completely

$$\text{iff } \forall t \in R_i, \exists t' \in R_1 \bowtie \dots \bowtie R_m, t' [A_{R_i}] = t$$

$$\text{iff } \forall t \in R_i, t \in \pi_{A_{R_i}}(R_1 \bowtie \dots \bowtie R_m)$$

$$\text{iff } R_i = \pi_{A_{R_i}}(R_1 \bowtie \dots \bowtie R_m)$$

$$\times: \Rightarrow R_i \subseteq \pi_{A_{R_i}}(R_1 \bowtie \dots \bowtie R_m) \text{ by assumption}$$

$$R_i \supseteq \pi_{A_{R_i}}(R_1 \bowtie \dots \bowtie R_m) \text{ by def.}$$

2. We simply have to prove that $R_i = \pi_{S_i}(R_1 \bowtie \dots \bowtie R_m)$.

We have that $R_1 \bowtie \dots \bowtie R_m = \pi_{\bigcup_i S_i}(R)$ and so

$$\pi_{S_i}(R_1 \bowtie \dots \bowtie R_m) = \pi_{S_i}(\pi_{\bigcup_i S_i}(R)) = \pi_{S_i}(R) = R_i.$$

Exercise 2.7.

We have to have $A \cap B$ as primary keys of R .

It is not sufficient.

Exercise 2.8.

$$(R \bowtie S) \div S = (R \times S) \div S = S$$

Exercise 2.9. ♥

1.