## **Controls Development**

- ▶ The controller for the reaction wheel system is a simple PID loop
- ► The top-level controller design procedure was as follows:
  - 1. Determine the transfer functions from dynamics analysis of free body diagrams of the system
  - 2. Create simulation in GNU Octave
  - **3.** Design the controller using iterative testing (with comparisons to the model) and classical Bode techniques
- The forces acting on the cube are the torques created by the motors  $T_i^0$ , damping effects  $b_1\dot{\theta}_{cube}$ , and spring effects  $G_1\theta_{cube}$ . Summing the moments around the center of gravity gives the following equation (for the x-axis):

$$\sum M_0^{+\circlearrowleft} = I_{x,cube} \ddot{\theta}_{x,cube} = T_{Ax}^0 + T_{Bx}^0 - T_{Cx}^0 - T_{Dx}^0 + T_x^0 - \dot{\theta}_{x,cube} - G_x \theta_{x,cube}.$$

▶ By setting the system to Standard Equilibrium Position (at SEP the input perturbations are set to zero), considering only a single input, substituting the torque-inertia relation, and taking the Laplace transform we arrive at the (incredibly simple) transfer function of the cube:

$$G_{A}(s) = \frac{\theta_{x,cube}(s)}{\theta_{A}(s)} = \frac{s^{2}}{\frac{I_{x,cube}}{\sin(45^{\circ})I_{rw}}s^{2} + \frac{b_{x}}{\sin(45^{\circ})I_{rw}}s + \frac{G_{x}}{\sin(45^{\circ})I_{rw}}}.$$