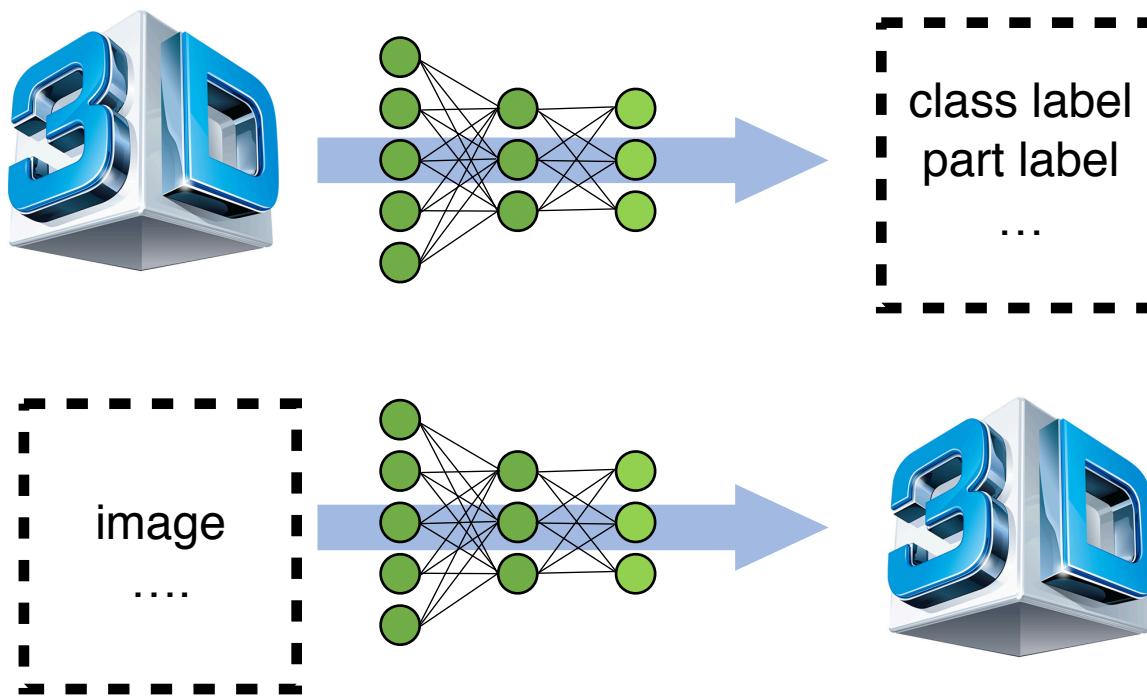


# CS468: 3D Deep Learning on Point Cloud Data

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Hao Su  
Stanford  
University

May 10, 2017

# Agenda

- **Point cloud analysis**
  - PointNet
  - PointNet++
- Joint embedding learning for cross-modality image-shape retrieval

# Applications of Point Set Learning

- **Robot Perception**

What and where are the objects in a LiDAR scanned scene?

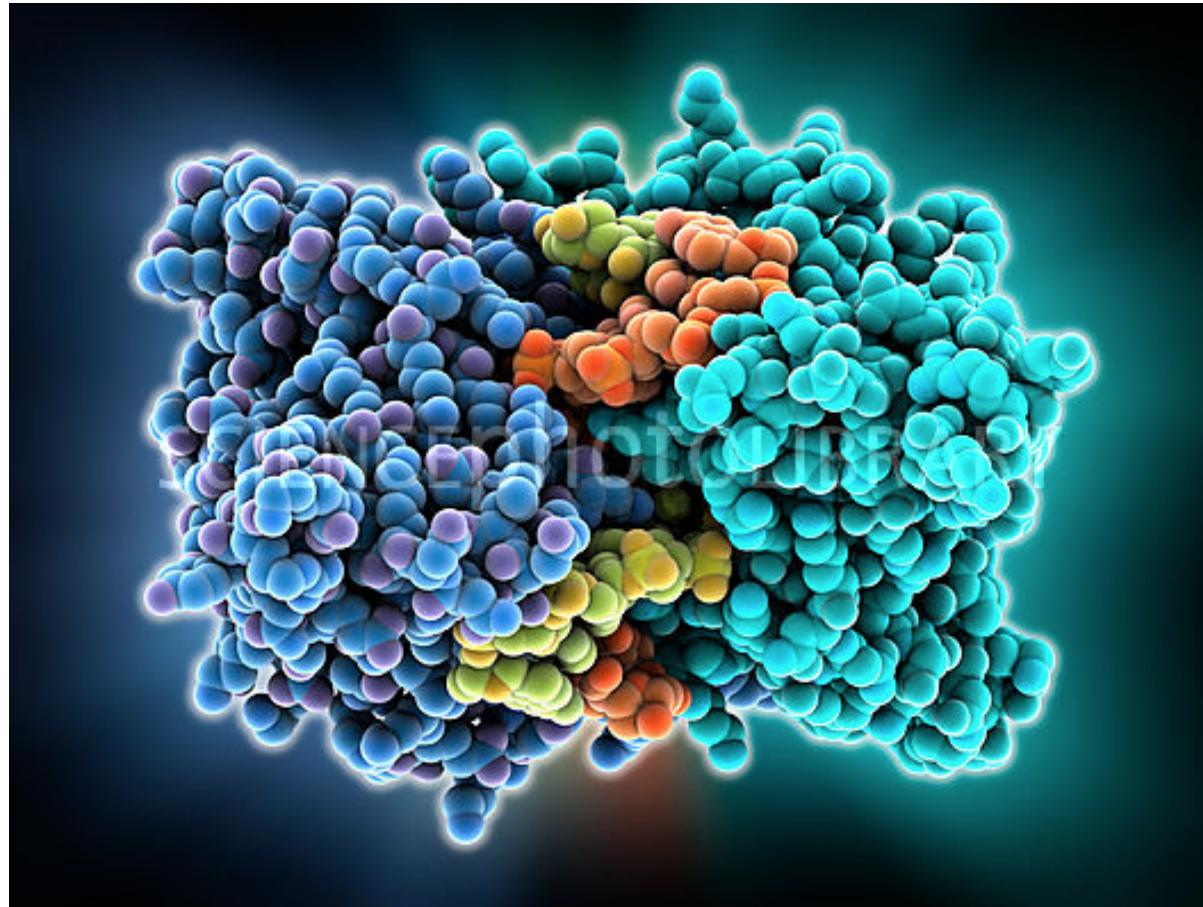


<https://3dprint.com/116569/self-driving-cars-privacy/>

# Applications of Point Set Learning

- Molecular Biology

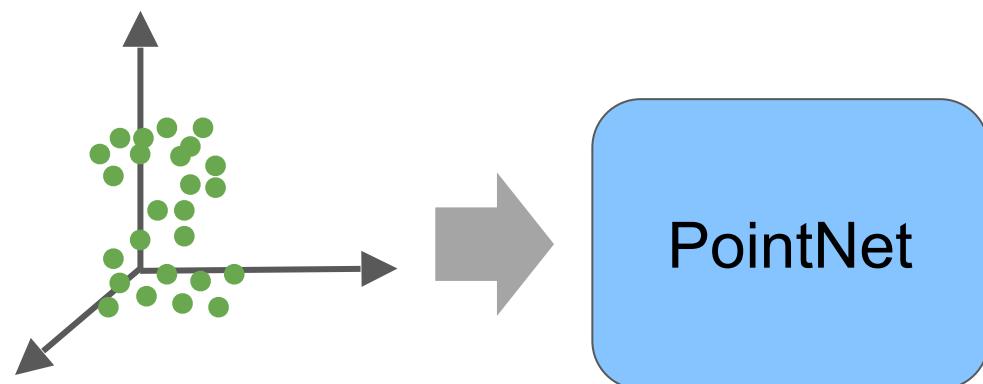
Can we infer an enzyme's category (reactions they catalyze) from its structure?



*EcoRV restriction enzyme molecule, LAGUNA DESIGN/SCIENCE PHOTO LIBRARY*

# Directly process point cloud data

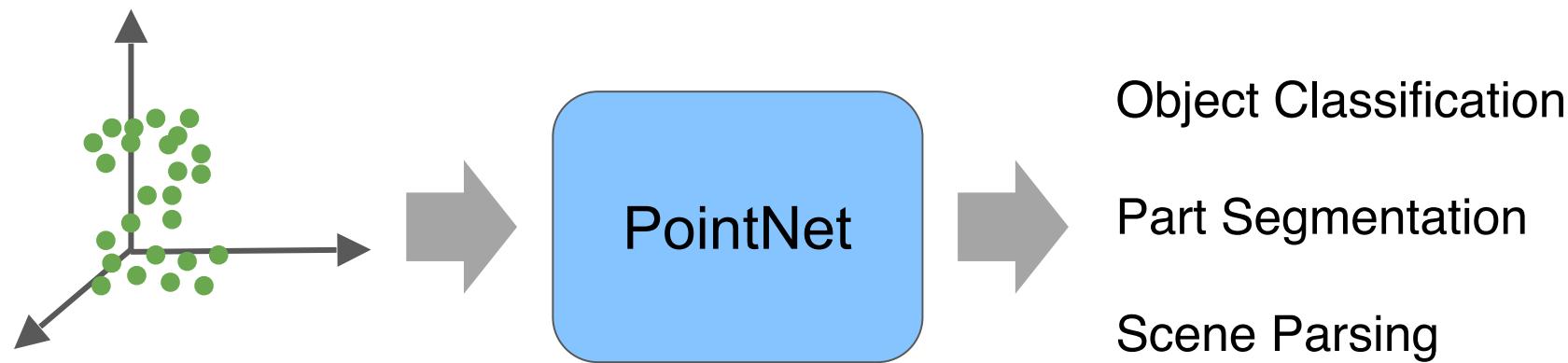
End-to-end learning for **unstructured, unordered** point data



# Directly process point cloud data

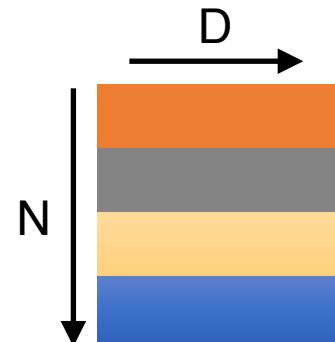
End-to-end learning for **unstructured, unordered** point data

**Unified** framework for various tasks



# Properties of a desired neural network on point clouds

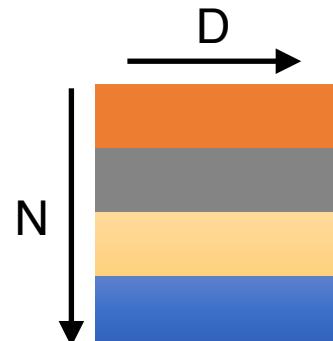
Point cloud: N **orderless** points, each represented by a D dim coordinate



2D array representation

# Properties of a desired neural network on point clouds

Point cloud: N **orderless** points, each represented by a D dim coordinate



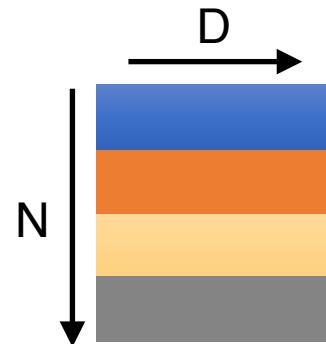
2D array representation

## Permutation invariance

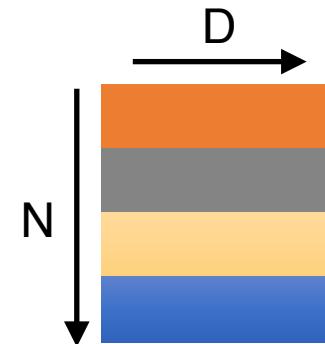
## Transformation invariance

# Properties of a desired neural network on point clouds

Point cloud: N **orderless** points, each represented by a D dim coordinate



represents the same **set** as



2D array representation

## Permutation invariance

# Permutation invariance: Symmetric function

$$f(x_1, x_2, \dots, x_n) \equiv f(x_{\pi_1}, x_{\pi_2}, \dots, x_{\pi_n}), \quad x_i \in \mathbb{R}^D$$

## Examples:

$$f(x_1, x_2, \dots, x_n) = \max\{x_1, x_2, \dots, x_n\}$$

$$f(x_1, x_2, \dots, x_n) = x_1 + x_2 + \dots + x_n$$

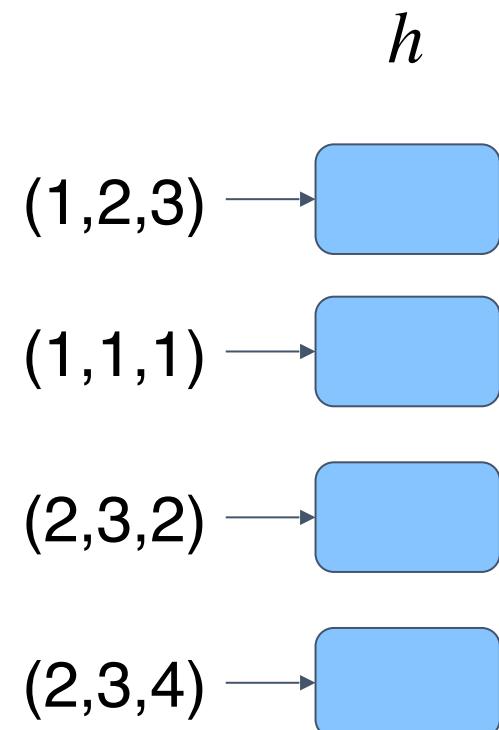
...

# Construct symmetric function family

**Observe:**  $f(x_1, x_2, \dots, x_n) = \gamma \circ g(h(x_1), \dots, h(x_n))$  is symmetric if  $g$  is symmetric

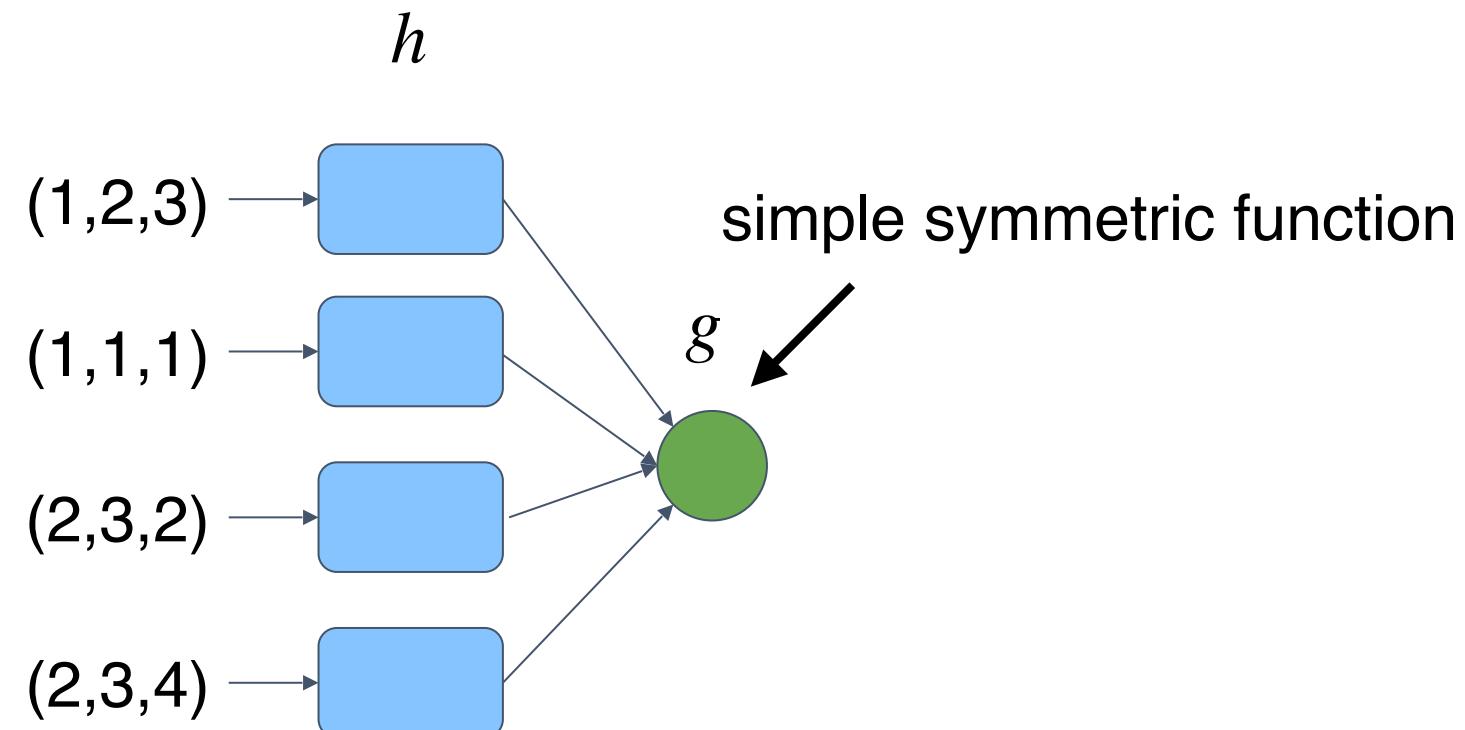
# Construct symmetric function family

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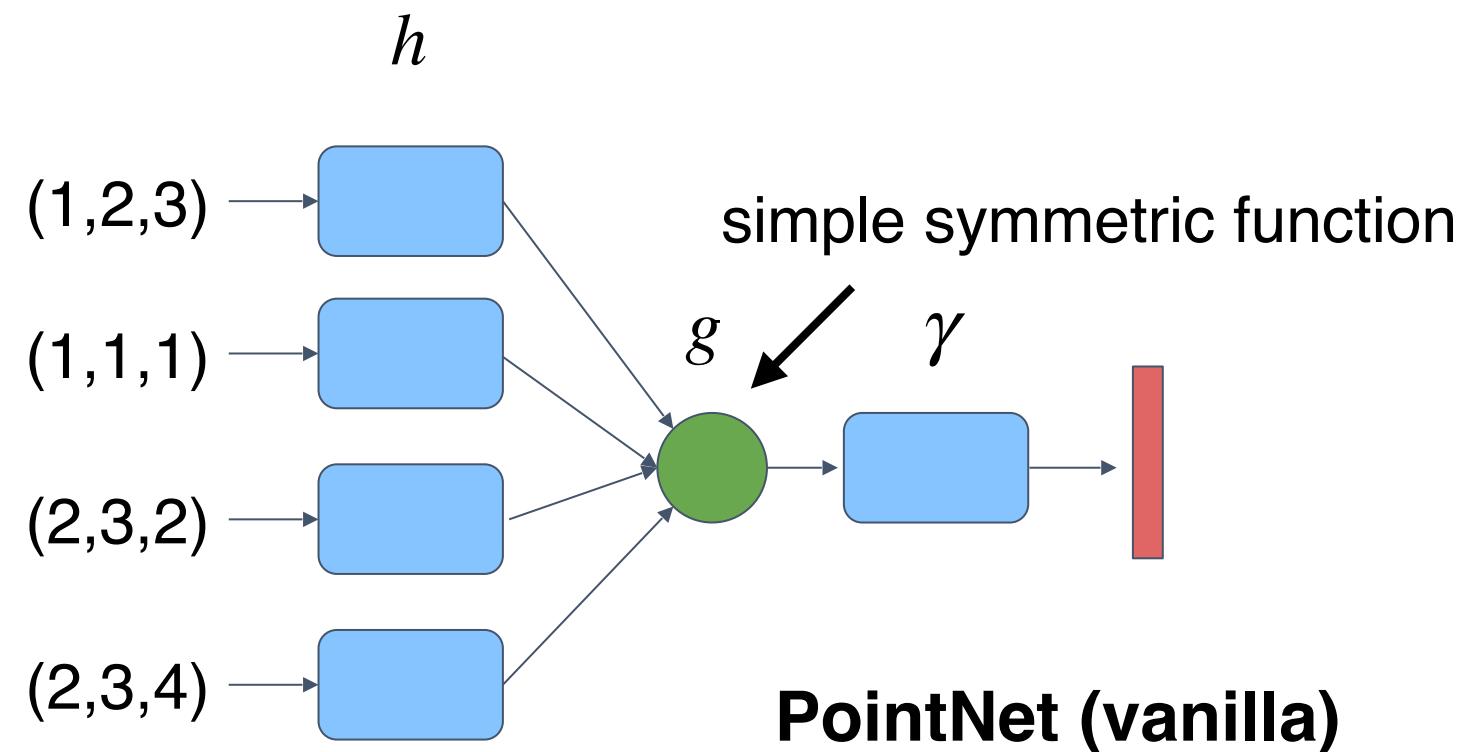
# Construct symmetric function family

**Observe:**  $f(x_1, x_2, \dots, x_n) = \gamma \circ g(h(x_1), \dots, h(x_n))$  is symmetric if  $g$  is symmetric

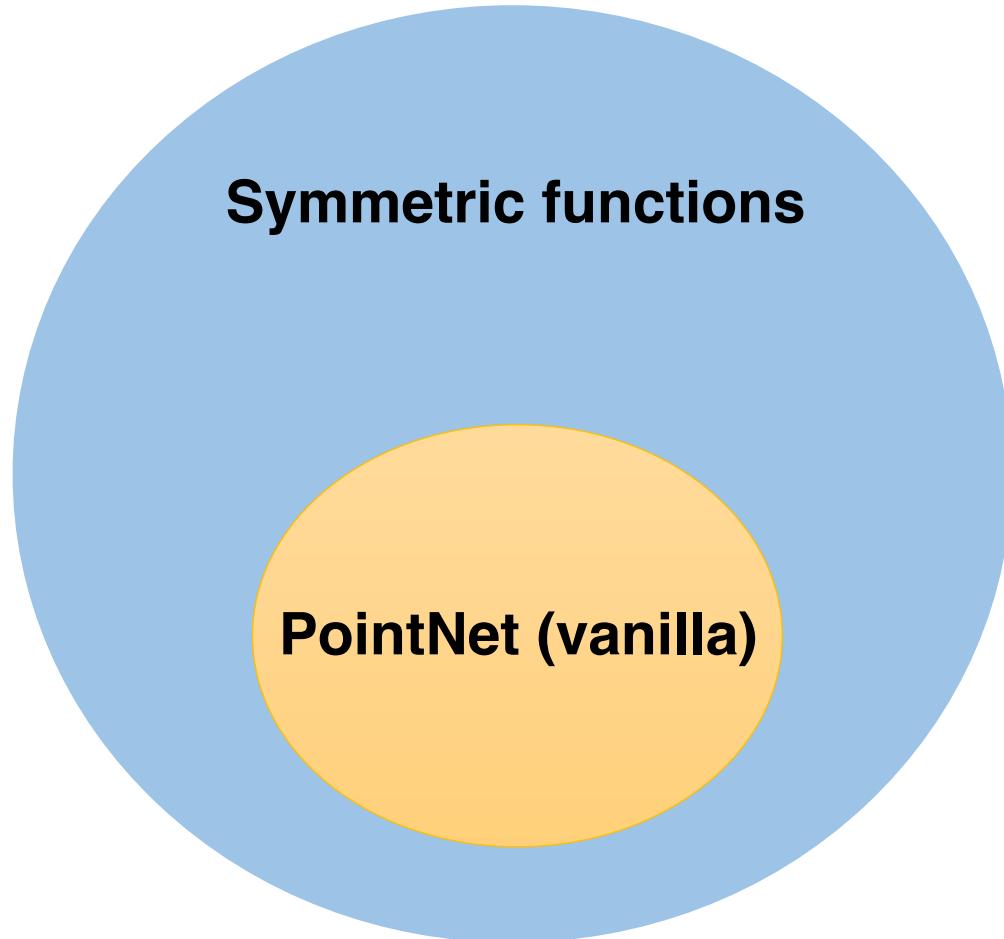


# Construct symmetric function family

**Observe:**  $f(x_1, x_2, \dots, x_n) = \gamma \circ g(h(x_1), \dots, h(x_n))$  is symmetric if  $g$  is symmetric



# Q: What symmetric functions can be constructed by PointNet?

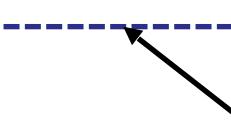


# A: Universal approximation to **continuous** symmetric functions

## Theorem:

A Hausdorff continuous symmetric function  $f : 2^X \rightarrow \mathbb{R}$  can be arbitrarily approximated by PointNet.

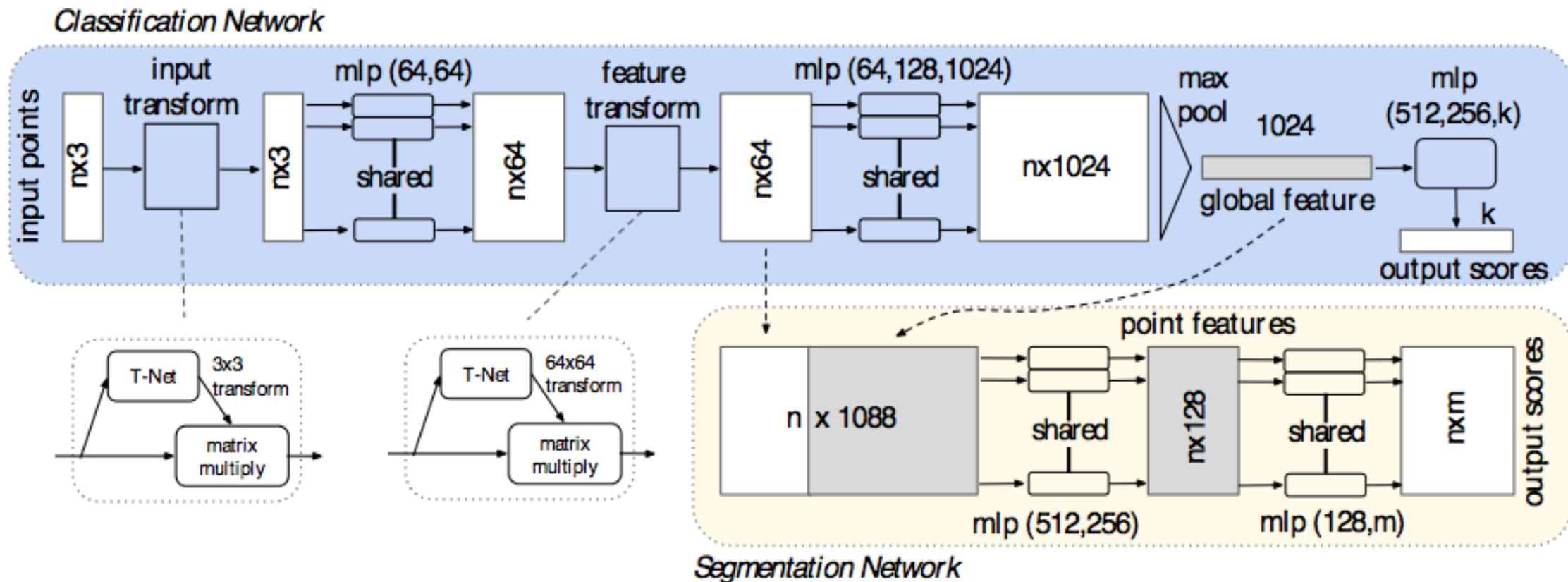
$$\left| f(S) - \gamma \left( \underset{x_i \in S}{\text{MAX}} \{ h(x_i) \} \right) \right| < \epsilon$$



$$S \subseteq \mathbb{R}^d,$$

**PointNet (vanilla)**

# PointNet Architecture

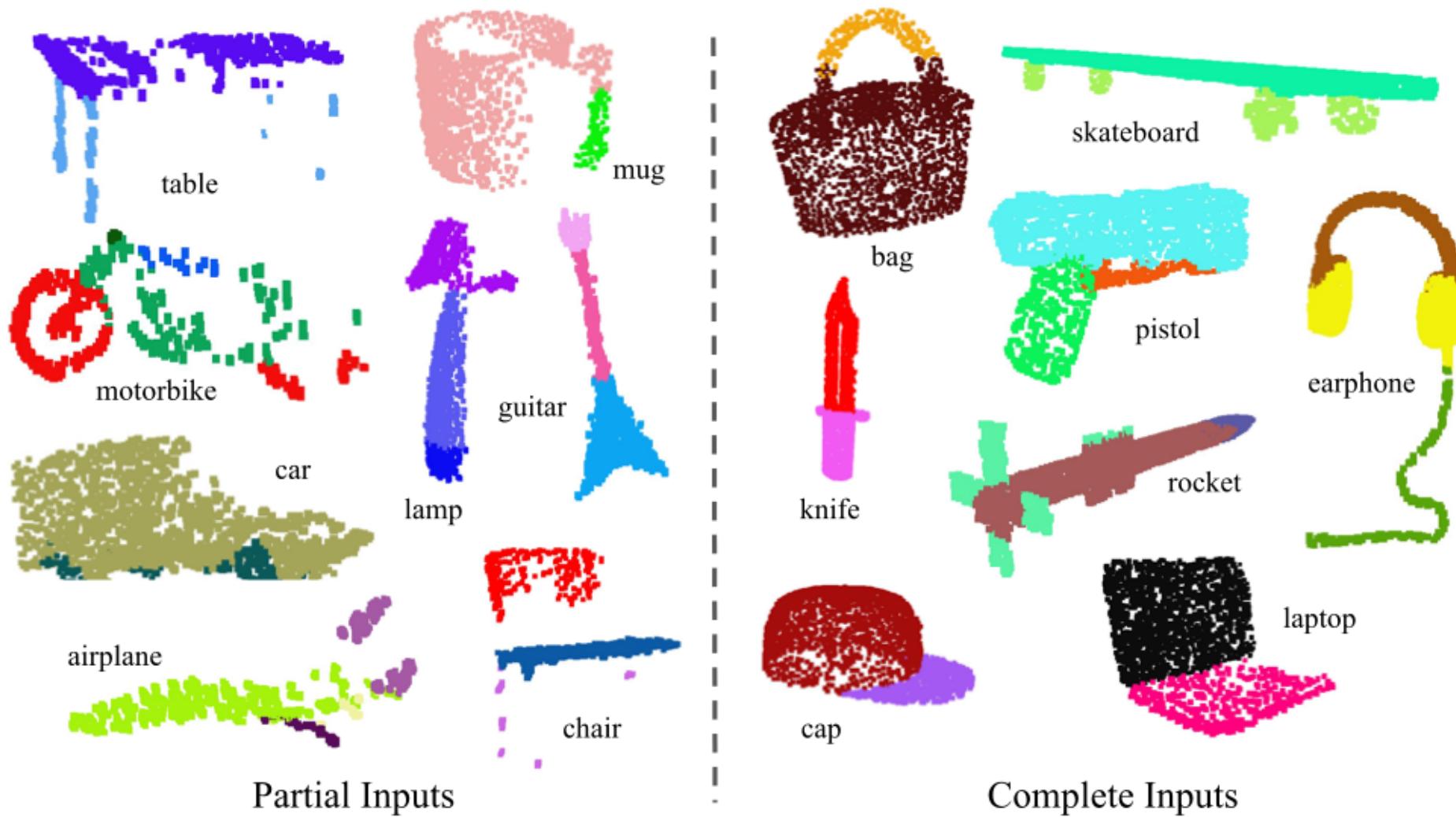


# Results on Object Classification

Object Classification Accuracy on ModelNet40

	input	#views	accuracy avg. class	accuracy overall
SPH [12]	mesh	-	68.2	-
3DShapeNets [29]	volume	1	77.3	84.7
VoxNet [18]	volume	12	83.0	85.9
Subvolume [19]	volume	20	86.0	<b>89.2</b>
LFD [29]	image	10	75.5	-
MVCNN [24]	image	80	<b>90.1</b>	-
Ours baseline	point	-	72.6	77.4
Ours PointNet	point	1	86.2	<b>89.2</b>

# Results on Object Part Segmentation



# Results on Object Part Segmentation

Part Segmentation mIoU on ShapeNet Part Dataset

	mean	aero	bag	cap	car	chair	ear phone	guitar	knife	lamp	laptop	motor	mug	pistol	rocket	skate board	table
# shapes		2690	76	55	898	3758	69	787	392	1547	451	202	184	283	66	152	5271
Wu [28]	-	63.2	-	-	-	73.5	-	-	-	74.4	-	-	-	-	-	-	74.8
Yi [30]	81.4	81.0	78.4	77.7	<b>75.7</b>	87.6	61.9	<b>92.0</b>	85.4	<b>82.5</b>	<b>95.7</b>	<b>70.6</b>	91.9	<b>85.9</b>	53.1	69.8	75.3
3DCNN	79.4	75.1	72.8	73.3	70.0	87.2	63.5	88.4	79.6	74.4	93.9	58.7	91.8	76.4	51.2	65.3	77.1
Ours	<b>83.7</b>	<b>83.4</b>	<b>78.7</b>	<b>82.5</b>	74.9	<b>89.6</b>	<b>73.0</b>	91.5	<b>85.9</b>	80.8	95.3	65.2	<b>93.0</b>	81.2	<b>57.9</b>	<b>72.8</b>	<b>80.6</b>

# Results on Semantic Scene Segmentation



# Results on Semantic Scene Parsing

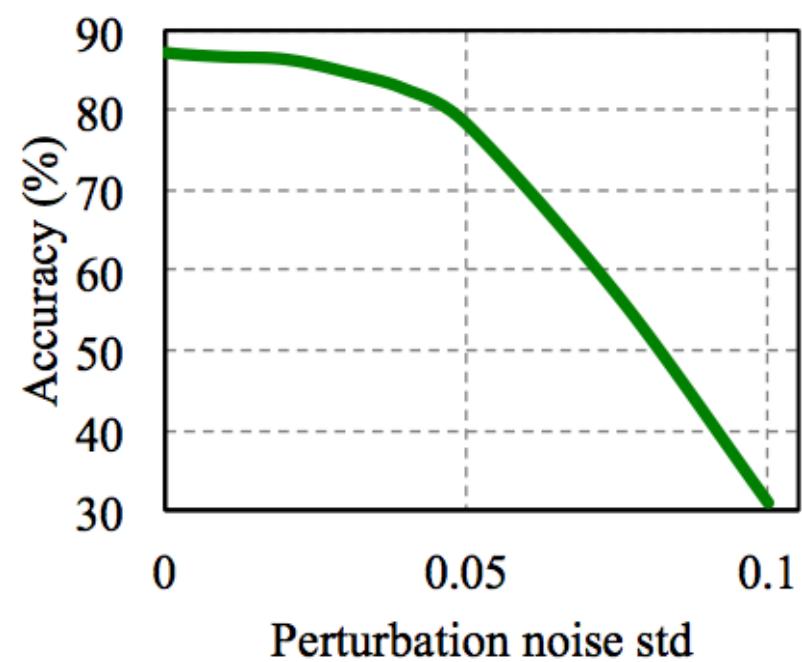
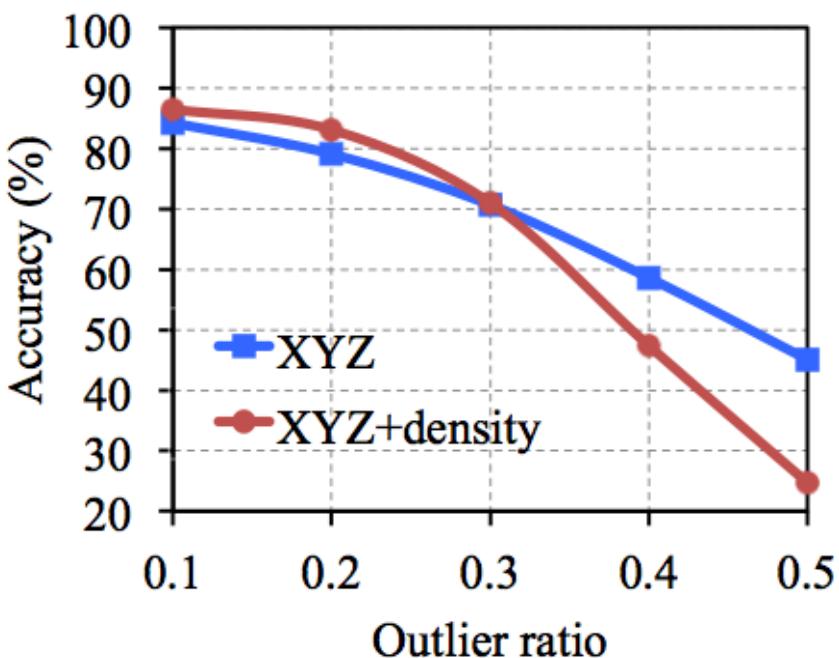
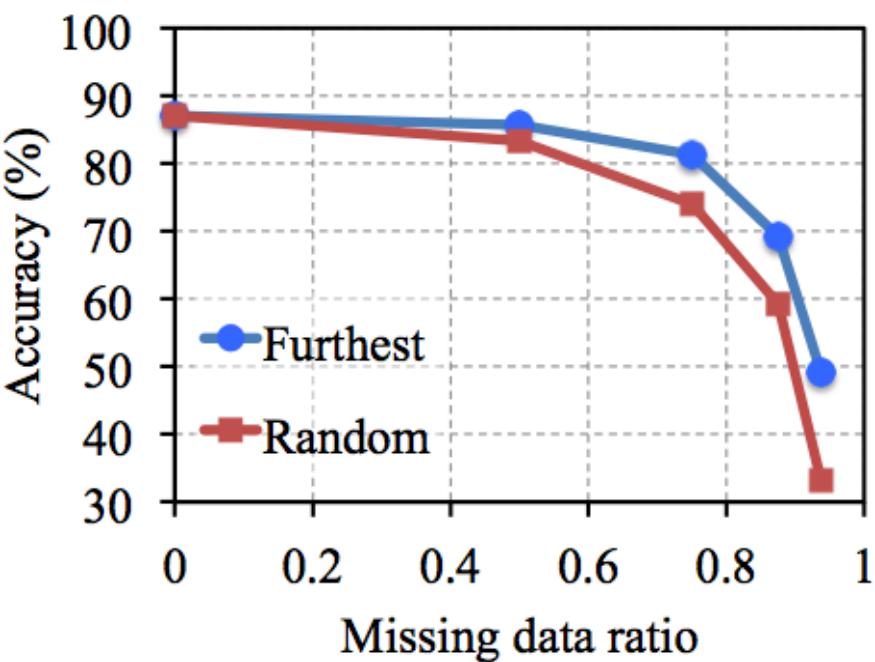
Semantic Segmentation (point based)  
on Stanford Semantic Parsing dataset

	mean IoU	overall accuracy
Ours baseline	20.12	53.19
Ours PointNet	<b>47.71</b>	<b>78.62</b>

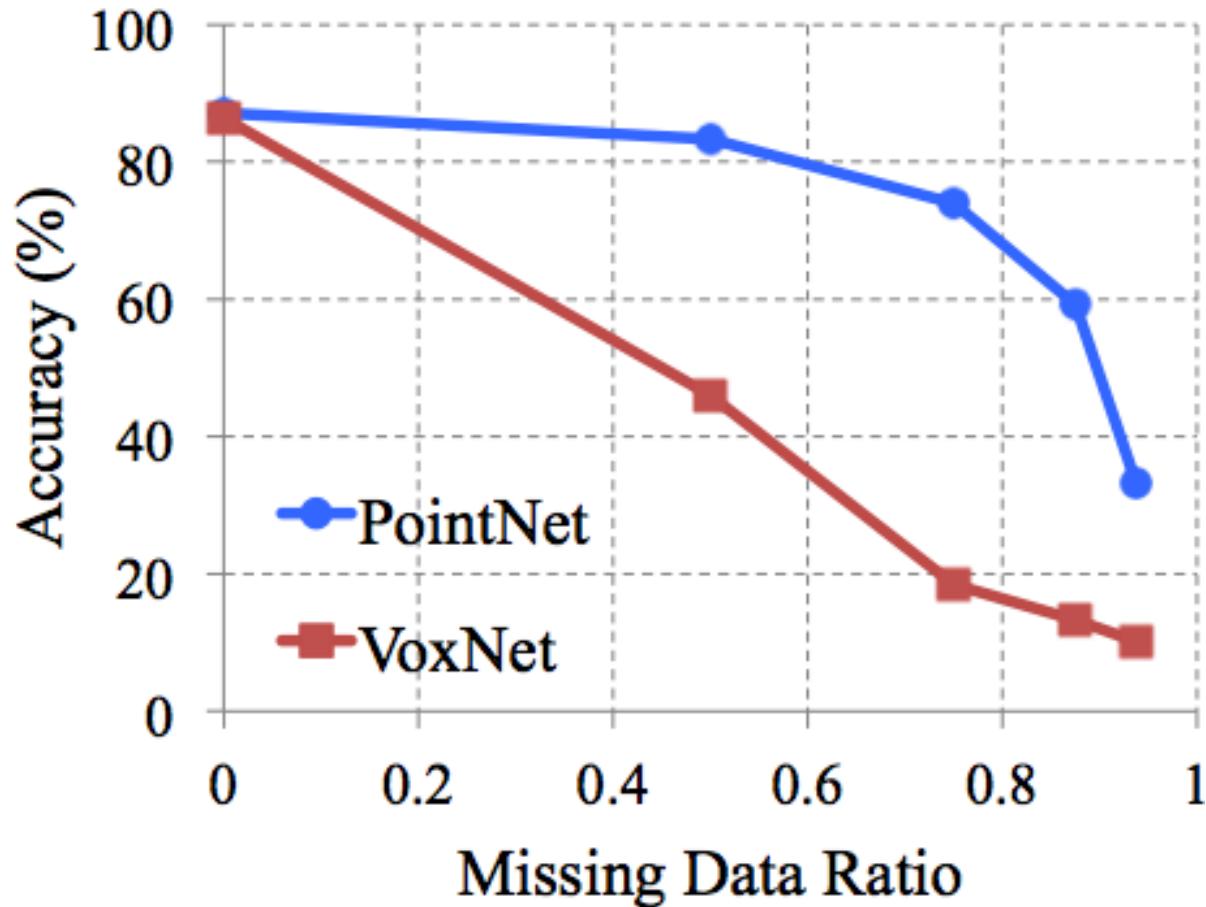
3D Object Detection (bounding box based)

	table	chair	sofa	board	mean
# instance	455	1363	55	137	
Armeni et al. [2]	46.02	16.15	<b>6.78</b>	3.91	18.22
Ours	<b>46.67</b>	<b>33.80</b>	4.76	<b>11.72</b>	<b>24.24</b>

# Robustness to Data Corruption

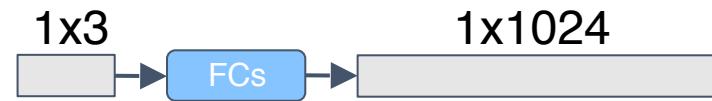


# Robustness to Data Corruption

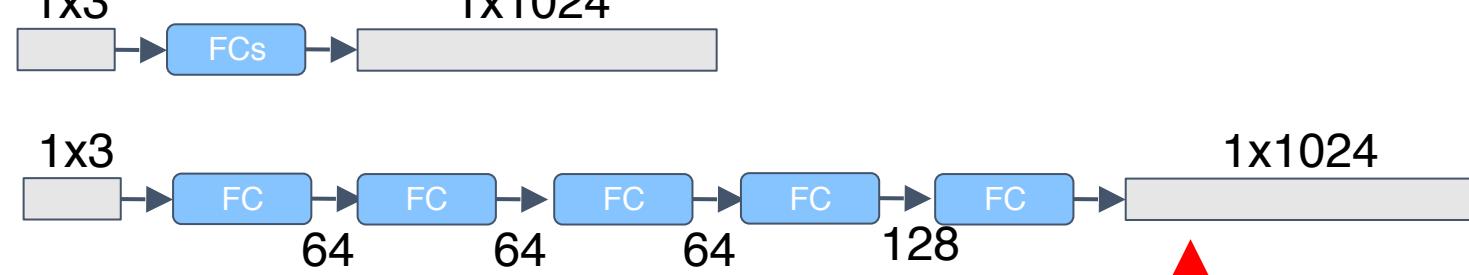


# Visualizing Point Functions

Compact View:



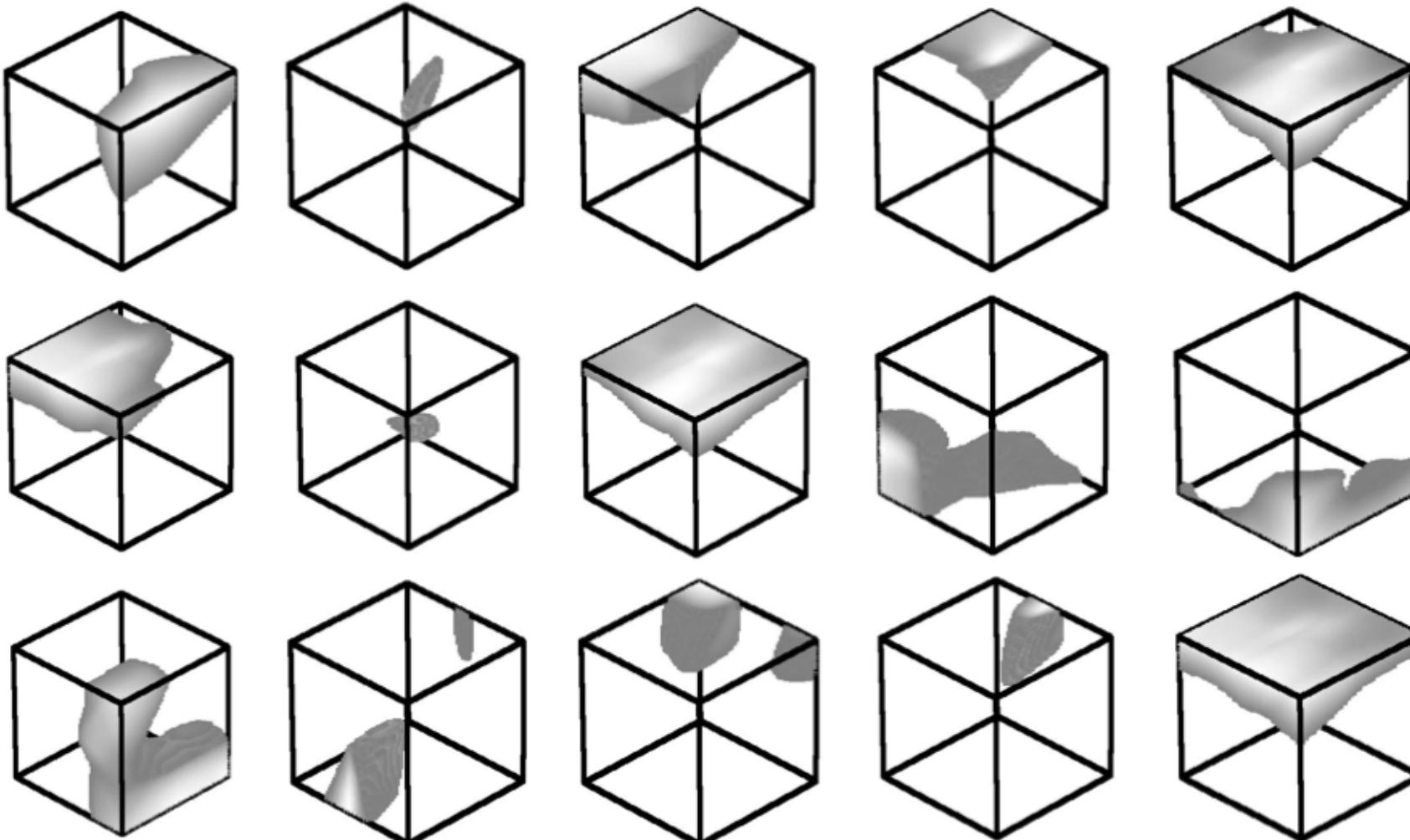
Expanded View:



**Which input point will activate neuron j?**

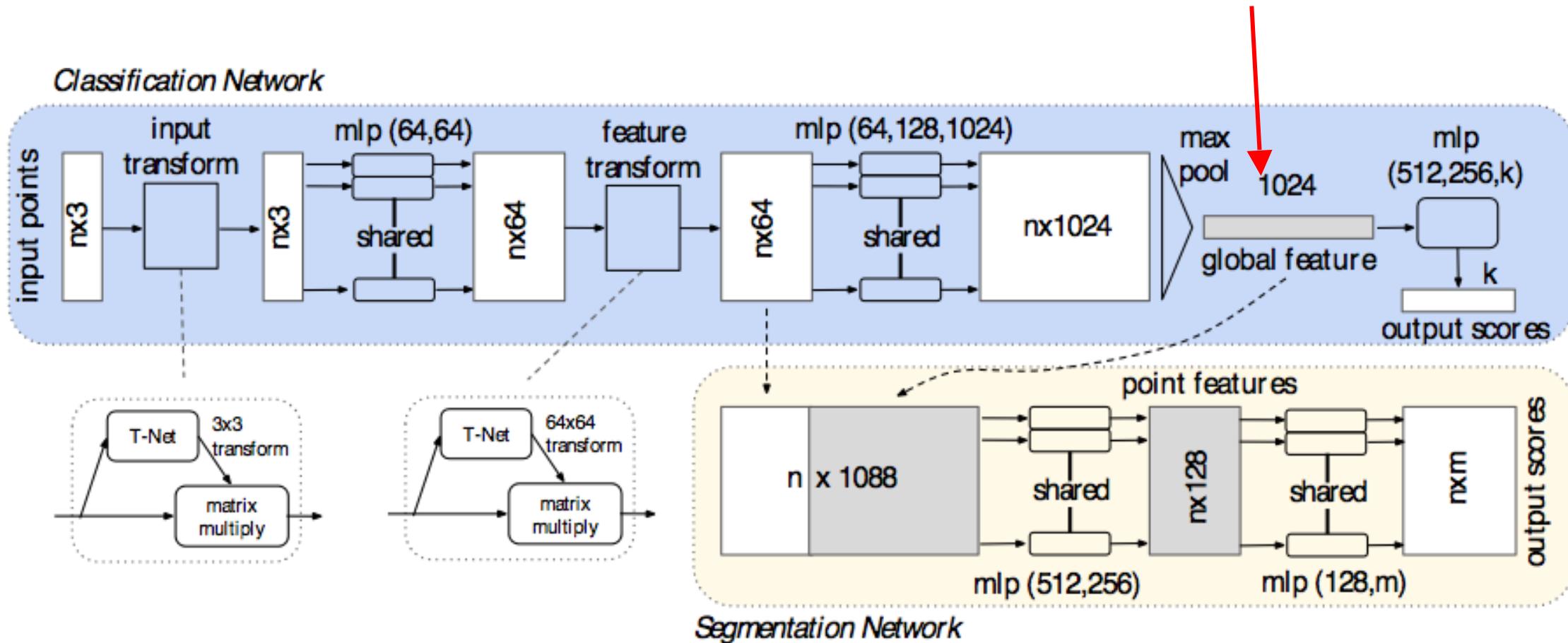
Find the top-K points in a dense volumetric grid that activates neuron j.

# Visualizing Point Functions

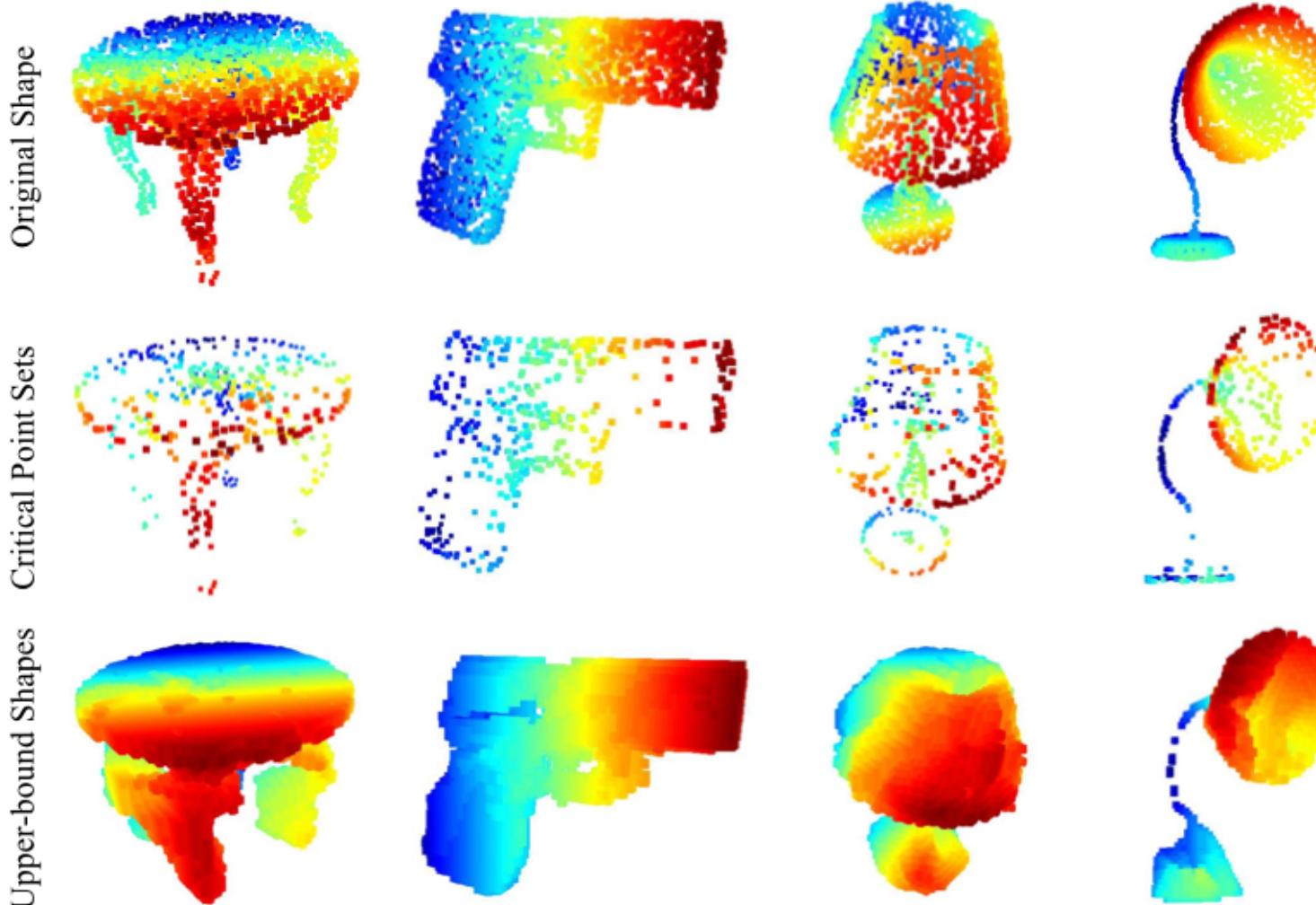


# Visualizing Global Point Cloud Features

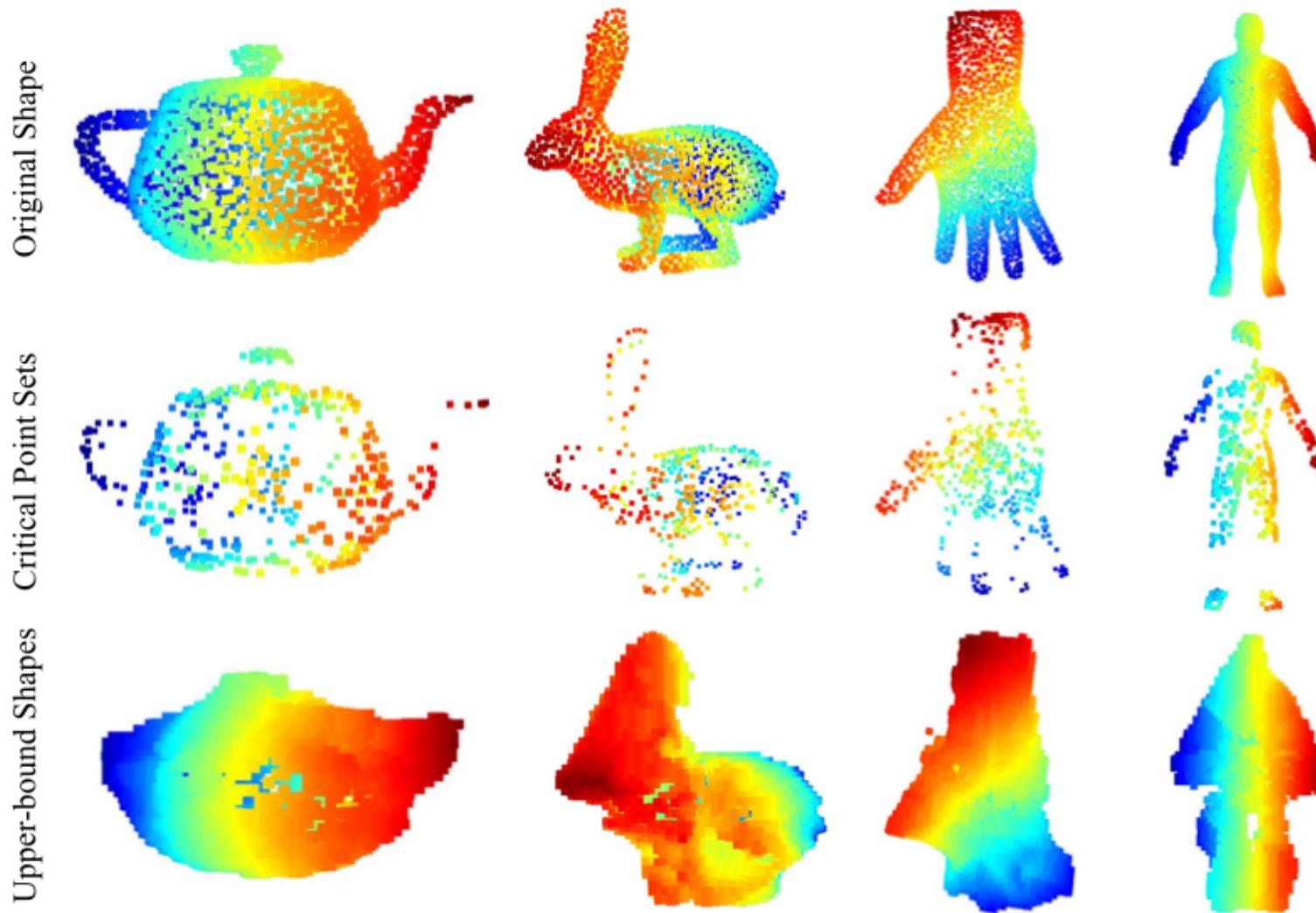
*What's captured and left out here?*



# Visualizing Global Point Cloud Features

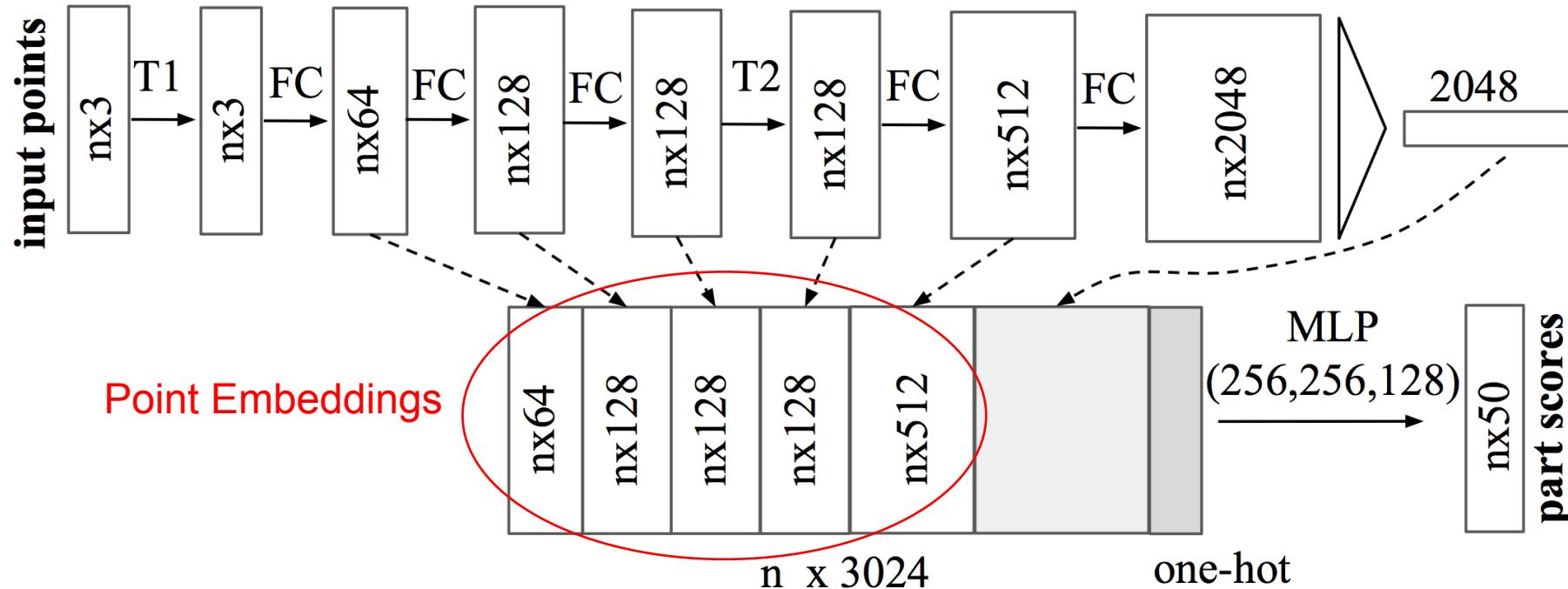


# Visualizing Global Point Cloud Features (OOS)



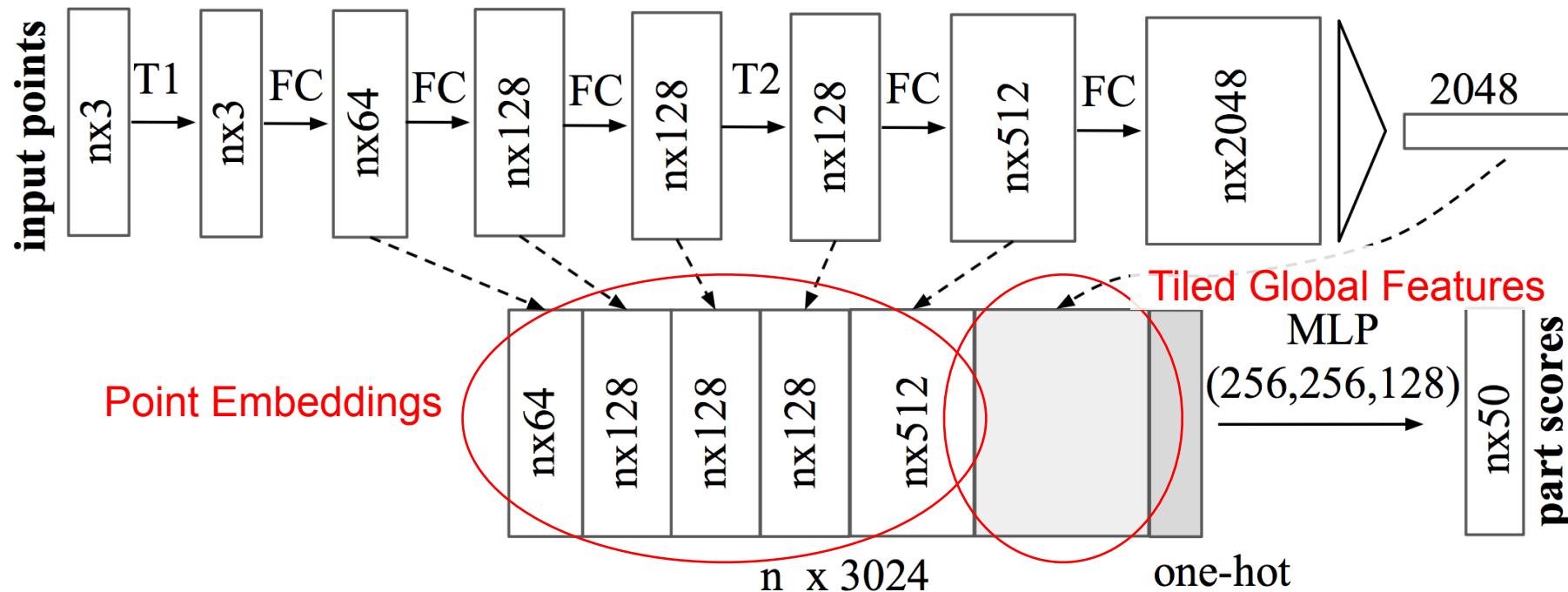
# Previous Work: PointNet v1.0

## *Segmentation Network*



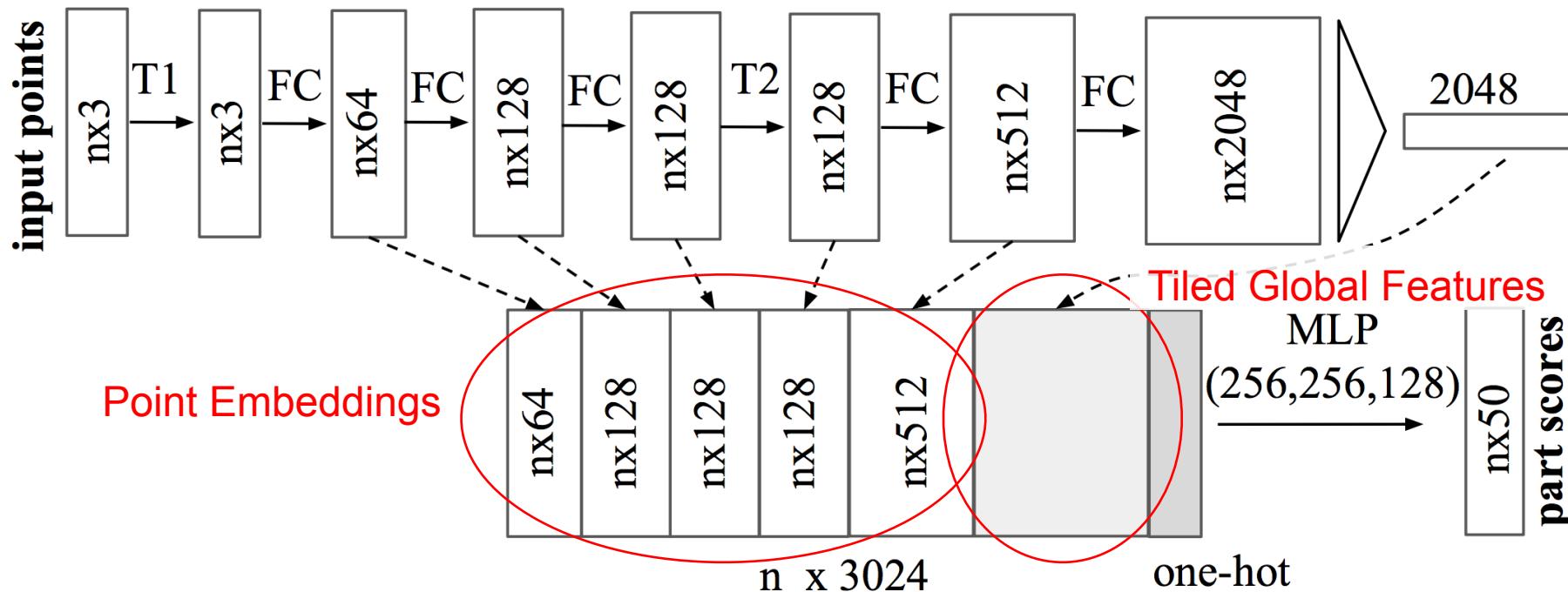
# Previous Work: PointNet v1.0

## *Segmentation Network*



# Previous Work: PointNet v1.0

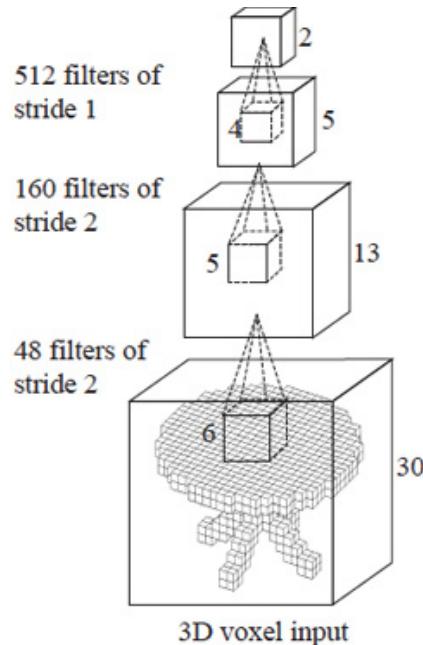
## *Segmentation Network*



- No local context for each point!

# Limitations of PointNet v1.0

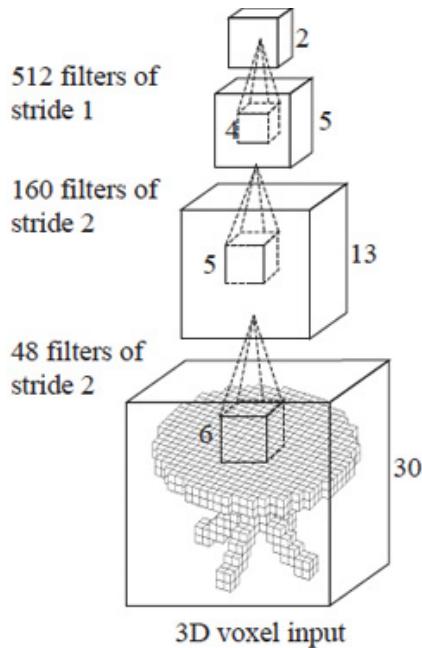
- Hierarchical Feature Learning
- Increasing receptive field



3D CNN (Wu et al.)

# Limitations of PointNet v1.0

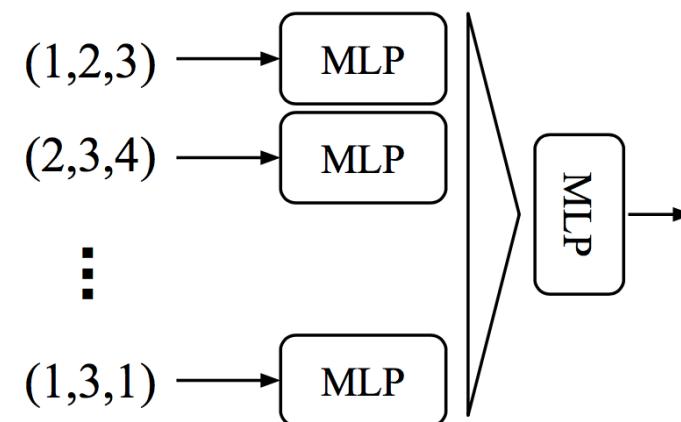
- Hierarchical Feature Learning
- Increasing receptive field



3D CNN (Wu et al.)

Global Feature Learning  
Receptive field:  
one point OR all points

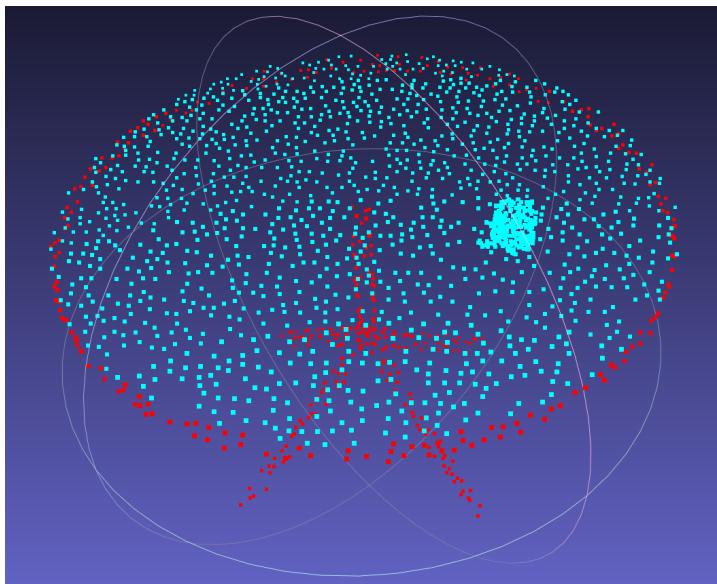
v.s.



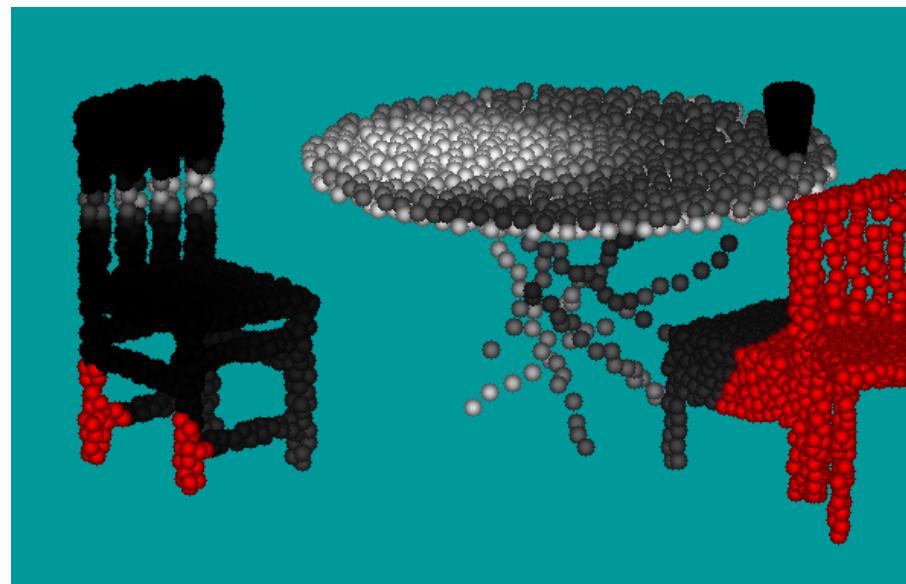
PointNet (vanilla) (Qi et al.)

# Limitations of PointNet v1.0

Artifacts in segmentation tasks:



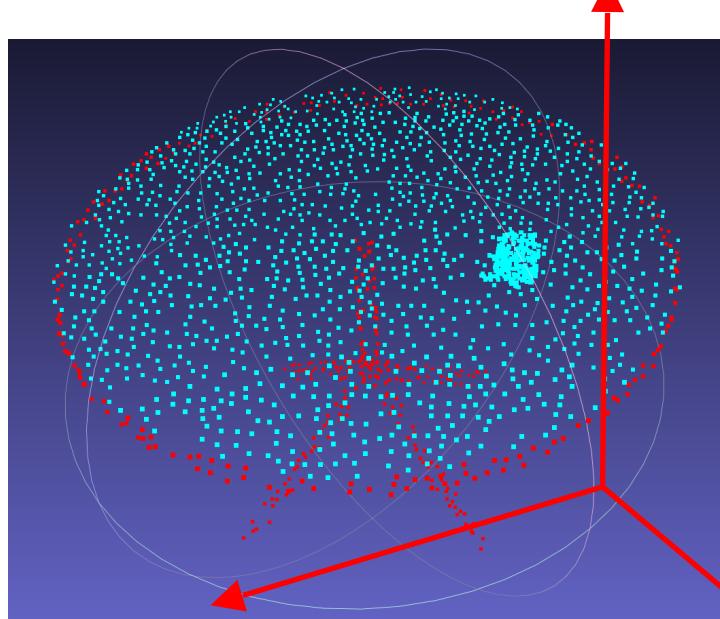
Semantic segmentation in randomly translated table-cup scene.



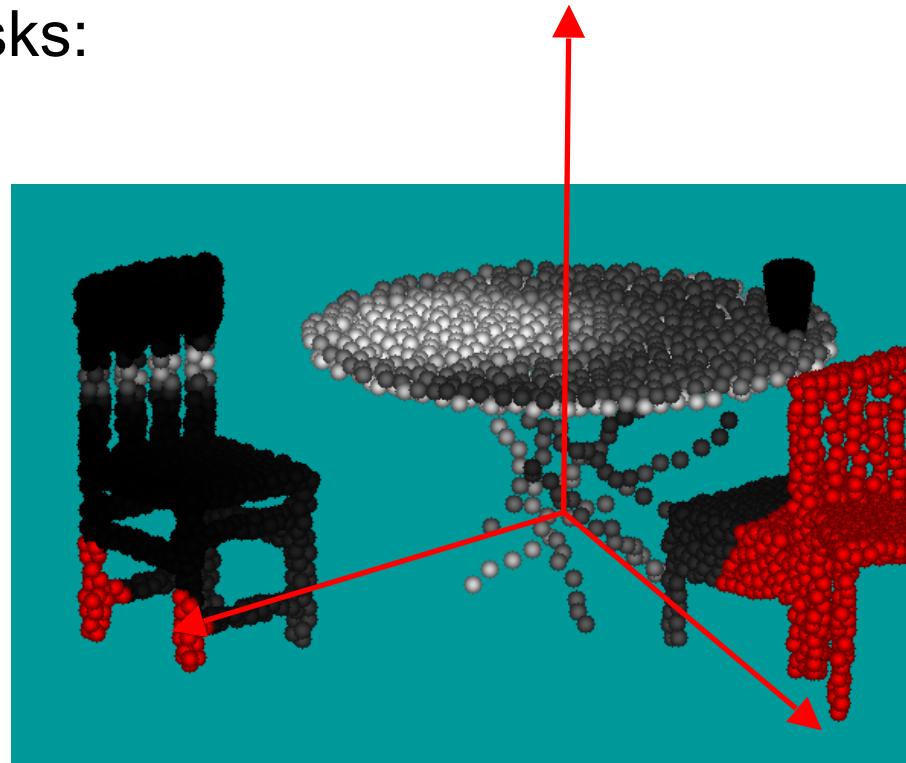
Instance segmentation in table-chair-cup scene

# Limitations of PointNet v1.0

Artifacts in segmentation tasks:



Semantic segmentation in randomly translated table-cup scene.



Instance segmentation in table-chair-cup scene

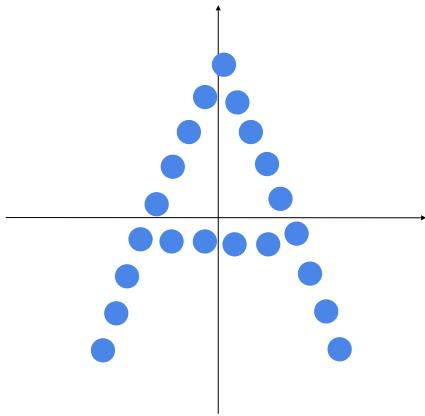
- Global feature depends on absolute XYZ!
- Hard to generalize to unseen point configurations

# Question

- How to learn local context feature for points?
- Use PointNet in local regions, aggregate local region features by PointNet again..
- 
- Hierarchical feature learning!

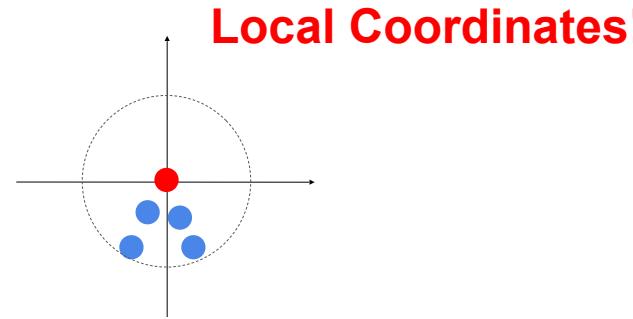
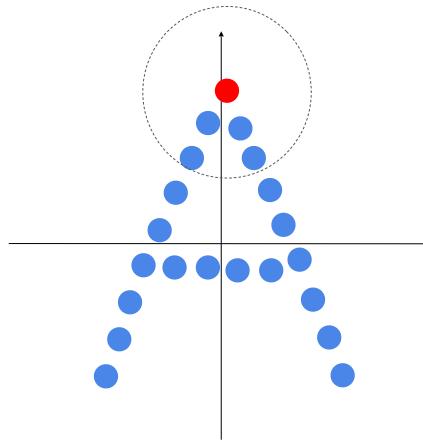
# Multi-Scale PointNet for Hierarchical Feature Learning

# PointNet v2.0: Multi-Scale PointNet

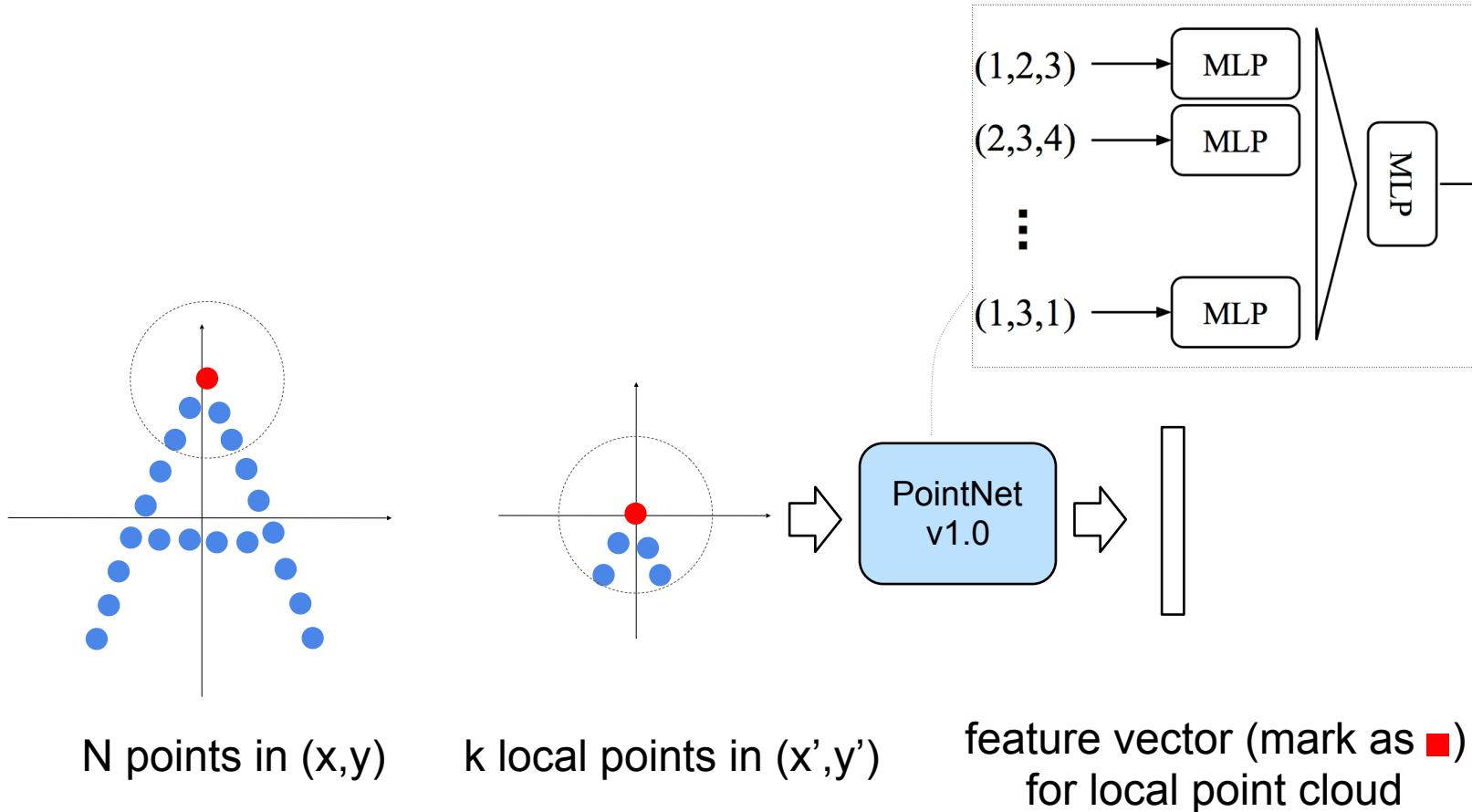


N points in (x,y)

# PointNet v2.0: Multi-Scale PointNet

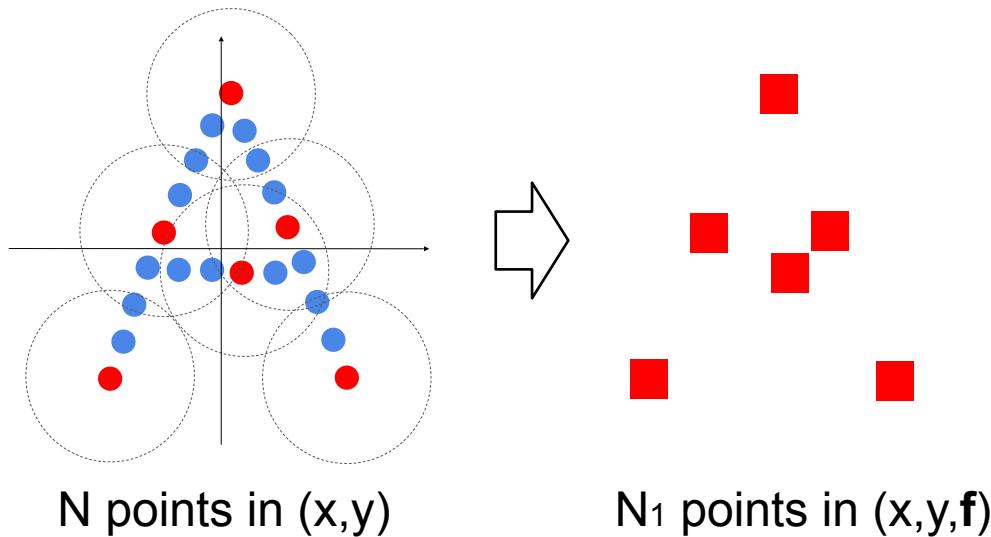


# PointNet v2.0: Multi-Scale PointNet

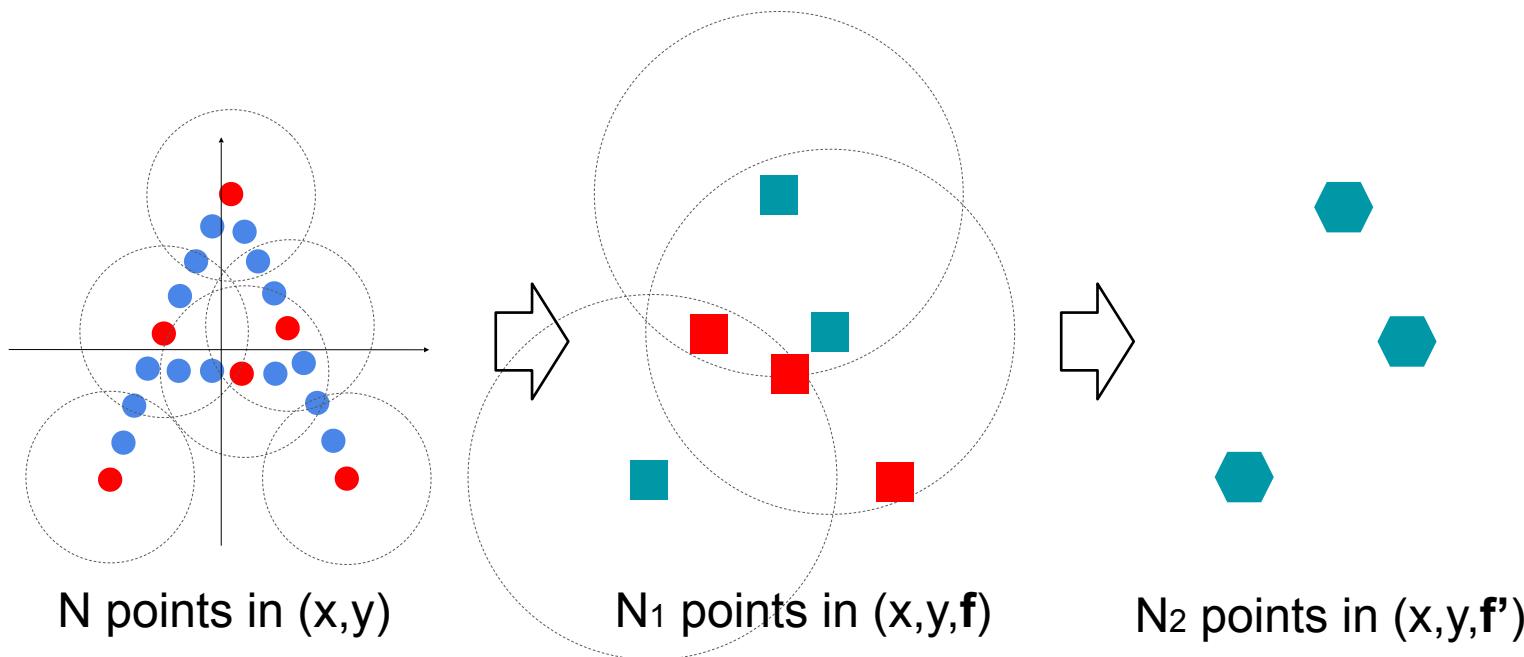


# PointNet v2.0: Multi-Scale PointNet

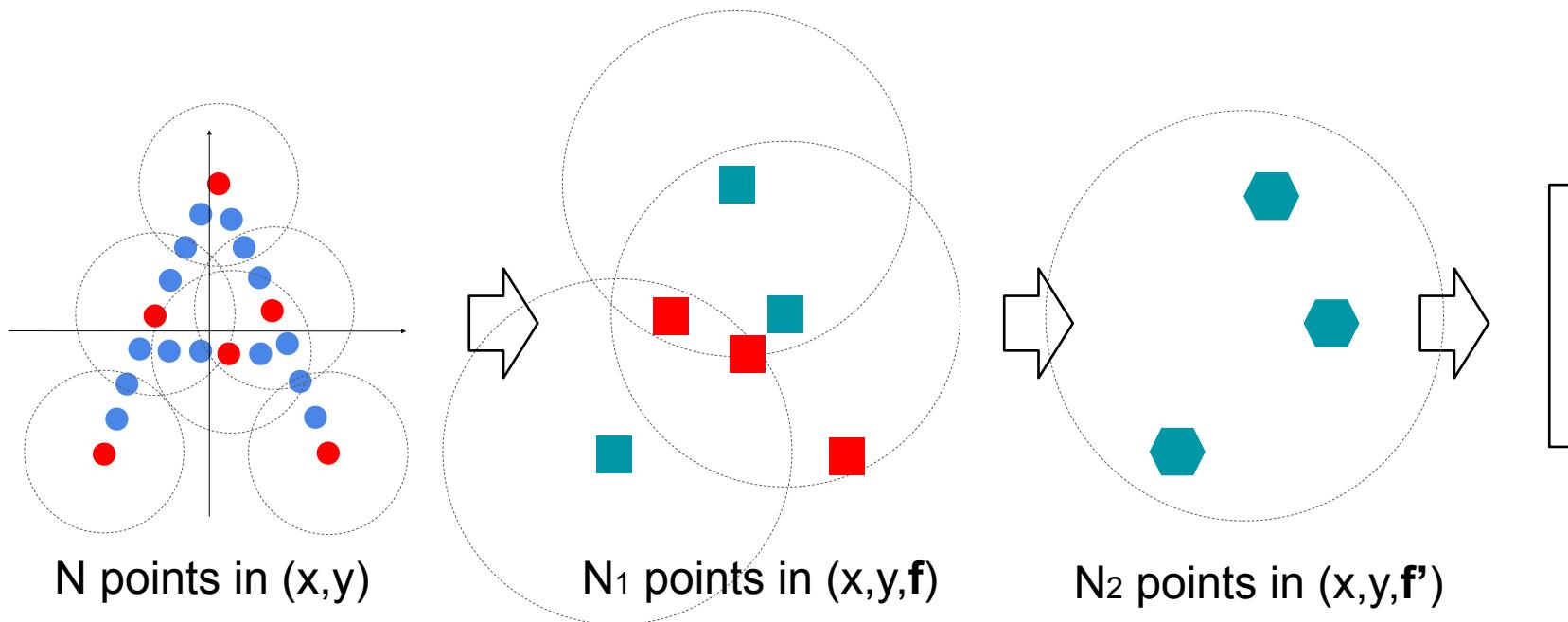
**PointNet Module/Layer:** Farthest Point Sampling + Grouping + PointNet v1.0



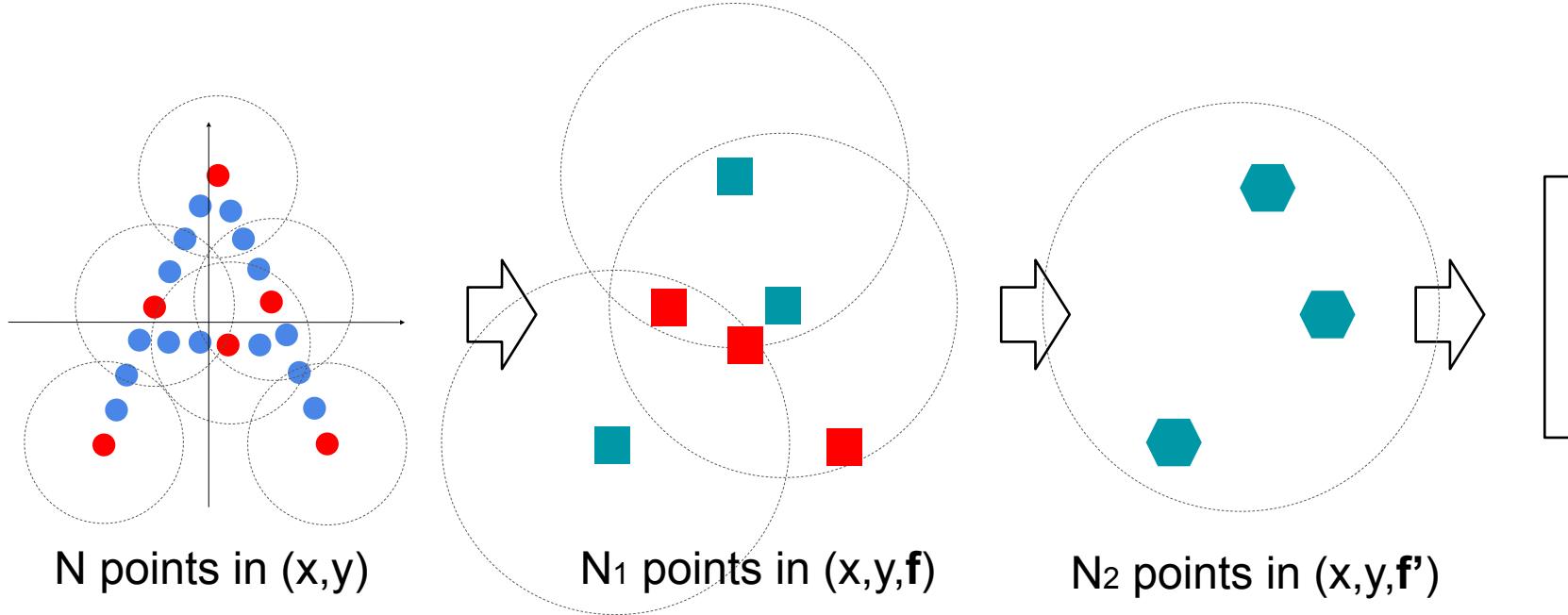
# PointNet v2.0: Multi-Scale PointNet



# PointNet v2.0: Multi-Scale PointNet



# PointNet v2.0: Multi-Scale PointNet

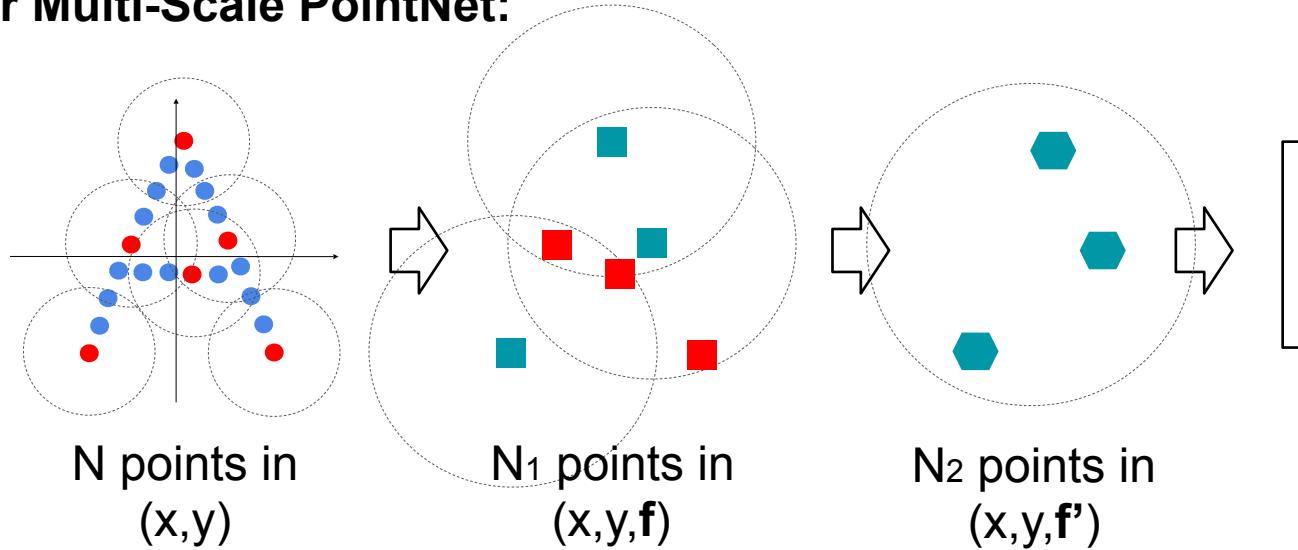


1. Larger receptive field in higher layers ✓
2. Less points in higher layers (more scalable) ✓
3. Weight sharing ✓
4. Translation invariance (local coordinates in local regions) ✓

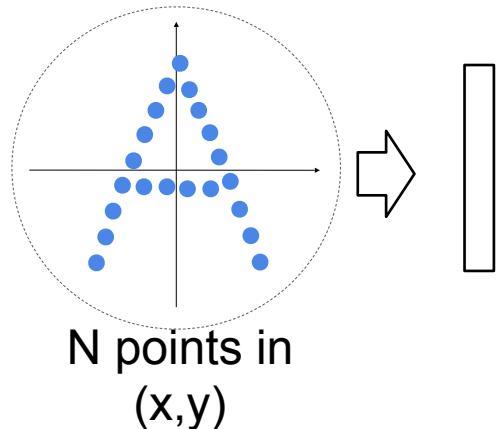
# Discussions on Multi-Scale PointNet

# Multi-Scale PointNet v.s. PointNet v1.0

**Three-layer Multi-Scale PointNet:**

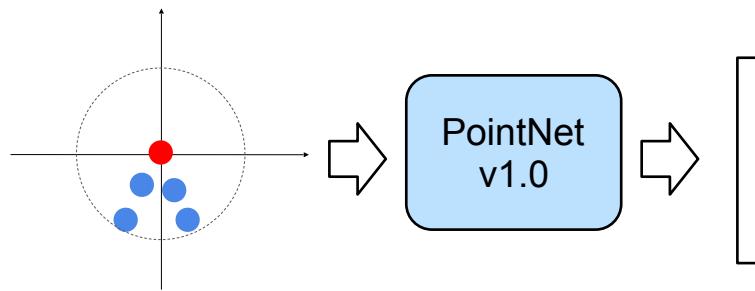


**One-layer Multi-Scale PointNet <=> PointNet v1.0**

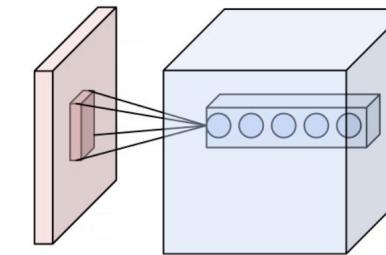


# PointNet Layer v.s. Convolution Layer

PointNet Layer



Convolution Layer



**Input:**

Point set

Dense array

**Operation:**

MLP + max pooling

Multiply and add

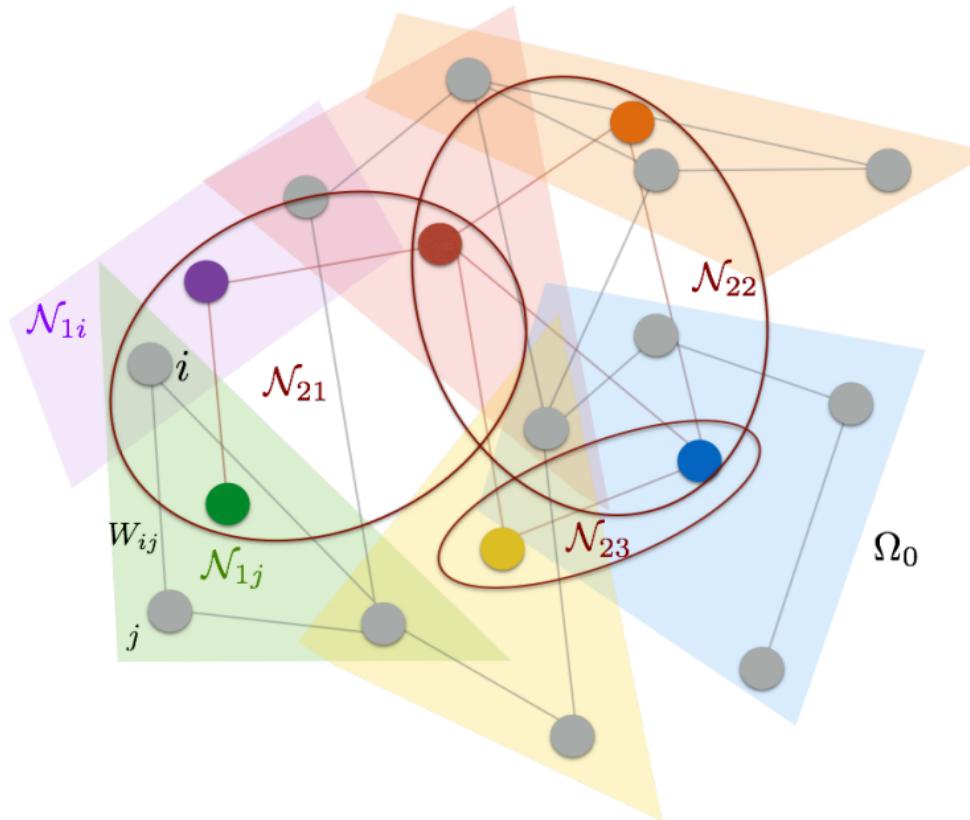
**Neighbor  
-hood:**

Distance query

Array index

# Multi-Scale PointNet v.s. Graph CNN

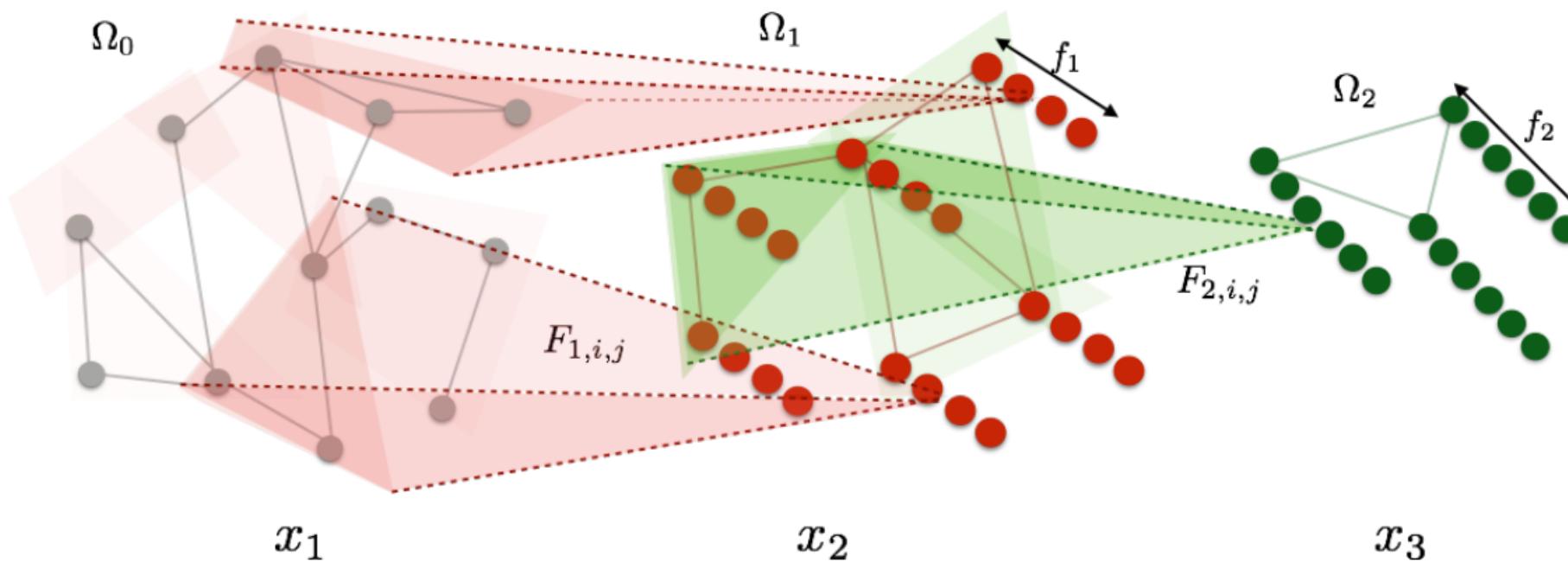
- Unexpectedly strong relation with Graph CNN:



*Joan Bruna et al. Spectral Networks and Deep Locally Connected Networks on Graphs. ICLR 2014*

# Multi-Scale PointNet v.s. Graph CNN

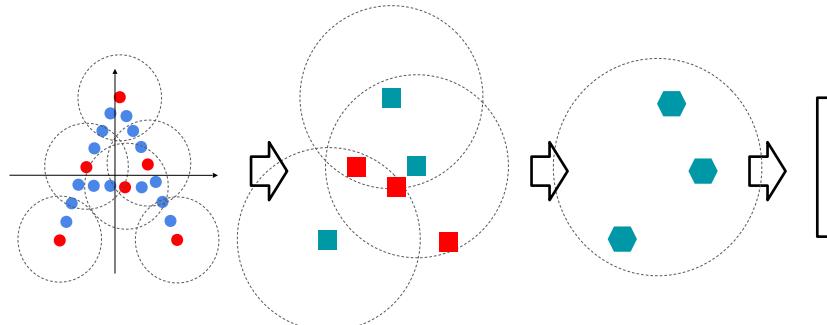
- Local feature extraction, graph coarsening, repeat..



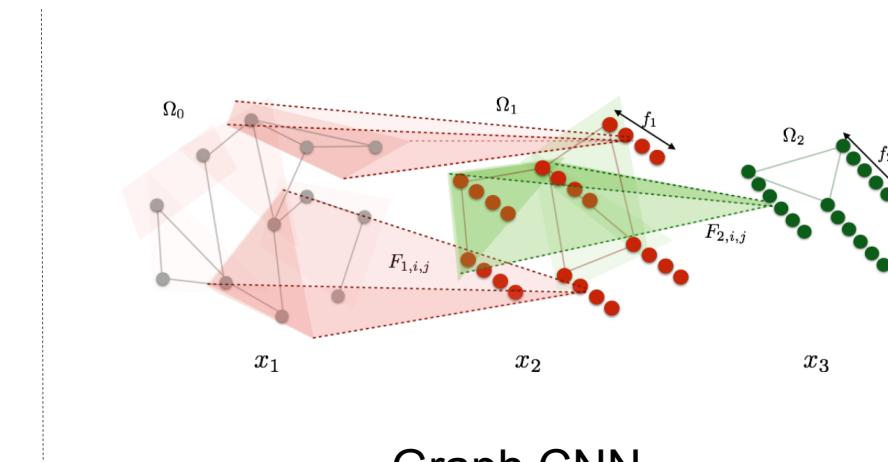
Joan Bruna et al. Spectral Networks and Deep Locally Connected Networks on Graphs. ICLR 2014

# Multi-Scale PointNet v.s. Graph CNN

- In Graph CNN's perspective:
- Multi-Scale PointNet defines
  1. Graph connectivity through Euclidean distance
  2. Graph coarsening by farthest point sampling
  3. Local feature extraction with PointNet (v1.0)



Multi-scale PointNet

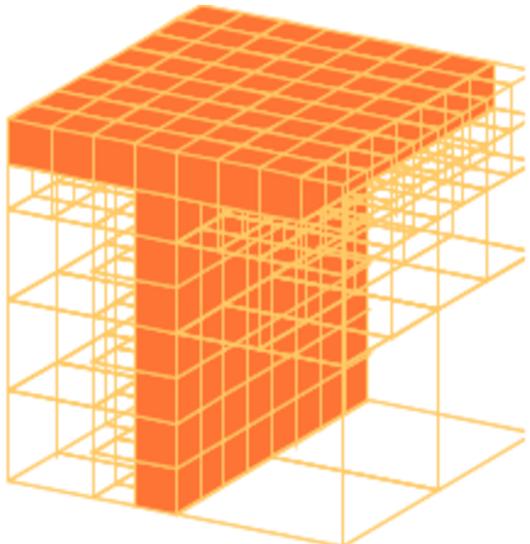


Graph CNN

# Relations to OctNet (Octree based 3D CNN)

OctNet in Graph CNN's perspective:

1. Both connectivity and graph coarsening are defined by the Octree.
2. Local feature extraction by convolution layer.



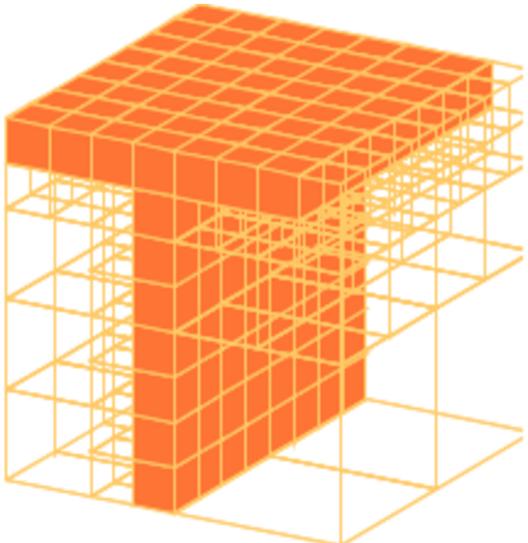
*OctNet: Learning Deep 3D Representations at High Resolutions*  
Gernot Riegler, Ali Osman Ulusoy and Andreas Geiger

# Relations to OctNet (Octree based 3D CNN)

OctNet in Graph CNN's perspective:

In Multi-Scale PointNet

1. Both connectivity and graph coarsening are **By ground distance** defined by the Octree.
2. Local feature extraction by convolution layer. **By PointNet (v1.0)**

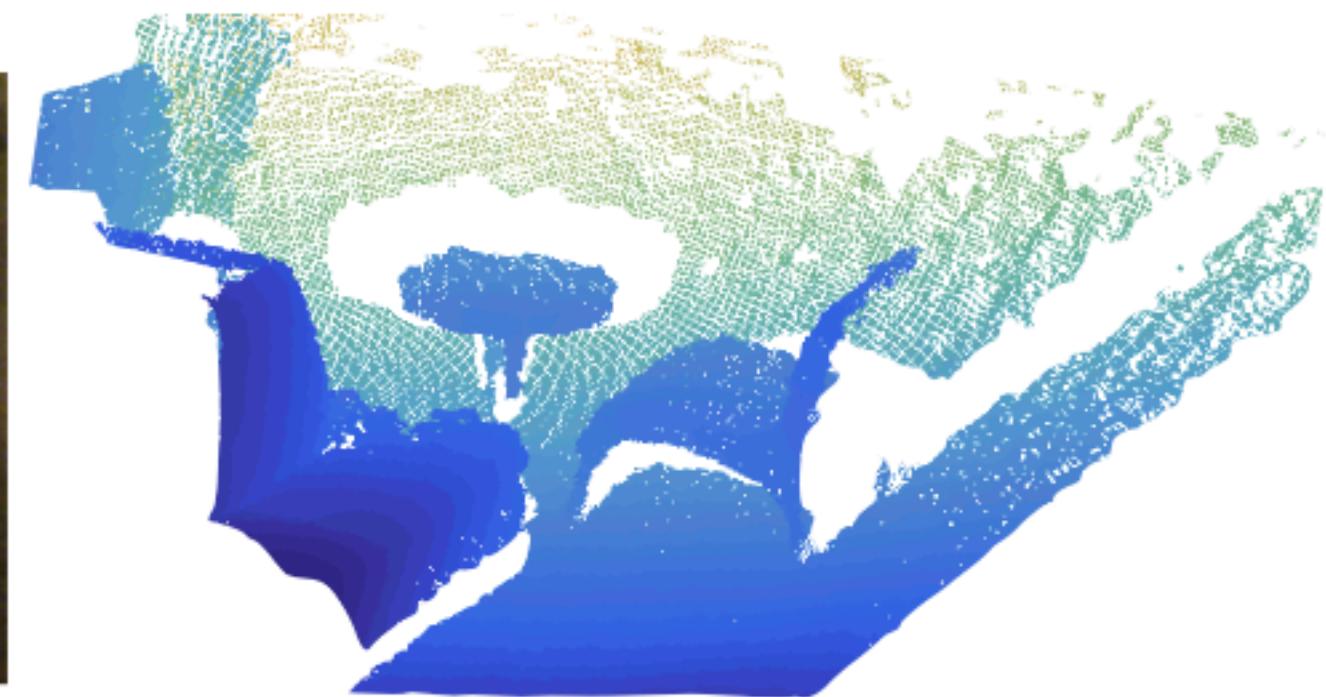


*OctNet: Learning Deep 3D Representations at High Resolutions*  
Gernot Riegler, Ali Osman Ulusoy and Andreas Geiger

# PointNet++: Addressing density variation of point cloud

Density variation is a common issue of 3D point cloud

- perspective effects, radial density variation, motion, etc



# Density variation affects hierarchy

- In CNN, small kernels are “always” better

Karen Simonyan & Andrew Zisserman, VERY DEEP CONVOLUTIONAL NETWORKS FOR LARGE-SCALE IMAGE RECOGNITION, ICLR2015

- Is it also true for point cloud learning?

# Density variation affects hierarchy

1024 points



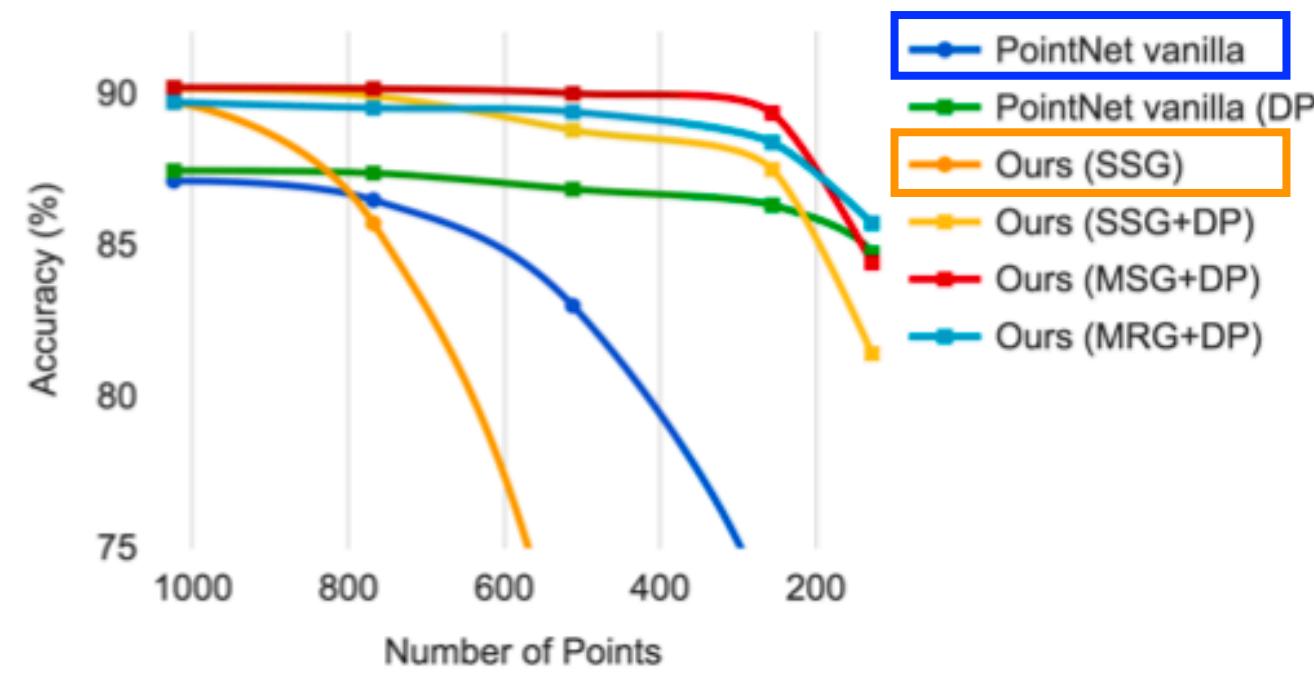
512 points



256 points



128 points

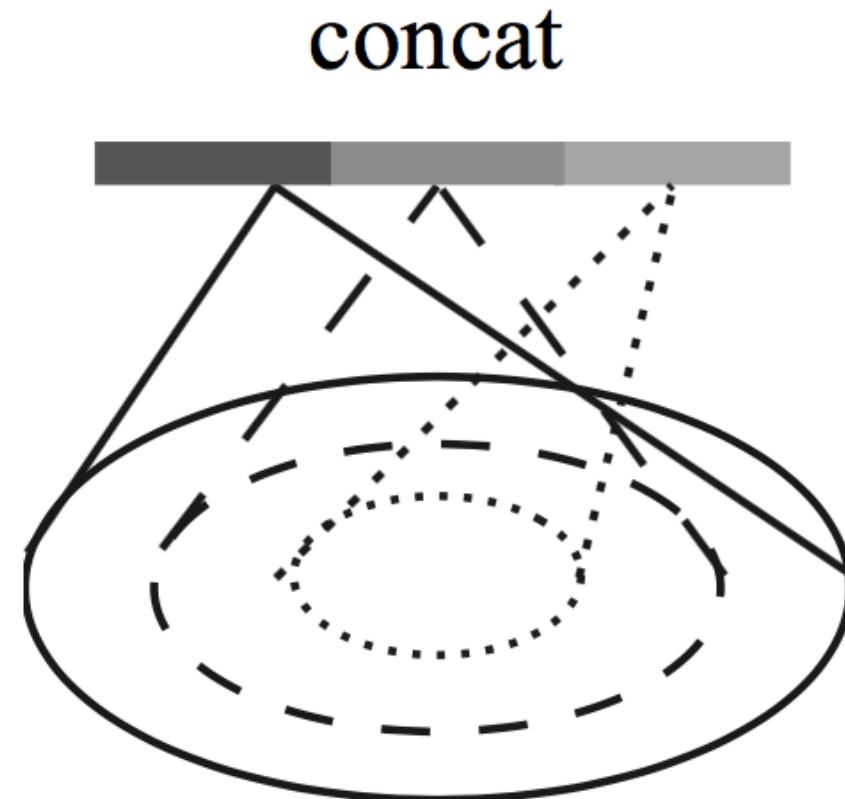


# Intuition

- At high density area, we should look more closely
- At low density area, we should look more broadly
- However, parameters at different scales cannot be shared

# Idea 1: Multi-scale grouping (MSG)

- Extract features at multiple scales and combine them
- Add random dropout to input point cloud to simulate scanning deficiency
- Dropout ratio is sampled uniformly in  $[0, 1]$



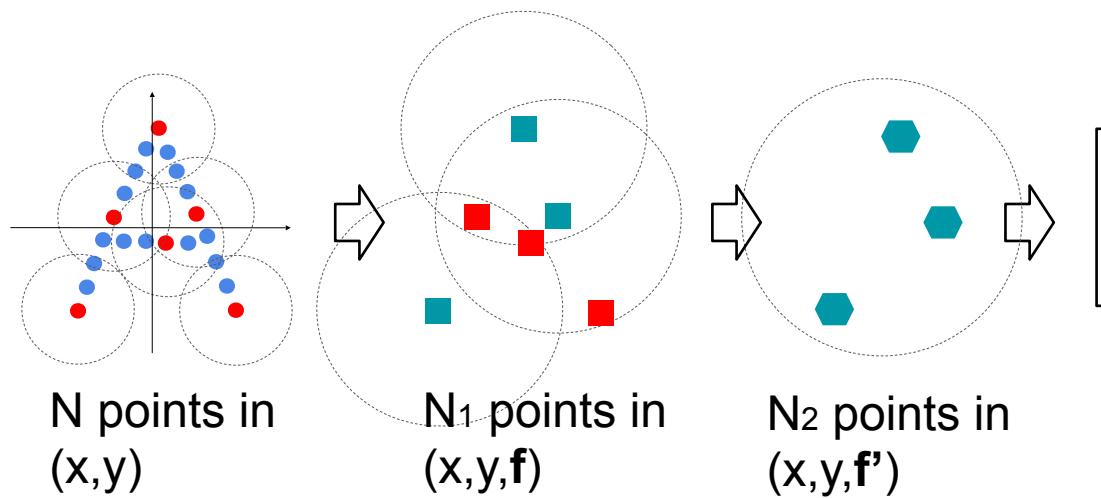
# Idea 2: Multi-resolution grouping (MRG)

- Drawback of MSG: expensive
  - Need to run PointNet on many neighborhoods
- Multi-resolution grouping: reuse the computation from different levels

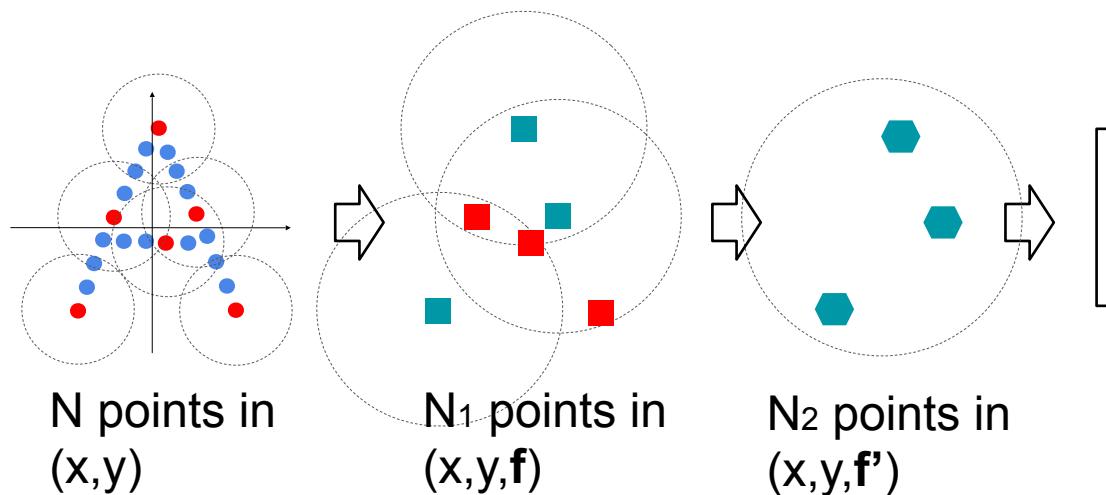


# Multi-Scale PointNet for Segmentation with “Up-convolution” Module

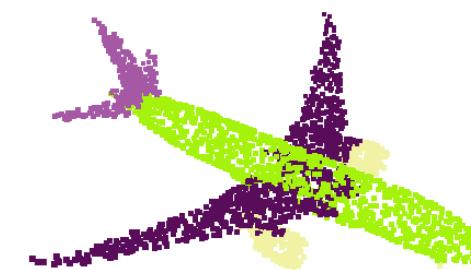
# “Up-convolution” in Multi-Scale PointNet



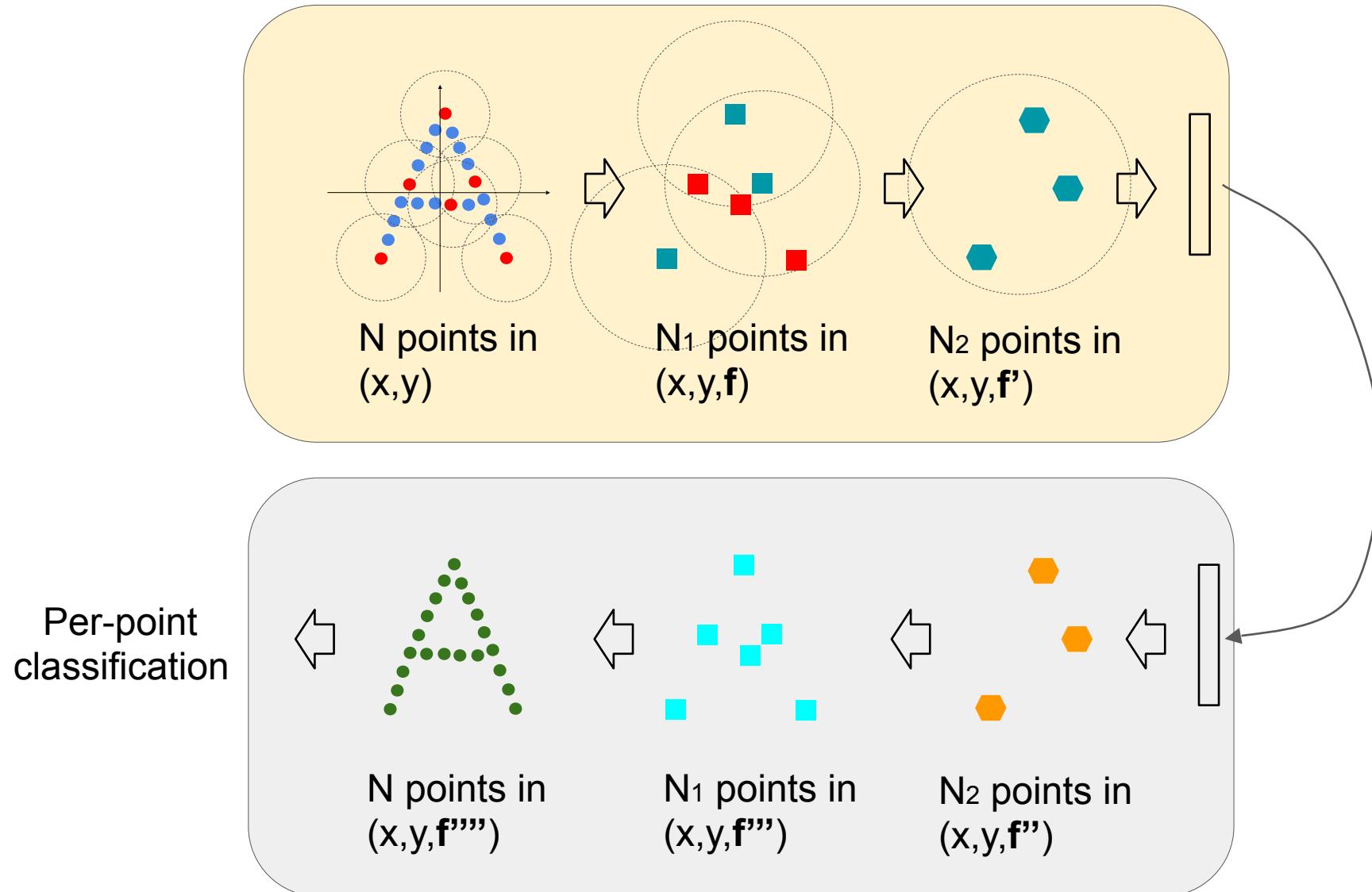
# “Up-convolution” in Multi-Scale PointNet



How to achieve segmentation?

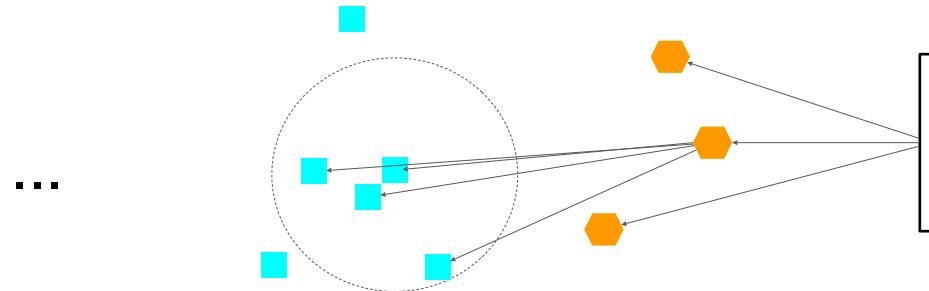


# “Up-convolution” in Multi-Scale PointNet



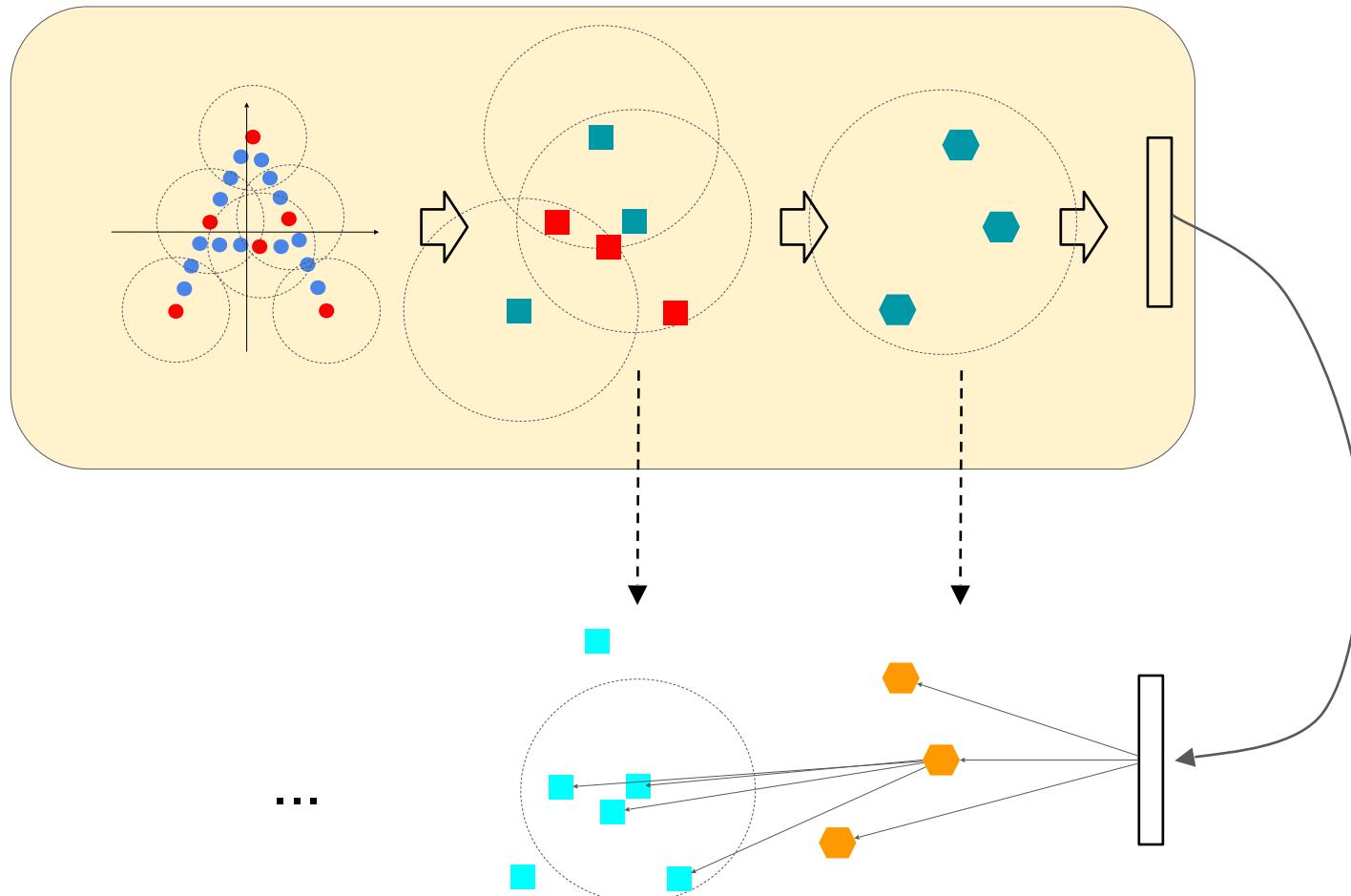
# “Up-convolution” Module

Naive solution: Broadcasting



# “Up-convolution” Module

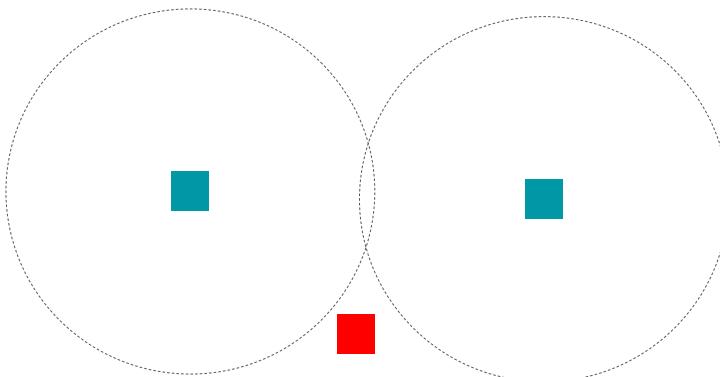
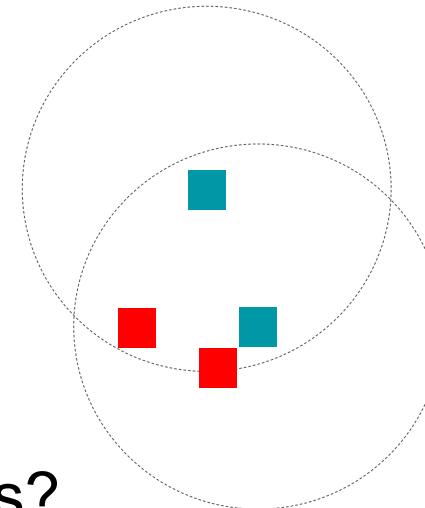
Naive solution Plus: Broadcasting + Skip links



# “Up-convolution” Module

Naive solution (broadcasting) Problems:

1. How to deal with points that belong to multiple regions?
2. What if some point belongs to no regions?



# “Up-convolution” Module with 3D Interpolation

Instead of broadcasting, use 3D interpolation.

- Nearest Neighbor
- Inverse distance weighting
- Using delaunay triangulation

...

# “Up-convolution” Module with 3D Interpolation

Instead of broadcasting, use 3D interpolation.

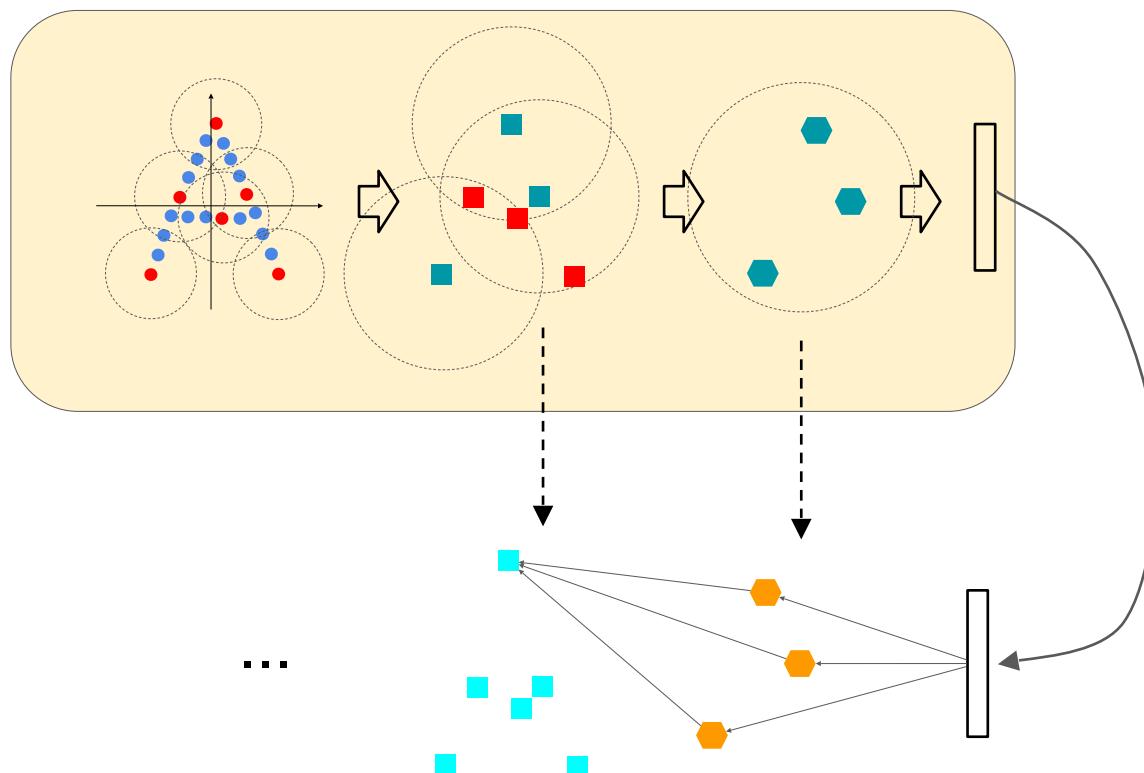
- Nearest Neighbor
- Inverse distance weighting
- Using delaunay triangulation

...

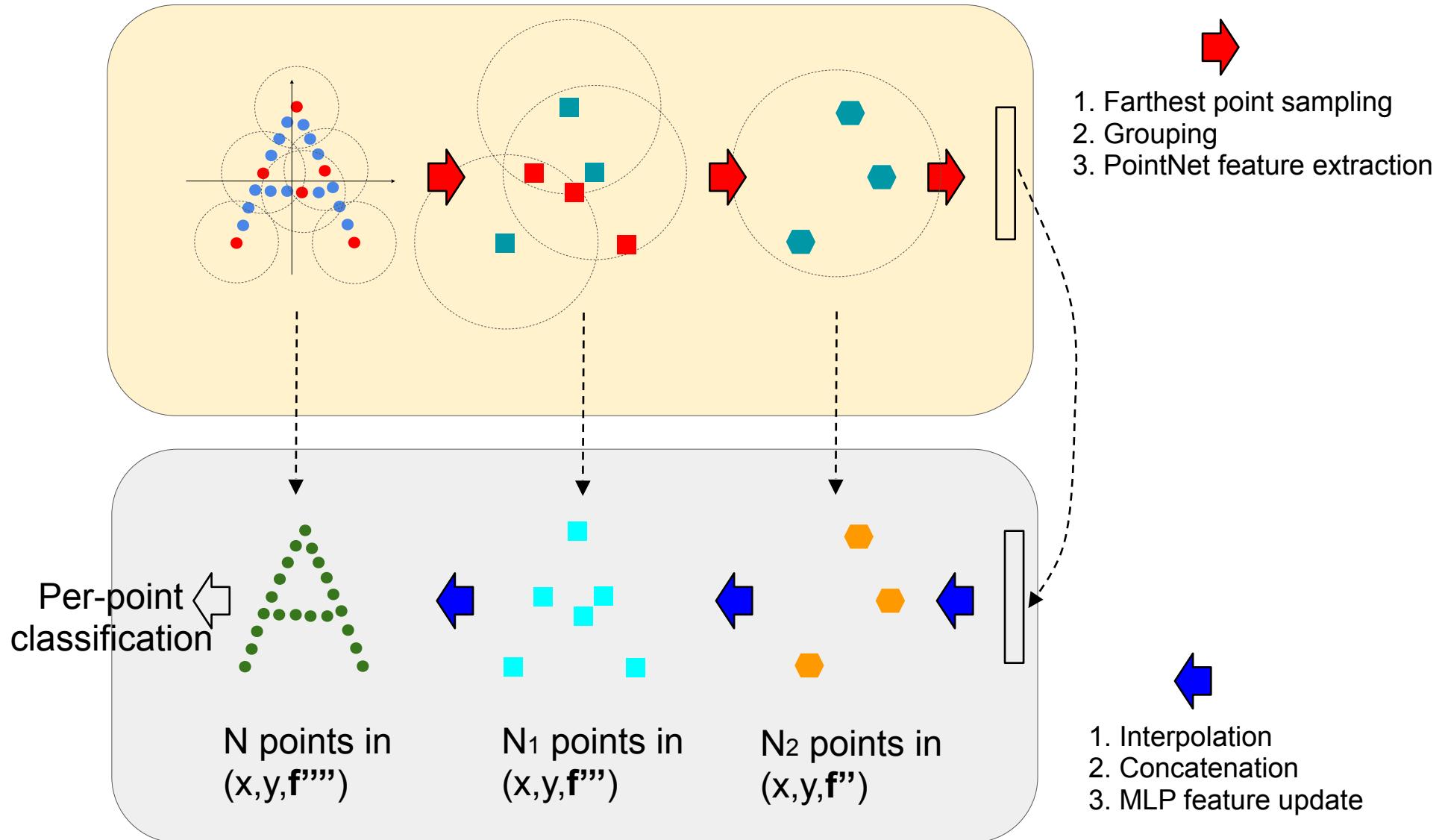
$$u(\mathbf{x}) = \begin{cases} \frac{\sum_{i=1}^N w_i(\mathbf{x}) u_i}{\sum_{i=1}^N w_i(\mathbf{x})}, & \text{if } d(\mathbf{x}, \mathbf{x}_i) \neq 0 \text{ for all } i \\ u_i, & \text{if } d(\mathbf{x}, \mathbf{x}_i) = 0 \text{ for some } i \end{cases}$$
$$w_i(\mathbf{x}) = \frac{1}{d(\mathbf{x}, \mathbf{x}_i)^p}$$

# “Up-convolution” Module

1. Feature Interpolation based on Euclidean distances to kNN
2. Skip link feature aggregation
3. MLP on aggregated feature for feature update and compression



# Multi-Scale PointNet: Segmentation Network



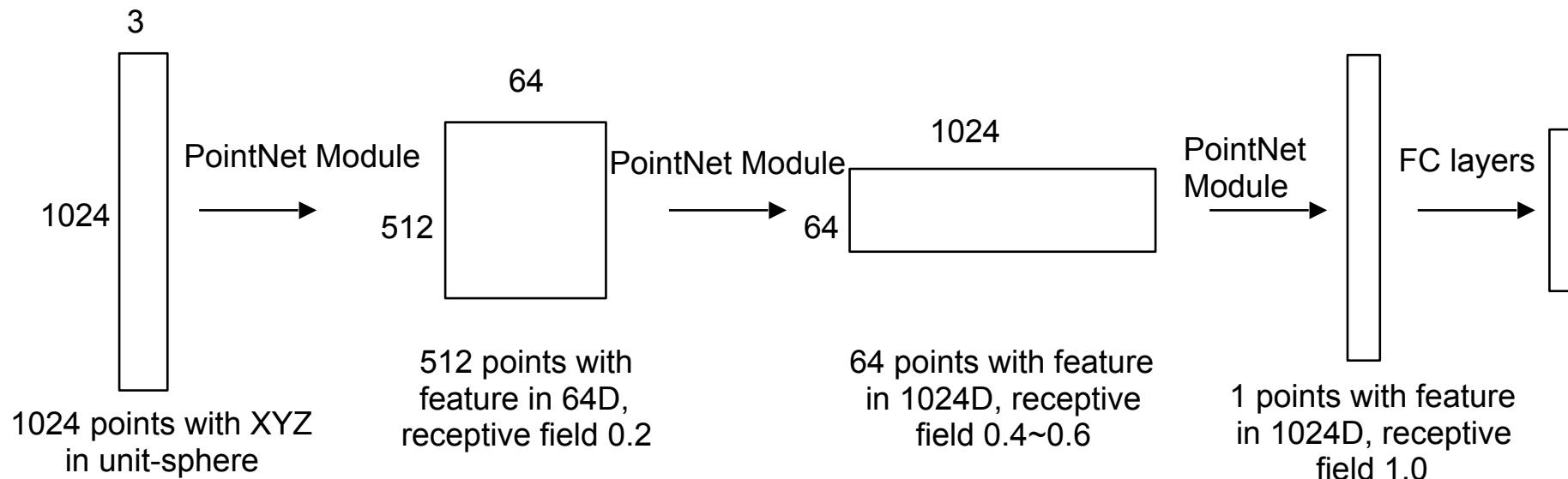
# Experimental Results (preliminary)

# ModelNet40 Classification Benchmark

	Accuracy
PointNet (vanilla)	87.2%
PointNet	89.2%
MultiScale PointNet	90.1%
MultiScale PointNet (voting)	<b>90.7%</b>

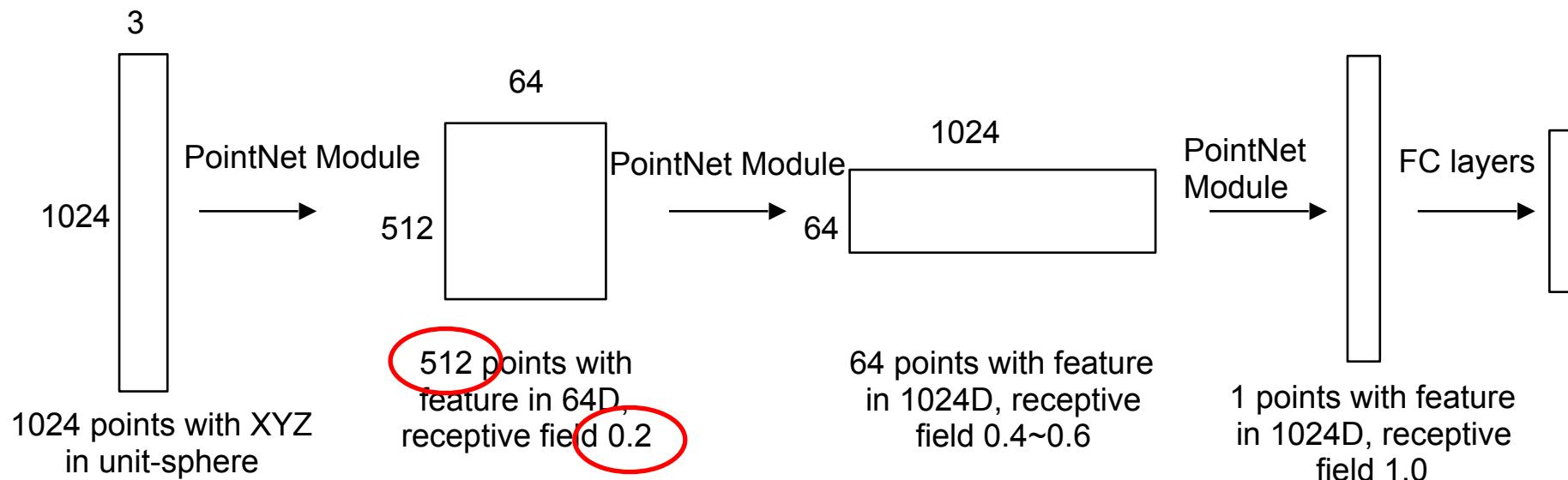
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# ShapeNet Part Segmentation Benchmark

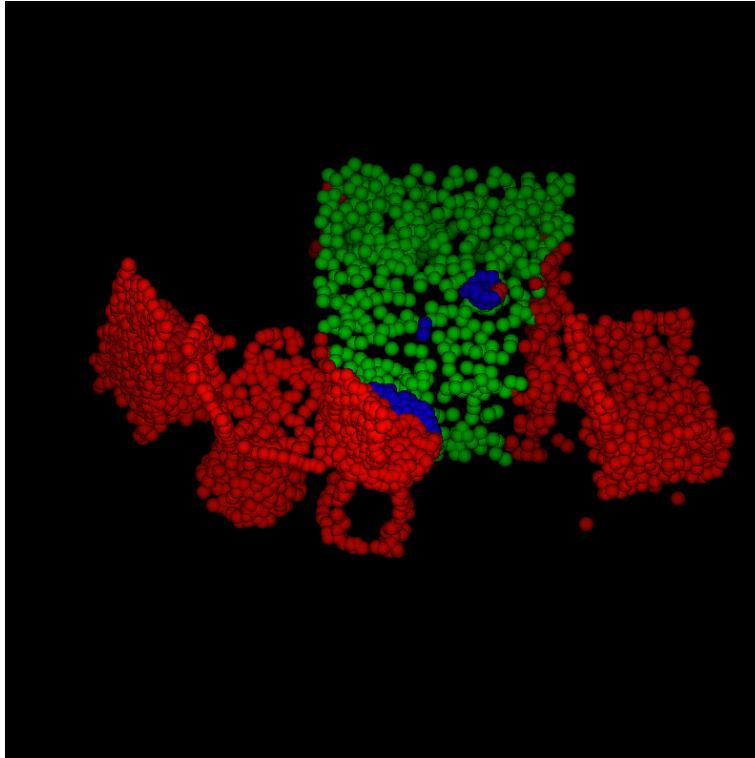
- First try...

	mIoU
PointNet	80.7%
PointNet + one-hot vector	82.7%
PointNet + one-hot vector + skip links etc.	83.7%
MultiScale PointNet	<b>83.8%</b>

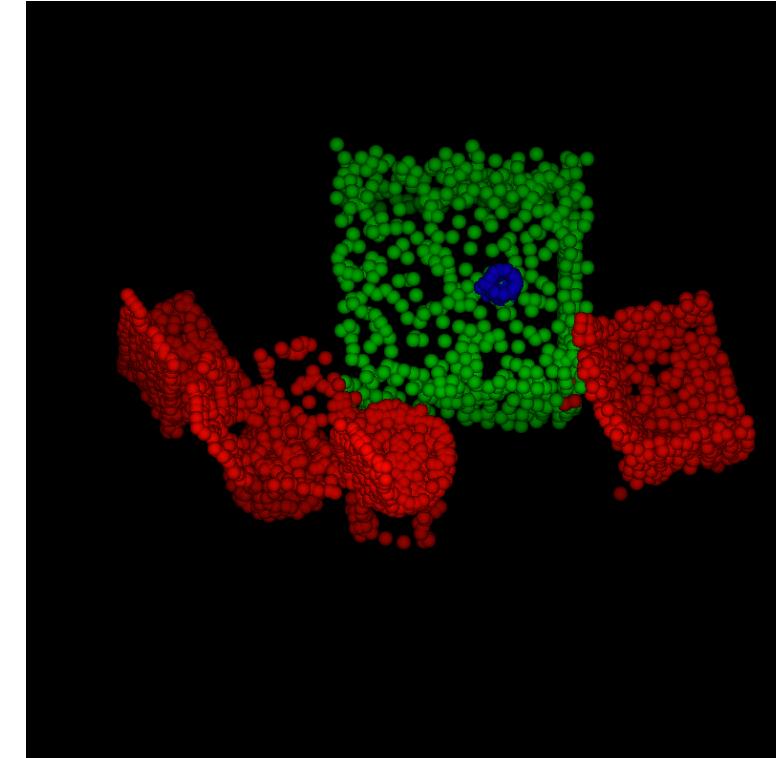
# Semantic Segmentation in Scenes

	mIoU
PointNet	75.5%
MultiScale PointNet	<b>94.6%</b>

PointNet v1.0



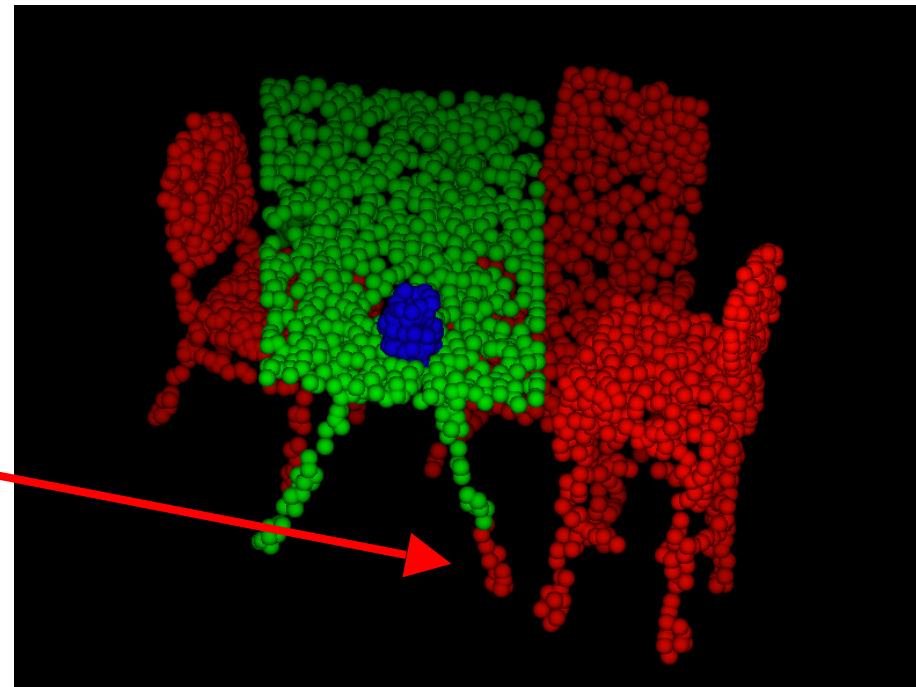
PointNet v2.0: Multi-Scale PointNet



# Semantic Segmentation in Scenes

	mIoU
PointNet	75.5%
MultiScale PointNet	<b>94.6%</b>

PointNet v2.0: Multi-Scale PointNet

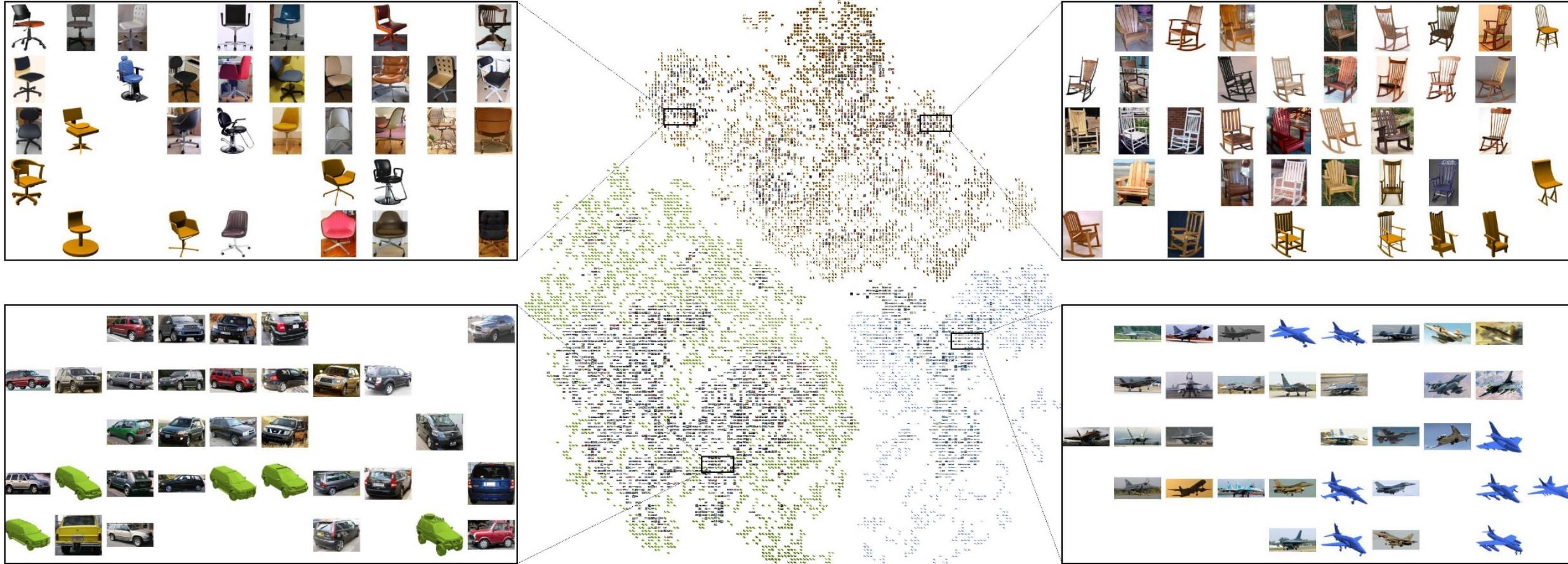


Misclassified table leg

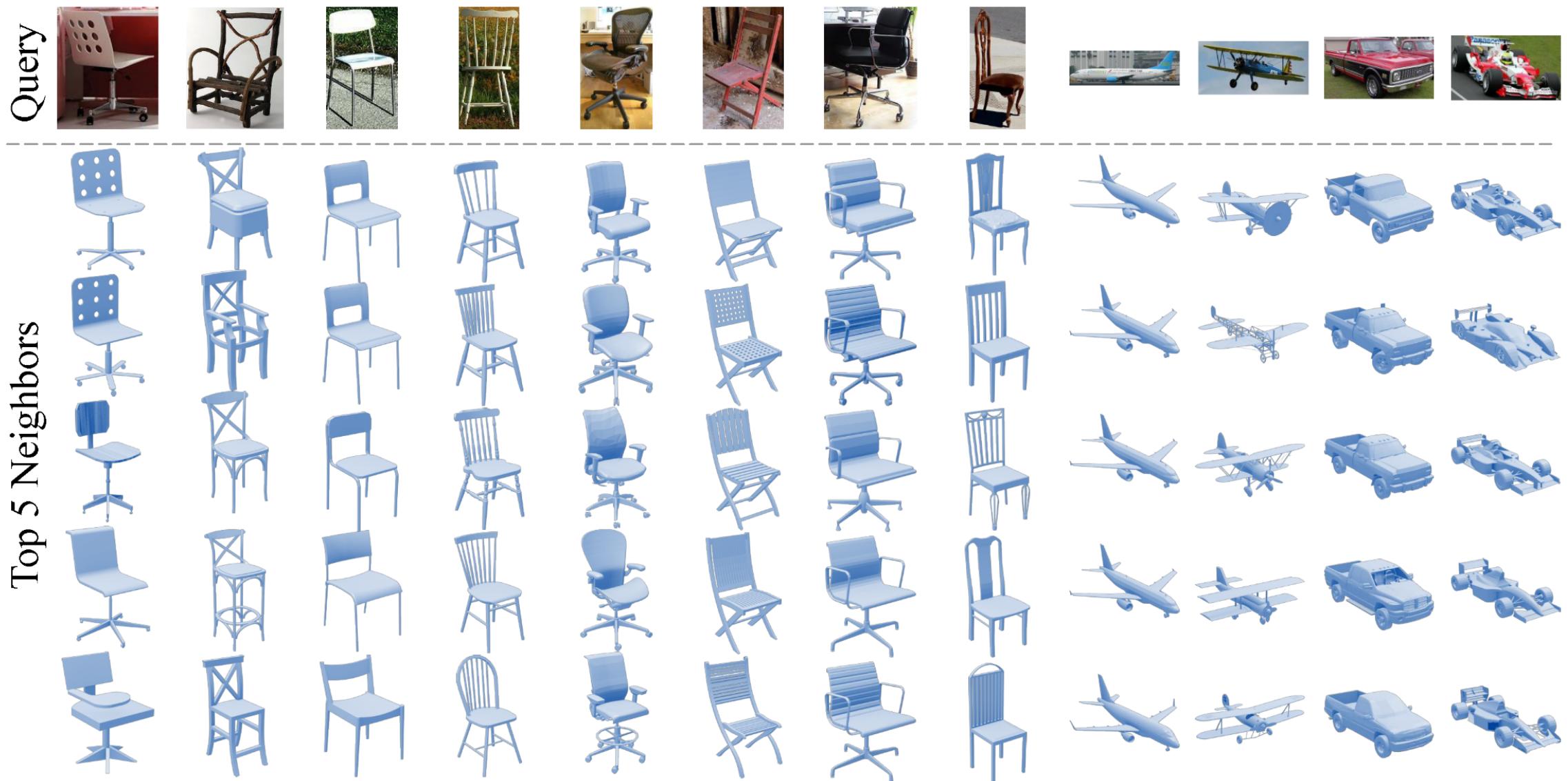
Geodesic distance based  
weights may help!

# Joint Embedding of 3D shapes and 2D images

# What is Joint Embedding of Shapes and Images?



# Application: Image-based Shape Retrieval



# Application: Shape-based Image Retrieval

Query



Top 5 Neighbors

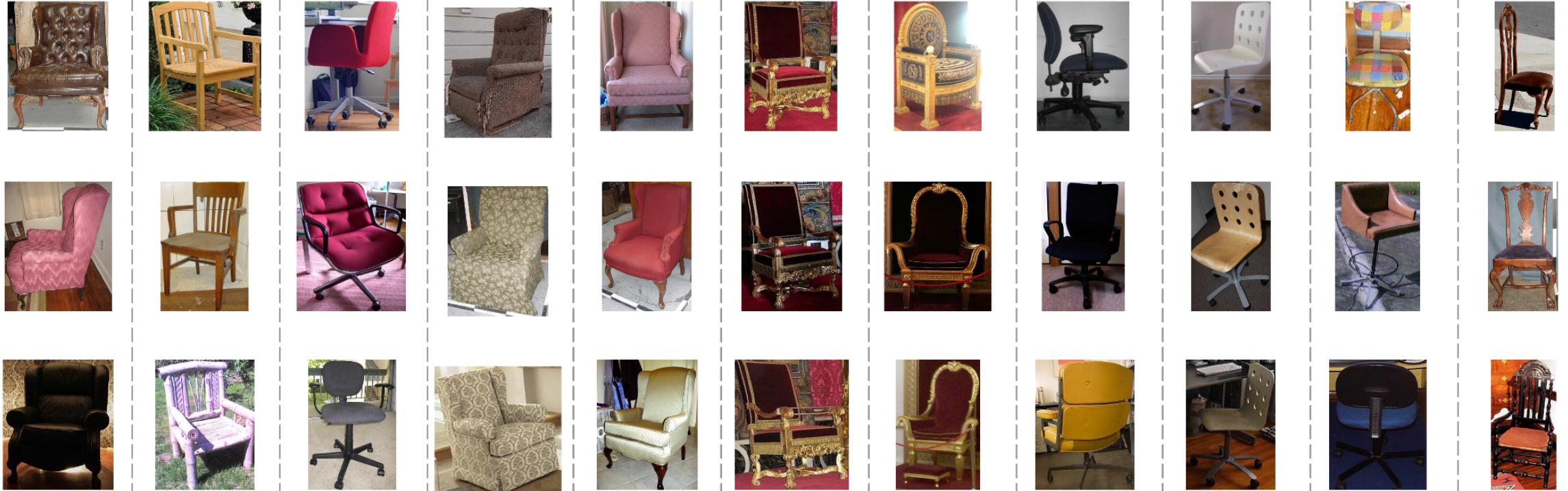


# Application: Cross-View Image Retrieval

Query

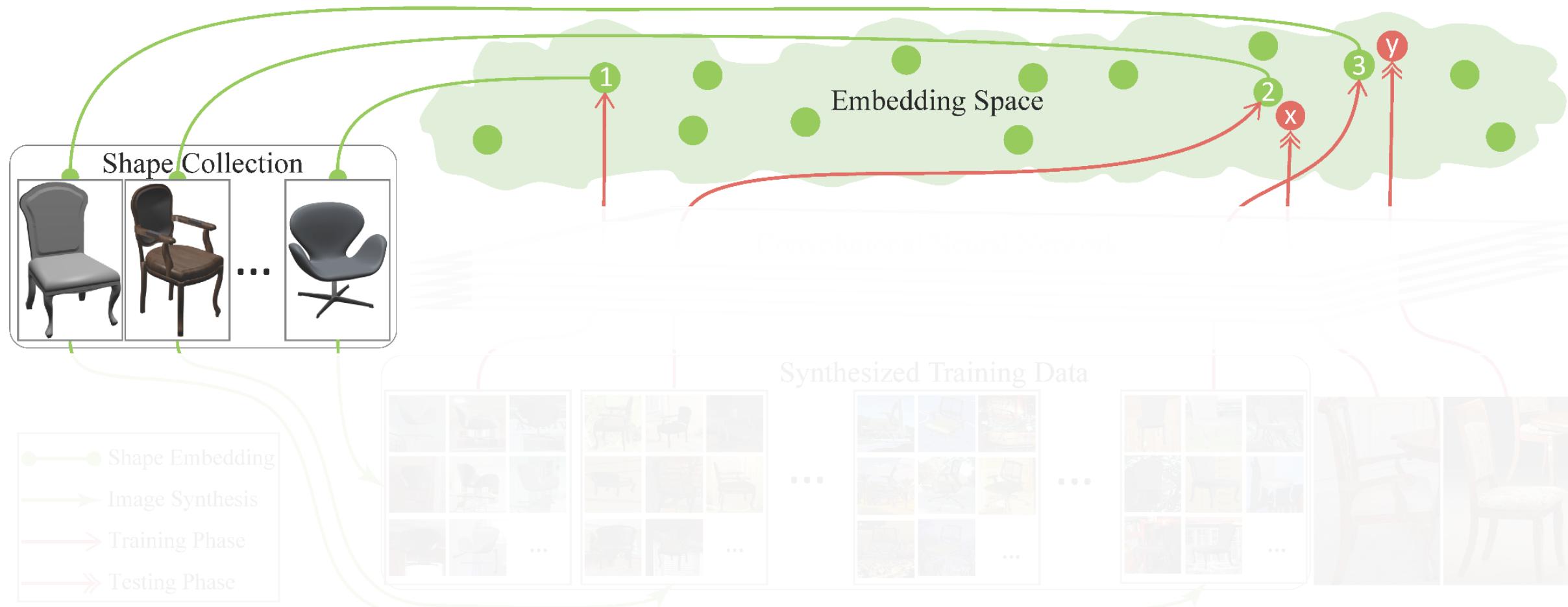


Top 3 Neighbors



# How to construct the joint embedding space?

## Step 1: Construct Shape Embedding Space



# Why not start from images?

- Object pose
- Lighting condition
- Texture variance
- Background clutterness
- ...



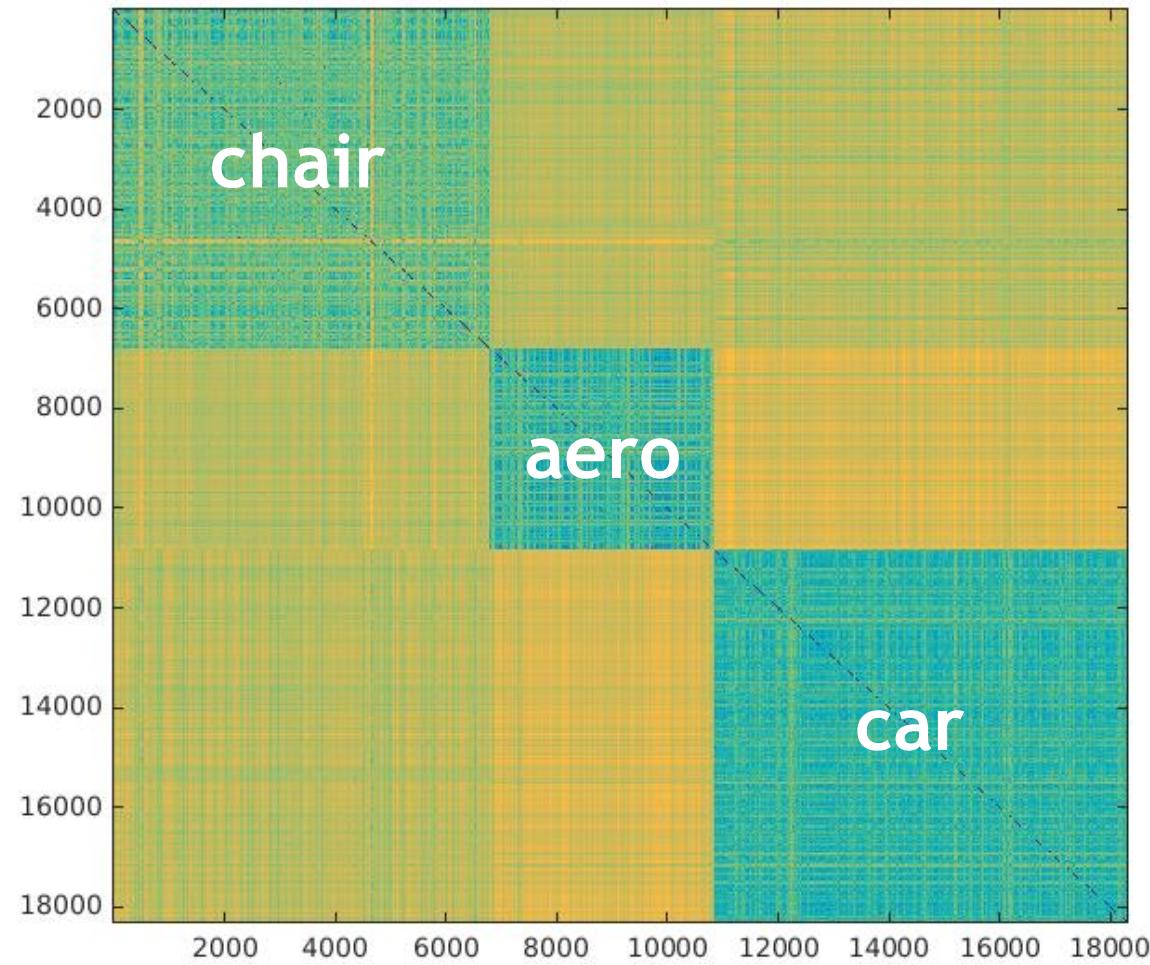
# Similarity between Shapes can be Easily Factored



# Step 1: Construct Shape Embedding Space

- Shape signature: Light Field Descriptor (with HoG feature)

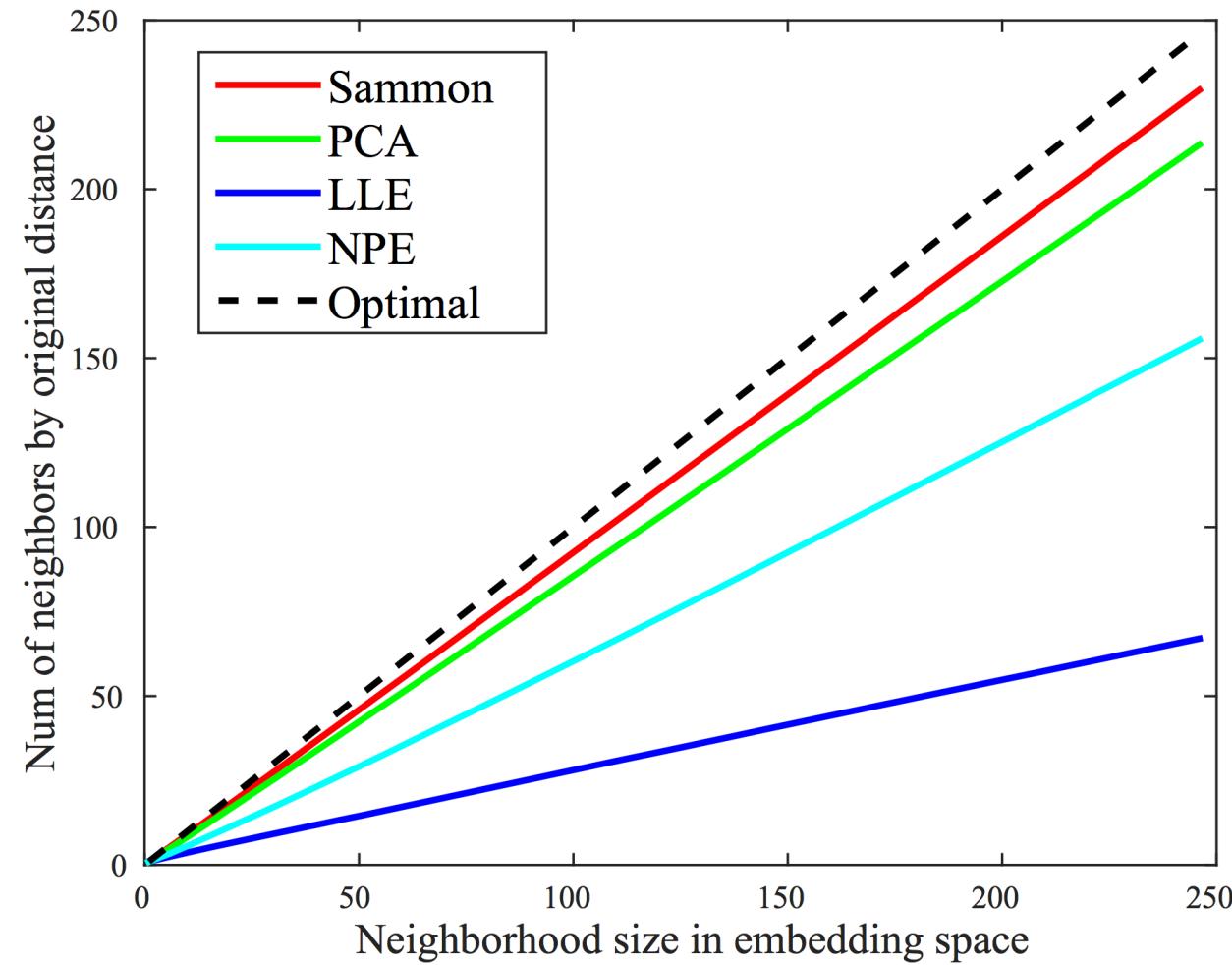
Pairwise distance matrix  
of 3D shapes



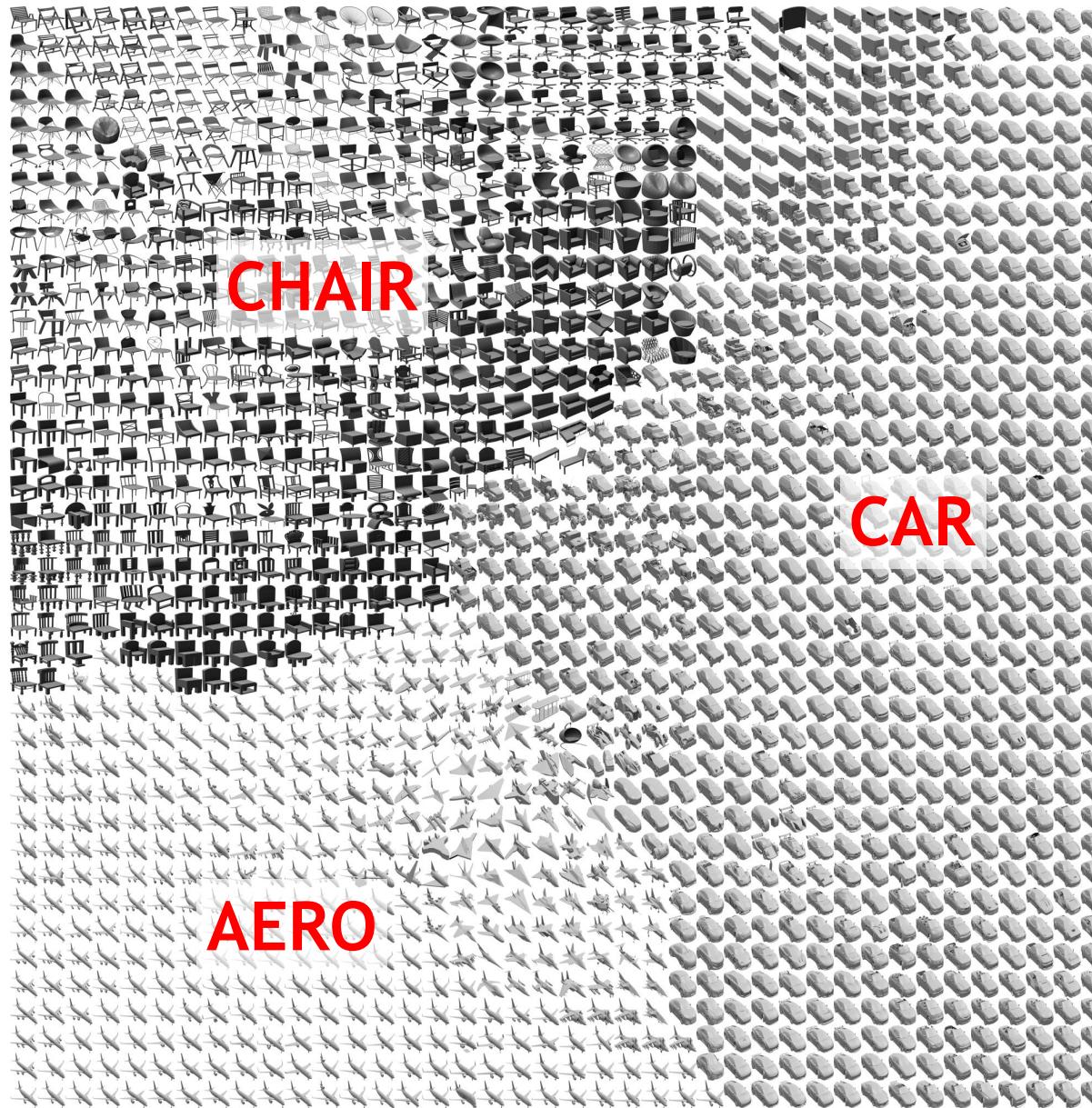
# Step 1: Construct Shape Embedding Space

- Dimension reduction (MDS with Sammon mapping)

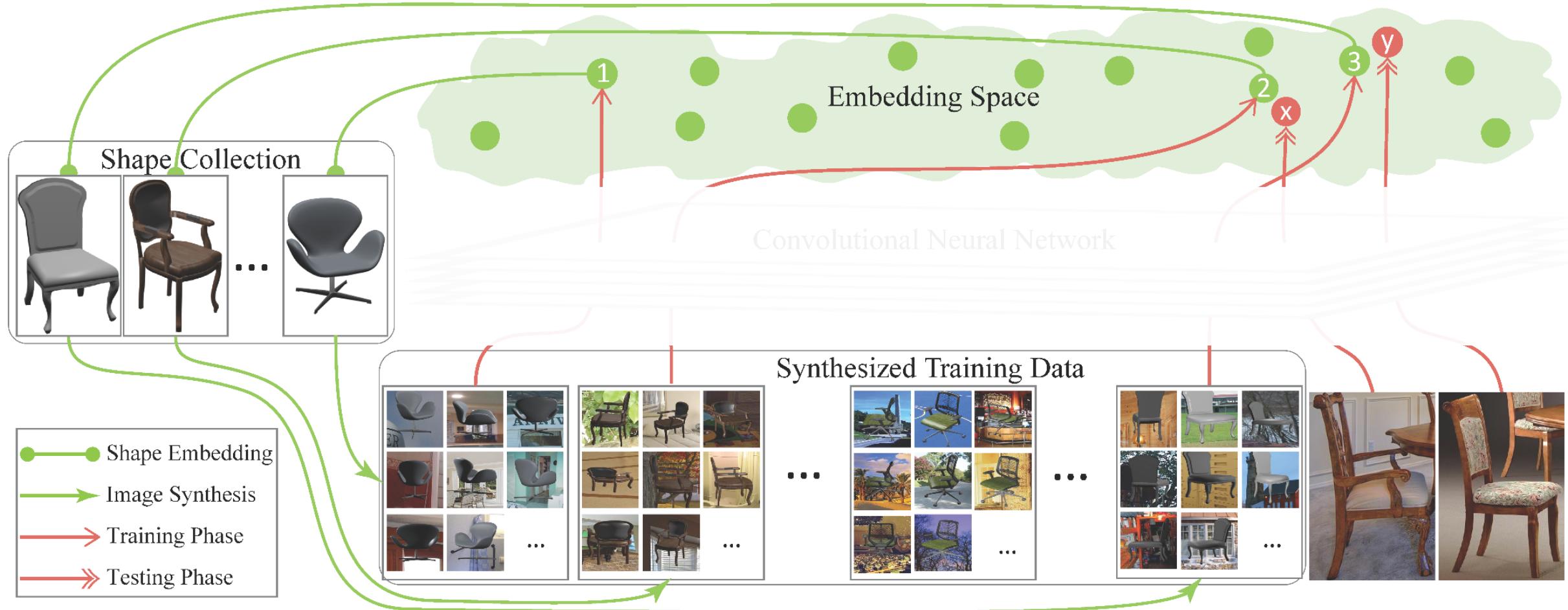
**Key idea:**  
We care more about **structure of local neighborhood**, instead of distances between very dissimilar objects.



# 2D Visualization of Shape Embeddings



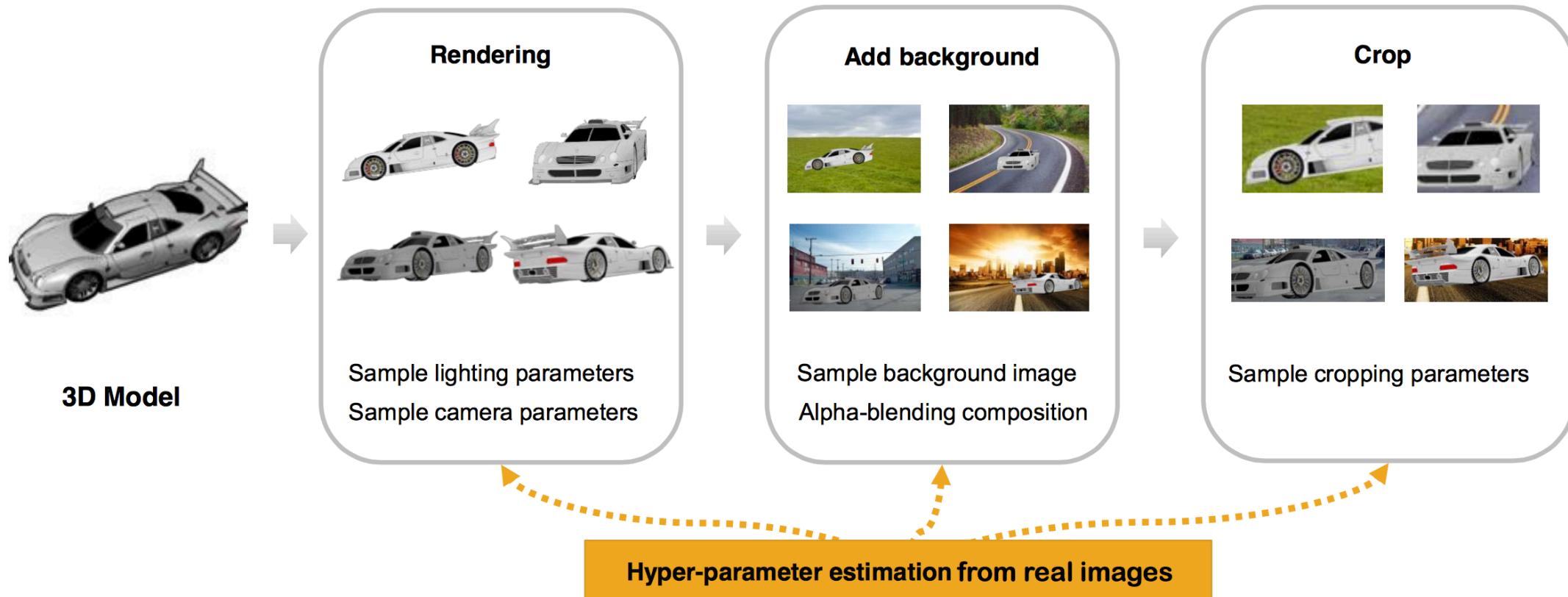
# How to construct the joint embedding space?



**Step 2: Projecting Images to the Joint Embedding space:  
Prepare training data.**

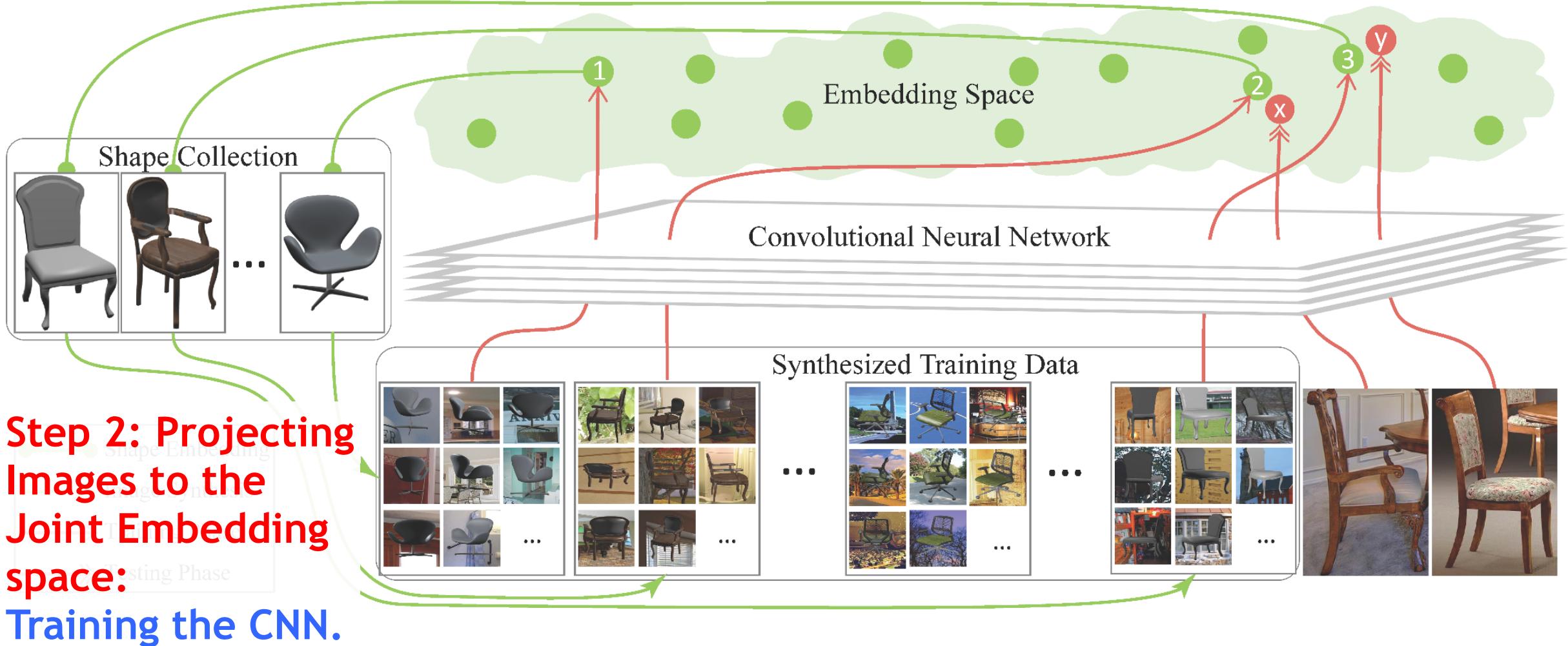
# Step 2: Projecting Images to Joint Embedding Space

## ■ Render for CNN Pipeline

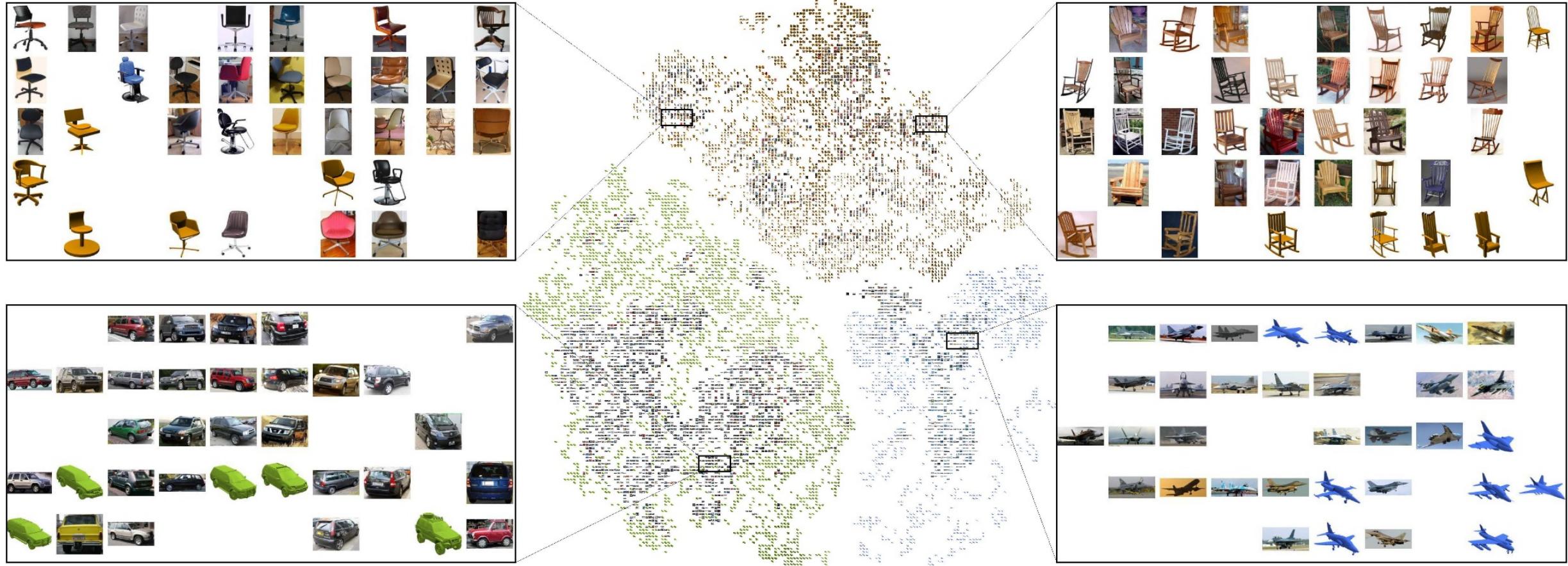


*Hao Su, Charles Qi, Yangyan Li, Leonidas Guibas, Render for CNN: Viewpoint Estimation in Images Using CNNs Trained with Rendered 3D Model Views, ICCV 2015 Oral Presentation*

# How to construct the joint embedding space?

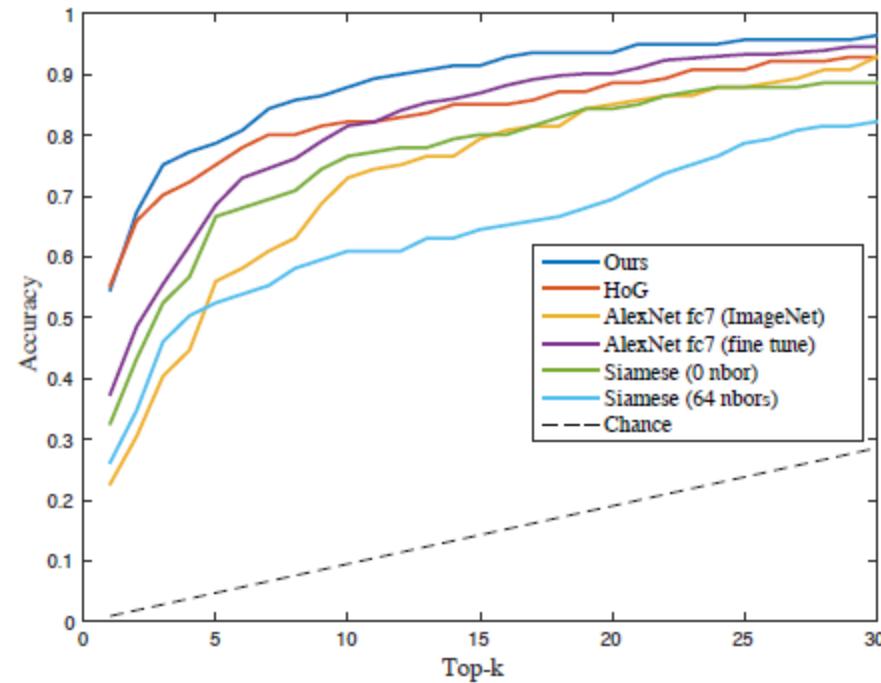


# Joint Embedding Space of Shapes and Images



t-SNE visualization. Embeddings are projected into 2D

# Results



**Figure 8:** Comparison of top- $k$  accuracy on image-based same-instance shape retrieval.

Median rank of	HoG	AlexNet fc7 (ImageNet)	AlexNet fc7 (fine tune)	Siamese (64 nbors)	Siamese (0 nbors)	Ours
first matched	<b>1</b>	7	5	3	3	<b>1</b>
last matched	32	84	71	94	49	<b>5</b>

Comparison of performance on shape-based same instance image retrieval

# Other approaches to build 3D shape space: GANs

## Learning a Probabilistic Latent Space of Object Shapes via 3D Generative-Adversarial Modeling

NIPS 2016



Jiajun Wu\*



Chengkai Zhang\*



Tianfan Xue



Bill Freeman



Josh Tenenbaum

MIT CSAIL

Google Research

\* indicates equal contribution