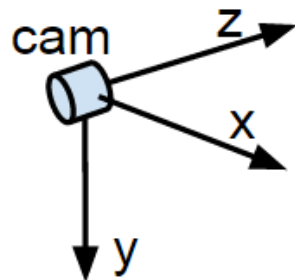
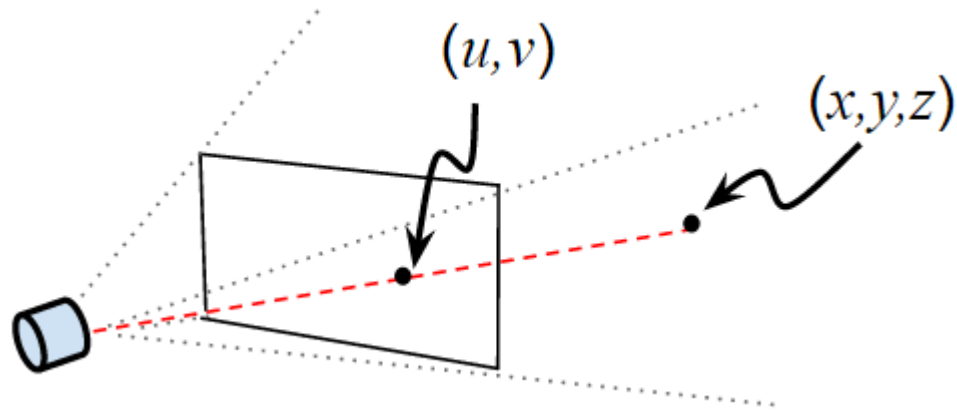


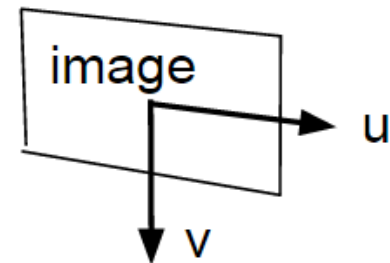
I. Ground Detection

II. RGB-Depth Image Alignment

# Preliminaries

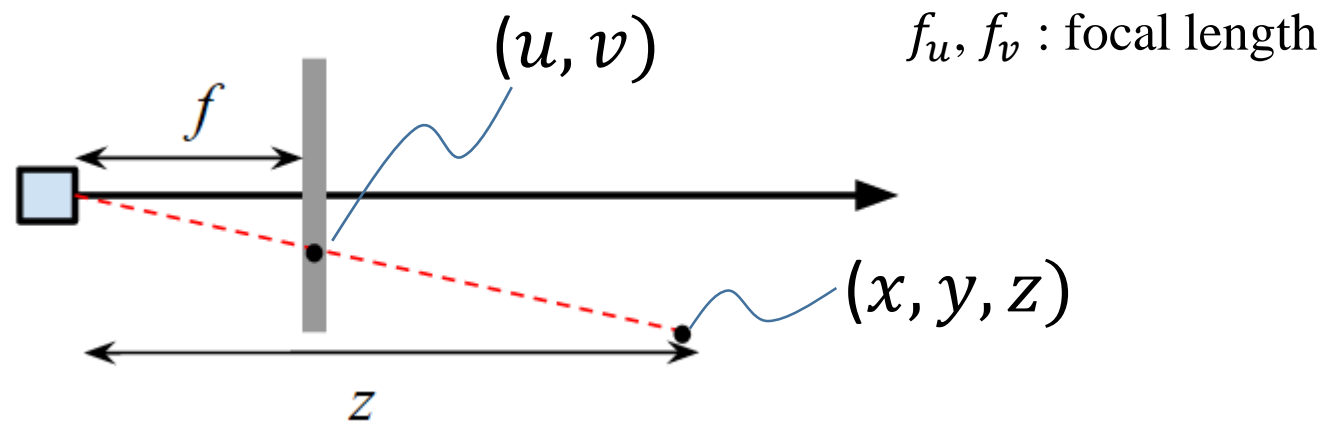


(3D) Camera coordinate frame



(2D) Image coordinate frame

# Preliminaries



$$\frac{u}{f_u} = \frac{x}{z} \qquad \frac{v}{f_v} = \frac{y}{z}$$

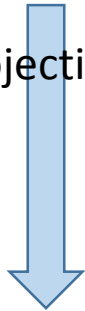
**Projection** of a 3D point on the image plane

# Preliminaries

- Plane model in  $x$ - $y$ - $z$  domain

$$a_0x + a_1y + a_2z + a_3 = 0$$

Projection



$$u = f_u \frac{x}{z} \quad v = f_v \frac{y}{z}$$

- Can use image ( $u$ - $v$ ) and inverse depth ( $d := z^{-1}$ ) domain

$$a'_0u + a'_1v + a'_2 + a'_3d = 0$$

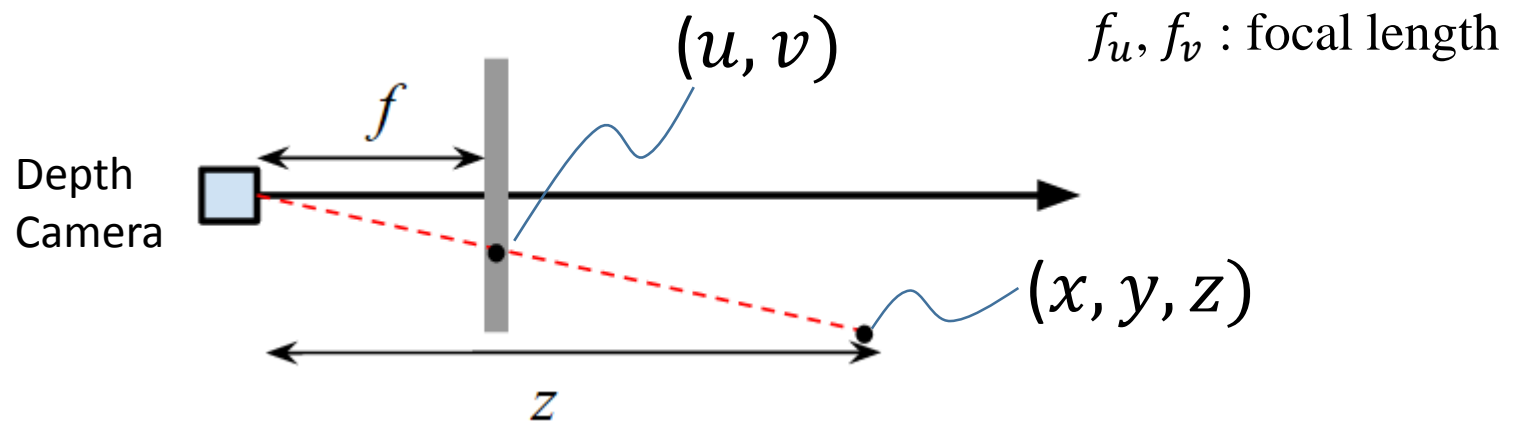
# I. Ground Detection

1) Aligned Camera

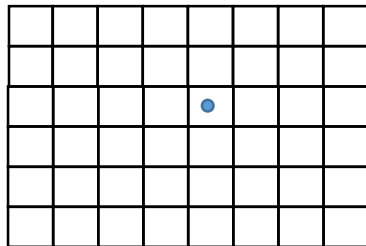
2) Rotated Camera

# II. RGB-Depth Image Alignment

# Understanding Depth Image

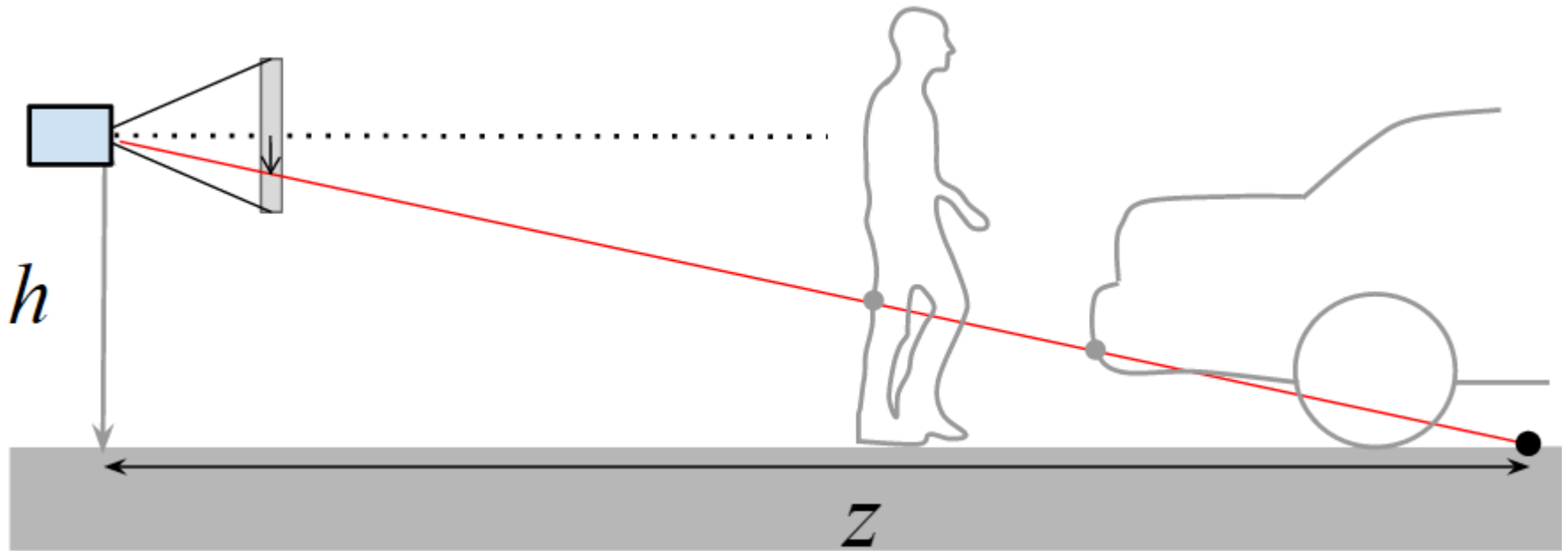


Depth Image



Pixel value at  $(u, v)$ :  $z$ -value of the point in 3D

# Ground Detection (1) *Aligned Camera*



Ground Plane model

$$y = h$$

Projection

$$\frac{v}{f_v} = \frac{y}{z}$$

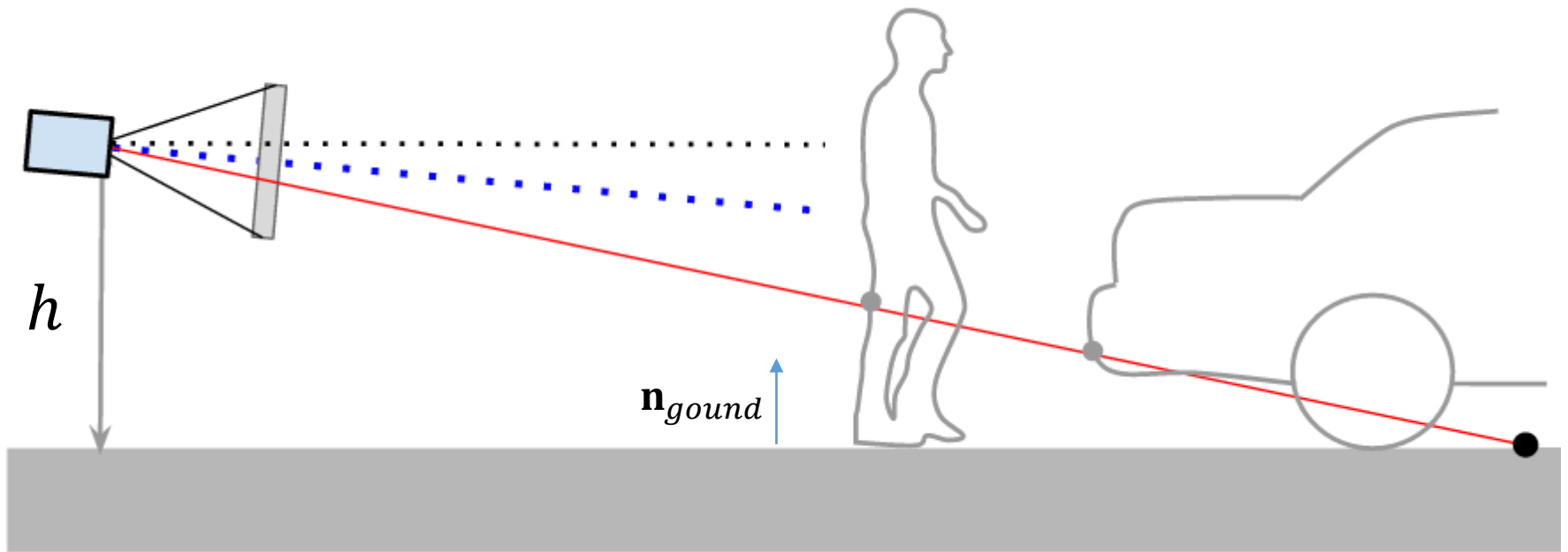
A ground point should satisfy this:

$$\left| \frac{v}{f_v} - \frac{h}{z} \right| < \varepsilon$$

\*h,f are constants!

# Ground Detection (2) *Rotated Camera*

(viewed in the global frame)

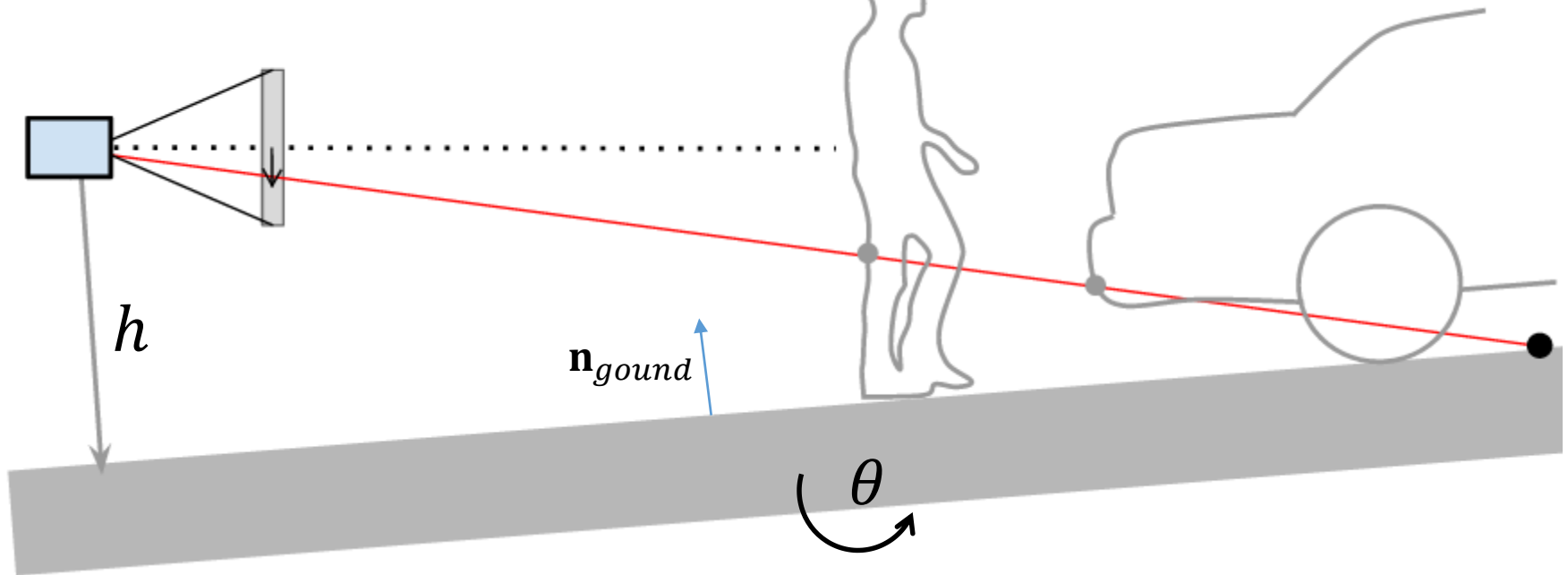


$$\mathbf{n}_{ground} = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$$



# Ground Detection (2) *Rotated Camera*

(viewed in the camera frame)



Ground Plane model

$$a_0x + a_1y + a_2z + a_3 = 0$$

Projection

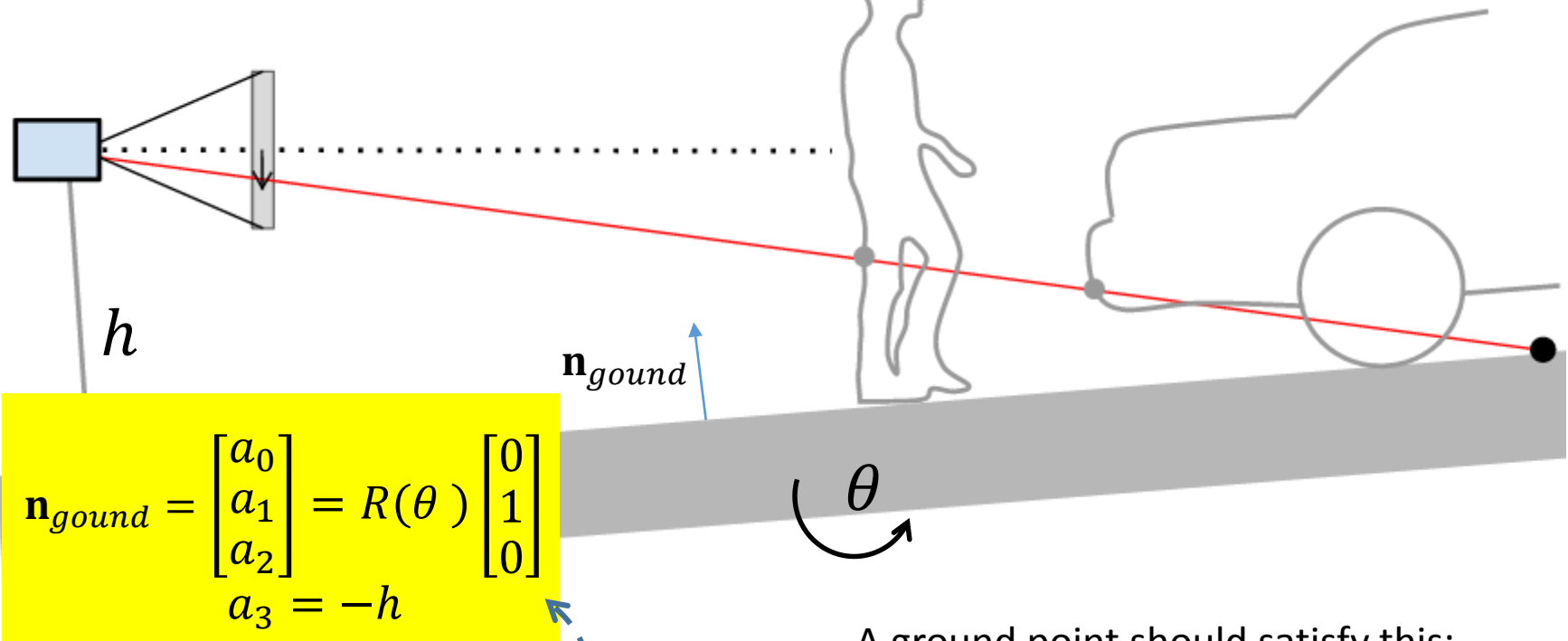


A ground point should satisfy this:

$$|a'_0u + a'_1v + a'_2 + a'_3d| < \varepsilon$$

# Ground Detection (2) *Rotated Camera*

(viewed in the camera frame)



Ground Plane model

$$a_0x + a_1y + a_2z + a_3 = 0$$

Projection

A ground point should satisfy this:

$$|a'_0u + a'_1v + a'_2 + a'_3d| < \varepsilon$$

**Coefficients are computed from this,  
where  $\theta$  is the camera pose.**

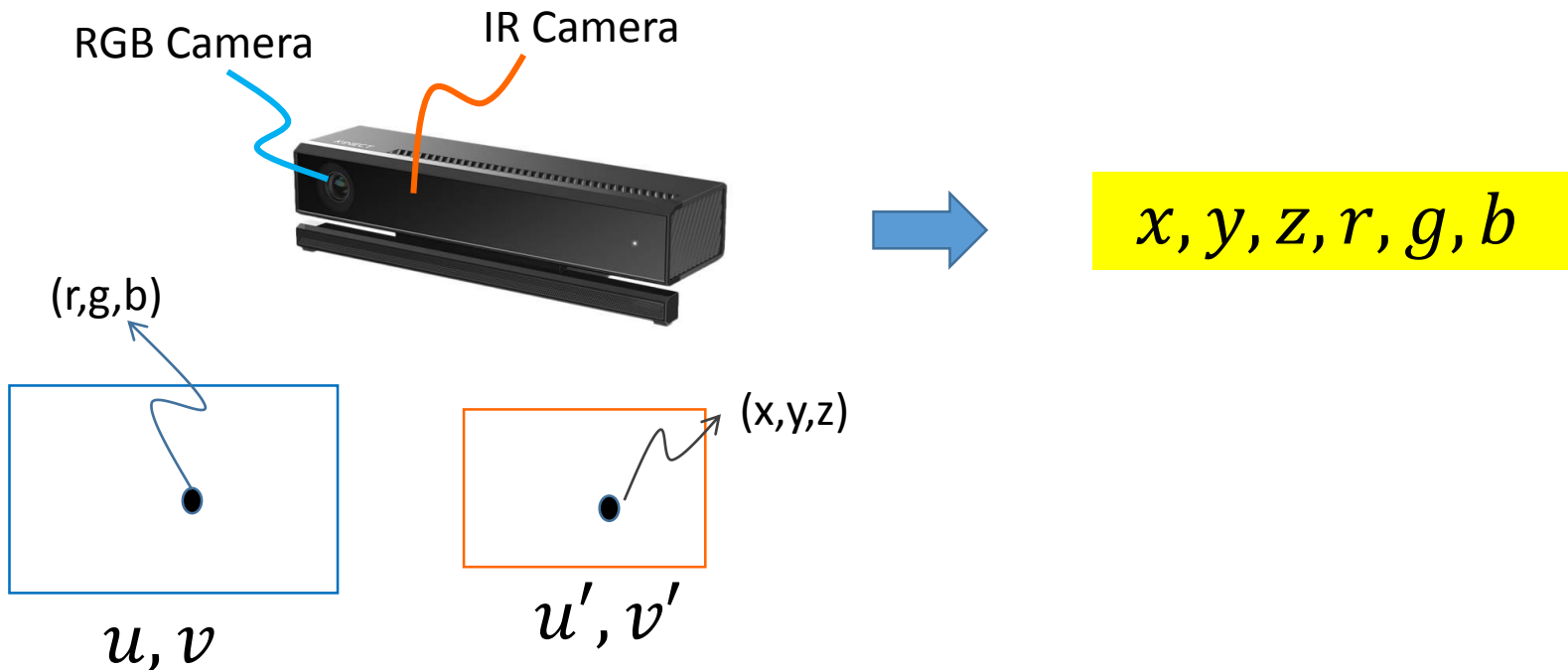
I. Ground Detection

II. RGB-Depth Image Alignment

# RGB-Depth Image Alignment

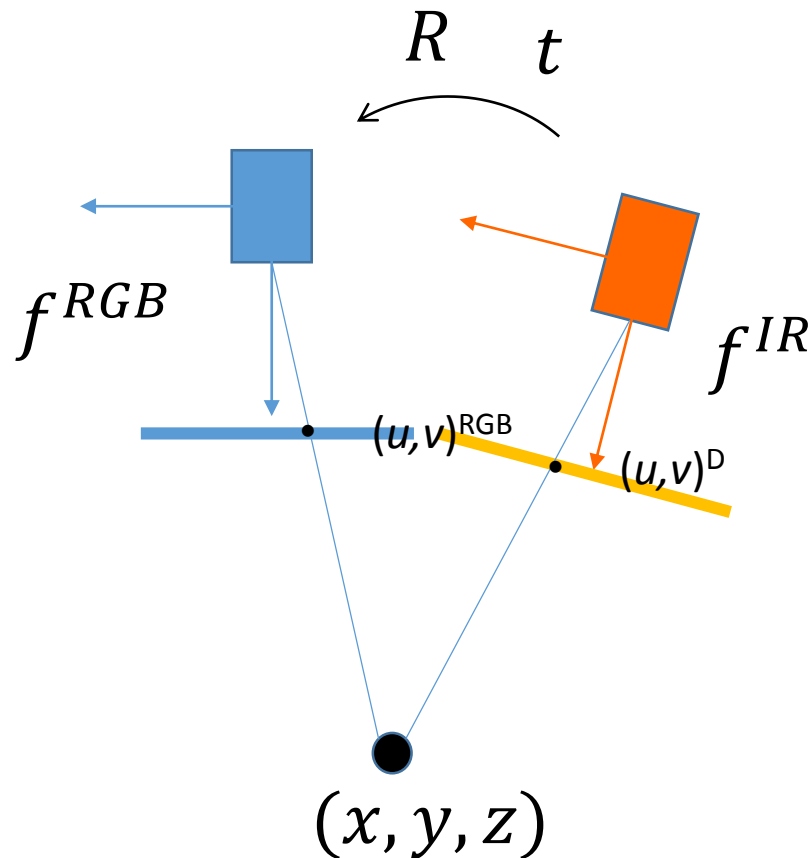
**Aim:** we want to obtain the tuple of 3d point and its color.

**Issue:** RGB images are obtained from the RGB camera, Depth images are from the IR camera. They are physically separated, and have different camera parameters.



# RGB-Depth Image Alignment

**Essential Problem:** Given all camera parameters( $R, t, f$ ), find the corresponding points of a RGB and a depth image.



# RGB-Depth Image Alignment

Recall this:

$$\frac{u}{f_u} = \frac{x}{z}$$

1) Compute the 3d coordinate  $X^{IR}$  in IR camera frame

$$x^{IR} = uz/f^{IR} \quad y^{IR} = vz/f^{IR} \quad X^{IR} = [x^{IR} \quad y^{IR} \quad z^{IR}]$$

2) Transform into the RGB camera frame

$$X^{RGB} = RX^{IR} + t$$

3) Reproject them on to the image plane

$$u^{RGB} = f^{RGB} \frac{x^{RGB}}{z^{RGB}} \quad v^{RGB} = f^{RGB} \frac{y^{RGB}}{z^{RGB}}$$

4) Read (r,g,b) at  $(u,v)^{RGB}$

# RGB-Depth Image Alignment

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4) Read (r,g,b) at  $(u,v)^{RGB}$

**This** is the color of **this** point.