

# ET-540 – Introduction to Digital Computer

## Homework 7 – Counter Design

Student's Name \_\_\_\_\_

### Instructions:

- Show all work to receive full credit.
- 

Design a synchronous counter that will display the following sequence and then repeat

0 → 2 → 6 → 8 → 7 → 5 → 3 → 1 (repeat)

**Step 1:** Write and sketch the sequence of the synchronous counter (3 points)

**Step 2:** Determine the number of flip flops that you need and the module number (3 points)

**Step 3 and 4:** Construct a truth table of the transition state with the PRESENT state and the NEXT state, and complete the J-K input for each flip flop using sequence diagram from Step 1.

Decimal	D(MSB)	PRESENT state			NEXT state			
		C	B	A (LSB)	D(MSB)	C	B	A (LSB)
0	0	0	0	0				
1	0	0	0	1				
2	0	0	1	0				
3	0	0	1	1				
4	0	1	0	0				
5	0	1	0	1				
6	0	1	1	0				
7	0	1	1	1				
8	1	0	0	0				
9	1	0	0	1				
10	1	0	1	0				
11	1	0	1	1				
12	1	1	0	0				
13	1	1	0	1				
14	1	1	1	0				
15	1	1	1	1				
Circuit excitation table for sequence 0 → 2 → 6 → 8 → 7 → 5 → 3 → 1								

Decimal	J-K State							
	J <sub>D</sub>	K <sub>D</sub>	J <sub>C</sub>	K <sub>C</sub>	J <sub>B</sub>	K <sub>B</sub>	J <sub>A</sub>	K <sub>A</sub>
0								
1								
2								
3								
4								
5								
6								
7								
8								
9								
10								
11								
12								
13								
14								
15								

**Step 5:** Create a k-map table for each J and K input and find the SOP equation of each.

<p style="text-align: center;"><b>J<sub>D</sub></b></p> <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <tr> <td></td> <td><math>\overline{B}\overline{A}</math></td> <td><math>\overline{B}A</math></td> <td><math>BA</math></td> <td><math>B\overline{A}</math></td> </tr> <tr> <td><math>\overline{D}\overline{C}</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>\overline{D}C</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>D\overline{C}</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>DC</math></td> <td></td><td></td><td></td><td></td> </tr> </table> <p>SOP :</p>		$\overline{B}\overline{A}$	$\overline{B}A$	$BA$	$B\overline{A}$	$\overline{D}\overline{C}$					$\overline{D}C$					$D\overline{C}$					$DC$					<p style="text-align: center;"><b>J<sub>C</sub></b></p> <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <tr> <td></td> <td><math>\overline{B}\overline{A}</math></td> <td><math>\overline{B}A</math></td> <td><math>BA</math></td> <td><math>B\overline{A}</math></td> </tr> <tr> <td><math>\overline{D}\overline{C}</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>\overline{D}C</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>D\overline{C}</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>DC</math></td> <td></td><td></td><td></td><td></td> </tr> </table> <p>SOP:</p>		$\overline{B}\overline{A}$	$\overline{B}A$	$BA$	$B\overline{A}$	$\overline{D}\overline{C}$					$\overline{D}C$					$D\overline{C}$					$DC$					<p style="text-align: center;"><b>J<sub>B</sub></b></p> <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <tr> <td></td> <td><math>\overline{B}\overline{A}</math></td> <td><math>\overline{B}A</math></td> <td><math>BA</math></td> <td><math>B\overline{A}</math></td> </tr> <tr> <td><math>\overline{D}\overline{C}</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>\overline{D}C</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>D\overline{C}</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>DC</math></td> <td></td><td></td><td></td><td></td> </tr> </table> <p>SOP:</p>		$\overline{B}\overline{A}$	$\overline{B}A$	$BA$	$B\overline{A}$	$\overline{D}\overline{C}$					$\overline{D}C$					$D\overline{C}$					$DC$				
	$\overline{B}\overline{A}$	$\overline{B}A$	$BA$	$B\overline{A}$																																																																									
$\overline{D}\overline{C}$																																																																													
$\overline{D}C$																																																																													
$D\overline{C}$																																																																													
$DC$																																																																													
	$\overline{B}\overline{A}$	$\overline{B}A$	$BA$	$B\overline{A}$																																																																									
$\overline{D}\overline{C}$																																																																													
$\overline{D}C$																																																																													
$D\overline{C}$																																																																													
$DC$																																																																													
	$\overline{B}\overline{A}$	$\overline{B}A$	$BA$	$B\overline{A}$																																																																									
$\overline{D}\overline{C}$																																																																													
$\overline{D}C$																																																																													
$D\overline{C}$																																																																													
$DC$																																																																													
<p style="text-align: center;"><b>J<sub>A</sub></b></p> <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <tr> <td></td> <td><math>\overline{B}\overline{A}</math></td> <td><math>\overline{B}A</math></td> <td><math>BA</math></td> <td><math>B\overline{A}</math></td> </tr> <tr> <td><math>\overline{D}\overline{C}</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>\overline{D}C</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>D\overline{C}</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>DC</math></td> <td></td><td></td><td></td><td></td> </tr> </table> <p>SOP :</p>		$\overline{B}\overline{A}$	$\overline{B}A$	$BA$	$B\overline{A}$	$\overline{D}\overline{C}$					$\overline{D}C$					$D\overline{C}$					$DC$					<p style="text-align: center;"><b>K<sub>D</sub></b></p> <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <tr> <td></td> <td><math>\overline{B}\overline{A}</math></td> <td><math>\overline{B}A</math></td> <td><math>BA</math></td> <td><math>B\overline{A}</math></td> </tr> <tr> <td><math>\overline{D}\overline{C}</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>\overline{D}C</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>D\overline{C}</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>DC</math></td> <td></td><td></td><td></td><td></td> </tr> </table> <p>SOP:</p>		$\overline{B}\overline{A}$	$\overline{B}A$	$BA$	$B\overline{A}$	$\overline{D}\overline{C}$					$\overline{D}C$					$D\overline{C}$					$DC$					<p style="text-align: center;"><b>K<sub>C</sub></b></p> <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <tr> <td></td> <td><math>\overline{B}\overline{A}</math></td> <td><math>\overline{B}A</math></td> <td><math>BA</math></td> <td><math>B\overline{A}</math></td> </tr> <tr> <td><math>\overline{D}\overline{C}</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>\overline{D}C</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>D\overline{C}</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>DC</math></td> <td></td><td></td><td></td><td></td> </tr> </table> <p>SOP:</p>		$\overline{B}\overline{A}$	$\overline{B}A$	$BA$	$B\overline{A}$	$\overline{D}\overline{C}$					$\overline{D}C$					$D\overline{C}$					$DC$				
	$\overline{B}\overline{A}$	$\overline{B}A$	$BA$	$B\overline{A}$																																																																									
$\overline{D}\overline{C}$																																																																													
$\overline{D}C$																																																																													
$D\overline{C}$																																																																													
$DC$																																																																													
	$\overline{B}\overline{A}$	$\overline{B}A$	$BA$	$B\overline{A}$																																																																									
$\overline{D}\overline{C}$																																																																													
$\overline{D}C$																																																																													
$D\overline{C}$																																																																													
$DC$																																																																													
	$\overline{B}\overline{A}$	$\overline{B}A$	$BA$	$B\overline{A}$																																																																									
$\overline{D}\overline{C}$																																																																													
$\overline{D}C$																																																																													
$D\overline{C}$																																																																													
$DC$																																																																													
<p style="text-align: center;"><b>K<sub>B</sub></b></p> <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <tr> <td></td> <td><math>\overline{B}\overline{A}</math></td> <td><math>\overline{B}A</math></td> <td><math>BA</math></td> <td><math>B\overline{A}</math></td> </tr> <tr> <td><math>\overline{D}\overline{C}</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>\overline{D}C</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>D\overline{C}</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>DC</math></td> <td></td><td></td><td></td><td></td> </tr> </table> <p>SOP :</p>		$\overline{B}\overline{A}$	$\overline{B}A$	$BA$	$B\overline{A}$	$\overline{D}\overline{C}$					$\overline{D}C$					$D\overline{C}$					$DC$					<p style="text-align: center;"><b>K<sub>A</sub></b></p> <table border="1" style="width: 100%; border-collapse: collapse; text-align: center;"> <tr> <td></td> <td><math>\overline{B}\overline{A}</math></td> <td><math>\overline{B}A</math></td> <td><math>BA</math></td> <td><math>B\overline{A}</math></td> </tr> <tr> <td><math>\overline{D}\overline{C}</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>\overline{D}C</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>D\overline{C}</math></td> <td></td><td></td><td></td><td></td> </tr> <tr> <td><math>DC</math></td> <td></td><td></td><td></td><td></td> </tr> </table> <p>SOP:</p>		$\overline{B}\overline{A}$	$\overline{B}A$	$BA$	$B\overline{A}$	$\overline{D}\overline{C}$					$\overline{D}C$					$D\overline{C}$					$DC$																														
	$\overline{B}\overline{A}$	$\overline{B}A$	$BA$	$B\overline{A}$																																																																									
$\overline{D}\overline{C}$																																																																													
$\overline{D}C$																																																																													
$D\overline{C}$																																																																													
$DC$																																																																													
	$\overline{B}\overline{A}$	$\overline{B}A$	$BA$	$B\overline{A}$																																																																									
$\overline{D}\overline{C}$																																																																													
$\overline{D}C$																																																																													
$D\overline{C}$																																																																													
$DC$																																																																													

**Step 6:** Complete and sketch the counter circuit using the SOP equation found in **step 5**