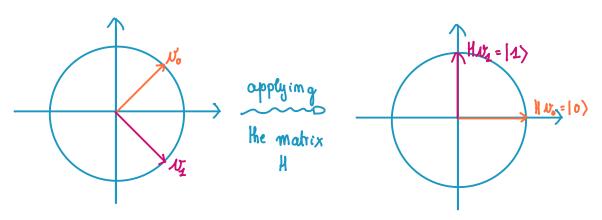
Q.1. To know whether system X is in state vo or v2 we can apply the Hadamard matrix:

$$H = \begin{pmatrix} 1/\sqrt{2} & 1/\sqrt{2} \\ 1/\sqrt{2} & -1/\sqrt{2} \end{pmatrix}.$$

We have that $HH = A_2$, $H(0) = V_0$, and $H(1) = V_1$. Thus, applying the Hadanard matrix again, we have that:

$$H v_0 = |0\rangle$$
 and $H v_1 = |1\rangle$.

We can distinguish the from the by measuring.



Q. 2. We will prove that $|\Psi\rangle := \begin{pmatrix} 1/\sqrt{2} \\ 0 \\ 1/\sqrt{2} \end{pmatrix}$ is entangled with a proof by contradiction. Suppose $|\Psi\rangle = 11 \otimes 11 = 0$ for some qubits 11 and 15, with $11 = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$ and $11 = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$.

Then, we have that

$$M \otimes D = \begin{pmatrix} a \begin{pmatrix} c \\ d \end{pmatrix} \\ b \begin{pmatrix} c \\ d \end{pmatrix} \end{pmatrix} = \begin{pmatrix} ac \\ ad \\ bc \\ bd \end{pmatrix} = \begin{pmatrix} 1/\sqrt{12} \\ 6 \\ 0 \\ 1/\sqrt{12} \end{pmatrix}.$$

In particular, we have that od=0, so either a=0 or d=0.

If a=0 then $ac \neq 1/\sqrt{2}$, absurd! If d=0 then $drd \neq 1/\sqrt{2}$, absurd!

We can conclude that (1/1/2) is entronglish.

END of ASSIGNMENT #1