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1. (a) For optimal portfolio
                                  \Delta max \tilde{E}(R_p) - \frac{\gamma}{2} Var(R_p) s.t. W'_1 = 1
                                            = max { Ro+ E[ = wi (Ri-Ro)] - f Var[ = (wi Ri)]
                                             = \max \left\{ R_0 + \tilde{\Gamma} \left[ \sum_{i=1}^{N} W_i \left( R_i - R_0 \right) \right] - \frac{Y}{2} \sum_{i=0}^{N} \sum_{i=0}^{N} Cov \left( W_i R_i, W_i R_i \right) \right\}
                                                                                                                                                                                                                                Ro represent risk-free asset
                                             = \max \left\{ R_0 + \sum_{i=1}^{N} \left[ W_i (M_i - R_0) \right] - \sum_{i=1}^{N} \sum_{j=1}^{N} AN \left( W_j R_i, W_j R_j \right) \right\}  Var (R_0) = 0
                                             = max { Ro + \( \frac{\x}{\x} \) ( \( w_i (u_i - Ro) \) - \( \frac{\x}{\x} \) \( \frac
                                 a first order condition:
                                           \frac{\partial \mathcal{U}(\omega)}{\partial W_i} = (\mathcal{U}_i - R_0) - 2 \cdot \sum_{i=1}^{N} W_i \text{ and } (R_i, R_j) = 0
                                                         Ui-Ro - Y Z Wj WV (Ri, Rj.)
                                                                                    = Y = Cov (ki, Wj Rj) = Y Cov (ki, kp)
                                                   for Ruzry, Rp= 5 WiRj)
                                                         Mi-14 = Y WO (Ri, Rp)
    (b)
                      from (a), we have Mi-ry = Y COV (Ri, Rp) = Y = and (Ri, Rj) . w
                      in vector form, M-rf1 = Y \(\Sigmu\), \(\Sigmu\) is weight vec.
                                                     w'(u-41) = Yw' Zw = Y8p
                                                                     W'(11-7-1)=Up-7-2 > 8p
                                                                Ui-ry = Y COV CRi, Rp)
                                                       (Ni-14) Y 8p = Y WV CRi, Rp) (Up-14)
                                                                                  : Mi- 1 = 14-14 (WCRi, Pp)
                                                                                                                  = Bi, plup-rt)
   (C)
                      from (b), we have u_i = R_f + \beta_{i,p} (u_p - R_f)
                     thus, we can set Ri = Bo + B, (Rp-Rp)+ Ei,
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$$Var(R_{f_{1}}) = Var(W_{1}R_{t} + (I + W_{1})R_{f_{1}})$$

$$= Var(W_{1}R_{t}) = W_{1}^{2}Var(R_{0}) = W_{1}^{2}S_{t}^{2}$$

$$Var(R_{f_{2}}) = W_{2}^{2}Var(R_{t}) = W_{2}^{2}S_{t}^{2}$$

$$\therefore SR_{f_{1}} = \frac{u_{1}R_{1}}{\delta f_{1}} = \frac{E(W_{1}R_{t} + (I + W_{1})R_{f_{1}}) \cdot R_{f_{1}}}{\delta f_{1}}$$

$$= \frac{w_{1}U_{t} - w_{1}R_{f_{1}}}{w_{1}S_{t}} = \frac{u_{t} \cdot R_{f_{1}}}{\delta t}$$

$$SR_{f_{1}} = \frac{E(W_{1}R_{1} + (I + W_{1})R_{f_{1}}) \cdot R_{f_{1}}}{\delta f_{2}} = \frac{w_{2}U_{t} - w_{2}R_{f_{1}}}{w_{2}S_{t}} = \frac{u_{t} \cdot R_{f_{1}}}{\delta t}$$

$$\therefore SR_{f_{1}} = SR_{f_{2}}, \quad = all \quad mean-variance \quad efficient \quad par(f_{2})tiv_{1} \quad have \quad same \quad SR$$