

CSSE2010 / CSSE7201 Lecture 3, /

Binary Arithmetic

School of Information Technology and Electrical Engineering
The University of Queensland



Today...

- Admin
- Recap on signed number representations in binary
 - Logic gates revisited from previous lecture
- Binary Arithmetic
 - Arithmetic Circuits
 - Questions: please put them on to the padlet and I will answer them after the lecture

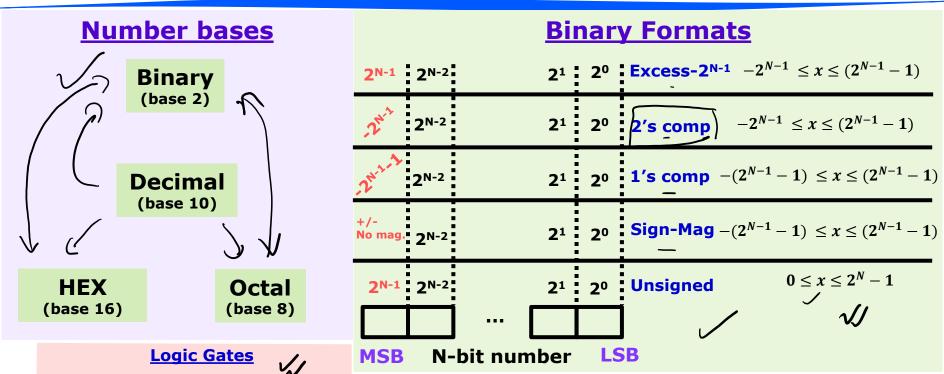


Admin

- Contact eait.mytimetable@uq.edu.au if not yet signed up or you're unable to attend the labs you are signed on to
- Two lab sessions per week from this week. Refer to week-by-week teaching outline on Blackboard.
- All labs are now online due to SEQ lockdown. Zoom information is on Blackboard.
- Weekly exercises (not assessed) are available on Blackboard
- Quiz 1 due this week Friday 4pm. Single attempt and need to submit (not auto submitted)



Quick Recap - Week 1 Lectures & Learning Lab



NOT, AND, OR, XOR, NAND, NOR, XNOR Symbols, Truth table, Boolean expression

Logic diagrams, schematic diagrams
Logic expressions, SOP, Simplification using Boolean algebra



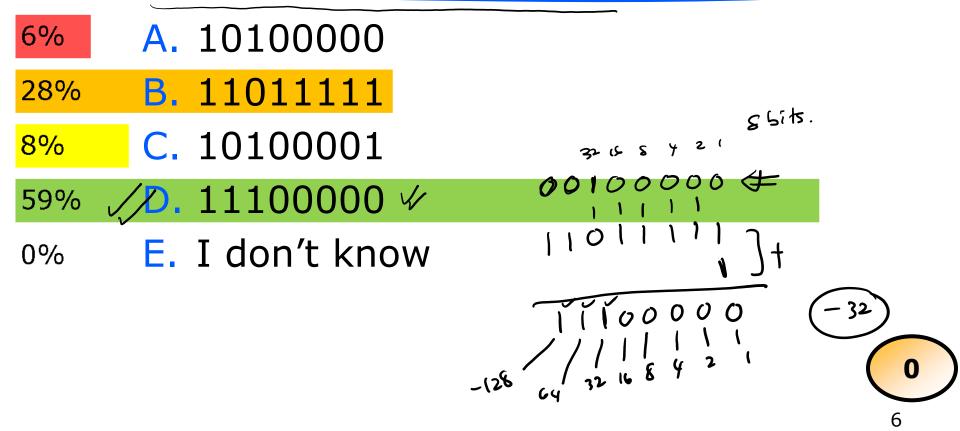
What is -32 (base 10) expressed in 8-bit signed magnitude format?

- 94% A. 10100000 V
- ^{1%} B. 10100001
- 1% C. 11011111
 - 1% D. 11100000
- 1% E. I don't know





What is -32 (base 10) expressed in 8-bit two's complement format?

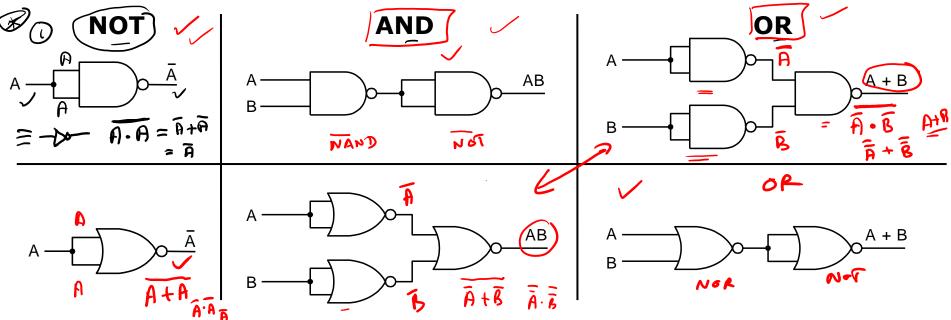




Equivalent Circuits



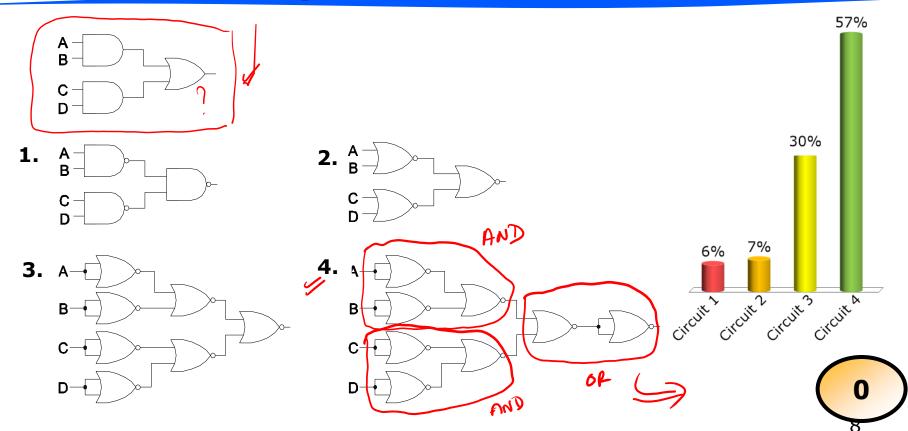
- All circuits can be constructed from NAND or NOR gates
 - These are called complete gates
- Examples:



Reason: Easier to build NAND and NOR gates from transistors



Which of the following is a NOR only implementation of





Binary Arithmetic

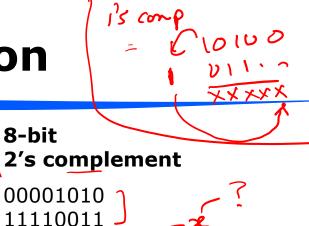
- Addition is quite simple in binary
- We shall see circuits that implement the addition operation later

Addend	0	0	1	1	
Augend	+0	+1	+0	+1	
Sum	(0)	1 ⁄	1	0 🗸	
Carry	<u>(0)</u>	0	0 🗸	1 🗸	i
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Above ignores carry in

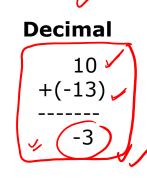


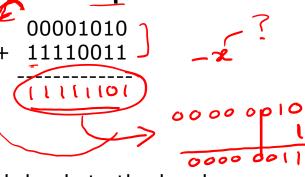
Binary Addition



```
Unsigned
Decimal
   10 <
+ 243 ~
```

8-bit





8-bit

- Format matters when you interpret the numbers
- Whatever the format is the bit-wise addition (which leads to the hardware circuit we will be looking at) is the same
- > Two's complement you don't need to do anything with the carry out from the MSB to get the correct result
- But in one's complement you will have to add the carry out from the MSB back to the result to get the correct answer – this is one drawback of one's complement representation - check by yourself



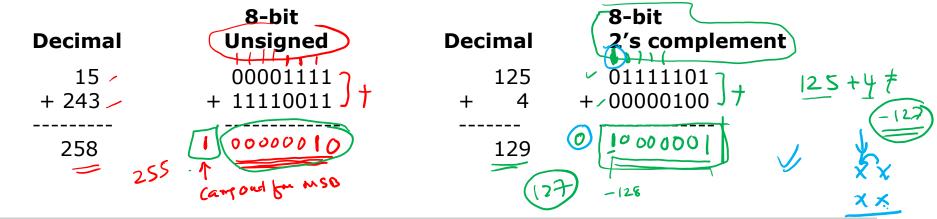
Short Break

Stand up and stretch



Overflow in Binary Addition



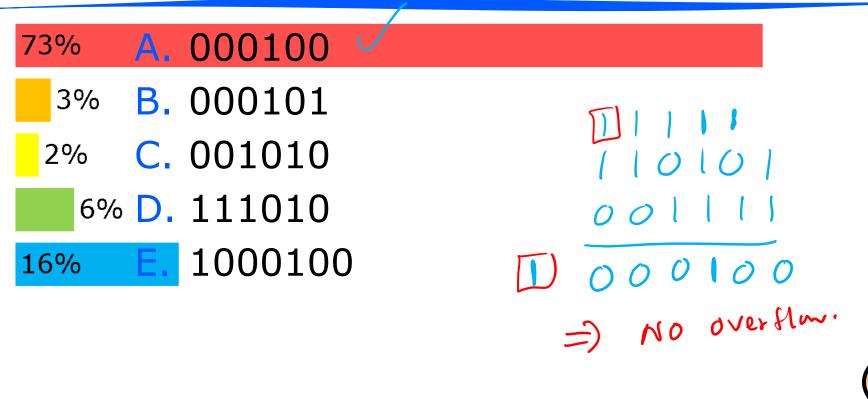


Overflow: Not enough bits to represent the answer. The result goes out of range. Thus, you get a wrong answer.

How is overflow detected:

- Unsigned: carry-out from the MSB -> overflow
- 2's comp: carry-in to the MSB and carry-out from the MSB are different → overflow
 - Equivalently, overflow occurs if (in 2's comp)
 - Two negatives added together give a positive, or
 - □ Two positives added together give a negative

What is the result of adding the two 6-bit two's complement numbers 110101 and 001111 in 6-bits?

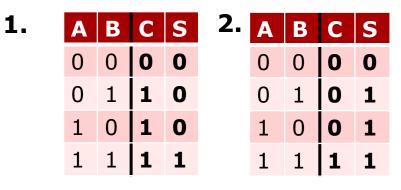


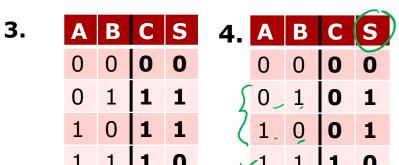


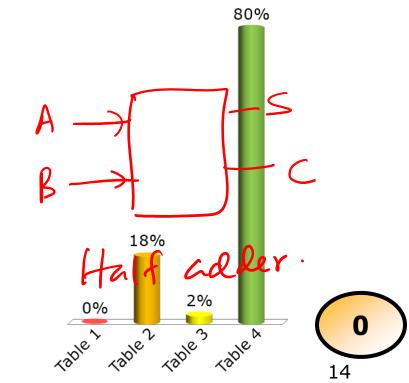
What's the truth table for an adder?

Inputs = A, B

Outputs = S(Sum), C(Carry)



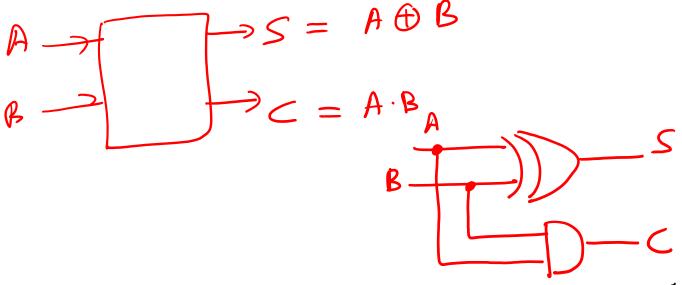






Binary Addition

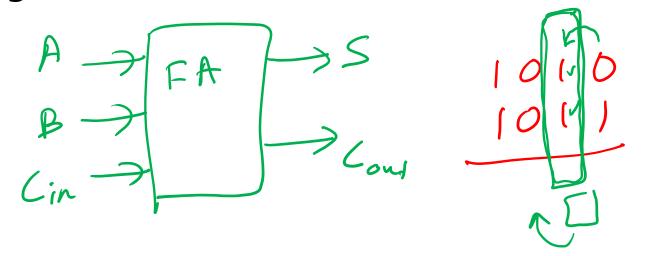
 A device which adds 2 bits (with no carryin) is called a half-adder





Binary Addition

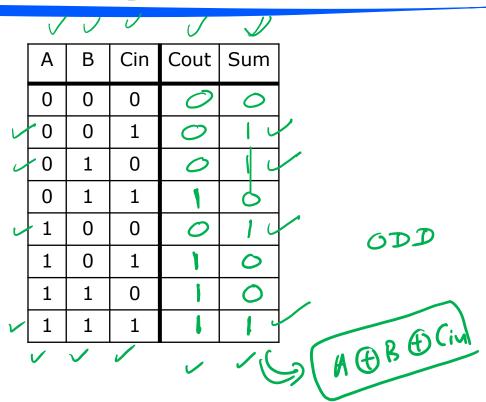
 We have to deal with carry-in. There might be a carry-in from the previous stage.





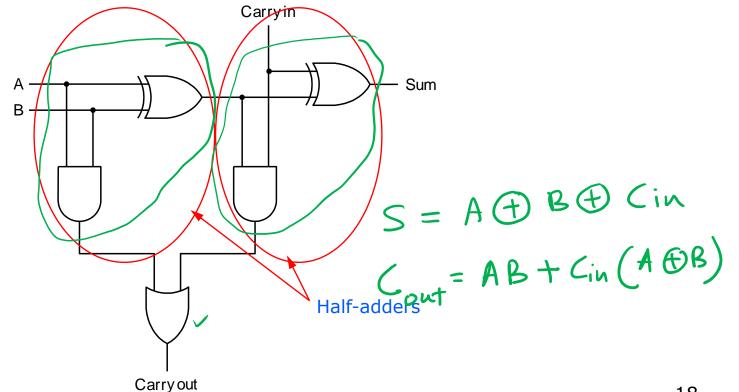
Addition of Binary Words

- Have to be able to deal with carry-in
- Truth table to be completed in class





Full Adder

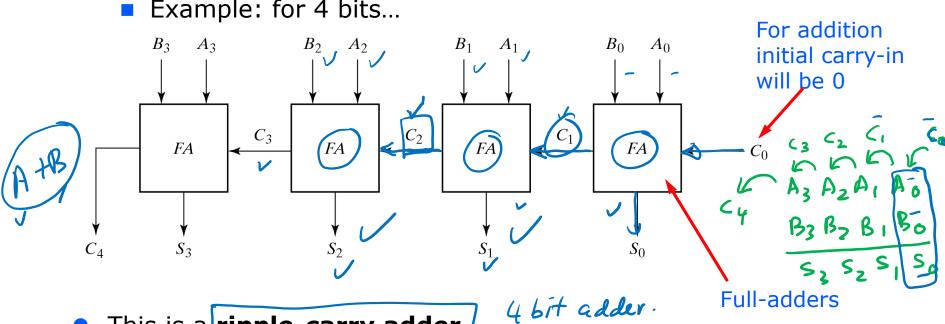


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Binary Adder

- Can cascade full adders to make binary adder
 - Example: for 4 bits...



This is a **ripple-carry adder**

[Figure from Mano, "Digital Design", 3rd edition]



Reminders for this week

- Lab classes

 - Mon-Tue: Lab 2 (Logic Gates)Wed-Fri: Lab 3 (Binary Arithmetic)
- Quiz due this week Friday 4pm
 - This week's labs
- IN students: if you have borrowed kits then use the kits. Otherwise use the Logisim software to simulate the logic circuits.
 - EX students: Use Logisim software to simulate the logic circuits. Start acquiring Arduino based hardware required in week 6.