## CSSE2010 / CSSE7201 – Introduction to Computer Systems Exercises – Week One Bits, Bytes & Binary; Intro to Logic Gates

## **Exercises**

Many of the problems below are taken from or based on questions in Tanenbaum, Structured Computer Organisation, 5<sup>th</sup> edition, Appendix A and Appendix B.

- 1. Convert the following decimal numbers to binary (unsigned representation): 1984, 4000, 8192.
- 2. What is 1001101001 (binary, unsigned) in decimal? In octal? In hexadecimal?
- 3. How many different positive integers can be expressed in k digits using radix r numbers?
- 4. One of the earliest computers (the Manchester Mark 1, 1949) was programmed with a radix-32 number system. Suppose such a number system has digits represented by the characters 0, 1, ... 9, A, B, ... U, V.
  - (a) Describe how a binary number can be converted into a radix-32 number.
  - (b) Describe how a decimal number can be converted into a radix-32 number.
  - (c) Convert the decimal numbers 1300 and 2300 to radix-32 representations.
- 5. What's the largest unsigned integer that can be represented in
  - (a) 10 bits
  - (b) 9 decimal digits
  - (c) 8 hexadecimal digits
- 6. What's the largest number that can be counted to on ten fingers, if each finger can be considered to have two positions? Compare your answer to that in 5(a).
- 7. For each of the following decimal numbers, write down the 8-bit binary representation using signed magnitude, one's complement, two's complement and excess 128 formats.
  - (a) -1
  - (b) 16
  - (c) -99
- 8. What are the smallest and largest integers that can be represented in the following binary representations:
  - (a) 16 bit two's complement
  - (b) n bit one's complement
  - (c) excess 2<sup>m-1</sup>
- 9. Draw the logic symbol, write the Boolean function and write down the truth table for:
  - (a) a 4 input NOR gate
  - (b) a 3 input XOR gate (i.e. the odd function)