

1. Pseudo Code:

```

div(RatPoly v):
   $u_d$  = degree of u
   $v_d$  = degree of v;
  r = u
   $i = u_d - v_d$ 
  if  $i < 0$ 
    return ZERO
  create array Q with length( $u_d - v_d + 1$ )
  while( $i \geq 0$ ){
     $j = v_d$ 
     $Q[i] = r[i + j] / v[j]$ 
    while( $j \geq 0$ ){
       $r[i + j] = r[i + j] - Q[i] * v[j]$ 
       $j --$ 
    }
     $i --$ 
  }
  return RatPoly(Q)

```

2. Main Loop LI:

$$Q * v + r = u$$

Proof:

Base case:

$r = u, Q = 0$, therefor the base case is true

Assume Step k is true

Proof that Step k+1 is true

$$Q_{k+1} = Q_k + Q[k - 1] * x^{k-1}$$

The inner loop guarantee that $r_{post} = r_{new} + Q[i] * v * x^i$

$$\text{therefore } r_{k+1} = r_k - Q[k - 1] * v * x^{k-1}$$

$$Q[k - 1] = r_k / v[v_d]$$

$$\text{therefore } r_{k+1} + Q_{k+1} = r_k - Q[k - 1] * v * x^{k-1} + Q_k + Q[k - 1] * x^{k-1} = r_k + Q_k * v = u$$

therefore It is true for step k+1

therefore It is true for each step

3. Decrementing function:

$$D = i$$

i decrements by 1 for each step

$$D_{min} = -1$$

The loop will exit at $i = -1$