

CSSE2002/7023

Semester 2, 2021

Programming in the Large

Week 11.2: Recursion & Sorting

In this Session

- Recursion
- Sorting in Java
- Merge Sort
- Quick Sort

Recursion — Reminder

- Functions call themselves
 - possibly indirectly
- Make sure the recursion will stop eventually
 - base case
- Recursive calls should be a reduction case
 - smaller / simpler instances
- Beware stack overflow

Why Recursion?

Some people may say “It’s easier”.

- Ok, what does “easier” mean?
- ...to read?
- ...to write?
- ...for whom?
 - Me?
 - Someone else?

Is the person saying it:

- A theoretical computer scientist?
 - Is it “easy” because of 20 years experience?
- A fan of “functional programming” languages¹?
 - Not that there is anything wrong with that.
 - These are designed around using a recursive model of computation. So it probably is easier.

¹Lisp, Haskell, Erlang, ...

Why Not Iteration?

Can't we use iteration² instead?

Sort of.

There is a theoretical result that yes, recursive algorithms can be converted into algorithms which use loops (and a stack).

- Using a loop, we would have to manually manage the call stack (can become tedious). This is done automatically if we use recursion.

But, there are some algorithms which are easier and simpler to express in a recursive form. e.g. Fibonnaci

$$F(1) = 1$$

$$F(2) = 1$$

$$F(n) = F(n-1) + F(n-2)$$

How would we express this iteratively in a loop?

²loops

Iteration to Recursion Example

Write a recursive method `reverseWordsInString` that given a string as a parameter, will reverse the order of the words in the string, and return the result.

E.g. Passing “this is a sentence” as the parameter would return “sentence a is this”.

You cannot use the `split()` method or regular expressions, in any way.

All other methods are allowed though.

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```
public static String reverseWordsInString(String text) {
    String result = ""; // the entire string
    String word = ""; // current word
    int previousSpace = 0;

    // need to work out if there is another word to check
    int nextSpace = text.indexOf(' ', previousSpace);

    // base case. i.e. there is no more words
    if (nextSpace == -1) {
        return text;
    }

    // continue case. There is at least one more word.
    else {
        // get the next word
        word = text.substring(previousSpace, nextSpace);
        previousSpace = nextSpace + 1;
        // calls the same function.
        // append result of function call to start of result.
        return reverseWordsInString(text.substring(previousSpace))
            + " " + word + result;
    }
}
```

Recursion to Iteration Example

```
public class DataProcessor {
    public static int process(int[] data, int i, int l) {
        if (l == 1) { // base case
            return data[i];
        }
        else { // continue case
            int value = process(data, i + 1, l - 1);
            if (data[i] < value) {
                return data[i];
            }
            return value;
        }
    }

    public static void main(String[] args) {
        int[] data = {4, 6, 2, 8, 1, 9};

        System.out.print(process(data, 0, data.length)); //usage example
    }
}
```

a) In the code above, explain the purpose of the publicly accessible function `process(int[] data, int i, int l)`?

b) Write an iterative version of the function `process(int[] data, int i, int l)`, called `processIter`, which achieves the same functionality. You can use any number parameters, and the data type for the parameters is not restricted. You cannot use any additional Java functions or Java libraries in your implementation

Recursion to Iteration Example

a) This program finds the smallest number in an array of numbers.

b)

```
public static int processIter(int [] data) {  
    int smallestValue = 0;  
    smallestValue = data[0];  
    for (int i = 0; i < data.length; i++) {  
        if (data[i] < smallestValue) {  
            smallestValue = data[i];  
        }  
    }  
    return smallestValue;  
}
```

Sorting

We'll look at sorting algorithms as an example of a task which recursion can make easier.

Sorting a List in Java

```
List l;  
...  
l.sort(null);    // use default ordering
```

See: Sort.java

Doesn't give us much insight into how Java's sort() method works though.

Read the implementation note for insight:

<https://docs.oracle.com/javase/8/docs/api/java/util/List.html#sort-java.util.Comparator->

Merge Sort

Task: sort `arr` — an array of n ints.

- Suppose we know how to sort $n/2$ ints.
- Split `arr` in half
- Sort each half
- Merge the two sorted parts into one sorted whole

See: `MSort.java`

- Works because a single element array is automatically sorted
- Sorts “bottom up”

Quick Sort

Suppose we have a method `partition(arr)`

- Returns the index of one element in `arr` which is guaranteed to be in the correct place.
- Everything to the left of that element is \leq to it.
- Everything to the right of that element is \geq to it.

See: `QSort.java`

Which is Better?

It depends ...

| Criterion | Better |
|------------------------|---------------|
| Simplicity | Mergesort |
| Worst case performance | Mergesort |
| Expected performance | Quicksort |
| Memory requirements | Quicksort |

Why? See an algorithms course (COMP3506).

Further Exploration

<https://visualgo.net/en/sorting>

<https://www.cs.usfca.edu/~galles/visualization/ComparisonSort.html>

<http://sorting.at/>