

LSSP: a Linear Solver Package for Sparse Matrix

VERSION 1.0

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Chapter 1

Introduction

1.1 Overview

LSSP is a **L**inear **S**olver library for **S**Parse linear system, $Ax = b$. The package is designed for Linux, Unix and Mac systems. It is also possible to compile under Windows. The code is written by C++ and C, and it is serial.

LSSP has implemented many solvers and preconditioners, and it also has interfaces to external packages, such as PETSc, MUMPS, FASP, UMFPACK (SUITESPARSE), KLU (SUITESPARSE), LSPACK, ITSOL, LIS, QR_MUMPS, PARDISO, SUPERLU, and HSL MI20.

1.2 Cite

If you like our LSSP library, you may cite it like this,

```
@misc{lssp-library,  
  author="Hui Liu",  
  title="LSSP: a Linear Solver Package for Sparse Matrix",  
  year="2019",  
  note={\url{https://github.com/huiscliu/lssp/}}  
}
```

1.3 Website

The official website for LSSP is <https://github.com/huiscliu/lssp/>.

Chapter 2

Installation

LSSP has interfaces to some external packages, such as PETSc, MUMPS, FASP, UMFPACK (SuiteSparse), KLU (SuiteSparse), LAPACK, ITSOL, LIS, QR_MUMPS, PARDISO, SUPERLU, and HSL MI20. All these packages are optional. Most packages are enabled by default. However, they will be disabled if not found by configuration script.

LSSP uses `autoconf` and `make` to detect these packages and system parameters, to build and to install.

2.1 Configuration

The simplest way to configure is to run command:

```
./configure
```

This command will try to find optional packages from certain directories. Searching details can be read from `configure.in` and some are explained below. It also sets system parameters.

2.2 Options

The script `configure` has many options, if user would like to check, run command:

```
./configure --help
```

Output will be like this,

```
'configure' configures this package to adapt to many kinds of systems.
```

```
Usage: ./configure [OPTION]... [VAR=VALUE]...
```

To assign environment variables (e.g., CC, CFLAGS...), specify them as VAR=VALUE. See below for descriptions of some of the useful variables.

Defaults for the options are specified in brackets.

Configuration:

-h, --help	display this help and exit
--help=short	display options specific to this package
--help=recursive	display the short help of all the included packages
-V, --version	display version information and exit
-q, --quiet, --silent	do not print 'checking ...' messages
--cache-file=FILE	cache test results in FILE [disabled]
-C, --config-cache	alias for '--cache-file=config.cache'
-n, --no-create	do not create output files
--srcdir=DIR	find the sources in DIR [configure dir or '..']

Installation directories:

--prefix=PREFIX	install architecture-independent files in PREFIX [/usr/local/lssp]
--exec-prefix=EPREFIX	install architecture-dependent files in EPREFIX [PREFIX]

By default, 'make install' will install all the files in '/usr/local/lssp/bin', '/usr/local/lssp/lib' etc. You can specify an installation prefix other than '/usr/local/lssp' using '--prefix', for instance '--prefix=HOME'.

For better control, use the options below.

Fine tuning of the installation directories:

--bindir=DIR	user executables [EPREFIX/bin]
--sbindir=DIR	system admin executables [EPREFIX/sbin]
--libexecdir=DIR	program executables [EPREFIX/libexec]
--sysconfdir=DIR	read-only single-machine data [PREFIX/etc]
--sharedstatedir=DIR	modifiable architecture-independent data [PREFIX/com]
--localstatedir=DIR	modifiable single-machine data [PREFIX/var]
--libdir=DIR	object code libraries [EPREFIX/lib]
--includedir=DIR	C header files [PREFIX/include]
--oldincludedir=DIR	C header files for non-gcc [/usr/include]
--datarootdir=DIR	read-only arch.-independent data root [PREFIX/share]
--datadir=DIR	read-only architecture-independent data [DATAROOTDIR]
--infodir=DIR	info documentation [DATAROOTDIR/info]
--localedir=DIR	locale-dependent data [DATAROOTDIR/locale]
--mandir=DIR	man documentation [DATAROOTDIR/man]
--docdir=DIR	documentation root [DATAROOTDIR/doc/PACKAGE]
--htmldir=DIR	html documentation [DOCDIR]

2.2. Options

```
--dvidir=DIR          dvi documentation [DOCDIR]
--pdfdir=DIR          pdf documentation [DOCDIR]
--psdir=DIR           ps documentation [DOCDIR]
```

System types:

```
--build=BUILD        configure for building on BUILD [guessed]
--host=HOST           cross-compile to build programs to run on HOST [BUILD]
```

Optional Features:

```
--disable-option-checking  ignore unrecognized --enable/--with options
--disable-FEATURE          do not include FEATURE (same as --enable-FEATURE=no)
--enable-FEATURE[=ARG]    include FEATURE [ARG=yes]
--enable-omp               enable OpenMP
--disable-omp              disable OpenMP (default)
--with-omp-flags=FLAGS     compiler flags for OpenMP
--disable-openmp           do not use OpenMP
--enable-rpath             enable use of rpath (default)
--disable-rpath           disable use of rpath
--with-rpath-flag=FLAG     compiler flag for rpath (e.g., "-Wl,-rpath,")
--disable-assert          turn off assertions
--enable-opt              enable OPTION support (default)
--disable-opt             disable OPTION support
--enable-blas              enable BLAS support (default)
--disable-blas            disable BLAS support
--with-blas=blas BLAS lib
--enable-lapack            enable LAPACK support (default)
--disable-lapack          disable LAPACK support
--with-lapack=lapack LAPACK lib
--enable-laspack          enable LASPACK support (default)
--disable-laspack         disable LASPACK support
--with-laspack-libdir=DIR  path for LASPACK library
--with-laspack-incdir=DIR  path for LASPACK header file
--enable-sspars           enable SSPARSE support (default)
--disable-sspars          disable SSPARSE support
--with-sspars-libdir=DIR  path for SSPARSE library
--with-sspars-incdir=DIR  path for SSPARSE header file
--enable-mumps            enable MUMPS solver (default)
--disable-mumps           disable MUMPS solver
--with-mumps-incdir=DIR   MUMPS header files directory
--with-mumps-libdir=DIR   MUMPS libraries directory
--enable-petsc            enable PETSC solver (default)
--disable-petsc           disable PETSC solver
--with-petsc-incdir=DIR   PETSC header files directory
--with-petsc-libdir=DIR   PETSC libraries directory
--enable-itsol            enable ITSOL support (default)
--disable-itsol           disable ITSOL support
--with-itsol-libdir=DIR   path for ITSOL library
```

```

--with-itsol-incdir=DIR path for ITSOL header file
--enable-lis      enable LIS support (default)
--disable-lis     disable LIS support
--with-lis-libdir=DIR path for LIS library
--with-lis-incdir=DIR path for LIS header file
--enable-qrmumps  enable QR_MUMPS support (default)
--disable-qrmumps disable QR_MUMPS support
--with-qrmumps-libdir=DIR path for QR_MUMPS library
--with-qrmumps-incdir=DIR path for QR_MUMPS header file
--enable-fasp     enable FASP support (default)
--disable-fasp    disable FASP support
--with-fasp-libdir=DIR path for FASP library
--with-fasp-incdir=DIR path for FASP header file
--enable-superlu  enable SUPERLU support (default)
--disable-superlu disable SUPERLU support
--with-superlu-libdir=DIR path for SUPERLU library
--with-superlu-incdir=DIR path for SUPERLU header file
--enable-pardiso  enable PARDISO support (default)
--disable-pardiso disable PARDISO support
--with-pardiso-libdir=DIR path for PARDISO library
--with-pardiso-incdir=DIR path for PARDISO header file
--enable-hslmi20  enable HSL_MI20 support (default)
--disable-hslmi20 disable HSL_MI20 support
--with-hslmi20-libdir=DIR path for HSL_MI20 library
--with-hslmi20-incdir=DIR path for HSL_MI20 header file

```

Some influential environment variables:

CC	C compiler command
CFLAGS	C compiler flags
LDFLAGS	linker flags, e.g. -L<lib dir> if you have libraries in a nonstandard directory <lib dir>
LIBS	libraries to pass to the linker, e.g. -l<library>
CPPFLAGS	(Objective) C/C++ preprocessor flags, e.g. -I<include dir> if you have headers in a nonstandard directory <include dir>
CXX	C++ compiler command
CXXFLAGS	C++ compiler flags
FC	Fortran compiler command
FCFLAGS	Fortran compiler flags
CPP	C preprocessor

Use these variables to override the choices made by ‘configure’ or to help it to find libraries and programs with nonstandard names/locations.

The options follow the same convention,

- `--enable-pack`, to enable package pack, such as `--enable-itsol`;

2.3. Compilation

- `--disable-pack`, to disable package `pack`, such as `--disable-itsol`;
- `--with-pack-libdir=DIR`, to set `DIR` as the library path of package `pack`, such as `--with-itsol-libdir=/usr/local/itsol/lib/`;
- `--with-pack-incdir=DIR`, to set `DIR` as the include path of package `pack`, such as `--with-itsol-incdir=/usr/local/itsol/include/`;

The configuration script tries to find package from `/usr/local/`, and `/opt/`, such as `/usr/local/itsol/`, and it tries to set correct include path, library path, and specific libraries. However, if configure cannot find correct information, users can help configure by using options.

2.3 Compilation

After configuration, `Makefile` and related scripts will be set correctly. A simple `make` command can compile the package,

```
make
```

2.4 Installation

Run command:

```
make install
```

The package will be installed to a directory. The default is `/usr/local/lssp/`. A different directory can be set by `--prefix=DIR`.

2.5 Optional Packages

2.5.1 BLAS

The BLAS (Basic Linear Algebra Subprograms) are routines that provide standard building blocks for performing basic vector and matrix operations. The Level 1 BLAS perform scalar, vector and vector-vector operations, the Level 2 BLAS perform matrix-vector operations, and the Level 3 BLAS perform matrix-matrix operations. Because the BLAS are efficient, portable, and widely available, they are commonly used in the development of high quality linear algebra software, LAPACK for example.

Official website: <http://www.netlib.org/blas/>

BLAS search directories:

```
/usr/local/lib
/usr/local/lib64
/usr/local/blas/lib
/usr/local/blas*/lib
/usr/local/blas/
/usr/local/blas*/
/usr/lib
/usr/lib64
/opt/blas/lib
/opt/blas*/lib
```

2.5.2 LAPACK

LAPACK is written in Fortran 90 and provides routines for solving systems of simultaneous linear equations, least-squares solutions of linear systems of equations, eigenvalue problems, and singular value problems. The associated matrix factorizations (LU, Cholesky, QR, SVD, Schur, generalized Schur) are also provided, as are related computations such as reordering of the Schur factorizations and estimating condition numbers. Dense and banded matrices are handled, but not general sparse matrices. In all areas, similar functionality is provided for real and complex matrices, in both single and double precision.

Official website: <http://www.netlib.org/lapack/>

LAPACK search directories:

```
/usr/local/lib
/usr/local/lib64
/usr/local/lapack/lib
/usr/local/lapack*/lib
/usr/local/lapack/
/usr/local/lapack*/
/usr/lib
/usr/lib64
/opt/lapack/lib
/opt/lapack*/lib
```

2.5.3 LASPack

LASPack is a package for solving large sparse systems of linear equations like those which arise from discretization of partial differential equations. It contains classical as well as selected

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state-of-the-art algorithms which are commonly used for large sparse systems such as CG-like methods for non-symmetric systems (CGN, GMRES, BiCG, QMR, CGS, and BiCGStab) and multilevel methods such as multigrid and conjugate gradient method preconditioned by multigrid and BPX preconditioners. LASPack is written in ANSI C and is thus largely portable.

Official website: http://www.netlib.org/utk/misc/sw_survey/urc/html/LASPack.1.html

LASPack search directories (include and lib):

```
/usr/local/laspack/  
/usr/local/laspack*/  
/usr/local/  
/usr/  
/opt/laspack/  
/opt/laspack*
```

The include and lib directories are sub-directories of above directories, such as /usr/local/laspack/include and /usr/local/laspack/lib. Users can also set customized directories with options: `-with-laspack-libdir=DIR` and `-with-laspack-incdir=DIR`.

2.5.4 SuiteSparse

A Suite of Sparse matrix software, including UMFPACK, CHOLMOD, SPQR, KLU, BTF, and ordering methods (AMD, CAMD, COLAMD, and CCOLAMD).

Official website: <https://github.com/jluttine/suitesparse>

Official website: <http://www.suitesparse.com>

SuiteSparse search directories:

```
/usr/local/SuiteSparse  
/usr/local/SuiteSparse*  
/usr/local  
/usr  
/opt/SuiteSparse  
/opt/SuiteSparse*
```

The include and lib directories are sub-directories of above directories. Users can also set customized directories with options.

2.5.5 MUMPS

MUMPS (MULTifrontal Massively Parallel sparse direct Solver) is a software application for the solution of large sparse systems of linear algebraic equations on distributed memory parallel

computers. It was developed in European project PARASOL (1996–1999) by CERFACS, IRIT-ENSEEIH and RAL. The software implements the multifrontal method, which is a version of Gaussian elimination for large sparse systems of equations, especially those arising from the finite element method. It is written in Fortran 90 with parallelism by MPI and it uses BLAS and ScaLAPACK kernels for dense matrix computations. Since 1999, MUMPS has been supported by CERFACS, IRIT-ENSEEIH, and INRIA.

Official website: <http://mumps.enseeiht.fr/>

MUMPS search directories:

```
/usr/local/mumps-seq/
/usr/local/mumps*-seq/
/usr/local/
/usr/
/opt/mumps-seq/
/opt/mumps*-seq/
```

The include and lib directories are sub-directories of above directories. Users can also set customized directories with options.

2.5.6 PETSC

PETSc, pronounced PET-see (the S is silent), is a suite of data structures and routines for the scalable (parallel) solution of scientific applications modeled by partial differential equations. It supports MPI, and GPUs through CUDA or OpenCL, as well as hybrid MPI-GPU parallelism. PETSc is intended for use in large-scale application projects, many ongoing computational science projects are built around the PETSc libraries. PETSc is easy to use for beginners. Moreover, its careful design allows advanced users to have detailed control over the solution process. PETSc includes a large suite of parallel linear, nonlinear equation solvers and ODE integrators that are easily used in application codes written in C, C++, Fortran and now Python. PETSc provides many of the mechanisms needed within parallel application codes, such as simple parallel matrix and vector assembly routines that allow the overlap of communication and computation. In addition, PETSc includes support for parallel distributed arrays useful for finite difference methods.

Official website: <https://www.mcs.anl.gov/petsc/>

PETSC search directories:

```
/usr/local/petsc-seq
/usr/local/petsc*-seq/
/opt/petsc-seq/
/opt/petsc*-seq/
```

The include and lib directories are sub-directories of above directories. Users can also set

2.5. Optional Packages

customized directories with options.

2.5.7 ITSOL

TSOL is a library of iterative solvers for general sparse linear systems of equations. ITSOL can be viewed as an extension of the itsol module in SPARSKIT. It is written in C and offers a selection of recently developed preconditioners. The preconditioner suite includes: ILUK, ILUT, ILUC, VBILUK, VBILUT, and ARMS.

Official website: <http://www-users.cs.umn.edu/~saad/software/ITSOL/index.html>

ITSOL search directories:

```
/usr/local/itsol
/usr/local/itsol*
/usr/local
/usr
/opt/itsol
/opt/itsol*
```

The include and lib directories are sub-directories of above directories. Users can also set customized directories with options.

2.5.8 LIS

Lis (Library of Iterative Solvers for linear systems, pronounced [lis]) is a parallel software library for solving linear equations and eigenvalue problems that arise in the numerical solution of partial differential equations using iterative methods.

Official website: <http://www.ssisc.org/lis/>

LIS search directories:

```
/usr/local/lis
/usr/local/lis*
/usr/local
/usr
/opt/lis
/opt/lis*
```

The include and lib directories are sub-directories of above directories. Users can also set customized directories with options.

2.5.9 QR_MUMPS

QR_MUMPS is a software package for the solution of sparse, linear systems on multicore computers. It implements a direct solution method based on the QR factorization of the input matrix. Therefore, it is suited to solving sparse least-squares problems and to computing the minimum-norm solution of sparse, underdetermined problems. It can obviously be used for solving square problems in which case the stability provided by the use of orthogonal transformations comes at the cost of a higher operation count with respect to solvers based on, e.g., the LU factorization. It supports real and complex, single or double precision arithmetic.

Official website: http://buttari.perso.enseeiht.fr/qr_mumps/

QR_MUMPS search directories:

```
/usr/local/qr_mumps
/usr/local/qr_mumps*
/usr/local
/usr
/opt/qr_mumps
/opt/qr_mumps*
```

The include and lib directories are sub-directories of above directories. Users can also set customized directories with options.

2.5.10 FASP

FASP team plans to construct a pool of discrete problems arising from partial differential equations (PDEs) or PDE systems and efficient linear solvers for these problems. They mainly utilize the methodology of Auxiliary Space Preconditioning (ASP) to construct efficient linear solvers. A set of Krylov solvers and AMG solvers have been implemented.

Official website: <http://fasp.sourceforge.net/>

FASP search directories:

```
/usr/local/fasp
/usr/local/fasp*
/usr/local
/usr
/opt/fasp
/opt/fasp*
```

The include and lib directories are sub-directories of above directories. Users can also set customized directories with options.

2.5.11 SUPERLU

SuperLU is a general purpose library for the direct solution of large, sparse, nonsymmetric systems of linear equations on high performance machines. The library is written in C and is callable from either C or Fortran. The library routines will perform an LU decomposition with partial pivoting and triangular system solves through forward and back substitution. The LU factorization routines can handle non-square matrices but the triangular solves are performed only for square matrices.

Official website: <http://crd-legacy.lbl.gov/~xiaoye/SuperLU/>

SUPERLU search directories:

```
/usr/local/superlu
/usr/local/superlu*
/usr/local
/usr
/opt/superlu
/opt/superlu*
```

The include and lib directories are sub-directories of above directories. Users can also set customized directories with options.

2.5.12 PARDISO

The package PARDISO is a thread-safe, high-performance, robust, memory efficient and easy to use software for solving large sparse symmetric and unsymmetric linear systems of equations on shared-memory and distributed-memory multiprocessors.

Official website: <http://www.pardiso-project.org/>

PARDISO search directories:

```
/usr/local/intel
/opt/intel

/usr/local/pardiso
/usr/local/pardiso*
/usr/local/lib
/usr/local/lib64
/usr/lib
/usr/lib64
/opt/pardiso
/opt/pardiso*
```

2.5.13 HSL MI20 (AMG)

An AMG package using classical method.

Official website: http://www.hsl.rl.ac.uk/catalogue/hsl_mi20.html

HSL MI20 search directories:

```
/usr/local/hsl_mi20
/usr/local/hsl_mi20*
/opt/hsl_mi20
/opt/hsl_mi20*
```

2.5.14 SXAMG

An AMG package using classical method.

Official website: <https://github.com/exasc/sxamg/>

SXAMG search directories:

```
/usr/local/sxamg
/usr/local/sxamg*
/opt/sxamg
/opt/sxamg*
```

The include and lib directories are sub-directories of above directories. Users can also set customized directories using options.

Chapter 3

Matrix and Vector

3.1 Matrix Definition

LSSP uses `int` for integer and `double` for floating-point number. In this library, matrix indices and array indices follow C style, which start from 0. Three matrix types are defined, include `lssp_mat_csr`, `lssp_mat_coo`, and `lssp_mat_bcsr`, which are CSR matrix, COO matrix and block-wise CSR matrix. They are defined as,

```
typedef struct lssp_mat_csr_  
{  
    int num_rows;  
    int num_cols;  
    int num_nnz;   
    int *Ap;  
    int *Aj;  
    double *Ax;  
  
} lssp_mat_csr;
```

```
typedef struct lssp_mat_coo_  
{  
    int num_rows;  
    int num_cols;  
    int num_nnz;   
    int *Ai;  
    int *Aj;  
    double *Ax;  
  
} lssp_mat_coo;
```

```
typedef struct lssp_mat_bcsr_  
{  
    int num_rows;  
    int num_cols;  
    int num_nnz;   
    int *Ap;  
    int *Aj;  
    double *Ax;  
  
} lssp_mat_bcsr;
```

```
{
    int num_rows;
    int num_cols;
    int num_nnz;
    int blk_size;
    int *Ap;
    int *Aj;
    double *Ax;
} lssp_mat_bcsr;
```

The definitions of `lssp_mat_csr` and `lssp_mat_coo` are the same as standard definitions. For `lssp_mat_bcsr`, each block has the same size, which is defined by `blk_size`. It uses column-major style as Fortran.

3.2 Matrix Management

3.2.1 Initialize

`lssp_mat_init` initializes a matrix, which set row, column and non-zero to zero and set arrays to NULL.

```
void lssp_mat_init(lssp_mat_csr &A);
```

```
void lssp_mat_init(lssp_mat_coo &A);
```

```
void lssp_mat_init(lssp_mat_bcsr &A);
```

3.2.2 Create

`lssp_mat_create` creates a CSR matrix.

```
lssp_mat_csr lssp_mat_create(int nrow, int ncol, int *Ap, int *Aj, double *Ax);
```

3.2.3 Destroy

`lssp_mat_destroy` destroys a matrix object and releases memory.

```
void lssp_mat_destroy(lssp_mat_csr &csr);
```

3.2. Matrix Management

```
void lssp_mat_destroy(lssp_mat_coo &coo);
```

```
void lssp_mat_destroy(lssp_mat_bcsr &csr);
```

3.2.4 Conversion

[lssp_mat_csr_to_bcsr](#) converts a CSR matrix to block CSR matrix.

```
lssp_mat_bcsr lssp_mat_csr_to_bcsr(const lssp_mat_csr A, int bs);
```

[lssp_mat_bcsr_to_csr](#) converts a block CSR matrix to a CSR matrix.

```
lssp_mat_csr lssp_mat_bcsr_to_csr(const lssp_mat_bcsr A);
```

[lssp_mat_csr_to_coo](#) converts a CSR matrix to a COO matrix.

```
lssp_mat_coo lssp_mat_csr_to_coo(const lssp_mat_csr A);
```

[lssp_mat_coo_to_csr](#) converts a COO matrix to CSR matrix.

```
lssp_mat_csr lssp_mat_coo_to_csr(const lssp_mat_coo coo);
```

[lssp_mat_transpose](#): CSR matrix transpose.

```
lssp_mat_csr lssp_mat_transpose(const lssp_mat_csr A);
```

3.2.5 Sort

[lssp_mat_sort_column](#) sorts a CSR matrix in ascending order.

```
void lssp_mat_sort_column(lssp_mat_csr &A);
```

[lssp_mat_csr_is_sorted](#) checks if a CSR matrix is sorted.

```
bool lssp_mat_csr_is_sorted(const lssp_mat_csr A);
```

[lssp_mat_bcsr_is_sorted](#) checks if a block CSR matrix is sorted.

```
bool lssp_mat_bcsr_is_sorted(const lssp_mat_bcsr A);
```

[lssp_mat_adjust_zero_diag](#) changes zero diagonal element to some small value.

```
lssp_mat_csr lssp_mat_adjust_zero_diag(const lssp_mat_csr A, double tol);
```

3.3 Vector Definition

```
typedef struct lssp_vec_  
{  
    int n;  
    double *d;  
  
} lssp_vec;
```

`lssp_vec` has two members, which are vector length (`n`) and data (memory, `d`).

3.4 Vector Management

3.4.1 Create

`lssp_vec_create` creates a length `n` floating-point vector.

```
lssp_vec lssp_vec_create(int n);
```

3.4.2 Destroy

`lssp_vec_destroy` destroys a vector.

```
void lssp_vec_destroy(lssp_vec &v);
```

3.4.3 Set Value

`lssp_vec_set_value`, `lssp_vec_set_value_by_array` and `lssp_vec_set_value_by_index` set vector values.

`lssp_vec_set_value` sets the vector to the same value.

```
void lssp_vec_set_value(lssp_vec x, double val);
```

`lssp_vec_set_value_by_array` sets vector value by a buffer, which has the same length as vector.

```
void lssp_vec_set_value_by_array(lssp_vec x, double *val);
```

`lssp_vec_set_value_by_index` sets value to the i -th component.

3.5. BLAS 1

```
void lssp_vec_set_value_by_index(lssp_vec x, int i, double val);
```

3.4.4 Get Value

`lssp_vec_get_value` copies vector's values to a buffer, which should have the same length as the vector.

```
void lssp_vec_get_value(double *val, lssp_vec x);
```

`lssp_vec_get_value_by_index` gets the value of the i -th component.

```
double lssp_vec_get_value_by_index(lssp_vec x, int i);
```

3.4.5 Copy

`lssp_vec_copy` copies data from source to destination.

```
void lssp_vec_copy(lssp_vec des, const lssp_vec src);
```

3.5 BLAS 1

`lssp_vec_axpby` computes: $y = \beta * y + \alpha * x$.

```
void lssp_vec_axpby(double alpha, const lssp_vec x, double beta, lssp_vec y);
```

`lssp_vec_axpbyz` computes: $z = \beta * y + \alpha * x$.

```
void lssp_vec_axpbyz(double alpha, const lssp_vec x, double beta,  
    lssp_vec y, lssp_vec z);
```

`lssp_vec_dot` computes dot product.

```
double lssp_vec_dot(const lssp_vec x, const lssp_vec y);
```

`lssp_vec_norm` computes L2 norm.

```
double lssp_vec_norm(const lssp_vec x);
```

`lssp_vec_scale` scales a vector.

```
void lssp_vec_scale(lssp_vec x, double a);
```

3.6 BLAS 2

`lssp_mv_amxpby` computes: $y = \beta * y + \alpha * A * x$.

```
void lssp_mv_amxpby(double alpha, const lssp_mat_csr A, const lssp_vec x, \
    double beta, lssp_vec y);
```

`lssp_mv_amxpbyz` computes: $z = \beta * y + \alpha * A * x$.

```
void lssp_mv_amxpbyz(double alpha, const lssp_mat_csr A, const lssp_vec x, \
    double beta, const lssp_vec y, lssp_vec z);
```

`lssp_mv_amxy` computes: $y = a * A * x$.

```
void lssp_mv_amxy(double a, const lssp_mat_csr A, const lssp_vec x, lssp_vec y);
```

`lssp_mv_mxy` computes: $y = A * x$.

```
void lssp_mv_mxy(const lssp_mat_csr A, const lssp_vec x, lssp_vec y);
```


Chapter 4

Linear Solvers and Preconditioners

4.1 Solver Types

The solver type is defined as LSSP_SOLVER_TYPE,

```
/* solver type */
typedef enum LSSP_SOLVER_TYPE_
{
    LSSP_SOLVER_GMRES,      /* gmres(m) */
    LSSP_SOLVER_LGMRES,     /* lgmres(m, k) */
    LSSP_SOLVER_BICGSTAB,   /* bicgstab */
    LSSP_SOLVER_BICGSTABL,  /* bicgstab(l) */
    LSSP_SOLVER_BICGSafe,   /* bicgsafe */
    LSSP_SOLVER_CG,         /* cg */
    LSSP_SOLVER_CGS,        /* cgs */
    LSSP_SOLVER_GPBICG,     /* gpbicg */
    LSSP_SOLVER_CR,         /* cr */
    LSSP_SOLVER_CRS,        /* crs */
    LSSP_SOLVER_BICRSTAB,   /* bicrstab */
    LSSP_SOLVER_BICRSafe,   /* bicrsafe */
    LSSP_SOLVER_GPBICR,     /* gpbicr */
    LSSP_SOLVER_QMRCGSTAB,  /* qmrcgstab */
    LSSP_SOLVER_TFQMR,      /* tfqmr */
    LSSP_SOLVER_ORTHOMIN,   /* orthomin */
    LSSP_SOLVER_IDRS,       /* idrs */

#ifdef USE_LASPACK
    LSSP_SOLVER_LASPACK,    /* laspack */
#endif

#ifdef USE_SSPARSE
    LSSP_SOLVER_UMFPACK,    /* ssparse, umf */

```

```

    LSSP_SOLVER_KLU,      /* ssparse, klu */
#endif

#if USE_MUMPS
    LSSP_SOLVER_MUMPS,    /* mumps */
#endif

#if USE_PETSC
    LSSP_SOLVER_PETSC,    /* petsc */
#endif

#if USE_LIS
    LSSP_SOLVER_LIS,      /* lis */
#endif

#if USE_QR_MUMPS
    LSSP_SOLVER_QR_MUMPS, /* qr-mumps */
#endif

#if USE_FASP
    LSSP_SOLVER_FASP,      /* FASP */
    LSSP_SOLVER_AMG,        /* amg from FASP */
    LSSP_SOLVER_FMG,        /* fmg from FASP */
#endif

#if USE_SUPERLU
    LSSP_SOLVER_SUPERLU,   /* superlu */
#endif

#if USE_PARDISO
    LSSP_SOLVER_PARDISO,   /* pardiso */
#endif

#if USE_HSL_MI20
    LSSP_SOLVER_MI20AMG,   /* MI20 AMG */
#endif

#if USE_SXAMG
    LSSP_SOLVER_SXAMG,     /* SXAMG */
#endif

} LSSP_SOLVER_TYPE;

```

LSSP implements many solvers, including GMRES, LGMRES, BICGSTAB, BICGSTABL, BICGSAFE, CG, CGS, GPBICG, CR, CRS, BICRSTAB, BICRSAFE, GPBICR, QMRCGSTAB, TFQMR, ORTHOMIN, and IDRS.

LSSP also implements interfaces to other famous linear solver packages, such as LASPACK, SSPARSE, MUMPS, PETSC, LIS, QR_MUMPS, FASP, SUPERLU, PARDISO, HSL_MI20 and SXAMG.

4.2 Preconditioner Types

```
typedef enum LSSP_PC_TYPE_
{
    LSSP_PC_NON,
    LSSP_PC_ILUK,          /* ILUK */
    LSSP_PC_ILUT,          /* ILUT */

#ifdef USE_BLAS
#ifdef USE_LAPACK
    LSSP_PC_BILUK,          /* block-wise ILUK */
#endif
#endif

#ifdef USE_ITSOL
    LSSP_PC_BILUT,          /* block-wise ILUT */
    LSSP_PC_VBILUT,         /* var block-wise ILUT */
    LSSP_PC_VBILUK,         /* var block-wise ILUK */
    LSSP_PC_ARMS,           /* multi-level */
#endif

#ifdef USE_FASP
    LSSP_PC_AMG,            /* AMG from FASP */
    LSSP_PC_FMG,            /* FMG from FASP */
#endif

#ifdef USE_HSL_MI20
    LSSP_PC_MI20AMG,        /* AMG from HSL MI20 */
#endif

#ifdef USE_SXAMG
    LSSP_PC_SXAMG,          /* AMG from SXAMG */
#endif

    LSSP_PC_USER,           /* user defined */
} LSSP_PC_TYPE;
```

There are some internal preconditioners, including NON (no preconditioner), ILUK (point-wise ILU(k)), ILUT (point-wise ILUT(p, tol)), and BILUK (block-wise ILU(k)). However, BILUK requires BLAS and LAPACK. Users can set their own preconditioner if preconditioner type is set

to `LSSP_PC_USER`. In this case, user should provide three functions, whose types are defined as `LSSP_PC_ASSEMBLE`, `LSSP_PC_SOLVE` and `LSSP_PC_DESTROY`.

LSSP also provides some external preconditioners, which are `BILUT` (block-wise ILUT(p, tol)), `VBILUT` (variable block-wise ILUT(p, tol)), `VBILUK` (variable block-wise ILU(k)) and `ARMS` (multi-level method) from package `ITSOL`, `AMG` (algebraic multi-grid method) and `FMG` (full multi-grid method) from package `FASP`, and `MI20AMG` (MI20 AMG) from package `HSL MI20`.

4.3 Solver and Preconditioner Management

Figure 4.1 shows solution process, which includes the following steps:

1. setup matrix, unknown vector and right hand side vector, and initialize values;
2. create solver and preconditioner;
3. set solver and preconditioner parameters;
4. assemble solver and preconditioner;
5. solve the linear system;
6. get values and return to caller;
7. destroy solver, preconditioner, matrix and vectors;

4.3.1 Create

`lssp_solver_create` creates solver object and preconditioner object using solver type and preconditioner type.

```
void lssp_solver_create(LSSP_SOLVER &s, LSSP_SOLVER_TYPE s_type, LSSP_PC &pc, \
    LSSP_PC_TYPE p_type);
```

4.3.2 Assemble

`lssp_solver_assemble` assembles solver object and preconditioner object.

```
void lssp_solver_assemble(LSSP_SOLVER &s, lssp_mat_csr &Ax, lssp_vec x, \
    lssp_vec b, LSSP_PC &pc);
```

4.3. Solver and Preconditioner Management

```
{
    lssp_mat_csr A;
    LSSP_SOLVER solver;
    LSSP_PC pc;
    lssp_vec x;
    lssp_vec b;

    /* 1: setup A, x, b */
    x = lssp_vec_create(n);
    b = lssp_vec_create(n);

    A = lssp_mat_create(int nrows, int ncols, int *Ap, int *Aj, double *Ax);
    for (i = 0; i < n; i++) {
        lssp_vec_set_value_by_index(x, i, double val);
        lssp_vec_set_value_by_index(b, i, double val);
    }

    /* 2: create solver and pc */
    lssp_solver_create(solver, LSSP_SOLVER_BICGSTAB, pc, LSSP_PC_ILUK);

    /* 3: settings */
    lssp_solver_set_restart(solver, m);
    lssp_solver_set_maxit(solver, itr_max);

    /* 4: assemble solver and preconditioner */
    lssp_solver_assemble(solver, A, x, b, pc);

    /* 5: solve */
    lssp_solver_solve(solver, pc);

    /* 6: get value */
    for (i = 0; i < n; i++) {
        value = lssp_vec_get_value_by_index(x, i);
    }

    /* 7: destroy pc and solver */
    lssp_solver_destroy(solver, pc);
    lssp_mat_destroy(A);
    lssp_vec_destroy(x);
    lssp_vec_destroy(b);
}
```

Figure 4.1: Solution process

4.3.3 Solve

`lssp_solver_solve` solves linear system.

```
int lssp_solver_solve(LSSP_SOLVER &solver, LSSP_PC &pc);
```

4.3.4 Destroy

`lssp_solver_destroy` destroys solver and preconditioner objects and releases internal memory.

```
void lssp_solver_destroy(LSSP_SOLVER &s, LSSP_PC &pc);
```

4.4 Solver Settings

4.4.1 General Settings

`lssp_solver_reset_rhs` resets right-hand side.

```
void lssp_solver_reset_rhs(LSSP_SOLVER &s, lssp_vec rhs);
```

`lssp_solver_reset_unknown` resets initial guess and solution vector.

```
void lssp_solver_reset_unknown(LSSP_SOLVER &s, lssp_vec x);
```

`lssp_solver_reset_type` resets solver type.

```
void lssp_solver_reset_type(LSSP_SOLVER &s, LSSP_SOLVER_TYPE type);
```

`lssp_solver_set_rtol` sets relative tolerance.

```
void lssp_solver_set_rtol(LSSP_SOLVER &s, double tol);
```

`lssp_solver_set_atol` sets absolute tolerance.

```
void lssp_solver_set_atol(LSSP_SOLVER &s, double tol);
```

`lssp_solver_set_rbtol` sets relative b norm tolerance.

```
void lssp_solver_set_rbtol(LSSP_SOLVER &s, double tol);
```

```
/* set maximal number of iteration */
```

```
void lssp_solver_set_maxit(LSSP_SOLVER &s, int maxit);
```

4.4. Solver Settings

[`lssp_solver_set_restart`](#) set the number of restart.

```
void lssp_solver_set_restart(LSSP_SOLVER &s, int m);
```

[`lssp_solver_set_augk`](#) sets aug_k for LGMRES(m).

```
void lssp_solver_set_augk(LSSP_SOLVER &s, int k);
```

[`lssp_solver_set_bgs1`](#) set bgs1 for BICGSTAB(l).

```
void lssp_solver_set_bgs1(LSSP_SOLVER &s, int k);
```

[`lssp_solver_set_idrs`](#) sets idrs for IDRS solver.

```
void lssp_solver_set_idrs(LSSP_SOLVER &s, int k);
```

[`lssp_solver_reset_verbosity`](#) resets verbosity of a solver.

```
void lssp_solver_reset_verbosity(LSSP_SOLVER &s, int v);
```

[`lssp_solver_get_residual`](#) gets residual.

```
double lssp_solver_get_residual(LSSP_SOLVER s);
```

[`lssp_solver_get_nits`](#) gets number of iteration.

```
int lssp_solver_get_nits(LSSP_SOLVER s);
```

[`lssp_solver_set_log`](#) sets log file handler.

```
void lssp_solver_set_log(LSSP_SOLVER &s, FILE *io);
```

4.4.2 AMG Solver Setting

[`lssp_solver_amg_reset_pars`](#) sets new parameters to AMG solver.

```
void lssp_solver_amg_reset_pars(LSSP_SOLVER &s, AMG_param par);
```

4.4.3 FASP Solver Setting

[`lssp_fasp_set_pars`](#) resets default parameters. If parameter pointer is not `NULL`, default parameters will be overridden.

```
void lssp_fasp_set_pars(LSSP_SOLVER *solver, input_param *inparam,
    itsolver_param *itsparam, AMG_param *amgparam, ILU_param *iluparam,
    Schwarz_param *schparam);
```

4.4.4 LIS Solver Setting

`lssp_solver_lis_set_pars` sets solver id and preconditioner id.

```
static const char * lis_solver[] = {
    "-i bicgstab",
    "-i bicgstabl",
    "-i cg",
    "-i cgs",
    "-i bicg",
    "-i bicgsafe",
    "-i bicr",
    "-i cr",
    "-i bicrstab",
    "-i bicrsafe",
    "-i idrs",
    "-i crs",
    "-i gpbicr",
    "-i gpbicg",
    "-i tfqmr",
    "-i orthomin",
    "-i gmres",
    "-i fgmres",
    "-i minres",
};

static const char * lis_pc[] = {
    "-p none",
    "-p ilut",
    "-p ilu -ilu_fill 1",
    "-p is",
    "-p sainv",
    "-p saamg -saamg_unsym -saamg_theta 0.5",
    "-p hybrid",
    "-p iluc",
    "-p ssor",
    "-p jacobi",
};

void lssp_solver_lis_set_pars(LSSP_SOLVER &solver, unsigned int solver_id,
```


4.5. Preconditioner Settings

```
unsigned int pc_id);
```

4.4.5 SXAMG Setting

[lssp_solver_sxamg_set_pars](#) resets default parameters.

```
void lssp_solver_sxamg_set_pars(LSSP_SOLVER *solver, SX_AMG_PARS *pars);
```

4.4.6 PETSc Setting

[lssp_solver_petsc_setting](#) resets PETSc default parameters by a function.

```
typedef void (*solver_petsc_setting)(void *ksp, void *pc);  
  
void lssp_solver_petsc_setting(solver_petsc_setting func);
```

4.5 Preconditioner Settings

4.5.1 ILUK Setting

[lssp_pc_iluk_set_level](#) sets ILUK level.

```
void lssp_pc_iluk_set_level(LSSP_PC &pc, int level);
```

4.5.2 ILUT Setting

[lssp_pc_ilut_set_drop_tol](#) and [lssp_pc_ilut_set_p](#) sets `tol` and `p` parameters of ILUT(`tol`, `p`), which overrides default parameters.

```
void lssp_pc_ilut_set_drop_tol(LSSP_PC &pc, double tol);  
void lssp_pc_ilut_set_p(LSSP_PC &pc, int p);
```

4.5.3 AMG Setting

[lssp_pc_amg_set_pars](#) sets new parameters, which overrides default settings.

```
void lssp_pc_amg_set_pars(LSSP_PC &pc, AMG_param *amgparam);
```

4.5.4 SXAMG Setting

`lssp_pc_sxamg_set_pars` sets new parameters, which overrides default parameters.

```
void lssp_pc_sxamg_set_pars(LSSP_PC &pc, SX_AMG_PARS *pars);
```

Chapter 5

Utilities

5.1 Print

`lssp_set_log` sets log file handler.

```
void lssp_set_log(FILE *io);
```

`lssp_printf` outputs to stdout and default log file if set.

```
int lssp_printf(const char *fmt, ...);
```

`lssp_error` prints output error message and quits with error code.

```
void lssp_error(int code, const char *fmt, ...);
```

`lssp_warning` print warning info.

```
void lssp_warning(const char *fmt, ...);
```

5.2 Memory

The following functions provide memory allocation, calloc, reallocation, freeing and copying.

```
template <typename T> T * lssp_malloc(const int n);
```

```
template <typename T> T * lssp_calloc(const int n);
```

```
template <typename T> T * lssp_realloc(T * old, const int n);
```

```
template <typename T> void lssp_free(T * &p);
```

```
template<typename T> void lssp_memcpy_on(T *dst, const T *src, const int n);  
  
template <typename T> T * lssp_copy_on(const T *src, const int n);
```

5.3 Performance

`lssp_get_time` gets current time.

```
double lssp_get_time();
```

`lssp_get_mem_usage` returns current memory usage. If `peak` is not `NULL`, then peak memory is returned to `peak`.

```
double lssp_get_mem_usage(double *peak);
```