

Introduction to Digital Computer Theory

Homework 9 - flip flops, counters, shift registers, and pulse

Instructions:

- Show all work to receive full credit.

Reference

Function Table – NOR S-R Flip flop				
Inputs		Outputs		Comments
S	R	Q	Q~	
0	0	Q	Q~	No Change
0	1	0	1	Reset
1	0	1	0	Set
1	1	Invalid		

Function Table – J-K Flip flop				
Inputs		Outputs		Comments
J	K	Q	Q~	
0	0	Q	Q~	No Change
0	1	0	1	Reset
1	0	1	0	Set
1	1	Q~	Q	Toggle, invert the previous state

Function Table – D Flip flop				
Input		Outputs		Comments
D	Clock	Q	Q~	
0	0	Q	Q~	No Change
0	1	0	1	Reset
1	0	Q	Q~	No Change
1	1	1	0	Set

Transition at output	PRESENT State Q(N)	NEXT State Q(N+1)	J	K
0 → 0	0	0	0	x
0 → 1	0	1	1	x
1 → 0	1	0	x	1
1 → 1	1	1	x	0
J-K FF excitation table				

555 Timer

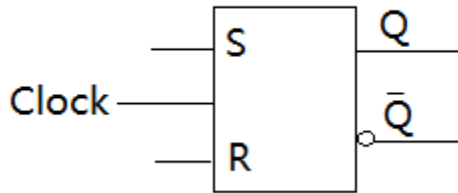
$$T_{HI} = 0.693 \cdot (R_1 + R_2) \cdot C_1$$

$$T_{LO} = 0.693 \cdot R_2 \cdot C_1$$

$$\text{Duty cycle} = (T_{HI} / \text{Period}) \cdot 100\%$$

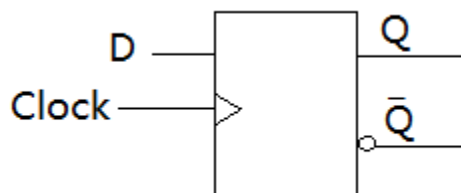
$$\text{Period} = T = T_{HI} + T_{LO}$$

Question 1) For a given S-R FF, find the output Q and Q~ assuming that Q_{initial} = 1



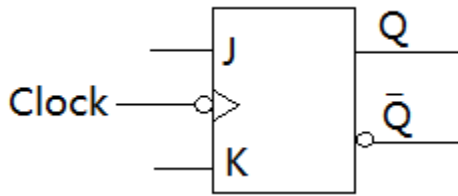
Clock								
	0	1	2	3	4	5	6	7
S								
R								
Q								
Q~								
	0	1	2	3	4	5	6	7

Question 2) For the following D-FF, sketch output Q assuming Q_{initial} = 0



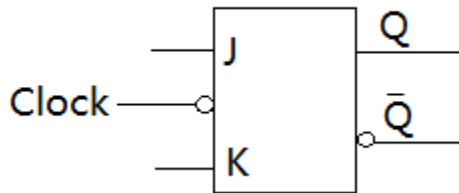
Clock								
	0	1	2	3	4	5	6	7
D								
Q								
Q~								
	0	1	2	3	4	5	6	7

Question 3) For the following J-K-FF, sketch output Q assuming $Q_{\text{initial}} = 1$



Clock	0	1	2	3	4	5	6	7	8
J	0	1	2	3	4	5	6	7	8
K	0	1	2	3	4	5	6	7	8
Q									
Q~									
	0	1	2	3	4	5	6	7	8

Question 4) For the following J-K-FF, sketch output Q assuming $Q_{\text{initial}} = 0$



Clock	0	1	2	3	4	5	6	7	8
J	0	1	2	3	4	5	6	7	8
K	0	1	2	3	4	5	6	7	8
Q									
Q~									
	0	1	2	3	4	5	6	7	8

Question 5) Design a synchronous counter that will display odd number as the following:

1→3→5→6 repeats (COUNTER SEQUENCE)

Step 1: Write and sketch the sequence of the synchronous counter (3 points)

Step 2 and 3: Construct a truth table of the transition state with the PRESENT state and the NEXT state, and complete the J-K input for each flip flop using sequence diagram from Step 1.

PRESENT state				NEXT state			J-K State					
Decimal	C	B	A	C	B	A	J _C	K _C	J _B	K _B	J _A	K _A
0	0	0	0									
1	0	0	1									
2	0	1	0									
3	0	1	1									
4	1	0	0									
5	1	0	1									
6	1	1	0									
7	1	1	1									

Circuit excitation table for sequence 1,3,5,6

Step 4: Create a k-map table for each J and K input and find the SOP equation of each.

<p style="text-align: center;">J_C</p> <table> <tr> <td></td><td>\bar{C}</td><td>C</td></tr> <tr> <td>$\bar{A}\bar{B}$</td><td></td><td></td></tr> <tr> <td>$\bar{A}B$</td><td></td><td></td></tr> <tr> <td>AB</td><td></td><td></td></tr> <tr> <td>$A\bar{B}$</td><td></td><td></td></tr> </table> <p>SOP :</p>		\bar{C}	C	$\bar{A}\bar{B}$			$\bar{A}B$			AB			$A\bar{B}$			<p style="text-align: center;">J_B</p> <table> <tr> <td></td><td>\bar{C}</td><td>C</td></tr> <tr> <td>$\bar{A}\bar{B}$</td><td></td><td></td></tr> <tr> <td>$\bar{A}B$</td><td></td><td></td></tr> <tr> <td>AB</td><td></td><td></td></tr> <tr> <td>$A\bar{B}$</td><td></td><td></td></tr> </table> <p>SOP:</p>		\bar{C}	C	$\bar{A}\bar{B}$			$\bar{A}B$			AB			$A\bar{B}$			<p style="text-align: center;">J_A</p> <table> <tr> <td></td><td>\bar{C}</td><td>C</td></tr> <tr> <td>$\bar{A}\bar{B}$</td><td></td><td></td></tr> <tr> <td>$\bar{A}B$</td><td></td><td></td></tr> <tr> <td>AB</td><td></td><td></td></tr> <tr> <td>$A\bar{B}$</td><td></td><td></td></tr> </table> <p>SOP:</p>		\bar{C}	C	$\bar{A}\bar{B}$			$\bar{A}B$			AB			$A\bar{B}$		
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K _C		
	\bar{C}	C
$\bar{A}\bar{B}$		
$\bar{A}B$		
AB		
$A\bar{B}$		

SOP :

K _B		
	\bar{C}	C
$\bar{A}\bar{B}$		
$\bar{A}B$		
AB		
$A\bar{B}$		

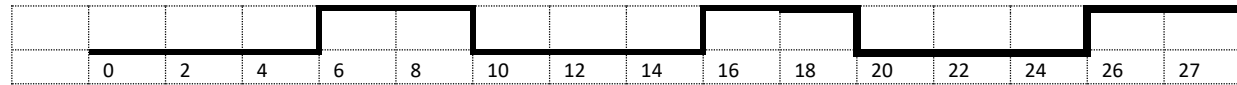
SOP:

K _A		
	\bar{C}	C
$\bar{A}\bar{B}$		
$\bar{A}B$		
AB		
$A\bar{B}$		

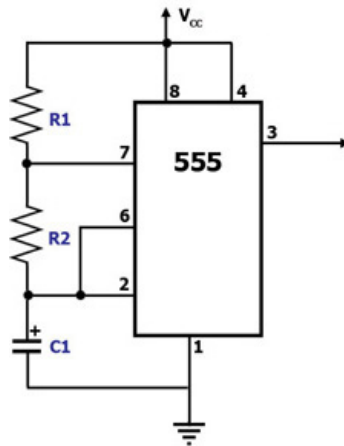
SOP:

Step 5: Complete and sketch the counter circuit using the SOP equation found in **step 4**

c. Duty cycle



c. Duty cycle



----- Homework Ends Here -----