Din = De e 3- 1 28+ 30+1 - dividend process gui = Paga + of Eg (++1) - stock. component Ra+1 = A+1+ Pan - goss seturn E[R4] = ei+k. - expeded return PD+ = P/D+ pd+ = log PD+

(a) k=0 yt => et = const.; pg=0 => E[g,+1]=0 River = Property => Pr = Property Price $E[R_{++1}] = e^{\overline{k} \cdot k_1} = e^{\overline{k}}$; $Q_{++1} = P_+ e^{\overline{3} - \frac{1}{2} \frac{\sqrt{3}}{3} + \frac{1}{2} \frac{\sqrt{3}}{3}} = Q_+ e^{\overline{3}}$ (since volatility of a constant = 0) Pt = D1 e3 + E1 Pm] where E[[++1] = D1 e3 + E1 Pm2] =>

 $= > \frac{D_4}{e^{F_4}} + \frac{D_4}{e^{F_6}(e^{F_4})} + \frac{E[P_{4+2}]}{e^{2F_6}}$

Applying the brute force approach and substituting further Effirm I we get the following equation: P. = D, =(k-3) = ek-3) + (+) E, [P. N]

Assuming no bubble condition and taking the lim gives: lim (tx) E[[P. II] = 0. Thus, we have: P = D = (k-g) = = (k-g)k

Since we assume that the price is divite $\hat{g} < k$ has to hold and we have the dollowing equation in the limit: P4 = D4 e 3-k 1- (1-k) = D+ 2 D+ 2 K-4 => the PD ratio is constant

The results are not consistent with the emperical result. According to the emperical results the volatility is not constant and the price volatility is 5 to 10 times higher than the dividend volatility. The condition under which such difference is possible (assuming constant volatility): 25 × 1 × 210

2.236 < 21-1 < 3/62

0,447 > 0.316

1,447 > ex-3 > 1,316

0,369 > K-g > 0,275 => the condition that is highly unlikely to hold in real life.

B P = 0 => k = p k + 5 = (++1) We need to find a function that PD = PD(g, k) that solves a tixed point: E[Rass] : Ex[Dass on on] Equivalently, et. 4 = Ex[exp(\(\bar{g} - \dagger \dagg

(C) pd, = pd(g+; k+) = A+Bg+ Ck+

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We need to approximate the following function: \log(1+\exp(A+B_{gn}+Ck_{n})) around pd=A \log(1+\exp(A+B_{g}+Ck_{n}))=\log(1+e^{A})+\frac{e^{A}}{1+e^{A}}(A+D_{gn}+Ck_{gn}-A)
                                   e + k = E = ( exp(g - 10 + g + g + + log (1+ e1) + e1 + (A+Bg + + Ck + + - A) - (A + Bg + + Ck + )) 7
                                    exp( = - 25 + cg 14 e') - A - Bg+ - Ck+) Ex[ exp( g ... (++ e B) + e Ck+1)]
                         Let's plug in go, and king
                    ek+k1 = exp(g-1052+ lg(1+e1)-A-10,-Ck1) Ex[exp(()2,g++0g & (+1))(1+eAB)+ eAC())kk++0x & (+1)))]=
                      = exp(\vec{g} - \frac{1}{2} \sigma_{\vec{g}}^2 + Log(1+e^4) - A - B_{3+} - Ck_+ + p_3 g_+ (1+\frac{e^4}{1+e^4} B) + p_k k_+ \frac{e^4}{1+e^4} C) E_+ [exp(\vec{g} \varepsilon_3 \varepsilon_3 (1+1)(1+\frac{e^4}{1+e^4} B) + \vec{g} \varepsilon_k \varepsilon_1 (1+\vec{e^4} B) + \vec{g} \varepsilon_2 (1+\vec{e^4} B) + \vec{g} \varepsilon_1 (1+\vec{e^4} B) + \vec{g} \varepsilon_1 (1+\vec{e^4} B) + \vec{g} \varepsilon_2 (1+\vec{e^4} B) + \vec{g} 
                               Sinc we know that the random variables are normally distributed (iid), we can use the moment generating function: E.[eleg(+1)]= e2
                                In order to compute an expectation:
                            Ex[exp(\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi}_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\pi_{\overline{\overline{\overline{\pi_{\overline{\overline{\pi_{\overline{\overline{\o
                               K+K+ = 3-153+ log(1+e4)-A+ g+ (p3(1+1+0)-B)+k+ (p+1+0)-C+ 1(52+(1+0)-C+ 1(52+(1+0)-C+ 1(1+0)-C+ 1)-C+ 1(1+0)-C+ 1(1+
                               Mutching the coefficients gives:
                                    \( \bar{k} = \bar{q} - \frac{1}{2} \sigma_{\delta}^2 + \log (1+e^4) - A + \frac{1}{2} (\sigma_{\delta}^2 (1+\frac{e^4}{1+e^4} B)^2 + \sigma_k C^2 \frac{e^{2A}}{(1+e^4)^2} )
                                < Kx: PK # C - C = 1
                                   ge: pg (1+ e B)-B=0
                                   From the system we have :
                                C = \frac{1}{P_{K}} \frac{e^{A}}{(1+e^{A})^{-1}} = \frac{1+e^{A}}{e^{A}(P_{K}-1)-1}
                            B( = 1 = 1) = -P3 => B = 2P3 (He1) = -P3 (He1) = P8 (He1) = P8 (He1) = P8 (1-P3)+1
                                   A= \( \bar{k} - \bar{k} - \bar{2} \dag{\dag{2} + \langle q (1+e^{\alpha}) + \bar{2} (\sigma_{\beta}^2 (1+\frac{e^{\alpha}}{1+e^{\alpha}} \beta)^2 + \sigma_{\beta}^2 \cap 2 \frac{e^{\alpha}}{(1+e^{\alpha})^2} \)
1 P1 = PK = OK = 0
                  Plugging it into previous solution gives:
                  \\ \B=0 \\ \c=-
                       C=-1
                    [ k = \bar{g} - \frac{1}{2}\sigma_2^2 + log(1 + e^4) - A + \frac{1}{2}\sigma_3 = \bar{g} + log(1 + e^4) - A = \bar{g} - log(\frac{e^n}{(1 + e^4)})
                       It follows that pd=A. It matches the results in point @
                      \log\left(\frac{e^{A}}{1+e^{A}}\right) = \hat{g} - \bar{k}
e^{\bar{g} - \bar{k}} = \frac{e^{A}}{1+e^{A}} = 1 + \frac{1}{e^{A}} = 2 + e^{A} = \frac{1}{e^{\bar{k} \cdot \bar{g}} - 1} = PD,
                        For the stochastic process to be mean-reverting it has to be stationary, which means the distribution doesn't depend on t
                         In our case the autocorrelation is represented by Px and Pg. It can be expressed as Px. Cov (kx keil) (WSS process). It can be noticed
                           that in order to have stationry process, P has to be strictly less than one in absolute value. If p=0 => the process is
                             a random walk and if p=1=2 unit root. => random walk. Thus, either px or pa 70 and $1 vill result in predictable process.
                    1) Let's suppose p_k \in (0,1) and p_g = 0. Thus, we have:
                              pd.,,= A+ Bg., + Ck.,, = A+ Bog & (++1) + C(P.k. + on &, (++1)) = A+ p.k. C+'( ox & (++1)C+ og & (++1)B)
                                Since Kz is the only parameter that depends on the past information and px 6(0,1) => the process is stationary
                     2) Now W's suppose Pz = (0,1) and Px = 0
                                pd. = A + B(pg. + Jeg(+1)) + Corex(+11) = A + pg. B + (oge (+1)D + oxex(+11)C)
                           Since gis the only parameter that depends on the past information and pre(0,1) => the process is stationary
                                Since empirically dividend growth is iid. (pg=0). If px 6(0;1), it will guarantee that the pdx is stochastic mean-reverting process =>
                             the expected return E,[R,,] has to be predictable
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