#### **Introduction to Circuit Analysis Laboratory**

## Lab Experiment 12

# Thevenin's Theorem and Maximum Power Transfer

#### Introduction

#### Part 1- Thevenin's Theorems

Thevenin's Theorem is applied to analyze a load does not care where it gets its energy from. As a matter of fact, as long as a load gets the same required energy, it "does not know" what circuit it is connected to. To this, Thevenin said that instead of using the original circuit to supply the required energy to the load, he will substitute the original circuit with a battery in series with a resistor, each of the proper value of course, and this combination will supply the load with the same required energy as the original circuit.

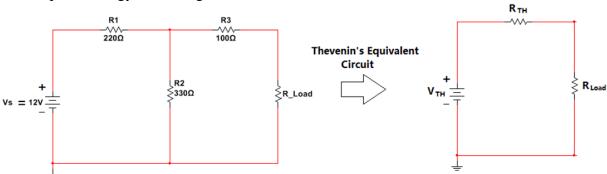


Figure 12.1 – Thevenin's Equivalent Circuit

#### Part 2 - Maximum Power Transfer

One important fact of circuit analysis is to find the conditions that should be imposed on the source and load resistance to ensure that it will deliver the maximum power to the load.

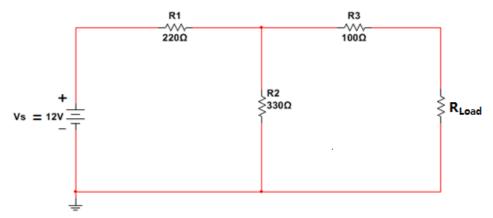
The maximum power transfer theorem states that <u>a load will receive maximum power from a network when its resistance is exactly equal to the Thevenin resistance of the network applied to the load.</u>

$$R_L = R_{TH}$$

#### Lab Experiment Procedure

#### Part 1: Original Circuit Measurements

Circuit 12.1 shows a circuit with a 12V battery connected to a series parallel circuit consisting of  $R_1$ ,  $R_2$  and  $R_3$ . This circuit feeds energy to a load resistor  $R_L$  (1 k $\Omega$  potentiometer). The expected values of load current, load voltage and power to the load are also shown. You will be asked to confirm these values in your write-up.



Circuit 12.1 Original Circuit Feeding Load Resistor

- Obtain 220  $\Omega$ , 330  $\Omega$ , and 100 $\Omega$  resistor from your components kit. Measure their resistance individually, and record the measured values in Table 12.1.
- Obtain a 1 k $\Omega$  potentiometer and measure the highest resistance of the 1 k $\Omega$  potentiometer. Record measurement in Table 12.1
- Set the potentiometer to 500  $\Omega$  and record the measurement in Table 12.1

| Given Resistance   | Measured Resistance<br>(Include unit) | Percent of difference $\left(\frac{\textit{Measured} \textit{Given}}{\textit{Given}}\right) *100\%$ |
|--|---------------------------------------|---|
| $R1 = 220 \Omega$  |                                       |   |
| $R2 = 330 \Omega$  |                                       |   |
| $R3 = 100 \Omega$  |                                       |   |
| $\mathbf{R}_{\mathbf{Load}} = 1 \ \mathbf{k} \mathbf{\Omega} \ \mathbf{pot}$ |                                       |   |
|  |                                       |   |
| Table 12.1 – Resistance measurement  |                                       |   |

- Build Circuit 12.1 in a protoboard.
- Prepare the DMM and circuit to measure current
- Measure the current through R<sub>Load</sub>. Record measurement in Table 12.2

- Prepare the DMM and circuit to measure voltage
- Measure the voltage across R<sub>Load</sub>. Record measurement in Table 12.2
- Multiply the voltage and the current through  $R_{\text{Load}}$  to obtain the power. Record the power in Table 12.2

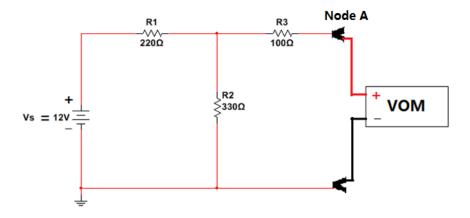
|  | $\begin{array}{c} Voltage~across~the\\ load~resistance,~V_L \end{array}$ | Current through the load resistance, $I_{\rm L}$ | Power dissipation at the load resistance, $P_{\rm L}$ |
|--|--|--|---|
| Measured Value                           |  |  |   |
| (Include Unit)                           |  |  |   |
| Table 12.2 Original Circuit Measurements |  |  |   |

Part 2 - Thevenin's Equivalent Circuit

#### Circuit With R<sub>Load</sub> Removed - Thevenin's Voltage

Circuit 12.2 shows the circuit with the load resistor removed. The open circuit voltage from Node A to ground is the Thevenin Voltage [V<sub>TH</sub>].

- Remove the load resistor,  $500 \Omega$  (potentiomenter), from the circuit and place jumper wires where the connections of  $R_{Load}$  were. Check Circuit 12.2 for reference
- Prepare the DMM to measure voltage (VOM)
- Measure the voltage across the open circuit where R<sub>Load</sub> was connected, between Node A and ground. This voltage is known as the Thevenin's voltage.
- Record this measured value in Table 12.3

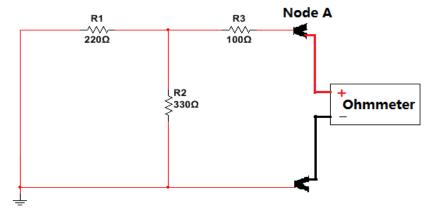


Circuit 12.2 Thevenin Voltage Measurement

#### Measuring the Thevenin's resistance

- Move one terminal of R1, the one that is connected to + power, to ground. Check Circuit 12.3 for reference.
- Prepare the DMM to measure resistance

- Measure the resistance in between the open circuit where  $R_{Load}$  was connected, between Node A and ground. This resistance is known as the Thevenin's resistance.
- Record this measured value in Table 12.3.
- Disassemble the circuit, turn off of lab equipment, organize the equipment leads, and organize the lab components.
- Proceed with calculations.

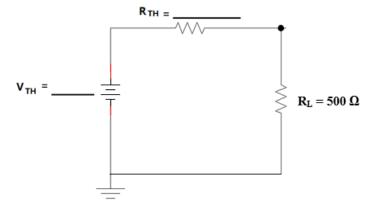


Circuit 12.3 Thevenin's resistance measurement

| Thevenin's Equivalent Circuit Measurements                              |  |                              |  |
|---|--|------------------------------|--|
|   | Voltage across the open circuit Thevenin's voltage, V <sub>TH</sub> Resistance between the open circuit Thevenin's resistance, R <sub>TH</sub> |                              |  |
| Measurements  | VIII   | The vening of esistance, Rem |  |
| (Include all unit)  Table 12.3 Thevenin Equivalent Circuit Measurements |  |                              |  |

### Calculating the voltage, current, and power at the $R_{\text{Load}}$ using the Thevenin's Equivalent circuit

Fill up the Circuit 12.4, which is the Thevenin's equivalent circuit, with measured values from Table 12.4.



Circuit 12.4 – Thevenin's equivalent Circuit

- Calculate the voltage, current, and power through  $R_L = 500\Omega$
- Record calculation in table 12.4

| Load Resistance calculation using the Thevenin's Equivalent Circuit |   |  |  |  |
|---|---|--|--|--|
|   | $ \begin{array}{ c c c c c c c c c c c c c c c c c c c$ |  |  |  |
| Calculations  |   |  |  |  |
| (Include all unit)  |   |  |  |  |
| Table 12.4 – Load analysis from the Thevenin's Equivalent Circuit   |   |  |  |  |

— Use the information in Table 12.2 and Table 12.4, and calculate the percent of difference between the original circuit and the Thevenin's equivalent circuit in Table 12.5

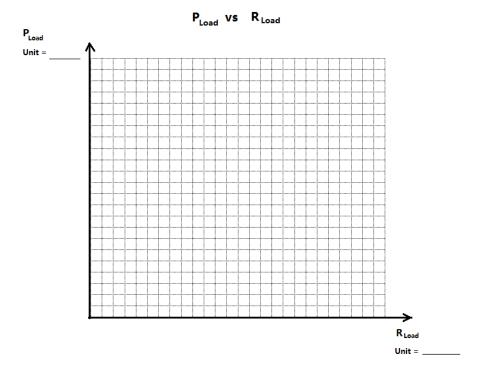
| Load Resistor Analysis                                     |  |   |  |
|--|--|---|--|
|  | Voltage across<br>the load<br>resistance, V <sub>L</sub> | Current through<br>the load<br>resistance, I <sub>L</sub> | Power dissipation<br>at the load<br>resistance, P <sub>L</sub> |
| Original Circuit   |  |   |  |
| <b>Table 12.2</b>  |  |   |  |
| Thevenin's Equivalent                                      |  |   |  |
| <b>Table 12.4</b>  |  |   |  |
| $\% = \left(\frac{Original - Thevenin's}{Original}\right)$ |  |   |  |
| × 100%   |  |   |  |
| Table 12.5 – Load Resistance Analysis                      |  |   |  |

#### Part 3 - Maximum Power Transfer Analysis

- Build the Thevenin's equivalent circuit with its respective  $R_{TH}$  and  $V_{TH}$  values as shown in Circuit 12.4. Note: if you don't have the exact  $R_{TH}$  resistor in your components' kit, you can use another potentiometer and set it to the resistance of  $R_{TH}$ .
- Set the  $R_{Load}$  potentiometer to  $0 \Omega$
- Prepare the multimeter and circuit to measure voltage.
- Measure the voltage across R<sub>Load</sub> and record the measurement in Table 12.6
- Increment the resistance of  $R_{Load}$  according to Table 12.6, measure the voltage across  $R_{Load}$ , and record the measurement in Table 12.6.
- Once all data are recorded, disassemble the circuit, turn off of lab equipment, organize the equipment leads, and organize the lab components.

| Power Analysis Through R <sub>Load</sub>          |  |  |  |
|---|--|--|--|
| $rac{R_{Load}}{\Omega}$                          | Measured V <sub>Load</sub><br>(Include unit) | $Load\ Power, P_{Load} = \frac{(V_{Load})^2}{R_{Load}}$ (Include unit) |  |
| 0 Ω   |  |  |  |
| 50 Ω  |  |  |  |
| 100 Ω   |  |  |  |
| 175 Ω   |  |  |  |
| 225 Ω   |  |  |  |
| 275 Ω   |  |  |  |
| 350 Ω   |  |  |  |
| 375 Ω   |  |  |  |
| 400 Ω   |  |  |  |
| 500 Ω   |  |  |  |
| 600 Ω   |  |  |  |
| 800 Ω   |  |  |  |
| 1000 Ω  |  |  |  |
| Table 12.6 – Power dissipation through $R_{Load}$ |  |  |  |

Using the measurements from Table 12.6, plot  $P_{\text{Load}}$  versus  $R_{\text{Load}}$ 



Graph 12.1 – Maximum Power Transfer Plot -  $P_{Load}$  vs  $R_{Load}$ 

- From Graph 12.1, estimate or measure the *Maximum Power Transfer* through load resistor, R<sub>Load</sub> and record the measurement in Table 12.7
- Calculate the Maximum Power Transfer through the load resistor using Formula 12.1. Record calculation in Table 12.7

| Maximum Power Transfer Analysis                               |  |                 |  |
|---|--|-----------------|--|
| Measured Maximum<br>Power from Graph 12.1<br>(Include Unit)   | Calculated Maximum Power using Formula 12.1 (Include Unit) | % of difference |  |
|   |  |                 |  |
| Table 12.7 – Maximum Power Transfer Analysis for Circuit 12.1 |  |                 |  |

#### Questions

- 1. Does Thevenin's Equivalent supply the load with the same power as the original circuit? Explain your answer.
- 2. From the Thevenin's Equivalent circuit, Circuit12.4, would the polarity of V<sub>TH</sub> affect the load voltage and current measurement? Explain your answer.
- 3. From Table 12.6, explain the power behavior with respect to the R<sub>Load</sub>
- 4. Can you estimate the maximum power through the load by using the data from Table 12.6? How? Explain your answer.
- 5. Thevenin's equivalent circuit, Circuit 12.4, was used to obtain the power behavior for Table 12.6. If the original circuit, Circuit 12.1, was used instead of Circuit 12.4, would the power behavior be the same or different? Explain your answer.

| Student's Name: | Lab Instructor's Signature |  |
|-----------------|----------------------------|--|
|                 | Lab Experiment Ends Here   |  |