HW4 code

Hengchang Hu 10/2/18

Chapter 2.2

```
(a)
indicators <- read.table("C:/Users/hugo1/Documents/MA575/HW4/indicators.txt", header = TRUE)
# import the dataset
OLS_priceloan <- lm(PriceChange~LoanPaymentsOverdue, indicators)
# get the least square model
esti_beta1_pl <- coef(summary(OLS_priceloan))[, "Estimate"]["LoanPaymentsOverdue"][[1]]</pre>
print(paste("The estimation of beta_1 is ", esti_beta1_pl))
## [1] "The estimation of beta_1 is -2.24851978357815"
# show estimation value of beta_1
std_beta1_pl <- coef(summary(OLS_priceloan))[, "Std. Error"]["LoanPaymentsOverdue"][[1]]
print(paste("The Standard error of beta_1 is ", std_beta1_pl))
## [1] "The Standard error of beta_1 is 0.903311332218041"
# show standard error value of beta_1
print(paste("The 95% CI of beta_1 is [", esti_beta1_pl -
              qt(0.975,16) * std_beta1_pl, esti_beta1_pl
            + qt(0.975,16) * std_beta1_pl, "]"))
## [1] "The 95% CI of beta 1 is [ -4.16345426359378 -0.333585303562513 ]"
# 95% confidence interval of beta_1
```

From above we can tell that there is evidence of a significant negative linear association.

```
(b)
newdata <- list("LoanPaymentsOverdue" = 4) # type in newdata
esti_pl_4 <- predict(OLS_priceloan, newdata)[[1]] # estimation value
print(paste("When X = 4, E(Y|X) = ", esti_pl_4)) # show estimation value
## [1] "When X = 4, E(Y|X) = -4.47958536542933"</pre>
```

From above we can tell that 0% is not in the 95% CI for E(Y|X=4), so it is not a feasible value.

Chapter 2.3

(a)

Through the output of R, $\hat{\beta_0}$ is 0.6417099, $se(\hat{\beta_0})$ is 0.1222707, Degree of Freedom is 28. Therefore, the 95% CI for β_0 is [0.3912497, 0.8921701].

(b)

From the output of R, we can know that $\hat{\beta}_1=0.0112916$, and the $se(\hat{\beta}_1)=0.0008184$. Since the statistics $T=\frac{(\hat{\beta}_1-\beta_1)}{se(\hat{\beta}_1)}=$ 1.5782014, and the acceptance region is $\left[t(0.025,n-2),t(0.975,n-2)\right]=$ [-2.0484071, 2.0484071]. Therefore the T statistics fall into acceptance region, can not reject the null hypothesis.

(c)

When X = 130, $E(Y|X = 130) = 0.6417099 + 0.0112916 \times 130 =$ **2.1096179**. And the 95% CI for E(Y|X=130)% is [1.9862772, 2.2329586]

Chapter 2.6

(a)

$$(y_i - \hat{y}_i) = y_i - \hat{\beta}_0 - \hat{\beta}_1 x_i$$

= $y_i - (\bar{y} - \hat{\beta}_1 \bar{x}) - \hat{\beta}_1 x_i$
= $(y_i - \bar{y}) - \hat{\beta}_1 (x_i - \bar{x})$

(b)

$$(\hat{y}_i - \bar{y}) = \hat{\beta}_0 + \hat{\beta}_1 x_i - \bar{y}$$
$$= \bar{y} - \hat{\beta}_1 \bar{x} + \hat{\beta}_1 x_i - \bar{y}$$
$$= \hat{\beta}_1 (x_i - \bar{x})$$

(c)

$$\sum_{i=1}^{n} (y_i - \hat{y}_i)(\hat{y}_i - \bar{y}) = \sum_{i=1}^{n} \left[(y_i - \bar{y}) - \hat{\beta}_1(x_i - \bar{x}) \right] \hat{\beta}_1(x_i - \bar{x})$$

$$= \hat{\beta}_1 \left(\sum_{i=1}^{n} (y_i - \bar{y})(x_i - \bar{x}) - \hat{\beta}_1 \sum_{i=1}^{n} (x_i - \bar{x})^2 \right)$$

$$= \hat{\beta}_1 \left(SXY - \frac{SXY}{SXX} SXX \right)$$

$$= 0$$