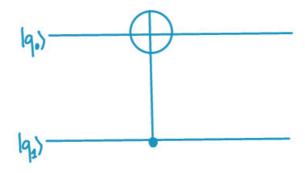
Q1. We can compute explicitely the unitary matrix of the quantum circuit:

$$\frac{1}{4} \left(\begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \otimes \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \right) \begin{pmatrix} 1 & 6 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix} \left(\begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \otimes \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \right) \\
\left(1 & 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix} \right)$$

$$= \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & A \\ 0 & 0 & A & 0 \\ 0 & 1 & 0 & 0 \end{pmatrix}$$

We can recognize the unitary matrix of the following quantum circuit:

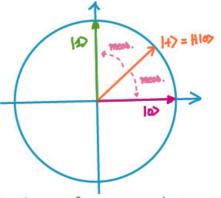


which is a lot simpler.

Q2. We get 1 qubit set at 10> from the machine. Then, we apply a Hadamard gate and measure in the 710>, 12> 7 basis.

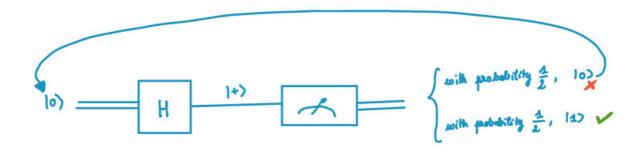
The result of this procedure will be:

~ 11) with probability 1/2; ~ 10) with probability 1/2.



If we have a 117, we one done, but if we have a 10>, we simply repeat the procedure again and again.

The number of iterations follows a geometric law $\mathcal{J}(1/2)$, thus we can "expect" to have to do $\mathbb{H}[X]=2$ iterations to obtain a |1>. Repeating 7 times the procedure will give us a |1> with more than 99% pao bability.



A more complex procedure could give us better odds.

END of ASSIGNMENT #2