

Aggregate Implications of Corporate Taxation over the Business Cycle^{*}

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Abstract

Corporate tax deductions are widely employed as countercyclical policies across countries, yet their impact on the business cycle and interactions with other policies remain largely understudied. I examine the cyclical implications of such deductions by developing a novel dynamic stochastic general equilibrium model in which firms face credit market imperfections and idiosyncratic productivity shocks. In my model, firms' investment decisions are distorted by collateralized borrowing and partial irreversibility due to corporate taxation. Investment expenditures can be deducted from taxable income in two ways: through targeted policy that grants full deductions to firms with smaller investments, or through untargeted policies that allows partial deductions. My model quantitatively replicates empirical estimates of the short-run elasticities of investment across firm size to changes in deduction policies. I show that raising deductions can reduce the severity and persistence of recessions by alleviating capital misallocation for productive firms. Applying my model to the policies in the 2017 Tax Cuts and Jobs Act, I find that the targeted policy is 50 percent more effective than the untargeted policy in stimulating aggregate output. Furthermore, combining both policies reduces the overall effectiveness by 13 percent, revealing potential inefficiencies in current US tax policy implementation.

Keywords: Tax shields, Collateral constraint, Business cycle, Firm dynamics

JEL Codes: E22, E32, E62, H25

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1 Introduction

Adjusting tax incentives to boost firm investment are key fiscal policies used by countries to accelerate recoveries during economic downturns. Even outside of downturns, countries continue to engage in significant corporate tax reforms. For example, the Tax Cuts and Jobs Act (TCJA) of 2017 in the United States was the largest business tax cut in four decades, with an estimated cost of 100 to 150 billion dollars per year¹. While individual firms' investment is sensitive to available tax incentives², it is empirically difficult to identify the impact of each policy³. Moreover, existing models tend to ignore heterogeneity in investment responses across firms towards different policies and the general equilibrium effects that follow changes in tax incentives on investment⁴. As I show, the heterogeneous responses to tax incentives across firms are essential in evaluating their aggregate impact, as they may resolve the misallocation of capital arising from firm-level frictions and boost aggregate productivity. On the other hand, investment tax deductions and the effects of such policies on interest rates induce large firms to over-invest, reducing aggregate productivity. The aggregate effects of raising tax incentives depend on the relative size of each channel and how they shape the underlying distribution of firms.

In this paper, I develop a dynamic stochastic general equilibrium model with heterogeneous firms, collateral constraints, and corporate tax deductions. In particular, I distinguish the faster tax depreciation rate from the physical capital depreciation rate to capture the regular investment depreciation schedule⁵. I empirically anchor my analysis by considering both targeted and untargeted policies within the US corporate tax code⁶. The targeted policy, which allows

¹The House [Committee on Ways and Means](#) (2003) explicitly states that the purpose of bonus depreciation is to “promote capital investment” and “help to spur an economic recovery”. Furthermore, the [Joint Committee on Taxation](#) (2017) has an estimated cost of 86 billion dollars on 10-year tax revenue for investment subsidy policies.

²[Zwick and Mahon](#) (2017) has estimated that the investment elasticity to increases in bonus depreciation rate ranges from -0.5 to -3.6 .

³[Ohrn](#) (2019) reports that the Annual Survey of Manufactures (ASM) data on firm-level investment is not precise. Besides the data quality, [Mills, Newberry and Trautman](#) (2002) and [Mills and Newberry](#) (2005) document empirical difficulties in reconciling the difference in income for financial statements (book income) and income for tax purposes (taxable income).

⁴[House and Shapiro](#) (2008) argue that the shadow value of capital would be unchanged with temporary investment subsidies, assuming all firms are representative. However, credit constraints yield a distribution of capital shadow values; most firms' capital stocks are below their efficient level. Thus, temporary investment subsidies can change the shadow value of capital. [Fernández-Villaverde](#) (2010) treats the fiscal policy as a shock, while the statement in the House [Committee on Ways and Means](#) (2003) clearly shows that the policy is not imposed at random.

⁵This is called Modified Accelerated Cost Recovery System (MACRS). MACRS defines the schedule based on the useful life of the equipment. This useful life of capital is meant to be shorter than the actual duration of capital to facilitate depreciation deduction.

⁶There are two federal policies in the United States: Section 179 expensing and bonus depreciation. Section 179 expensing as a target policy allows firms to immediately deduct all investment expenditures if their investment is

investment expenditure to be deductible up to a threshold, generates a larger boost to GDP growth during recoveries than the untargeted policy. This reduces capital misallocation by inducing self-selection so that productive firms invest more. In contrast, the untargeted policy does not trigger such a reallocation mechanism. Furthermore, the combination of targeted and untargeted policies within the US corporate tax system diminishes the policies' overall effectiveness at accelerating recoveries from economic downturns.

There are two frictions in my model that impede capital reallocation: financial friction and tax wedges. Following [Kiyotaki and Moore \(1997\)](#), forward-looking collateral constraints are added to limit the firm-level investment decision, hindering the growth of small and young firms. Tax wedges, on the other hand, distort firms' investment by inducing partial irreversibility. When firms invest, they are paying one unit of output in exchange for one unit of investment goods when there is no investment tax deduction. On the contrary, when the firm later sells its capital, its taxable income increases due to capital gains. As the tax depreciation rate is faster than the physical capital depreciation rate, the market price of capital is usually higher than the book value of the capital adjusted by the claimed depreciation deduction ([Hanlon, Maydew and Shevlin, 2008](#)). Therefore, selling one unit of investment good yields one unit of output good net of the adjusted basis of capital, reflecting the concept of partial irreversibility. This difference between purchasing and selling prices of capital leads firms to follow (S, s) rules regarding their capital decisions under corporate taxation.

Investment tax deductions may lead to negative taxable income, which has been ignored by the literature⁷. When a firm reports a negative taxable income (net operating losses) from deductions of investment expenditure, it does not result in direct tax rebates in the current tax year; it simply owes no taxes⁸. In other words, models that directly impose the tax wedges on the flow profit and cost of capital introduce additional distortions on investment incentives, as they suggest that firms can receive government transfers simply by increasing their investment.

Corporate tax deductions lead to changes in the relative prices of capital among firms while being implemented in two fashions: Section 179 expensing and bonus depreciation. Section 179 expensing, a targeted policy, allows firms that invest below a dollar value threshold⁹ to immediately deduct the full cost of qualifying equipment. In contrast, bonus depreciation, an untargeted policy, permits firms to deduct a higher fraction of the purchase price of equipment in the year it is acquired, and the remaining part is deferred to future tax years as deductible

lower than a certain threshold. Bonus depreciation, on the other hand, allows all firms to deduct a bonus fraction of investment expenditure immediately, and the rest of it follows MACRS.

⁷See [Barro and Furman \(2018\)](#) and [Chodorow-Reich, Smith, Zidar and Zwick \(2024\)](#) for recent examples.

⁸In IRS Publication 542, firms can carry forward the net operating losses to future tax years for deductions. In my model, I do not allow firms to undertake carryforward.

⁹The dollar threshold is specified in IRS Publication 946.

stocks. The coexistence of these two policies separates investing firms into two categories: those investing above the Section 179 threshold and those investing below it. These two types, together with those firms that do not pay corporate taxes, characterize the direct impact of tax policies on firms' investment by lowering the user cost of capital.

I offer two explanations for why Section 179 expensing perform better, both related to how tax incentives shape the costs and returns of investment. First, on the cost side, I find that bonus depreciation lead to substantial increases in dividend payments, while Section 179 expensing only mildly raise it. Increasing tax incentives lead to lower user costs of capital. For smaller, credit-rated firms, this reduction enables them to accumulate capital and expand production. In contrast, larger, financially unconstrained firms increase their dividend payments, as the lower cost of capital allows them to easily reach their target level of capital. Since Section 179 expensing is limited to small- to medium-sized firms, while bonus depreciation extends tax incentives to financially unconstrained firms, the latter policy results in higher dividend payment in equilibrium.

On the return side, the increased effectiveness of the targeted policy can be illustrated by the distribution of excess return on investment across firms, which reflects economy-wide capital misallocation. Compared with bonus depreciation, Section 179 expensing results in less dispersion of firm investments around the economically efficient level of zero excess returns. Furthermore, high-productivity firms disproportionately respond to the bonus depreciation, while the effects of Section 179 expensing are more diffuse. The combination of both policies, on the other hand, indicates that both policies are eroding the effectiveness of each other. As Section 179 expensing becomes more generous, the tax base for the bonus depreciation shrinks, eroding its effectiveness.

This paper is to my knowledge the first to explore how an economy with the current US tax system responds to shocks¹⁰. A negative TFP shock to my model economy generates nearly identical responses to standard models (Hansen, 1985; Khan and Thomas, 2013). On the contrary, I show that corporate tax deductions can alleviate the recession generated by a negative shock to the available credit because it lowers the need for investment loans. As the user cost of capital is lower with tax incentives, small firms rely less on debt financing to invest, further mitigating the deterioration in the aggregates and endogenous TFP.

There is a large body of literature investigating how tax incentives influence aggregate investment. The seminal work by Hall and Jorgenson (1967) was the first to evaluate a representative firm's response to tax credits through changes in the user cost of capital. My work builds

¹⁰The empirical and theoretical analyses often simplify impacts of tax incentives to changes in user costs of capital (Hall and Jorgenson, 1967) and ignore how tax incentives affect firms' value and resulting misallocation of capital. The misallocation tradition comes from Summers, Bosworth, Tobin and White (1981).

on this tradition by modeling differences in user costs based on firms' investment decisions. Firms investing below the threshold enjoy lower user costs compared to those investing above it, with the gap between these costs determined by the bonus depreciation rate. Additionally, [Summers, Bosworth, Tobin and White \(1981\)](#) introduced the concept of tax-adjusted Tobin's q , which assesses how tax policies influence the accumulation and valuations of capital, offering another channel through which fiscal policy impacts capital accumulation. In my model, both corporate taxes and investment subsidies affect firm value, allowing me to explore Tobin's q channel for tax credits.

Earlier empirical literature starts with data on public companies but oftentimes concludes that investment is not responsive to tax credits. [Goolsbee \(1998\)](#) uses data on the prices of capital by the Bureau of Economic Analysis (BEA) and concludes that the effect of the investment tax credit is offset by the increase in capital prices among public firms. [Cummins, Hassett and Hubbard \(1996\)](#) utilizes panel data among 14 OECD countries and identifies that the user cost of capital and the adjustment costs can explain such unresponsiveness. [House and Shapiro \(2008\)](#) matches the BEA data with Internal Revenue Service (IRS) depreciation schedules and analyzes the 2001 to 2002 bonus depreciation. They claim that the intertemporal elasticity of investment is high under two assumptions: capital is long-lived and investment tax credit is temporary and unexpected. Even though the conclusion by [House and Shapiro \(2008\)](#) highlights the importance of intertemporal substitution, they assume all tax responses are temporary price effects and not income effects, which contradicts the evidence documented in corporate finance literature (e.g., [Lamont \(1997\)](#)). While these studies do not find heterogeneity in tax-term elasticity among public firms, evidence from subsequent studies shows that small and private firms are most responsive to these policies.

Recent empirical literature has utilized firm-level data and state-level policy compliance and found substantial heterogeneity in investment response. [Zwick and Mahon \(2017\)](#) is the first empirical research that exploits business tax data from the IRS to estimate the heterogeneity of investment response to the tax credit. They examine the impact of bonus depreciation by comparing industries that use long duration of capital to industries that use short duration. They found that bonus depreciation increases the investment of eligible capital by 10 to 16 percent compared to ineligible capital. Also, small firms respond 95 percent more than big firms. [Ohrn \(2018\)](#) further investigates the effect of corporate tax deductions and concludes that the investment raises by 4.7 percent for those states that comply with federal policies. In a subsequent study, [Ohrn \(2019\)](#) identifies potential conflicts between bonus depreciation and Section 179 expensing as mentioned before. These heterogeneous responses from small and young firms are the calibration targets for my model.

Historically, theoretical explorations of firms' responses to fiscal policy changes have been studied using representative firm models. [Fernández-Villaverde \(2010\)](#) builds a dynamic stochastic general equilibrium (DSGE) model with a representative firm and financial constraints to analyze the response to fiscal shocks. [Occhino \(2022\)](#) analyzes the aggregate effects of the 2017 Tax Cuts and Jobs Act while abstracting from the heterogeneous response to tax credits, therefore does not explore the distortion created by Section 179 expensing. Later, [Occhino \(2023\)](#) evaluates the effect of corporate tax cuts with accelerated depreciation, assuming that the bonus depreciation rate followed an AR(1) process. This assumption ignores the countercyclical nature of these policies and may lead to underestimation of the policy responses. My contribution is to bring heterogeneity into the theoretical analysis and quantitatively evaluate the efficacy of corporate tax deductions.

The remainder of the paper proceeds as follows. Section [2](#) introduces the quantitative model, and Section [3](#) provides useful analysis for numerical calculation. Section [4](#) presents and discusses the calibration strategies. Section [5](#) presents stationary equilibrium, Section [6](#) investigate the long run effects of deduction policies by comparative statics, Section [7](#) shows results on the business cycle, and Section [8](#) concludes.

2 Model Environment

Time is discrete and infinite. I abstract from aggregate uncertainty and consider stationary equilibrium and transitional dynamics under exogenous shocks. In my model economy, there are three types of agents: firms, households, and government. A large number of heterogeneous firms produce homogeneous output using predetermined capital stocks and labor. Firms' capital accumulation is hindered by two key factors: partial irreversibility due to corporate taxation, and financial frictions arising from collateral constraints. They pay corporate taxes based on their taxable income, which is defined by their flow profit after investment tax deductions. Together with persistent idiosyncratic productivities, these yield substantial heterogeneity in production.

Households are identical and infinitely lived. They pay for their consumption with their after-tax labor income, one-period shares in firms, and one-period non-contingent bonds. The government collects labor income tax from households and corporate tax from firms to fund exogenous government spending. Corporate tax deduction is funded by a lump-sum tax on households.

2.1 Firms

2.1.1 Production and financial frictions

At the beginning of each period, firms produce output y with physical capital k and labor n . The production function is $y = z\varepsilon F(k, n)$, where $F(k, n) = k^\alpha n^\nu$ with both $\alpha, \nu < 1$ and $\alpha + \nu < 1$. The variable z denotes an exogenous TFP shock that is common among firms, while ε is a firm-specific productivity shock. I assume that ε is a Markov chain, i.e., $\varepsilon \in \mathbf{E} \equiv \{\varepsilon_1, \dots, \varepsilon_{N_\varepsilon}\}$, where $\Pr(\varepsilon' = \varepsilon_j | \varepsilon = \varepsilon_i) = \pi_{ij}^\varepsilon$, and $\sum_{j=1}^{N_\varepsilon} \pi_{ij}^\varepsilon = 1$. Capital accumulation is determined by the law of motion, $k' = (1 - \delta)k + I$, where $\delta \in (0, 1)$ is the physical capital depreciation rate, and I denotes investment. Meanwhile, firms are informed whether they will exit the market at the end of the current period. The ex-ante probability of exit is $\pi_d \in (0, 1)$ ¹¹.

Firms finance their investment by borrowing one-period debt from households, yet they face a collateralized borrowing limit. The amount of newly-issued debt b' is priced at q , and shall not exceed θ fraction firms' future capital choice k' , that is, $b' \leq \theta k'$. If the fraction θ is close to the risk-free real interest rate $\frac{1}{q}$, then the collateral constraints become looser. This assumption is based on the limited enforceability of financial contracts. The forward-looking nature of

¹¹Following [Khan and Thomas \(2013\)](#), this assumption is to prevent all firms from accumulating sufficient resources, and none are financially constrained.

collateral constraints follows the specification as in [Kiyotaki and Moore \(1997\)](#). I summarize the aggregate states used in transitional equilibrium as $s = (z, \theta)$.

2.1.2 Deductible stocks and deduction policies

Firms are subject to corporate taxes on flow income net of operating expenses. Expenses on nondurable items, such as wages, can be fully deducted from firms' taxable income immediately. The deduction on investment expenditure, on the other hand, depends on the regular depreciation schedule¹². The depreciation rate of this schedule, i.e., the tax depreciation rate, is faster than the physical capital depreciation rate¹³. Since the tax depreciation rate differs from the physical capital depreciation rate, the *deductible stock* ψ must be tracked separately from physical capital. The tax depreciation rate is defined as $\delta^\psi \in [\delta, 1)$, indicating the accelerated method used at the regular depreciation schedule.

As an accounting concept, the deductible stock is not directly involved in production; instead, it affects firms' user cost of capital and cash-on-hand. As the investment corporate tax deduction only applies to certain investment, I assume the firms have on average ω fraction of investment that is eligible for investment deductions. Under a regular schedule, firms can deduct a fraction ξ of current eligible investment expenses from their taxable income in the same period, essentially lowering the cost of capital by $\tau^c \xi \omega$. The remaining fraction, $1 - \xi$ is accumulated to the deductible stock for future deductions. Therefore, the law of motion for deductible stock can be described as

$$\psi' = (1 - \delta^\psi)\psi + (1 - \xi)\omega(k' - (1 - \delta)k).$$

This investment fraction ξ captures two key policies in the United States that are the core interests of this paper: Section 179 expensing and bonus depreciation. Section 179 expensing allows firms to immediately deduct all of the equipment expenses below a dollar threshold. If firms' investment is less than $(0, \bar{I}]$, then $\xi = 1$. Bonus depreciation, on the other hand, allows all firms to deduct an additional ξ fraction of their investment expenses, and the remaining part follows the depreciation schedule. Thus, the government may raise either ξ or \bar{I} during the recessions to boost recoveries from recessions.

¹²The depreciation schedule defined by Modified Accelerated Cost Recovery System (MACRS) in IRS publication 946.

¹³For tax purposes, investment depreciation typically follows the double declining balance method, allowing the tax depreciation rate to be twice as fast as the physical depreciation of the capital.

2.1.3 Taxable income and partial irreversibility

The taxable income, $\mathcal{I}(k', k, \psi, \varepsilon)$, is composed of the flow profit less the deduction from investment expenditure. To be specific,

$$\mathcal{I}(k', k, \psi, \varepsilon) = \max \{ z\varepsilon F(k, n) - wn - \mathcal{J}(k', k)(k' - (1 - \delta)k) - \delta^\psi \psi, 0 \}, \quad (1)$$

where $\mathcal{J}(k', k)$ is the indicator function for tax policies. If this firm is eligible for Section 179 expensing, i.e., $k' - (1 - \delta)k \leq \bar{I}$, then this firm can deduct all eligible investment immediately, $\mathcal{J}(k', k) = \omega$. Otherwise, $\mathcal{J}(k', k) = \xi\omega$ if $k' - (1 - \delta)k > \bar{I}$. The deduction from current investment, $\mathcal{J}(k', k)(k' - (1 - \delta)k)$, alters the effective tax rate per unit of capital invested, and the deduction from the past investment, $\delta^\psi \psi$, expand the firms' budget constraints.

When firms disinvest, i.e., $k' - (1 - \delta)k \leq 0$, their taxable income expands due to capital gain. When firms dispose of their depreciable assets, the basis for calculating capital gain or loss should be adjusted to the amount of depreciation deductions that have already been claimed¹⁴. In practice, the selling prices of the capital are usually higher than the adjusted basis because the tax depreciation rate is faster than the physical capital depreciation rate (Hanlon, Maydew and Shevlin, 2008). To be consistent with the (1), I assume the adjusted basis for one unit of capital sold is ω , and firms' taxable income is raised by $\omega(k' - (1 - \delta)k)$.

In principle, the government does not provide tax rebates when firms report negative taxable income. Instead, these firms simply owe no corporate taxes.¹⁵ Existing models (Barro and Furman, 2018; Chodorow-Reich, Smith, Zidar and Zwick, 2024) overlook the possibility of negative taxable income and instead directly impose tax wedges $(1 - \tau^c)$ on flow profits and investment subsidies $(1 - \tau^c\omega)$ on capital costs. This simplification risks mischaracterizing the distortion of investment incentives, as it implies that firms can receive tax rebates by increasing investment.

In light of this observation, I derive the upper bound for k' choice such that the firm is paying positive corporate tax,

$$\bar{k}(k, \psi, \varepsilon) \equiv \frac{z\varepsilon f(k, n) - wn - \delta^\psi \psi}{\mathcal{J}(k', k)\omega} + (1 - \delta)k.$$

Firms that invest higher than or equal to \bar{k} are not paying corporate tax, and their capital and bond decisions are different from firms that pay corporate tax.

As shown in figure 1, the natural threshold \bar{k} and the policy threshold \bar{I} divide the state

¹⁴See IRS Publication 544.

¹⁵According to IRS Publication 542, firms can carry forward the net operating losses to offset taxable income in future years. However, in my model, I assume that loss carryforwards are not permitted.

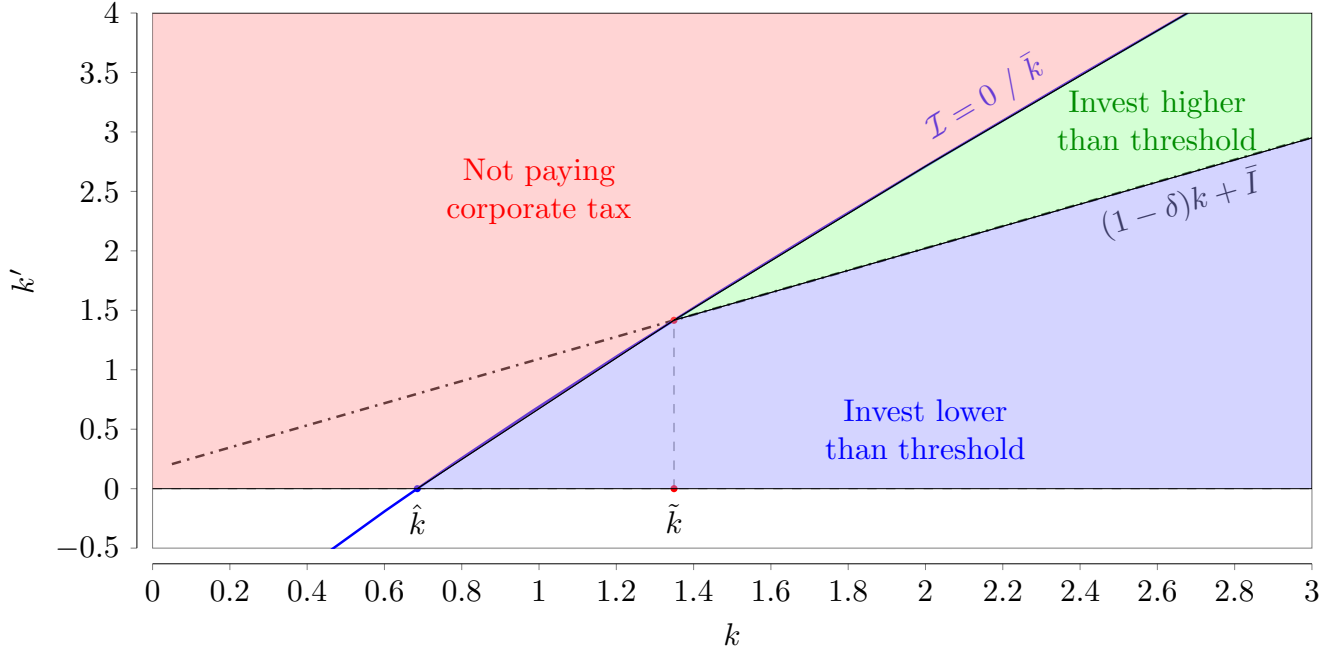


Figure 1: Capital choice state space

space into three regions, corresponding to three types of firms. If a firm's capital choice k' exceeds \bar{k} , the firm does not pay corporate taxes (red region), and I refer to these firms as N -type. Similarly, if the firm's k' falls between the policy threshold $(1 - \delta)k + \bar{I}$ and \bar{k} , the firm pays corporate taxes and invests above the policy threshold (green region), which I label as H -type firms. Finally, if the firm invests below the policy threshold or disinvests (blue region), I categorize them as L -type firms.

Firms undertake discrete choices among all three types, and such decisions can be characterized by firms' current capital stock k . The intersection of both natural threshold and policy threshold, $\bar{k} = (1 - \delta)k + \bar{I}$, leads to the first cutoff on capital stock \tilde{k} ,

$$\tilde{k} = \left(\frac{\delta^\psi \psi + \mathcal{J}(k', k) \bar{I}}{A(w) z^{\frac{1}{1-\nu}} \varepsilon^{\frac{1}{1-\nu}}} \right)^{\frac{1-\nu}{\alpha}},$$

where $A(w) = \left[\left(\frac{\nu}{w(s, \mu)} \right)^{\frac{\nu}{1-\nu}} - w(s, \mu) \left(\frac{\nu}{w(s, \mu)} \right)^{\frac{\nu}{1-\nu}} \right]$. Firms with large enough capital stock, $k > \tilde{k}$, can choose to invest in all three types. Firms with $k \leq \tilde{k}$, however, can only choose to be N -type or L -type, as investing higher than \bar{I} is equivalent to not paying corporate tax. Similarly, let \hat{k} be the intersection between \bar{k} and $k' = 0$. Firms with capital stock k lower than \hat{k} will not pay corporate tax for any k' choice.

Firms' budget constraints given corporate taxes are defined as

$$D = (1 - \tau^c)(z\varepsilon F(k, n) - wn) - b + qb' - (1 - \tau^c \mathcal{J}(k', k))(k' - (1 - \delta)k) + \tau^c \delta^\psi \psi.$$

If the government decreases the corporate tax τ^c to zero, the model falls back to the standard business cycle model. When $\mathcal{I}(k', k, \psi, \varepsilon)$ is positive, I combine the common terms and rewrite the budget constraint as

$$D = (1 - \tau^c)(z\varepsilon F(k, n) - wn) - b + qb' - (1 - \tau^c \mathcal{J}(k', k))(k' - (1 - \delta)k) + \tau^c \delta^\psi \psi.$$

Notice that one unit of investment now costs $1 - \tau^c \mathcal{J}(k', k)$ unit of final goods after deduction. In this manner, investment incentives through taxable income deductions reduce the relative prices of capital.

2.1.4 State spaces and firm distribution

At the beginning of each period, a firm is defined by four states:

1. its predetermined capital stock $k \in \mathbf{K} \subset \mathbb{R}_+$,
2. its level of one-period bond $b \in \mathbf{B} \subset \mathbb{R}$ issued one period ahead,
3. its deductible stock from investment $\psi \in \mathbf{\Psi} \subset \mathbb{R}_+$, and
4. its realized idiosyncratic productivity $\varepsilon \in \mathbf{E}$.

The distribution of firms is represented by a probability measure $\mu(k, b, \psi, \varepsilon)$, defined over the Borel σ -algebra generated by the open sets of the product space $\mathcal{S} = \mathbf{K} \times \mathbf{B} \times \mathbf{\Psi} \times \mathbf{E}$. Given all individual states, the firm maximizes the expected discounted value function by choosing current employment level n , future capital stock k' , and next-period debt level b' . For each unit of labor employed, the firm pays competitive wage $w(s, \mu)$, which depends on the distribution of the firms. The firm can issue one-period debt at a risk-free price q but subject to collateral constraint. The amount of newly-issued debt, b' , shall not exceed θ fraction firm's future capital choice k' , i.e., $b' \leq \theta k'$.

2.1.5 Firms' problem

I now start to illustrate the problem solved by each firm in the model. Let $v^0(k, b, \psi, \varepsilon; \mu)$ denote the expected discounted value of a firm at the beginning of the period before the realization of the exogenous exit shock π_d , and $v(k, b, \psi, \varepsilon; \mu)$ be the continuation value after the

exit shock. If exiting, the firm chooses labor demand n , sells capital, and repays debts. The functional equation is

$$v^0(k, b, \psi, \varepsilon; \mu) = \pi_d \max_n \left\{ z\varepsilon F(k, n) - wn - b + (1 - \delta)k - \tau^c \mathcal{I}(0, k, \psi, \varepsilon) \right\} + (1 - \pi_d)v(k, b, \psi, \varepsilon; \mu) \quad (2)$$

Conditional on survival, the continuation problem is a discrete choice among three options,

$$v(k, b, \psi, \varepsilon; \mu) = \max \left\{ v^H(k, b, \psi, \varepsilon; \mu), v^L(k, b, \psi, \varepsilon; \mu), v^N(k, b, \psi, \varepsilon; \mu) \right\} ., \quad (3)$$

where $v^L(k, b, \psi, \varepsilon; \mu)$ denotes the value of investing below the threshold level \bar{I} , $v^H(k, b, \psi, \varepsilon; \mu)$ represents the value of investing larger than \bar{I} , and $v^N(k, b, \psi, \varepsilon; \mu)$ denotes the value if the firm is not paying tax.

In either case, the firm is maximizing the current dividend D and expected discounted future firm value. Let $Q(s, \mu)$ denote the stochastic discounting factor for firms' next-period value given the distribution μ . The dynamic problem for those firms that undertake investments larger than \bar{I} is

$$v^H(k, b, \psi, \varepsilon_i; \mu) = \max_{D, k', b', n} D + Q(s, \mu) \sum_{j=1}^{N_\varepsilon} \pi_{ij}^\varepsilon v^0(k', b', \psi', \varepsilon_j; \mu'), \quad (4)$$

subject to

$$0 \leq D = (1 - \tau^c)(z\varepsilon F(k, n) - wn) - b + qb' - (1 - \tau^c \omega \xi)(k' - (1 - \delta)k) + \tau^c \delta^\psi \psi. \quad (5)$$

$$k' \in ((1 - \delta)k + \bar{I}, \bar{k}) \text{ and } k > \hat{k} \quad (6)$$

$$b' \leq \theta k' \quad (7)$$

$$\psi' = (1 - \delta^\psi)\psi + (1 - \xi)\omega(k' - (1 - \delta)k) \quad (8)$$

$$\mu' = \Gamma(s, \mu) \quad (9)$$

If we rewrite the above problem with $\xi = 1$, then we get the problem for firms that undertake investment below \bar{I} ,

$$v^L(k, b, \psi, \varepsilon_i; \mu) = \max_{D, k', b', n} D + Q(s, \mu) \sum_{j=1}^{N_\varepsilon} \pi_{ij}^\varepsilon v^0(k', b', \psi', \varepsilon_j; \mu'), \quad (10)$$

subject to

$$0 \leq D = (1 - \tau^c)(z\varepsilon F(k, n) - wn) - b + qb' - (1 - \tau^c\omega)(k' - (1 - \delta)k) + \tau^c\delta^\psi\psi. \quad (11)$$

$$k' < (1 - \delta)k + \bar{I} \text{ and } k > \tilde{k} \quad (12)$$

$$b' \leq \theta k' \quad (13)$$

$$\psi' = (1 - \delta^\psi)\psi \quad (14)$$

$$\mu' = \Gamma(s, \mu) \quad (15)$$

Notice that the law of motion of deductible stock is also changed with $\xi = 1$.

Similarly, if we rewrite the H -type firms' problem with $\tau^c = 0$, then we get the N -type firms' problem as

$$v^N(k, b, \psi, \varepsilon_i; \mu) = \max_{D, k', b', n} D + \beta \sum_{j=1}^{N_\varepsilon} \pi_{ij}^\varepsilon V^0(k', b', \psi', \varepsilon_j; \mu'), \quad (16)$$

subject to

$$0 \leq D = z\varepsilon F(k, n) - wn - b + qb' - (k' - (1 - \delta)k) \quad (17)$$

$$k' \geq \max(\bar{k}, 0) \quad (18)$$

$$b' \leq \theta k' \quad (19)$$

$$\psi' = (1 - \delta^\psi)\psi + (1 - \mathcal{J}(k', k))\omega(k' - (1 - \delta)k) \quad (20)$$

$$\mu' = \Gamma(s, \mu) \quad (21)$$

Since there is no friction regarding the firm's employment decision, it pays the current wage bill after production, and the future capital decision does not affect current production. Therefore, the employment choice does not depend on the debt choice, deductible stock, or continuation value. Denote the policy functions associate to firm's employment be $N(k, \varepsilon; \mu)$, capital be $K(k, b, \psi, \varepsilon; \mu)$, debt be $B(k, b, \psi, \varepsilon; \mu)$, dividend be $D(k, b, \psi, \varepsilon; \mu)$, and remaining tax benefit be $\Psi(\psi, K(k, b, \psi, \varepsilon; \mu), k; \mu)$. I characterize these policy functions in section 3.

2.2 Household

I assume there is a unit measure of identical households in the model. In each period, households maximize their lifetime utility by choosing consumption, c , labor supply, n^h , future

firm shareholdings, λ' , and future bond holding, a' :

$$\begin{aligned}
V^h(\lambda, a; \mu) &= \max_{c, n^h, a', \lambda'} \left\{ u(c, 1 - n^h) + \beta V^h(\lambda', a'; \mu') \right\} \\
\text{s.t. } c + qa' + \int \rho_1(k', b', \psi', \varepsilon') \lambda' (d[k' \times b' \times \psi' \times \varepsilon']) + T & \\
&\leq (1 - \tau^n) w(\mu) n^h + a + \int \rho_0(k, b, \psi, \varepsilon) \lambda (d[k \times b \times \psi \times \varepsilon])
\end{aligned} \tag{22}$$

where $\rho_0(k, b, \psi, \varepsilon)$ is the dividend-inclusive price of the current share, $\rho_1(k', b', \psi', \varepsilon')$ is the ex-dividend price of the future share, τ^n is the labor tax rate, and T is the lump-sum tax imposed by the government. Let $C^h(\lambda, a; \mu)$ be the equilibrium consumption function, and $N^h(\lambda, a; \mu)$ is the labor supply function. Similarly, let $A^h(\lambda, a; \mu)$ denote the households' decision for bonds, and $\Lambda(\lambda, a; \mu)$ is the choice of firm shares.

2.3 Government

In my model economy, the government collects corporate taxes from firms and labor income taxes from households to fund exogenous government spending. The corporate tax revenue R is defined as

$$\begin{aligned}
R = \int_S \left\{ \tau^c \left[z\varepsilon F(k, N(k, \varepsilon; \mu)) - w(s, \mu) N(k, \varepsilon; \mu) - \mathcal{J}(K(k, b, \psi, \varepsilon; \mu), k) \right. \right. \\
\left. \left. \times (K(k, b, \psi, \varepsilon; \mu) - (1 - \delta)k) - \delta^\psi \psi \right] \right\} \mu(d[k \times b \times \psi \times \varepsilon]),
\end{aligned} \tag{23}$$

The government balances its budget following the following formula,

$$G = \tau^n w N^h(\lambda, a; \mu) + R + T, \tag{24}$$

where T is the lump-sum tax on households for raising bonus depreciation ξ or Section 179 threshold \bar{I} .

2.4 Recursive Equilibrium

A *recursive competitive equilibrium* is a set of functions including prices $(p, w, q, \rho_0, \rho_1)$, quantities $(N, K, \Psi, B, D, C^h, N^h, A^h, \Lambda)$, a distribution $\mu(k, b, \psi, \varepsilon)$, and (v^0, v^L, v^H, v, V^h) that solves firms' and households' optimization problems and clears the markets for assets, labor, and

output in the following conditions.

1. v^0 , v^L , v^H , and v solve (2), (3), (4), and (10). The associated policy functions for firms are (N, K, Ψ, B, D) .
2. V^h solves (22), and the associated policy functions for households are (C^h, N^h, A^h, Λ)
3. Labor market clears, i.e., $N^h(\lambda, a; \mu) = \int_{\mathcal{S}} N(k, \varepsilon; \mu) \mu(d[k \times b \times \psi \times \varepsilon])$.
4. Goods market clears, i.e.,

$$C^h(\mu, a; \mu) = \int_{\mathcal{S}} \left\{ z\varepsilon F(k, N(k, \varepsilon; \mu) - wN(k, \varepsilon; \mu)) \right. \\ \left. - (1 - \pi_d) [K(k, b, \psi, \varepsilon; \mu) - (1 - \delta)k] \right. \\ \left. + \pi_d((1 - \delta)k - k_0) \right\} \mu(d[k \times b \times \psi \times \varepsilon]) - G,$$

where k_0 is the capital allocated to entrants. I assume k_0 is a fixed fraction χ of the long-run aggregate capital stock,

$$k_0 = \chi \int k \tilde{\mu}(d[k \times b \times \psi \times \varepsilon]), \quad (25)$$

where $\tilde{\mu}$ is the steady-state distribution.

5. Government balances its budget in (24).
6. The distribution of firms, $\mu(k, b, \psi, \varepsilon)$, is a fixed point of Γ function. $\Gamma(s, \mu)$ is consistent with policy functions (K, B, Ψ) and law of motion of ε .

3 Analysis

Before solving the recursive competitive equilibrium, I reformulate the firm's problem by exploiting the optimality conditions implied by the household's problem. In equilibrium, the wage w is pinned down by the marginal rate of substitution between consumption and leisure, that is,

$$w(s, \mu) = \frac{D_2 u(c, 1 - n^h)}{(1 - \tau^n) D_1 u(c, 1 - n^h)}.$$

Similarly, the bond price q equals the inverse of the expected real interest rate. As there is no aggregate uncertainty in the economy, the expected real interest rate is $\frac{1}{\beta}$. The stochastic

discounting factor $Q(s, \mu)$ equals to household's discounting factor,

$$Q(s, \mu) = \beta \frac{D_1 u(c', 1 - n^{h'})}{D_1 u(c, 1 - n^h)}.$$

Without the loss of generality, I define $p(s, \mu)$ to be the marginal utility of consumption, $D_1 u(c, 1 - n^h)$. The $p(s, \mu)$ represents the output price that is used to evaluate the firm's current dividend.

After incorporating the household's optimality condition into the prices that firms face, I define a new value V as the product of $p(s, \mu)$ and v , and rewrite dynamic problem (2), (3), (4), and (10):

$$V^0(k, b, \psi, \varepsilon; \mu) = p(s, \mu) \pi_d \max_n \left\{ z\varepsilon F(k, n) - wn - b + (1 - \delta)k - \tau^c \mathcal{I}(0, k, \psi, \varepsilon) \right\} + (1 - \pi_d)v(k, b, \psi, \varepsilon; \mu) \quad (26)$$

where

$$V(k, b, \psi, \varepsilon; \mu) = \max \left\{ V^H(k, b, \psi, \varepsilon; \mu), V^L(k, b, \psi, \varepsilon; \mu), V^N(k, b, \psi, \varepsilon; \mu) \right\}. \quad (27)$$

The dynamic problem for firms who invest larger than the Section 179 deduction is

$$V^H(k, b, \psi, \varepsilon; \mu) = \max_{D, k', b', n} p(s, \mu) D + \beta \sum_{j=1}^{N_\varepsilon} \pi_{ij}^\varepsilon V^0(k', b', \psi', \varepsilon_j; \mu'), \quad (28)$$

subject to constraints (5)-(9). The counterpart for firms that undertake investment below the Section 179 deduction is

$$V^L(k, b, \psi, \varepsilon; \mu) = \max_{D, k', b', n} p(s, \mu) D + \beta \sum_{j=1}^{N_\varepsilon} \pi_{ij}^\varepsilon V^0(k', b', \psi', \varepsilon_j; \mu'), \quad (29)$$

subject to constraints (11)-(15). Moreover, the value function for firms not paying corporate tax is

$$V^N(k, b, \psi, \varepsilon; \mu) = \max_{D, k', b', n} p(s, \mu) D + \beta \sum_{j=1}^{N_\varepsilon} \pi_{ij}^\varepsilon V^0(k', b', \psi', \varepsilon_j; \mu') \quad (30)$$

subject to constraints (17)-(21).

I start my analysis by deriving the optimal labor choice $N(k, \varepsilon)$. Since there is no friction in the labor market, a firm's labor demand is independent of intertemporal choices. In other words, the optimal labor choice can be derived by solving $\pi(k, \varepsilon) \equiv \max_n z\varepsilon F(k, N(k, \varepsilon)) -$

$wN(k, \varepsilon)$ and get

$$N(k, \varepsilon) = \left(\frac{vz\varepsilon k^\alpha}{w} \right)^{\frac{1}{1-v}}.$$

Thus, the flow profit $\pi(k, \varepsilon)$ is rewritten as

$$\pi(k, \varepsilon) = A(w)z^{\frac{1}{1-v}}\varepsilon^{\frac{1}{1-v}}k^{\frac{\alpha}{1-v}}, \quad (31)$$

where $A(w) = \left[\left(\frac{v}{w} \right)^{\frac{v}{1-v}} - w \left(\frac{v}{w} \right)^{\frac{1}{1-v}} \right]$.

To characterize a firm's intertemporal decision, I follow [Khan and Thomas \(2013\)](#) and [Jo and Senga \(2019\)](#) and separate firms into *unconstrained* and *constrained*. Financial frictions limit firms' ability to finance externally, and thus they have to accumulate financial savings, $b < 0$, to fund their investment. Unconstrained firms are those that have already accumulated enough financial savings such that the collateral constraints will never bind in all possible states. Thus, they are indifferent between paying dividends and financial savings. Following [Khan and Thomas \(2013\)](#), I resolve this indeterminacy by requiring unconstrained firms to adopt *minimum saving policy*, i.e., they prioritize dividend payment and accumulate the lowest financial saving b' to stay unconstrained. In section 3.2, I detail the minimum saving policy.

3.1 Decisions among unconstrained firms

Let W function be the value function for unconstrained firms. The start-of-period value before the realization of exit shocks, W^0 , is

$$W^0(k, b, \psi, \varepsilon; \mu) = p(s, \mu)\pi_d \max_n \left\{ z\varepsilon F(k, n) - wn - b + (1 - \delta)k - \tau^c \mathcal{I}(0, k, \psi, \varepsilon) \right\} \\ + (1 - \pi_d)W(k, b, \psi, \varepsilon; \mu).$$

Upon survival, unconstrained firms undertake binary choice similar to (3),

$$W(k, b, \psi, \varepsilon; \mu) = \max \left\{ W^H(k, b, \psi, \varepsilon; \mu), W^L(k, b, \psi, \varepsilon; \mu), W^N(k, b, \psi, \varepsilon; \mu) \right\}.$$

As the capital decision of the unconstrained firm is orthogonal to its bond decision, I express the firm's current value as $W(k, b, \psi, \varepsilon; \mu) = W(k, 0, \psi, \varepsilon; \mu) - pb$ and the start-of-period value as $W^0(k, b, \psi, \varepsilon; \mu) = W^0(k, 0, \psi, \varepsilon; \mu) - pb$. Given these transformation, I rewrite (4), (10), and (16)

as

$$\begin{aligned}
W^H(k, b, \psi, \varepsilon_i; \mu) &= p(1 - \tau^c)\pi(k, \varepsilon) - pb + p(1 - \tau^c\omega\xi)(1 - \delta)k + p\tau^c\delta^\psi\psi \\
&\quad + \max_{k' \in [(1-\delta)k + \bar{I}, \bar{k})} \left\{ -p(1 - \tau^c\omega\xi)k' + \beta \sum_{j=1}^{N_\varepsilon} \pi_{ij}^\varepsilon W^0(k', 0, \psi', \varepsilon_j; \mu') \right\}, \\
W^L(k, b, \psi, \varepsilon_i; \mu) &= p(1 - \tau^c)\pi(k, \varepsilon) - pb + p(1 - \tau^c\omega)(1 - \delta)k + p\tau^c\delta^\psi\psi \\
&\quad + \max_{k' \leq \bar{I} + (1-\delta)k} \left\{ -p(1 - \tau^c\omega)k' + \beta \sum_{j=1}^{N_\varepsilon} \pi_{ij}^\varepsilon W^0(k', 0, \psi', \varepsilon_j; \mu') \right\}, \\
W^N(k, b, \psi, \varepsilon_i; \mu) &= p\pi(k, \varepsilon) - pb + p(1 - \delta)k \\
&\quad + \max_{k' \geq \max(\bar{k}, 0)} \left\{ -pk' + \beta \sum_{j=1}^{N_\varepsilon} \pi_{ij}^\varepsilon W^0(k', 0, \psi', \varepsilon_j; \mu') \right\},
\end{aligned}$$

where $\pi(k, \varepsilon)$ is defined by (31).

To search for the target capitals that solve the above two problems, it is necessary to find the conditional expected start-of-period value function, $W^0(k', 0, \psi', \varepsilon_j; \mu)$. As the future deductible expenses ψ' is a function of current deductible stock ψ and current capital stock k , all target capital stocks are functions of k , ψ , and ε . To be specific, let $k_H^*(k, \psi, \varepsilon)$ denotes the target capital for firms invest higher than threshold, $k_L^*(k, \psi, \varepsilon)$ be that for firms invest lower than threshold, and $k_N^*(k, \psi, \varepsilon)$ be that for firms not paying corporate tax,

$$\begin{aligned}
k_H^*(k, \psi, \varepsilon) &= \arg \max_{k' \in [(1-\delta)k + \bar{I}, \bar{k})} \left\{ -p(1 - \tau^c\omega\xi)k' + \beta \sum_{j=1}^{N_\varepsilon} \pi_{ij}^\varepsilon W^0(k', 0, \psi', \varepsilon_j; \mu') \right\}, \\
k_L^*(k, \psi, \varepsilon) &= \arg \max_{k' \leq (1-\delta)k + \bar{I}} \left\{ -p(1 - \tau^c\omega)k' + \beta \sum_{j=1}^{N_\varepsilon} \pi_{ij}^\varepsilon W^0(k', 0, \psi', \varepsilon_j; \mu') \right\}. \\
k_N^*(k, \psi, \varepsilon) &= \arg \max_{k' \geq \max(\bar{k}, 0)} \left\{ -pk' + \beta \sum_{j=1}^{N_\varepsilon} \pi_{ij}^\varepsilon W^0(k', 0, \psi', \varepsilon_j; \mu') \right\}.
\end{aligned} \tag{32}$$

Thus, the capital decision rule for unconstrained firms, $K^w(k, \psi, \varepsilon)$, follows the (S, s) policy

described below,

$$K^w(k, \psi, \varepsilon) = \begin{cases} k_L^*(k, \psi, \varepsilon) & \text{if } k \geq \frac{k_L^*(k, \psi, \varepsilon) - \bar{I}}{1 - \delta} \text{ and } W^L(\cdot) = \max \{W^H(\cdot), W^L(\cdot), W^N(\cdot)\} \\ (1 - \delta)k + \bar{I} & \text{if } k < \frac{k_L^*(k, \psi, \varepsilon) - \bar{I}}{1 - \delta} \text{ and } W^L(\cdot) = \max \{W^H(\cdot), W^L(\cdot), W^N(\cdot)\} \\ k_H^*(k, \psi, \varepsilon) & \text{if } k \in \left(\tilde{k}, \frac{k_H^*(k, \psi, \varepsilon) - \bar{I}}{1 - \delta} \right] \text{ and } W^H(\cdot) = \max \{W^H(\cdot), W^L(\cdot), W^N(\cdot)\} \\ \tilde{k} & \text{if } k \in \left(\frac{k_N^*(k, \psi, \varepsilon) - \bar{I}}{1 - \delta}, \tilde{k} \right] \text{ and } W^N(\cdot) = \max \{W^H(\cdot), W^L(\cdot), W^N(\cdot)\} \\ k_N^*(k, \psi, \varepsilon) & \text{if } k < k_N^*(k, \psi, \varepsilon) \text{ and } W^N(\cdot) = \max \{W^H(\cdot), W^L(\cdot), W^N(\cdot)\} \end{cases}.$$

For unconstrained firms, I now describe how tax policies affect firms' the *cost* and *benefit* of investment: the user cost of capital approach from [Hall and Jorgenson \(1967\)](#), and q -theory approach from [Summers, Bosworth, Tobin and White \(1981\)](#). The user cost of capital in [Hall and Jorgenson \(1967\)](#) is defined as the rental rate of capital. This rental rate is observably equivalent to the price difference between purchasing capital at date t and resale it at date $t + 1$ after discounting. Assume that a firm stay at type N across date t and $t + 1$. This firm buys one unit of capital for 1, produces one unit of output, and can resale the remaining $1 - \delta$ fraction at the same price with discounting, i.e.,

$$c^N = 1 - \beta(1 - \delta).$$

If this firm is L -type, then the cost and benefit of one unit of capital purchase is distorted by the corporate tax. It purchases one unit of capital costs $1 - \tau^c \omega$, produces $1 - \tau^c$ unit of output, and after-tax resale price of the capital is $(1 - \tau^c \omega)\beta(1 - \delta)$,

$$c^L = \frac{1 - \tau^c \omega}{1 - \tau^c} (1 - \beta(1 - \delta)).$$

For an H -type firm, the purchase of one unit of capital brings more taxable income deduction to date $t + 1$ through the deductible stock ψ . It acquires one unit of capital at cost $1 - \tau^c \omega \xi$, produces $1 - \tau^c$ unit of output, and the after-tax resale price is the same as L -type firms. However, as only ξ fraction of the tax benefit has been deducted, $1 - \xi$ fraction of the remaining benefit is accumulated in the deductible stock ψ as in (8). As a result, the firm gains additional $\beta \delta^\psi (1 - \xi) \tau^c \omega$ amount of deduction on its taxable income at date $t + 1$, and the corresponding user cost of capital is

$$c^H = \frac{1 - \tau^c \omega \xi}{1 - \tau^c} - \beta \delta^\psi (1 - \xi) \frac{\tau^c \omega}{1 - \tau^c} - \beta(1 - \delta) \frac{1 - \tau^c \omega}{1 - \tau^c}.$$

When the bonus rate ξ increases, the current cost ("down payment") of capital $1 - \tau^c \omega \xi$ is lower, while the benefit from future taxable income deduction is smaller. The fall in current

cost dominates, and c^H will be lower when the bonus rate ξ increases. As a result, raising the bonus rate will lead to a boost in investment for all firms. A similar mechanism exists when the Section 179 threshold \bar{I} is increased. This policy only applies to medium-sized firms experiencing a transition from H -type to L -type.

The effect of tax policies on the return on investment can be described by the marginal value of capital (marginal q). Let's ignore the discontinuity in the value function and focus on the case in which a firm remains H -type at the end of the period. One can derive the first-order derivative with respect to capital by the Benveniste-Scheinkman condition,

$$\beta \sum_{j=1}^{N_\varepsilon} \pi_{ij}^\varepsilon \left[\frac{\partial W^H(k', b', \psi', \varepsilon_j; \mu)}{\partial k'} + \frac{\partial W^H(k', b', \psi', \varepsilon_j; \mu)}{\partial \psi'} \frac{\partial \psi'}{\partial k'} \right]$$

The first partial derivative, $\frac{\partial W^H(k', b', \psi', \varepsilon_j; \mu)}{\partial k'}$, represents the positive *direct* effect of investment. The second partial derivative, the product of $\frac{\partial W^H(k', b', \psi', \varepsilon_j; \mu)}{\partial \psi'}$ and $\frac{\partial \psi'}{\partial k'}$, indicates the *indirect* effect of investment through deductible stocks.

As mentioned before, a higher ξ leads to a lower user cost of capital, and thus the k' choice will be larger. On the other hand, the rise in ξ results in an ambiguous indirect effect. Following the law of motion of deductible stock in (8), the increase in k' would raise ψ' . On the other hand, higher ξ leads to lower ψ' , which may hurt the marginal value on deductible stock, $\frac{\partial W^H(k', b', \psi', \varepsilon_j; \mu)}{\partial \psi'}$. In my model, the direct effect dominates the indirect effect, and thus raising the bonus rate will raise the firm value, conditional on dividend payment. Yet, in the next subsection, I will show that raising the bonus rate induces dividend payment, and the firms' value is lower under a higher bonus rate.

3.2 Minimum saving policy

The *minimum saving policy*, $B^w(k, \psi, \varepsilon)$, can be recursively calculated by the following two equations with both policy functions for labor, $N(k, \varepsilon)$, and capital, $K^w(k, \psi, \varepsilon)$,

$$\begin{aligned} B^w(k, \psi, \varepsilon) &= \min_{\varepsilon_j} (\tilde{B}(K^w(k, \psi, \varepsilon_i), \psi', \varepsilon_j)) \\ \tilde{B}(k, \psi, \varepsilon_i) &= (1 - \tau^c) \pi(k, \varepsilon_i) + \tau^c \delta^\psi \psi \\ &\quad - (1 - \tau^c \mathcal{J}(K^w(\cdot), k)) (K^w(k, \psi, \varepsilon_i) - (1 - \delta)k) \\ &\quad + q \min \{B^w(k, \psi, \varepsilon_i), \theta K^w(k, \psi, \varepsilon_i)\} \text{ if } \mathcal{I}(k', k, \psi, \varepsilon) > 0 \\ \tilde{B}(k, \psi, \varepsilon_i) &= \pi(k, \varepsilon_i) - (K^w(k, \psi, \varepsilon_i) - (1 - \delta)k) \\ &\quad + q \min \{B^w(k, \psi, \varepsilon_i), \theta K^w(k, \psi, \varepsilon_i)\} \text{ if } \mathcal{I}(k', k, \psi, \varepsilon) \leq 0 \end{aligned}$$

Above, $\tilde{B}(k, \psi, \varepsilon)$ represents the minimum level of saving (negative debt) that an unconstrained firm needs to put aside to remain unconstrained given the realization of ε_j next period. $B^w(k, \psi, \varepsilon)$, therefore, is the minimum of $\tilde{B}(K^w(\cdot), \psi', \varepsilon_j)$ over all possible ε_j to guarantee the unconstrained status of the firm for all possible future states. Notice that the accumulation of deductible stock, ψ' , enters this recursive definition, and thus firm's discrete investment choice will affect the threshold that distinguishes constrained and unconstrained firms. The current dividend D^w that unconstrained firms pay is

$$\begin{aligned} D^w(k, b, \psi, \varepsilon) &= (1 - \tau^c)\pi(k, \varepsilon) + \tau^c \delta^\psi \psi \\ &\quad - (1 - \tau^c \mathcal{J}(K^w(k, \psi, \varepsilon) - (1 - \delta)k))(K^w(k, \psi, \varepsilon) - (1 - \delta)k) \\ &\quad - b + q \min \{B^w(k, \psi, \varepsilon), \theta K^w(k, \psi, \varepsilon)\} \text{ if } \mathcal{I}(k', k, \psi, \varepsilon) > 0 \\ D^w(k, b, \psi, \varepsilon) &= \pi(k, \varepsilon) - (K^w(k, \psi, \varepsilon) - (1 - \delta)k) \\ &\quad - b + q \min \{B^w(k, \psi, \varepsilon), \theta K^w(k, \psi, \varepsilon)\} \text{ if } \mathcal{I}(k', k, \psi, \varepsilon) \leq 0 \end{aligned}$$

Both policy tools, ζ and \bar{I} , directly enter D^w through the indicator function $\mathcal{J}(k', k)$. As a result, raising investment subsidies will increase the dividend payment and lead to a fall in the unconstrained firms' value function. In my calculation, the bonus rate ζ creates a larger boost in the dividend issuance.

3.3 Decisions among constrained firms

I next consider the decisions of continuing firms identified by $(k, b, \psi, \varepsilon)$ that have a nonzero probability of facing a binding collateral constraint in the future states. They cannot adopt the unconstrained capital decision rules, and therefore bond policy functions implied by the minimum saving policy. Therefore, they do not issue dividend payments and accumulate financial savings, $b < 0$, to fund their capital investment. As a result, we can characterize their bond choices by zero dividend condition, $D = 0$ given a choice in capital. In particular, let's denote the capital decision rules as $K^c(k, b, \psi, \varepsilon)$, and bond decision rules as $B^c(k, b, \psi, \varepsilon)$. Let $J(k, b, \psi, \varepsilon; \mu)$ be the value function for constrained firms. They undertake the same binary choice between investing higher or lower than the Section 179 threshold:

$$J(k, b, \psi, \varepsilon; \mu) = \max \left\{ J^H(k, b, \psi, \varepsilon; \mu), J^L(k, b, \psi, \varepsilon; \mu), J^N(k, b, \psi, \varepsilon; \mu) \right\},$$

where J^H , J^L and J^N are the value function for H -type, L -type, and N -type firms.

For firms that invest higher than the threshold, their value function conditional on survival

is

$$\begin{aligned}
J^H(k, b, \psi, \varepsilon; \mu) &= \max_{k' \in \Omega_H(k, b, \psi, \varepsilon)} \beta \sum_{j=1}^{N_\varepsilon} \pi_{ij}^\varepsilon V^0(k', b_H(k'), \psi', \varepsilon_j; \mu'), \\
\text{subject to} & \\
b_H(k') &= \frac{1}{q} \left(- (1 - \tau^c) \pi(k, \varepsilon) + b - \tau^c \delta^\psi \psi + (1 - \tau^c \omega \xi)(k' - (1 - \delta)k) \right), \\
\psi' &= (1 - \delta^\psi) \psi + (1 - \xi)(k' - (1 - \delta)k),
\end{aligned} \tag{33}$$

The bond choice for H -type firms, $b_H(k')$, is formulated by The choice sets for H -type firms' problem are defined by

$$\Omega_H(k, b, \psi, \varepsilon) = [(1 - \delta)k + \bar{I}, \min \{ \bar{k}_H(k, b, \psi, \varepsilon), \bar{k}(k, \psi, \varepsilon), K^w(k, \psi, \varepsilon) \}],$$

where \bar{k}_H is the maximum affordable capital with binding collateral constraints for H -type firms,

$$\bar{k}_H = \frac{(1 - \tau^c) \pi(k, \varepsilon) - b + (1 - \tau^c \omega)(1 - \delta)k + \tau^c \delta^\psi \psi}{1 - \tau^c \omega \xi - q\theta}$$

Let the bonus depreciation rate $\xi = 1$, we get the Bellman equation for L -type firms

$$\begin{aligned}
J^L(k, b, \psi, \varepsilon; \mu) &= \max_{k' \in \Omega_L(k, b, \psi, \varepsilon)} \beta \sum_{j=1}^{N_\varepsilon} \pi_{ij}^\varepsilon V^0(k', b_L(k'), \psi', \varepsilon_j; \mu'), \\
\text{subject to} & \\
b_L(k') &= \frac{1}{q} \left(- (1 - \tau^c) \pi(k, \varepsilon) + b - \tau^c \delta^\psi \psi + (1 - \tau^c \omega)(k' - (1 - \delta)k) \right), \\
\psi' &= (1 - \delta^\psi) \psi.
\end{aligned} \tag{34}$$

The choice set $\Omega_L(k, b, \psi, \varepsilon)$ used above is defined as

$$\Omega_L(k, b, \psi, \varepsilon) = [0, \max \{ 0, \min \{ (1 - \delta)k + \bar{I}, \bar{k}_L(k, b, \psi, \varepsilon), K^w(k, \psi, \varepsilon) \} \}],$$

while the maximum affordable capital is

$$\bar{k}_L = \frac{(1 - \tau^c) \pi(k, \varepsilon) - b + (1 - \tau^c \omega)(1 - \delta)k + \tau^c \delta^\psi \psi}{1 - \tau^c \omega - q\theta}.$$

Lastly, the value function iteration for N -type firms is equivalent to setting $\tau^c = 0$ in H -type

firms' problem,

$$\begin{aligned}
J^N(k, b, \psi, \varepsilon; \mu) &= \max_{k' \in \Omega_N(k, b, \psi, \varepsilon)} \beta \sum_{j=1}^{N_\varepsilon} \pi_{ij}^\varepsilon V^0(k', b_N(k'), \psi', \varepsilon_j; \mu'), \\
&\text{subject to} \\
b_N(k') &= \frac{1}{q} \left(-\pi(k, \varepsilon) + b + (k' - (1 - \delta)k) \right), \\
\psi' &= (1 - \delta^\psi)\psi + (1 - \mathcal{J}(k', k))(k' - (1 - \delta)k),
\end{aligned} \tag{35}$$

The above choice set $\Omega_N(k, b, \psi, \varepsilon)$ is defined as

$$\Omega_N(k, b, \psi, \varepsilon) = [0, \min \{ \bar{k}_N, \max \{ \bar{k}, 0 \}, K^w(k, \psi, \varepsilon) \}]$$

while the maximum affordable capital is

$$\bar{k}_N = \frac{\pi(k, \varepsilon) - b + (1 - \delta)k}{1 - q\theta}.$$

Let the capital stock solving (33), (34), and (35) be $\hat{k}_H(k, b, \psi, \varepsilon)$, $\hat{k}_L(k, b, \psi, \varepsilon)$, and $\hat{k}_N(k, b, \psi, \varepsilon)$, respectively. The constrained firms' decision rules on capital are

$$K^c(k, b, \psi, \varepsilon) = \begin{cases} \hat{k}_H(k, b, \psi, \varepsilon) & \text{if } J(\cdot) = J^H(\cdot) \text{ and } k > \tilde{k} \\ \hat{k}_L(k, b, \psi, \varepsilon) & \text{if } J(\cdot) = J^L(\cdot) \text{ and } k > \hat{k} \\ \hat{k}_N(k, b, \psi, \varepsilon) & \text{if } J(\cdot) = J^N(\cdot) \end{cases} \tag{36}$$

Similarly, the bond decision rules are

$$B^c(k, b, \psi, \varepsilon) = \begin{cases} b^H(\hat{k}_H(k, b, \psi, \varepsilon)) & \text{if } J(\cdot) = J^H(\cdot) \text{ and } k > \tilde{k} \\ b^L(\hat{k}_L(k, b, \psi, \varepsilon)) & \text{if } J(\cdot) = J^L(\cdot) \text{ and } k > \hat{k} \\ b^N(\hat{k}_N(k, b, \psi, \varepsilon)) & \text{if } J(\cdot) = J^N(\cdot) \end{cases} \tag{37}$$

4 Calibration

Table 1 lists the parameter set obtained from calibration after some parameters are set outside the model. Table 2 summarizes the calibrated moments. Total factor productivity z is set to 1 in the steady state. I set the length of a period to one year to match the establishment-level investment data. The functional form of the representative household's utility is assumed to be

$u(c, l) = \log c + \phi l$, following Rogerson (1988). I assume Cobb-Douglas production function, $z\epsilon F(k, n) = z\epsilon k^\alpha n^\nu$. The initial capital k_0 is defined as a fraction of steady-state aggregate capital, as specified in (25). Both initial bond level b_0 and initial deductible stock ψ_0 are set to zero. The household's discount rate β is set to imply 4 percent of the annual interest rate. The disutility from working, ϕ , is determined to reproduce hours of work equal to one-third. The rate of capital depreciation, δ , corresponds to an investment-capital ratio of approximately 6.9 percent. Labor share ν is 60 percent, as seen in US postwar data.

To accurately assess the impact of partial irreversibility from corporate taxation on investment, my model must reproduce firm-level evidence on investment dynamics. I begin by assuming the idiosyncratic productivity shock ϵ follows log AR(1) process with persistence ρ_ϵ and standard deviation σ_{η_ϵ} . The evolution of ϵ is $\log \epsilon' = \rho_\epsilon \log \epsilon + \eta'_\epsilon$, with $\eta'_\epsilon \sim N(0, \sigma_{\eta_\epsilon}^2)$. I choose three parameters, ρ_ϵ , σ_{η_ϵ} , and average eligible investment ratio ω to match the moments of the investment rate distribution in Cooper and Haltiwanger (2006). In particular, I choose $\rho_\epsilon = 0.6$ to match the correlation of the investment rates, $\sigma_\epsilon = 0.1$ to match the standard deviation of the investment rates, and $\omega = 0.6$ to match the firm mass that has investment rates larger than 20 percents. Given the value specified in table 1, I use Tauchen (1986) method to discretize the firm's log-normal idiosyncratic productivity process with 7 values ($N_\epsilon = 7$) to obtain $\{\epsilon_j\}_{j=1}^{N_\epsilon}$ and $(\pi_{ij}^\epsilon)_{i,j=1}^{N_\epsilon}$.

I calibrate the value of two policy tools, ζ and \bar{I} , to the 2015 level of bonus rate and Section 179 threshold. In 2015, the bonus rate is 0.5, i.e., $\zeta = 0.5$. In the same year, the Section 179 threshold is \$500,000. To find the model counterpart of the Section 179 threshold, I calculate the average investment in 2015 using data from the Bureau of Economic Analysis and Statistics of U.S. Businesses. The investment in 2015 from BEA Table 3.7 is 2459.8 billion. Meanwhile, there are 5,900,731 firms in the US. This gives me an average investment of \$416,853. I calibrate the value of \bar{I} using the same proportionality between aggregate investment generated by the model and average investment in the data. The aggregate equals to the average in the model because of the unit measure of firm distribution. With this observation, the calibrated value of \bar{I} is 0.092.

To demonstrate the importance of investment deductions in replicating realistic investment dynamics, I compare two model-generated investment rate distribution, as shown in figure 2. The solid blue line shows the model with investment deductions under the parameters $\zeta = 0.5$ and $\bar{I} = 0.092$, while the dashed yellow line represents the model without investment deductions, essentially setting ζ and \bar{I} equals to zero. The Model with investment deductions closely matches the empirical investment rate distribution in Cooper and Haltiwanger (2006).

In the model without investment deductions, most firms will fall into the inaction region

implied by the (S, s) decision rules, and thus the spike of firms in the investment rate distribution. When investment deductions are implemented, firms previously in the inaction region invest up to the \bar{I} threshold. This leads to a shift in distribution with largest mass of firms now located at positive investment rates.

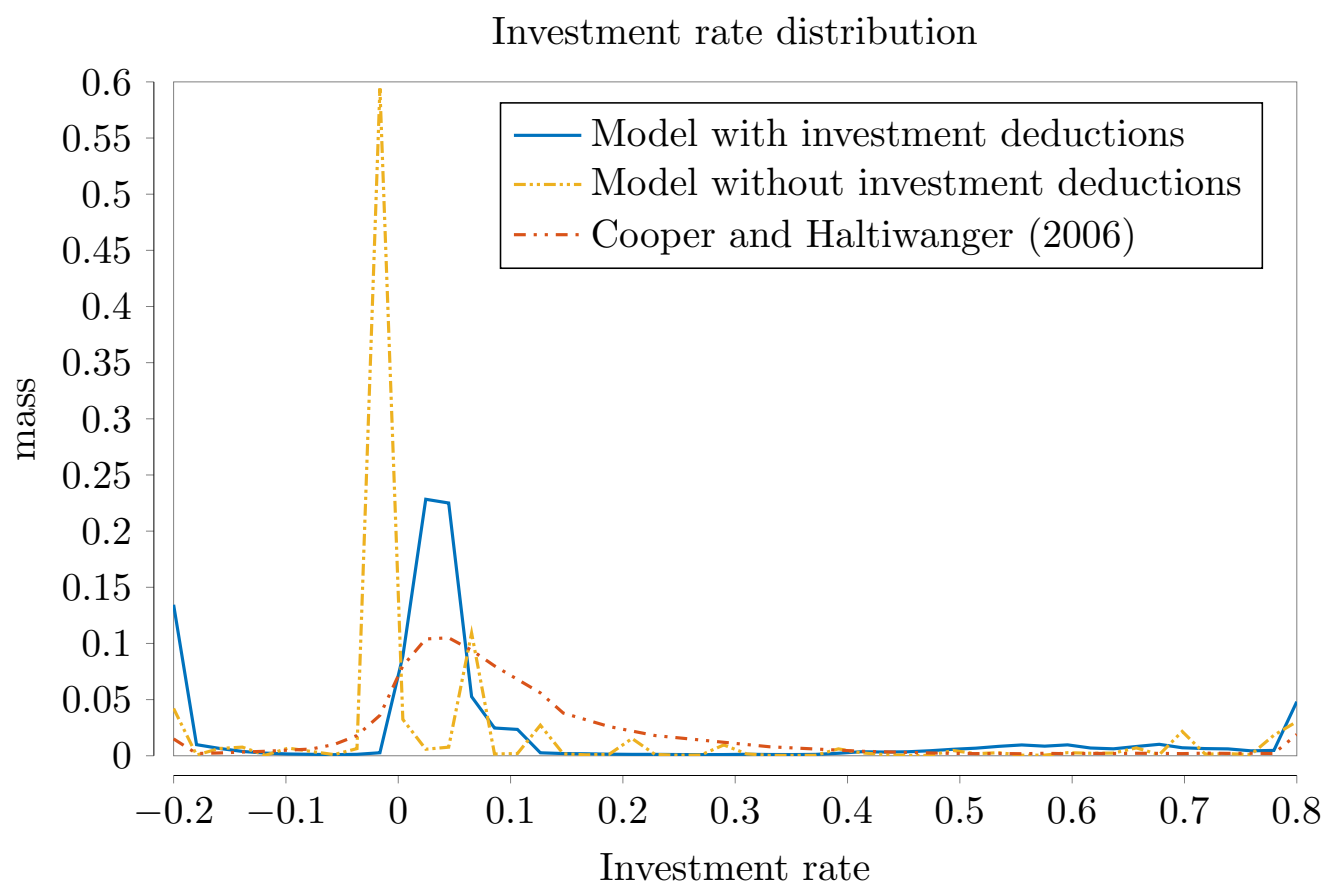
Furthermore, the variation in irreversibility results in a smoother distribution of investment rates. For L -type firms that are investing, their investment is not subject to any irreversibility. H -type firms, on the other hand, do face irreversibility as the purchasing price of capital is $1 - \tau^c \omega \xi$, while the after-tax selling price is $1 - \tau^c \omega$. Thus, the implied irreversibility is $1 - \frac{1 - \tau^c \omega}{1 - \tau^c \omega \xi} = 0.067$. Firms that face the highest irreversibility are N -type firms. The degree of irreversibility is $1 - \frac{1 - \tau^c \omega}{1} = 0.126$, much higher than H -type firms and the numbers in the literature¹⁶. Since firms facing high irreversibility are less likely to downsize their capital, this variation in irreversibility causes a more dispersed investment rate distribution compared to the model without deductions.

I further verify my model by replicating the investment-weight tax term elasticity documented in [Zwick and Mahon \(2017\)](#). To generate a comparable panel to [Zwick and Mahon \(2017\)](#), I include both constrained and unconstrained firms in my simulation. As the estimate comes from difference-in-difference around the policy window, I do not include general equilibrium effects regarding increase in bonus rate ξ . I simulate 50,000 firms for 100 period. I shock the economy with the credit parameter θ drop by 27% at date 79, and boost bonus rate from 0.5 to 1.0 at date 80. I calculate the tax term elasticity by the percentage change in investment between date 79 to date 80 over the percentage change in tax term, $\frac{1 - \tau^c \omega \xi}{1 - \tau^c}$. This exercise captures the background and policy implementation in 2010.

The aggregate tax term elasticity generated from my model is -1.23 , while the empirical estimate from [Zwick and Mahon \(2017\)](#) is -1.6 . Figure 3 shows the elasticity across firm size measured in sales. My model captures the negative relationship between firm size and responsiveness toward policy, and tightly matches the scale of responses for firms in the smallest three bins. Large firms in my model are free from financial frictions and already reach their target capital. Therefore, they do not change their investment even in a credit shock, resulting in responses smaller than empirical estimates.

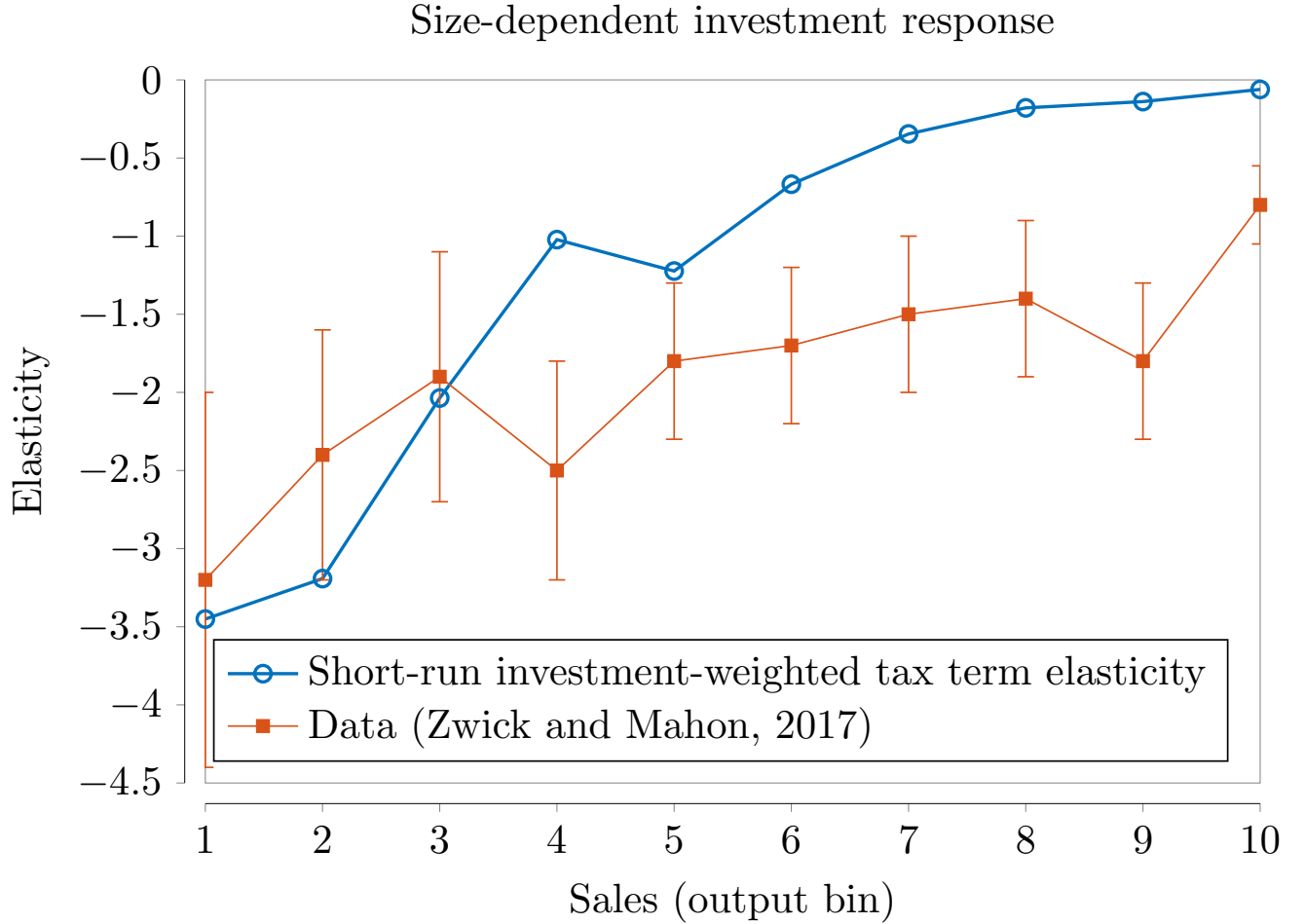
¹⁶[Khan and Thomas \(2013\)](#) has calibrated the degree of partial irreversibility as 0.046.

Figure 2: Investment rate distribution



Note: This figure shows the investment rate distribution of models with and without investment deductions, and the empirical dataset from [Cooper and Haltiwanger \(2006\)](#). Both models are solved to generate by simulating 50,000 unconstrained firms over 100 periods to create a comparable dataset to that in [Cooper and Haltiwanger \(2006\)](#).

Figure 3: Short-run size dependent tax term elasticity to investment



Note: This figure shows the short-run investment-weighted tax term elasticity to investment as defined in [Zwick and Mahon \(2017\)](#). I simulate 50,000 firms over 300 periods, and allow unexpected raise of bonus rate from 50% to 100% at period 240 using the partial equilibrium decision rules. I then compute the how much does the change in tax term, i.e., $\frac{1-\tau^c\omega^c}{1-\tau^c}$, affects the aggregate investment at each bin.

Table 1: Parameters for quantitative model

	Parameter	Value	Reason
<i>Calibrated parameters</i>			
Discount rate	β	0.96	4% real interest rate
Capital share	α	0.3	private capital-output ratio
Labor share	ν	0.6	labor share
Labor tax rate	τ^n	0.25	government spending-output ratio
Preference for leisure	φ	2.05	one-third of time endowment
Capital depreciation rate	δ	0.069	average investment-equipment ratio
Collateralizability	θ	0.54	debt-to-capital ratio
Credit crunch	θ_l	0.3942	26% decrease in debt
Persistence of ε	ρ_ε	0.6	investment distribution moments
Standard deviation of ε	$\sigma_{\eta_\varepsilon}$	0.113	investment distribution moments
Average ratio of eligible investment	ω	0.6	investment distribution moments
<i>Exogenous parameters</i>			
fraction of entrants capital endowment	χ	0.1	10% of aggregate capital
exogenous exit rate	π_d	0.1	10% entry and exit
Corporate tax rate	τ^c	0.21	US Tax schedule after TCJA
Tax benefit depreciation rate	δ^ψ	0.138	$\delta^\psi = 2\delta$ (Double-declining balance)
Bonus depreciation rate in baseline	ξ	0.5	2015 bonus rate
Section 179 threshold	\bar{I}	0.092	2015 threshold model counterpart

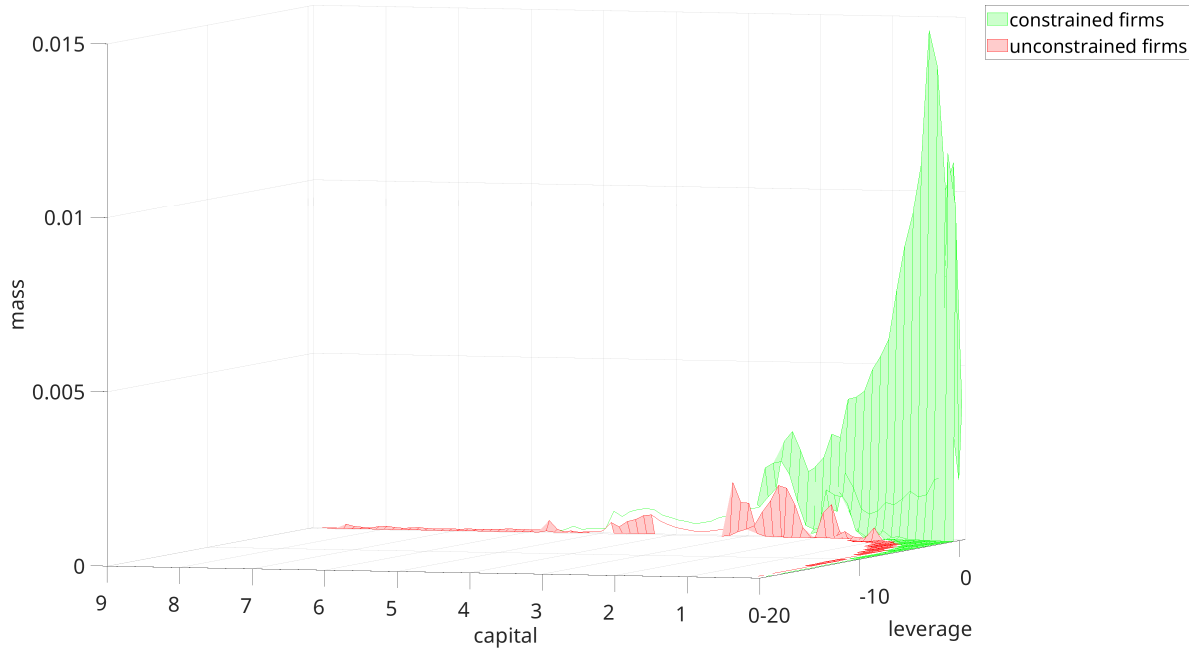
Table 2: Calibrated moments

Parameter	Target		Model
$\beta = 0.96$	real interest rate	= 0.04	0.04
$\alpha = 0.3$	private capital-output ratio	= 2.3	2.03
$\nu = 0.6$	labor share	= 0.6	0.6
$\tau^n = 0.25$	government spending-output ratio	= 0.21	0.201
$\delta = 0.069$	average investment-capital ratio	= 0.069	0.069
$\varphi = 2.05$	hours worked	= 0.33	0.33
$\theta = 0.54$	debt-to-assets ratio	= 0.37	0.371
$\theta_l = 0.3942$	decreases in debt	= 0.26	0.257
$\rho_\varepsilon = 0.6$	std. investment rate distribution	= 0.337	0.300
$\sigma_\varepsilon = 0.1$	corr. investment rate distribution	= 0.058	0.050
$\omega = 0.6$	lumpy investment > 20%	= 0.186	0.185

5 Steady State

Figure 4 presents the stationary distribution in my model over capital and leverage levels at the medium productivity. I collapse this distribution by summing over the deductible stock state variable. This figure effectively displays two distributions, the constrained firms' distribution in color green, and the unconstrained firms' distribution in color red. The highest spikes in the constrained firms' distribution represent 10 percent of entering firms, with zero debt and initial capital at k_0 . The spike gradually decreases as the capital stock increases, indicating how the forward-looking collateral constraints limit firms' capability to accumulate their capital. Once a firm becomes unconstrained, it follows the minimum saving policy implied by the unconstrained level of capital. What's different from the standard model is that there is a small mass of firms that are holding high levels of leverage and capital simultaneously.

Figure 4: Distribution: medium productivity



To explain why firms in my model hold high levels of capital and leverage, I present the policy functions for capital k' , deductible stock ψ' , and bond b' across capital levels for the highest level of idiosyncratic productivity ε , as shown in figure 5a. Three investment types— L , H , and N —are distinguished by two key thresholds: the Section 179 deduction threshold \bar{I} and the zero-taxable-income threshold \bar{k} . The green vertical line denotes the division between constrained firms (left) and unconstrained firms (right).

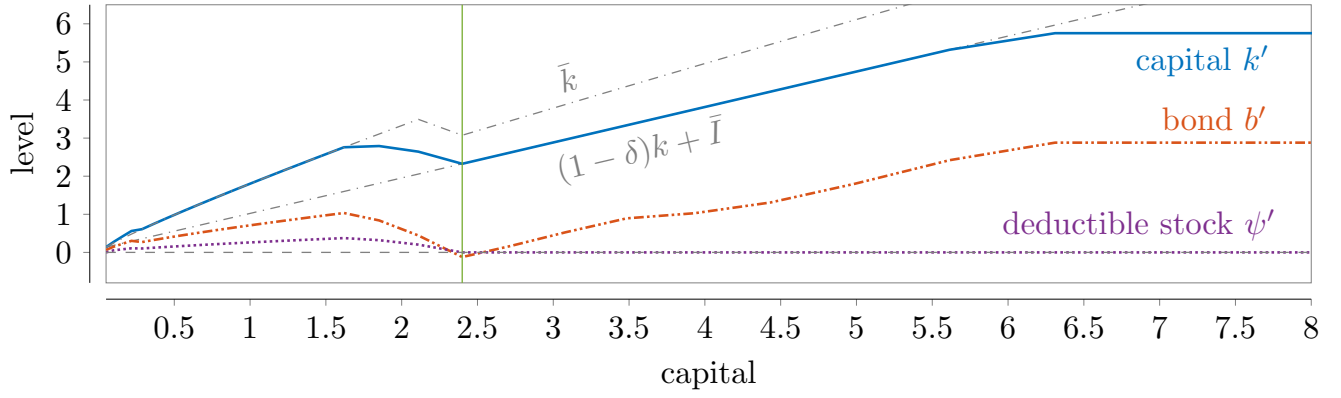
While constrained firms behavior is consistent with models without corporate taxes (Khan and Thomas, 2013; Jo and Senga, 2019), high productivity unconstrained firms exhibit positive size-leverage relationship as seen in Compustat (Chatterjee and Eyigungor, 2023). Constrained firms borrow to accumulate both capital and deductible stock, adhering to the zero-dividend condition $D = 0$. Once they reach the plateau at k_N^* , they invest up to the \bar{k} to avoid paying corporate taxes. When they become H -type firms, they slow down their capital accumulation and in turn accumulate financial savings because the return on investment are taxed. As their investment is equal to \bar{I} , they are eligible to Section 179 expensing, and their can deduct all of their investment expenditure immediately. This tax incentives induces them to invest up to \bar{I} and optimally accumulated debt to finance such investment, capturing the positive size-leverage relationship.

On the other hand, low productivity firms' behavior is similar to the standard model, as shown in figure 5b. They maintain the same level of debt and utilize the Section 179 expensing to invest up to \bar{I} . Once they reach the target capital, they start to deleverage and eventually accumulates financial savings when they are unconstrained. The comparison between firms with different productivity elucidates how corporate taxation distorts their decisions.

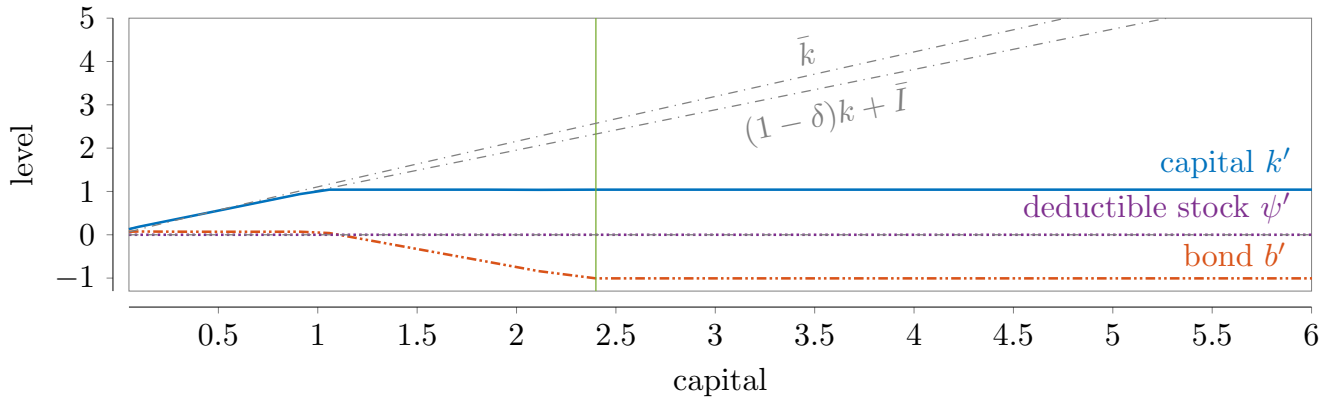
Figure 6a displays the average capital, deductible stock, and leverage choices for a cohort of 50,000 firms over 100 periods with exogenous entry and exit. On average, firms raise capital, deductible stock, and debt for the first 10 periods of their life. After this period, they begin reducing debt and start accumulating financial savings around period 20. By period 25, both the average capital and average deductible stock have reached their unconstrained levels, and average bond levels stabilize by period 30.

To illustrate how deductions affect the firms' life cycle, figure 6 compares average capital and bond levels in economies with and without deductions. The solid blue lines show the model with deductions, and the dashed orange lines represent model without deductions. Allowing more deductions induce firms to bear more debt for a faster capital accumulation in the early stage. Once their capital reach the unconstrained level, firms in the deduction-present economy save less than firms without deduction. The lower user cost of capital from deductions reduces the need to accumulate large financial savings to buffer against idiosyncratic productivity shocks.

Figure 5: Choice of capital, bonds, and deductible stock are plotted for each level of current capital stock



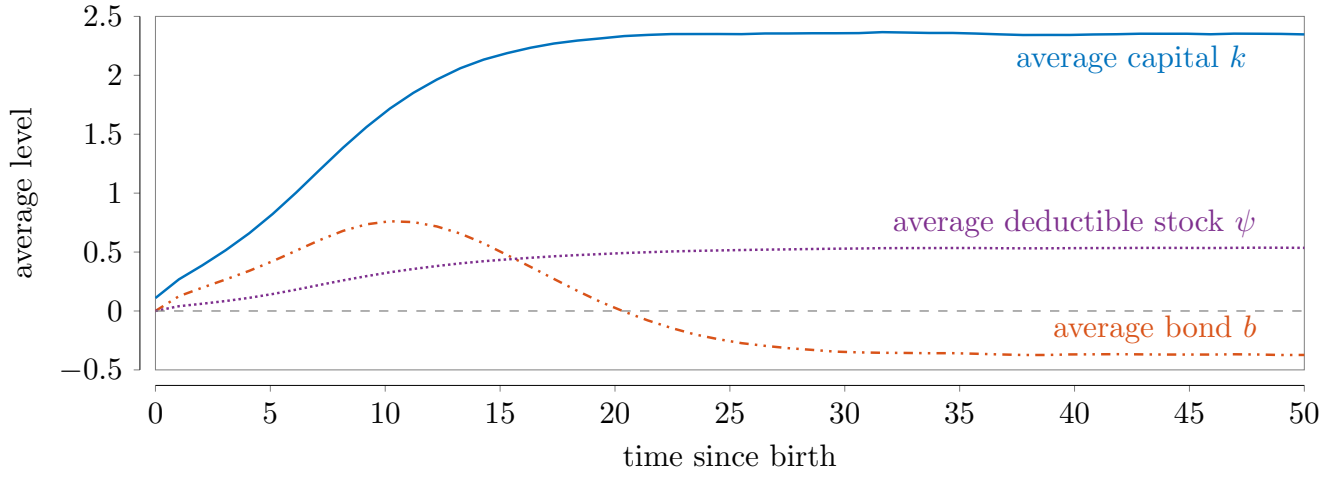
(a) Firm decision rules with high productivity ($\varepsilon = 1.1289$)



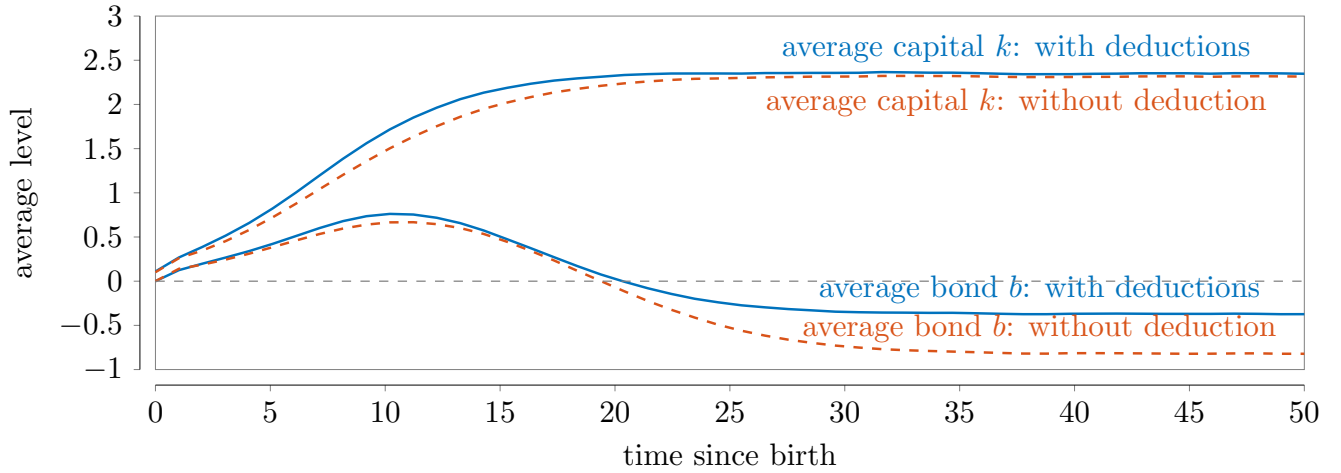
(b) Firm decision rules with low productivity ($\varepsilon = 0.7847$)

Note: Decision rules are plotted given zero current bond and zero current deductible stock.

Figure 6: Cohort average capital, bond, and deductible stock are constructed from a simulation of a balanced panel of firms.



(a) Cohort in steady state



(b) Comparing economy with and without deductions

Note: Model with deductions are calculated with $\zeta = 0.5$ and $\bar{I} = 0.092$, and model without deduction are calculated with both ζ and \bar{I} equals to zero.

6 Long-run effects of corporate tax deduction

I next examine the long-run effects of corporate tax deductions. First, I provide an overview of the policy experiments in my model. Next, I discuss the aggregate changes following a expansion of investment deductions in general equilibrium.

6.1 Overview of policy experiments

In my policy experiments, I compare the equilibrium outcomes of the baseline model from previous sections with the new steady states under each policy intervention. Specifically, I measure changes in equilibrium steady states under each policy relative to the baseline. The policy experiments are based on provisions in the Tax Cuts and Jobs Act (TCJA) of 2017, focusing on three key provisions: the bonus depreciation rate ξ , Section 179 expensing limit \bar{I} , and the corporate tax rate τ^c ¹⁷.

I conduct four policy experiments: (1) expanding Section 179 expensing limit \bar{I} (S179), (2) expanding bonus depreciation rate ξ (Bonus), (3) expanding both \bar{I} and ξ (S179 + Bonus), and (4) reducing the corporate tax rate τ^c (Tax Cut). To fairly assess the effectiveness of each policy, I set the value of each policy tool so that the implied cost of the policy \tilde{T} is 0.3 percent of steady-state output. This results in $\bar{I} = 0.292$, $\xi = 0.69$, and $\tau^c = 0.195$ for experiments 1, 2, and 4, respectively. For experiment 3, which combines \bar{I} and ξ , I set $\bar{I} = 0.239$ and $\xi = 0.566$ to ensure a policy cost consistent with the other experiments.

6.2 Aggregate results from policy experiments

Table 3 summarized the result from policy experiments. Comparing four policy experiments with the baseline model, I found that all experiments show a positive impact on aggregate output, consumption, capital, and investment, and raising the Section 179 threshold is the most effective. Output and consumption increase by 1.78 and 1.55 percent with the threshold is increased. On the other hand, raising the bonus rate only delivers 1.23 and 0.93 percent boost in output and consumption, respectively. Cutting corporate tax rate is the least effective among all policy considered, with only 0.81 percent boost in GDP and 0.56 percent increase in consumption. When both Section 179 expensing and bonus depreciation are implemented, the boost in output and consumption is 1.48 and 1.27 percent, smaller than the effect of raising

¹⁷Table 1 in Chodorow-Reich, Smith, Zidar and Zwick (2024) summarizes all domestic provisions in the TCJA, including the corporate tax rate reduction, accelerated depreciation, Domestic Production Activities Deduction (DPAD), alternative minimum tax, deductions for foreign-derived intangible income, and carryforward of net operating losses.

Section 179 threshold. The reason why both policies partially cancel each other is because both policies are sharing the same tax base. When Section 179 expensing become more generous, the tax base of bonus depreciation shrinks, eroding its effectiveness (Ohn, 2019).

Bonus depreciation is generally less effective as it also reduces the user cost of capital for unconstrained firms, allowing a fraction of taxpayer-funded deductions to be distributed as dividends rather than reinvested. Table 3 shows that while aggregate dividends increase across all three policy experiments, the increase is highest when the bonus rate is raised. Specifically, bonus depreciation leads to an 8.13 percent increase in dividend payments relative to the baseline, compared to only a 0.21 percent increase when the Section 179 threshold is raised.

This outcome stems from the untargeted nature of increasing the bonus rate. Unconstrained firms, which already free from financial frictions, benefit from the reduced user cost of capital, allowing them to more easily reach their target capital levels and distribute remaining cash as dividends. This endogenous interaction between firms' financial positions and investment decisions counteracts the policy goal of stimulating economic growth, as funds intended to encourage investment are diverted to dividends instead.

Figure 7 illustrates the increased effectiveness of Section 179 expensing by showing the cumulative distribution of excess returns on investment. The excess return on investment, defined as the marginal value of capital minus the cost of capital after accounting for investment deductions, represents the wedge in the investment Euler equation. Efficient investment results in zero excess returns, indicating firms are fully optimizing their capital allocations.

In the baseline model, only 16 % of firms invest efficiently. Under Section 179 expensing, this proportion increases to 27%, while bonus depreciation raises it to just 24%. Tax cuts are the least effective policy among all experiments, with only 16.7% of firms reaching efficient investment. The same trend appears in the average excess return on investment, confirming that Section 179 expensing is the most effective policy for alleviating capital misallocation.

Next, I investigate how firm heterogeneity interact with each policy. I calculate the percentage deviation in the average excess return on investment across different productivity levels, comparing each policy scenario to the baseline model in figure 8. Section 179 expensing encourages high-productivity firms to self-select into investment, leading to a more efficient allocation of capital. Low-productivity firms, however, move even farther from efficient investment, resulting in greater capital misallocation among them. In contrast, bonus depreciation distributes tax benefits broadly across firms, resulting in a more diffuse effect that does not contribute to production as effectively.

Figure 7: Cumulative distribution of excess return

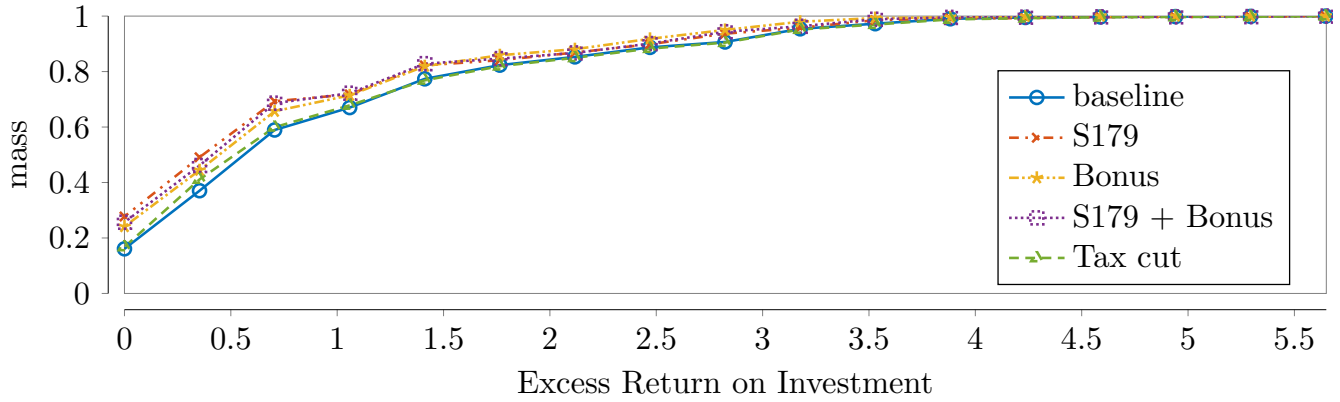


Figure 8: Policy comparison: average excess return across productivity

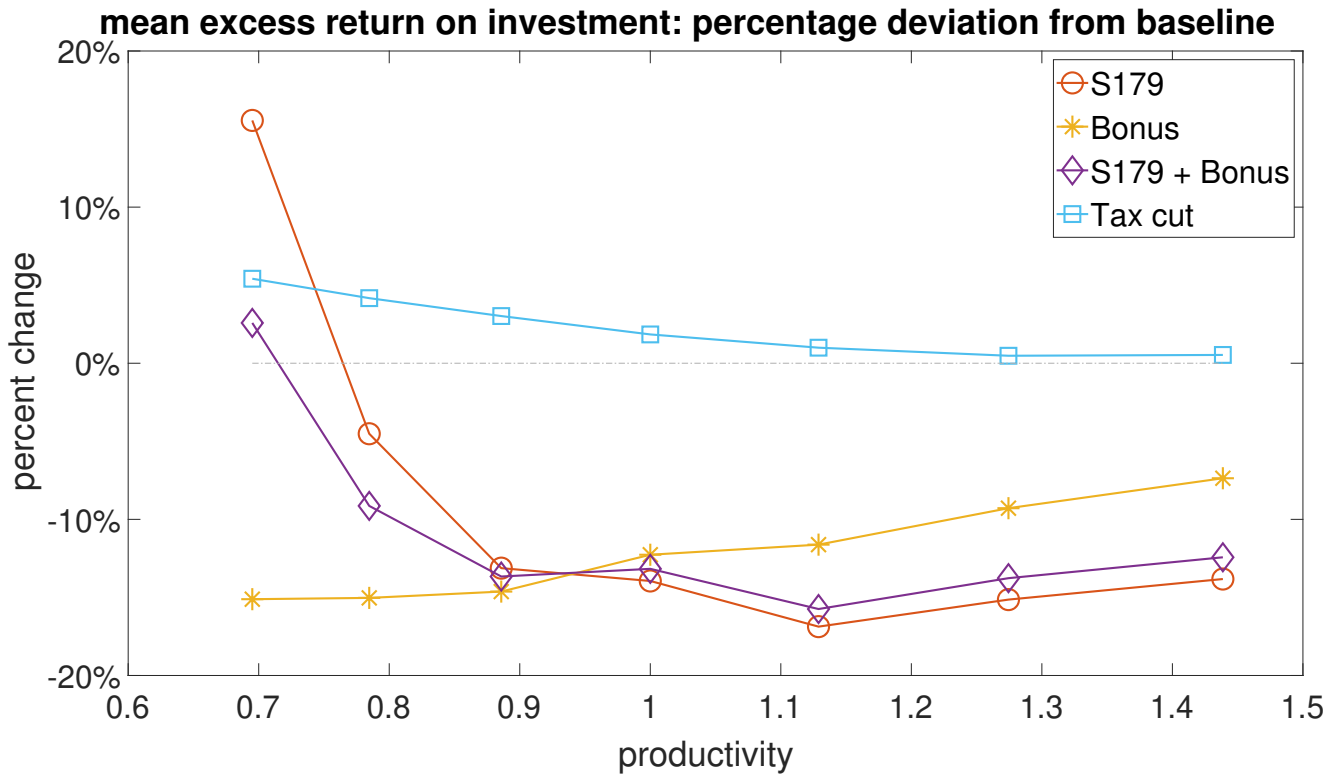


Table 3: Aggregate results from policy experiments

	Description	Baseline	S179	Bonus	S179 + Bonus	Tax cut
<i>Aggregates</i>						
Y	aggregate output	(0.54)	1.78%	1.23%	1.48%	0.81%
C	aggregate consumption	(0.36)	1.55%	0.93%	1.27%	0.56%
K	aggregate capital	(1.10)	4.43%	3.42%	3.60%	2.16%
I	aggregate investment	(0.08)	4.43%	3.42%	3.60%	2.16%
N	aggregate labor	(0.33)	0.22%	0.30%	0.21%	0.25%
$B > 0$	aggregate debt	(0.41)	7.02%	13.72%	5.97%	3.04%
R	corporate tax revenue	(0.03)	-3.70%	-3.87%	-3.85%	-4.46%
\hat{z}	measured TFP	(1.02)	0.33%	0.03%	0.28%	0.01%
<i>Prices</i>						
p	marginal utility of consumption	(2.80)	-1.53%	-0.92%	-1.25%	-0.55%
w	wage	(0.97)	1.55%	0.93%	1.27%	0.56%
<i>Distribution</i>						
μ_{unc}	unconstrained firm mass	(0.08)	14.84%	21.78%	1.77%	-13.17%
μ_{con}	constrained firm mass	(0.92)	-1.31%	-1.92%	-0.16%	1.16%
$\mu_{\text{unc}}K$	capital: unconstrained	(2.69)	-5.47%	0.01%	-6.85%	3.55%
$\mu_{\text{con}}K$	capital: constrained	(0.96)	4.78%	0.80%	5.95%	3.99%
<i>Financial Variables</i>						
D	dividend	(0.03)	0.21%	8.13%	1.10%	-3.88%
$\mu V(\cdot)$	average firm value	(3.43)	-2.56%	-6.43%	-2.64%	1.88%
μc	user cost of capital	(0.11)	-10.83%	-1.30%	-8.63%	67.55%

Notes: values in policy experiments are expressed as a percentage of the baseline value. Baseline model: $(\bar{I}, \bar{\xi}) = (0.092, 0.5)$. S179 model: $(\bar{I}, \bar{\xi}) = (0.292, 0.5)$. Bonus model: $(\bar{I}, \bar{\xi}) = (0.092, 0.69)$. S179 + Bonus model: $(\bar{I}, \bar{\xi}) = (0.239, 0.566)$.

7 Business cycles

Next, I consider business cycles within my model by examining responses to aggregate TFP shocks and credit shocks. I analyze both the extensive and intensive margins of investment deductions in dynamics. For the extensive margin, I compare responses between two economies: one with investment deductions and one without. For the intensive margin, I quantify the extent to which a temporary increase in investment deductions can mitigate the trough of recessions.

I use a perfect foresight transition approach to solve for these responses, abstracting from aggregate uncertainty. Impulse responses are computed over a horizon of \bar{T} periods following TFP and credit shocks. Throughout, government spending $\{\bar{G}_t\}_{t=1}^{\bar{T}}$ remains fixed, with any policy-induced changes funded through a lump-sum tax on households. The fiscal cost of these

policies is measured by the sequence of changes in corporate tax revenue $\{R\}_{t=1}^{\bar{T}}$.

7.1 Extensive margin

Figure 9 illustrates the responses of two economies to a 2.18% drop in TFP z at date 1 with persistence 0.909. The responses are nearly identical, with debt as the only exception. TFP shocks affect the return on investment but not the cost. Since investment deductions lower the user cost of capital without increasing firms' flow profit, raising tax incentives do not resolve the capital misallocation arise from TFP shocks.

On the contrary, investment deductions accelerate recoveries from recessions that is originated from credit shocks. Figure 10 shows the responses of two economies to a 27% drop in credit θ at date 1 with the same persistence. The half life of output decreased by 12.5%, from date 16 to 14. Additionally, investment deductions also mitigate the capital misallocation through the endogenous TFP channel, reducing the half life of endogenous TFP by 25%, from date 16 to 12. These results demonstrate the effectiveness of investment deductions in facilitating economy recoveries.

Why investment deductions mitigate recessions under credit shocks but not TFP shocks? Similar to what has been discussed previously, credit shocks increase the cost of investment by directly impacting the funding available to credit-rationed firms. Investment deductions reduce the need of external financing, easing the financial constraints. Another key difference is the distributional impact of these shocks: TFP shocks affect all firms equally, whereas credit shocks primarily impact financially constrained firms. As a result, government have limited leverage to reallocate resources across firms during TFP shocks, while investment deductions provide the largest benefit to firms most affected by the credit shock.

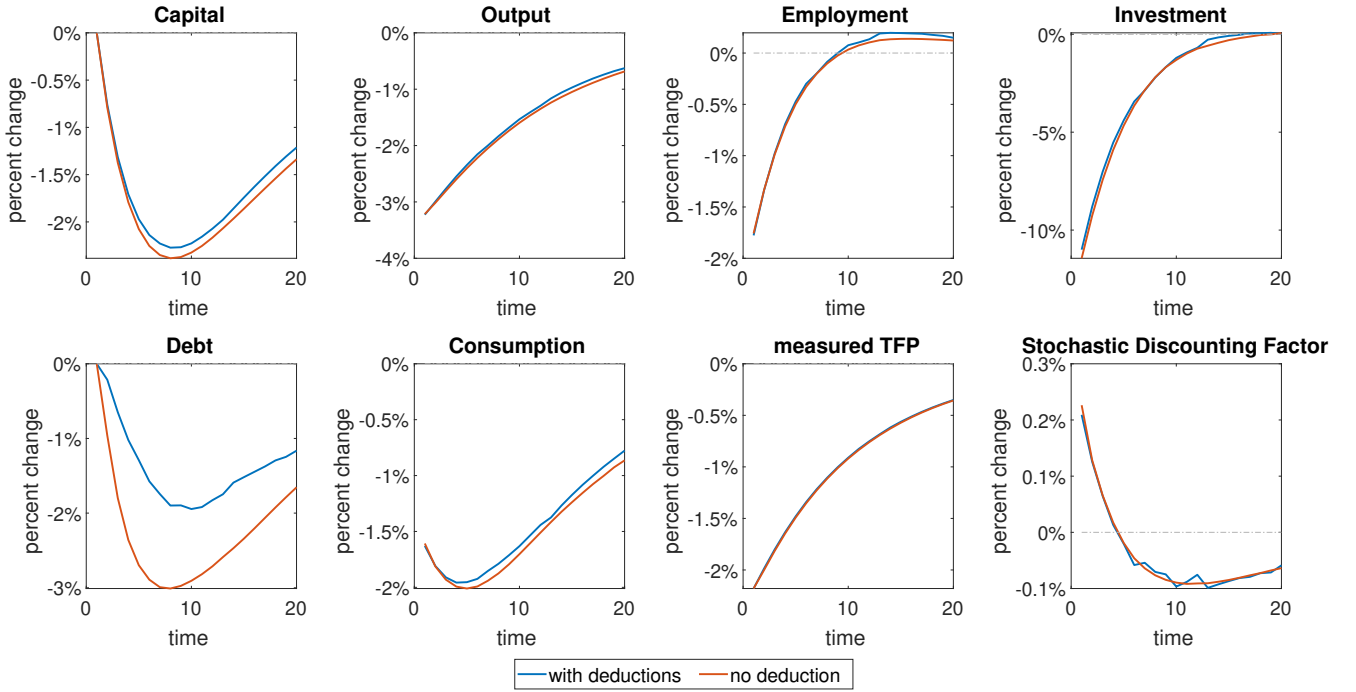
7.2 Intensive margin

Figure 11 plots dynamics of aggregate variables following a 2.18 percent drop in TFP with persistence 0.909. I chose the size of the shock to match the observed decline in measured TFP in the US from 2007 to 2009. The response from the baseline model is similar to the canonical business cycle model¹⁸. I implement all policy experiments at period 1 with the same value in Section 6. In empirical literature¹⁹, firms' investments respond to the immediate realization of tax benefits rather than potential future tax deductions. In my model, a temporary boost in either Section 179 deduction or bonus depreciation only generates a spike in investment

¹⁸See Hansen (1985), Khan and Thomas (2013)

¹⁹House and Shapiro (2008) and Zwick and Mahon (2017)

Figure 9: Comparing the responses to TFP shocks between model with deductions with model without deductions

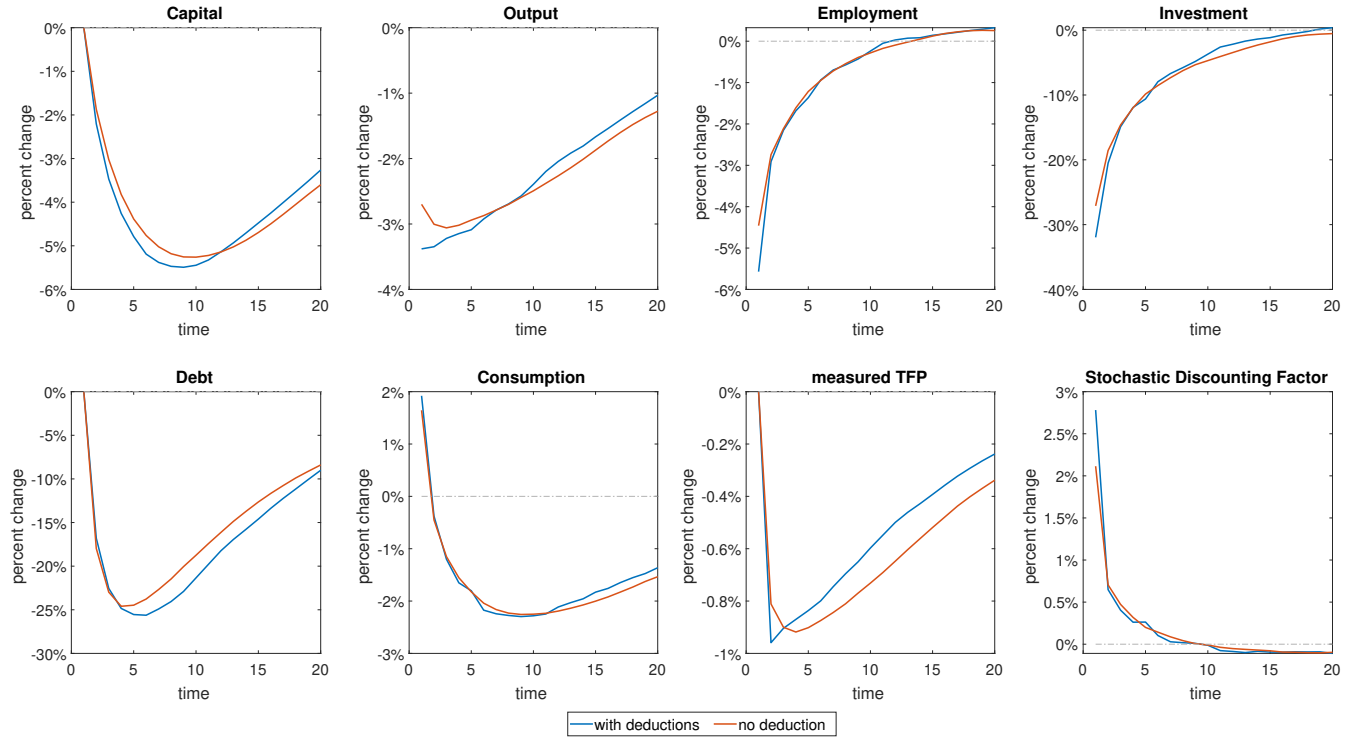


response at the year of policy implementation. However, as capital is a slow-moving object, such a temporary incentive mitigates the initial drop in capital, leading to a different trajectory compared with the baseline model.

This figure shows that the Section 179 threshold dominates bonus depreciation in its effectiveness of mitigating troughs during the recession. Such subsidy also encourages firms to raise their debt at the first few periods to undertake investment, rather than pay out as dividends. As a result, the trajectory of capital is much higher in the S179 model (*orange line*) than in the Bonus model (*yellow line*), leading to a boost in output, employment, and consumption. This boost in output also allows the government to repay the lump-sum tax. Implementation of both policies (*purple line*) resulted in an initial surge exceeding the S179 model, but this effect rapidly diminished, converging with the S179 trajectory in capital, output, and consumption.

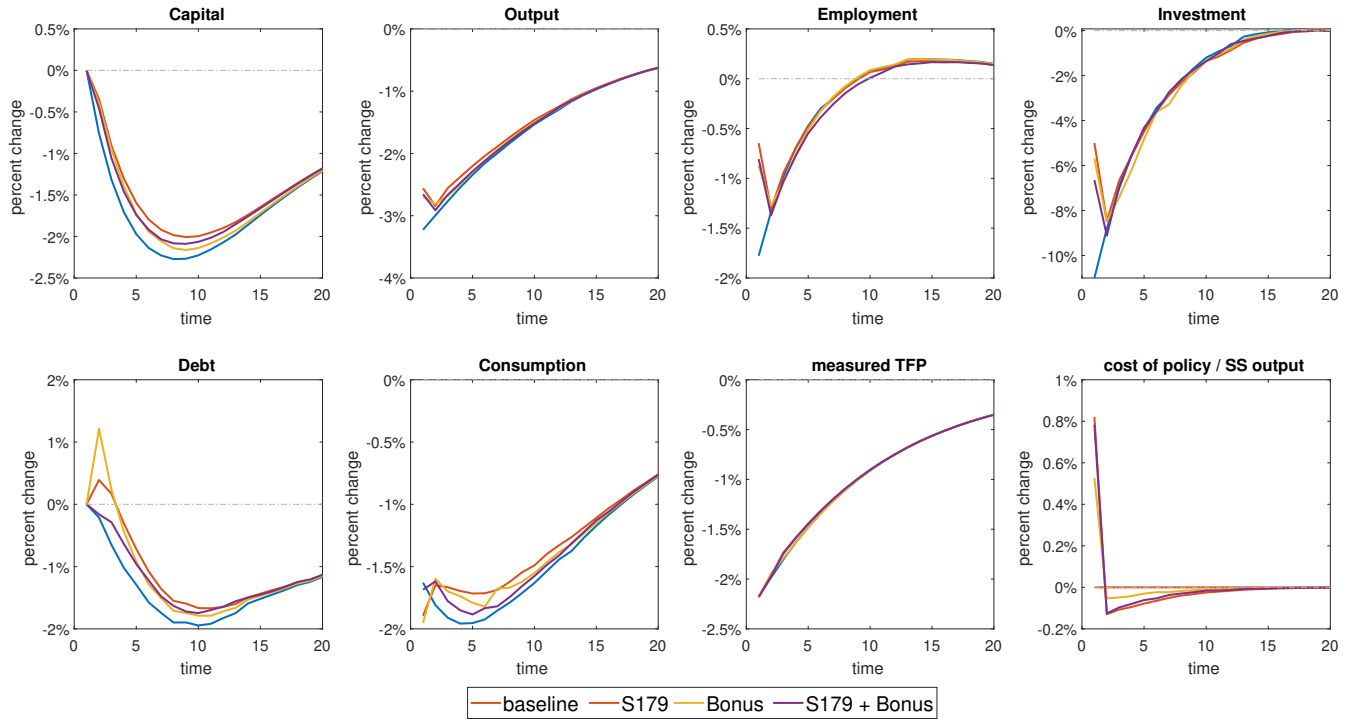
This pattern persists in policy response persist in credit shock. I define the credit shock as the drop of the credit parameter θ in the collateral constraint. The scale is set to 27 percent to replicate a 26 percent decrease in debt. The timing of the policy is set at period 4 to mimic the timing of both raising bonus depreciation and Section 179 threshold in 2010 while is recession started in late 2007. Figure 12 demonstrates the capability of Section 179 policy in terms of mitigating capital misallocation through the endogenous TFP channel. To avoid the anticipation effect, firms in figure 12 are not aware that the policies will be implemented at period 4 when they are

Figure 10: Comparing the responses to credit shocks between model with deductions with model without deductions



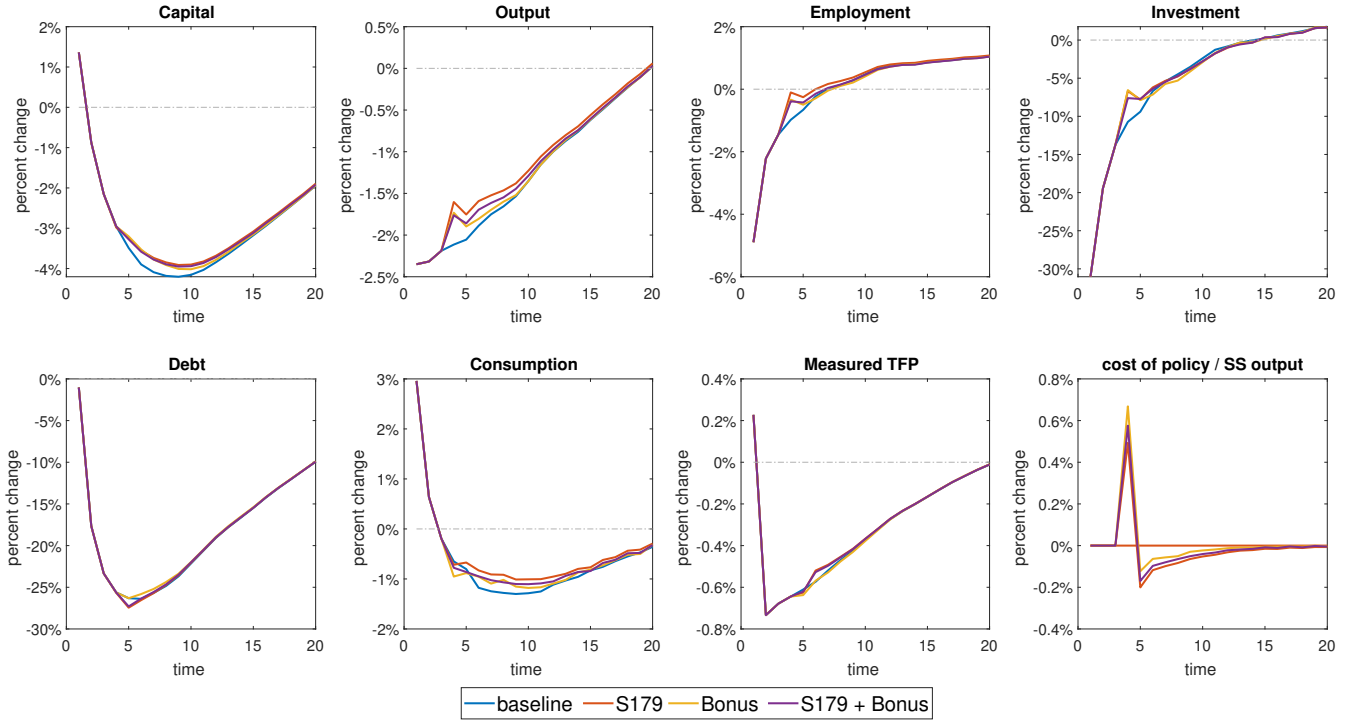
in the first three periods. Among all three experiments, the S179 model has the lowest cost of the policy and the highest mitigating effect against recession. We can see a hump in measured TFP around period 6, indicating the disparity between exogenous TFP and endogenous TFP has been alleviated by the S179 policy.

Figure 11: Impulse Response to 2.18 percent drop in total factor productivity with persistent 0.909



Notes: Three policy experiments are implemented at period 1. Starting from period 2, the policy tools fall back to baseline value. Baseline model: $(I, \xi) = (0.092, 0.5)$. S179 model: $(I, \xi) = (0.292, 0.5)$. Bonus model: $(I, \xi) = (0.092, 0.69)$. S179 + Bonus model: $(I, \xi) = (0.239, 0.566)$.

Figure 12: Impulse Response to 27 percent drop in credit parameter with persistent 0.909



Notes: Three policy experiments are implemented at period 4. Starting from period 5, the policy tools fall back to the baseline value. Baseline model: $(\bar{I}, \bar{\zeta}) = (0.092, 0.5)$. S179 model: $(\bar{I}, \bar{\zeta}) = (0.292, 0.5)$ Bonus model: $(\bar{I}, \bar{\zeta}) = (0.092, 0.69)$. S179 + Bonus model: $(\bar{I}, \bar{\zeta}) = (0.239, 0.566)$.

8 Concluding Remarks

I developed a general equilibrium model with heterogeneous firms and collateral constraints to evaluate the efficacy of investment subsidy policies. The model is calibrated to match aggregate economic moments and firm-level investment data, replicating the distribution of investment rates and investment elasticity to tax incentives across firms of different sizes. This model provides a realistic assessment of the aggregate effects of investment subsidies by capturing the evolution of firms' distributions over capital, debt, productivity, and deductible stock.

The effectiveness of investment subsidies in boosting aggregate output and productivity depends on their interaction with firms' saving motives and the partial irreversibility generated by corporate taxation. Firms respond to financial frictions by accumulating precautionary savings, ensuring that limited access to investment loans does not distort their investment. Partial irreversibility adding risk to investment by distorting the purchasing and selling prices of capital. Investment deductions lower the user cost of capital and mitigate capital misallocation, reducing the need for debt financing and negative impact from partial irreversibility. As a result, the economy with investment deductions recovers faster than the economy without under credit shocks that replicate the Great Recession.

Unlike typical policies, U.S. investment subsidies are implemented through both targeted and untargeted corporate tax deductions. My findings indicate that targeted policies are more effective at boosting aggregate GDP and productivity, while the current approach of combining both policies diminishes their overall stimulative effect. The increased effectiveness of targeted policy is demonstrated by the distribution of excess returns on investment, which reflects capital misallocation across the economy. Compared to untargeted subsidies, targeted policy result in less dispersion of firm investments around the efficient zero excess return level. Additionally, high-productivity firms respond more strongly to targeted policies, while untargeted policies have a more diffuse impact. Combining both types of policies, however, appears to reduce the effectiveness of each.

While my model currently assumes risk-free debt, introducing the possibility of default could affect firms' responses to investment subsidies. In the model, financially unconstrained and high productivity firms would incur debt to invest up to the dollar threshold. This results in a positive relationship between firm size and leverage. Allowing for default could lead to instances of large-firm defaults, amplifying the economy's response to aggregate shocks. Endogenous default would also create a channel through which corporate tax deductions could reduce firm defaults. An extended model incorporating default could quantify these effects and clarify the equilibrium outcomes of corporate tax deductions is left for future work.

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A Additional figures

Figure 13: Section 179 Deduction Limits and Bonus Depreciation Rates (2000-2024)

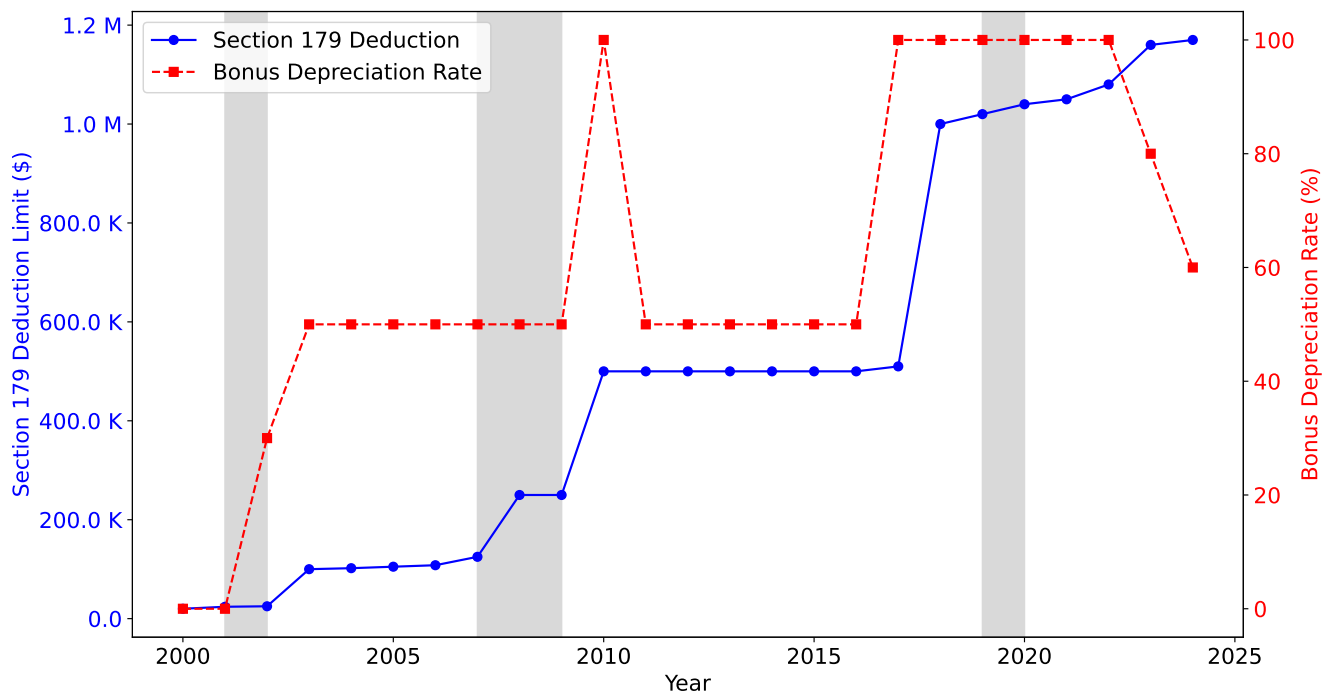


Figure 14: Distribution: minimum productivity

