Canonical Correlation Analysis

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#Step 1. Load dataset

```
mm <- read.csv("mmreg.csv")</pre>
# Rename columns for clarity
colnames(mm) <- c("Control", "Concept", "Motivation", "Read", "Write", "Math", "Science", "Sex")</pre>
colnames (mm)
## [1] "Control"
                     "Concept"
                                   "Motivation" "Read"
                                                              "Write"
## [6] "Math"
                     "Science"
                                   "Sex"
head (mm)
     Control Concept Motivation Read Write Math Science Sex
## 1
       -0.84
               -0.24
                            1.00 54.8 64.5 44.5
                                                     52.6
## 2
       -0.38
               -0.47
                            0.67 62.7 43.7 44.7
                                                     52.6
## 3
        0.89
                0.59
                            0.67 60.6 56.7 70.5
                                                     58.0
                0.28
## 4
        0.71
                            0.67 62.7
                                       56.7 54.7
                                                     58.0
                                                             0
## 5
       -0.64
                0.03
                            1.00 41.6 46.3 38.4
                                                     36.3
                                                             1
                            0.33 62.7 64.5 61.4
## 6
        1.11
                0.90
                                                     58.0
                                                             1
```

#Step 2. Descriptive statistics

```
summary(mm)
##
       Control
                          Concept
                                             Motivation
                                                                  Read
   Min.
          :-2.23000
                              :-2.620000
                                           Min.
                                                   :0.0000
                                                             Min.
                                                                    :28.3
                       Min.
                       1st Qu.:-0.300000
                                                             1st Qu.:44.2
   1st Qu.:-0.37250
                                           1st Qu.:0.3300
##
   Median : 0.21000
                       Median : 0.030000
                                           Median :0.6700
                                                             Median:52.1
          : 0.09653
                       Mean
                             : 0.004917
                                                   :0.6608
                                                             Mean
                                                                    :51.9
##
   3rd Qu.: 0.51000
                       3rd Qu.: 0.440000
                                           3rd Qu.:1.0000
                                                             3rd Qu.:60.1
##
   Max.
          : 1.36000
                       Max.
                             : 1.190000
                                           Max.
                                                 :1.0000
                                                             Max.
                                                                    :76.0
                                       Science
##
        Write
                         Math
                                                          Sex
           :25.50
                           :31.80
                                            :26.00
                                                            :0.000
   Min.
                    Min.
                                    Min.
                                                    Min.
   1st Qu.:44.30
                    1st Qu.:44.50
                                    1st Qu.:44.40
                                                     1st Qu.:0.000
##
## Median :54.10
                    Median :51.30
                                    Median :52.60
                                                    Median :1.000
                                           :51.76
## Mean
           :52.38
                    Mean
                           :51.85
                                    Mean
                                                    Mean
                                                            :0.545
   3rd Qu.:59.90
                    3rd Qu.:58.38
                                    3rd Qu.:58.65
                                                     3rd Qu.:1.000
## Max.
           :67.10
                           :75.50
                                           :74.20
                    Max.
                                    Max.
                                                    Max.
                                                            :1.000
```

```
## Sex
## 0 1
## 273 327
## **Tequency table for Sex
```

#Step 3. Load required packages

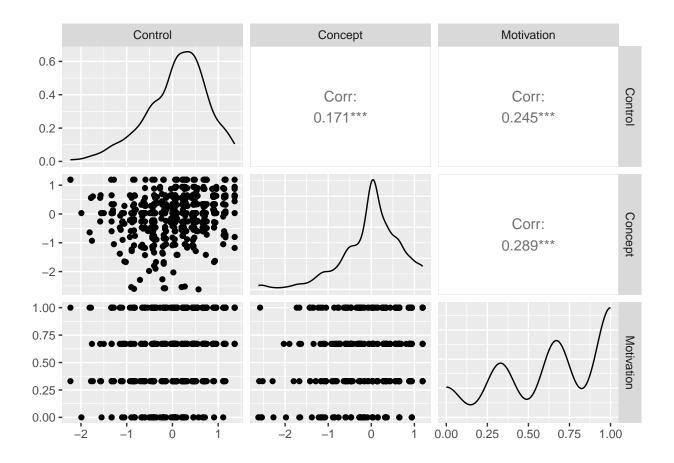
```
library(ggplot2)
library(GGally) # for ggpairs
library(CCA) # Canonical Correlation Analysis
library(CCP) # Significance testing of canonical correlations
```

#Step 4. Split dataset into psychological and academic variables

```
psych <- mm[, 1:3] # locus_of_control, self_concept, motivation
acad <- mm[, 4:8] # read, write, math, science, sex</pre>
```

#Step 5. Exploratory data analysis

```
ggpairs(psych) # pairwise plots for psychological variables
```



#Step 6. Compute correlation matrix between two sets

```
matcor(psych, acad)
## $Xcor
                          Concept Motivation
##
                Control
## Control
              1.0000000 0.1711878 0.2451323
## Concept
              0.1711878 1.0000000 0.2885707
## Motivation 0.2451323 0.2885707 1.0000000
##
## $Ycor
##
                  Read
                           Write
                                       Math
                                               Science
                                                                Sex
## Read
            1.00000000 0.6285909 0.6792757 0.6906929 -0.04174278
## Write
            0.62859089 1.0000000 0.6326664 0.5691498 0.24433183
            0.67927568 0.6326664 1.0000000 0.6495261 -0.04821830
## Math
## Science 0.69069291 0.5691498 0.6495261 1.0000000 -0.13818587
           -0.04174278 0.2443318 -0.0482183 -0.1381859 1.00000000
## Sex
##
## $XYcor
                            Concept Motivation
##
                Control
                                                      Read
                                                                 Write
                                                                             Math
              1.0000000 \quad 0.17118778 \ 0.24513227 \quad 0.37356505 \ 0.35887684
## Control
                                                                        0.3372690
              0.1711878 1.00000000 0.28857075 0.06065584 0.01944856
## Concept
                                                                        0.0535977
## Motivation 0.2451323 0.28857075 1.00000000 0.21060992 0.25424818 0.1950135
```

```
## Read
            0.3735650 0.06065584 0.21060992 1.00000000 0.62859089 0.6792757
## Write
            0.3588768 \quad 0.01944856 \ 0.25424818 \quad 0.62859089 \ 1.00000000 \quad 0.6326664
            0.3372690 0.05359770 0.19501347 0.67927568 0.63266640 1.0000000
## Math
## Science
            ## Sex
            0.1134108 -0.12595132 0.09810277 -0.04174278 0.24433183 -0.0482183
##
                Science
## Control
             0.32462694 0.11341075
## Concept
             0.06982633 -0.12595132
## Motivation 0.11566948 0.09810277
## Read
             0.69069291 -0.04174278
## Write
             0.56914983 0.24433183
             0.64952612 -0.04821830
## Math
## Science
             1.00000000 -0.13818587
            -0.13818587 1.00000000
## Sex
```

#Step 7. Perform canonical correlation analysis

```
cc1 <- cc(psych, acad)
# Display canonical correlations
cc1$cor</pre>
```

[1] 0.4640861 0.1675092 0.1039911

#Step 8. Compute canonical loadings

```
cc2 <- comput(psych, acad, cc1)
# Display canonical loadings (X & Y scores)
cc2[3:6]</pre>
```

```
## $corr.X.xscores
                                [,2]
##
                     [,1]
                                           [,3]
              -0.90404631 -0.3896883 -0.1756227
## Control
             -0.02084327 -0.7087386 0.7051632
## Concept
## Motivation -0.56715106 0.3508882 0.7451289
##
## $corr.Y.xscores
##
                 [,1]
                             [,2]
## Read
          -0.3900402 -0.06010654 0.01407661
## Write -0.4067914 0.01086075 0.02647207
## Math
          -0.3545378 -0.04990916 0.01536585
## Science -0.3055607 -0.11336980 -0.02395489
## Sex
          -0.1689796   0.12645737   -0.05650916
## $corr.X.yscores
                      [,1]
                                  [,2]
             -0.419555307 -0.06527635 -0.01826320
## Control
## Concept
             -0.009673069 -0.11872021 0.07333073
```

```
## Motivation -0.263206910 0.05877699 0.07748681
##
## $corr.Y.yscores
                [,1] [,2]
                                     [,3]
##
         -0.8404480 -0.35882541 0.1353635
## Read
## Write -0.8765429 0.06483674 0.2545608
## Math -0.7639483 -0.29794884 0.1477611
## Science -0.6584139 -0.67679761 -0.2303551
## Sex -0.3641127 0.75492811 -0.5434036
#Step 9. Tests of canonical dimensions
rho <- cc1$cor
n <- nrow(psych) # number of observations
p <- ncol(psych) # number of variables in set 1
q <- ncol(acad) # number of variables in set 2
# Calculate p-values using different F-approximations
p.asym(rho, n, p, q, tstat = "Wilks")
## Wilks' Lambda, using F-approximation (Rao's F):
                stat
                       approx df1 df2
                                              p.value
## 1 to 3: 0.7543611 11.715733 15 1634.653 0.000000000
## 2 to 3: 0.9614300 2.944459 8 1186.000 0.002905057
## 3 to 3: 0.9891858 2.164612 3 594.000 0.091092180
p.asym(rho, n, p, q, tstat = "Hotelling")
## Hotelling-Lawley Trace, using F-approximation:
##
                 stat
                        approx df1 df2
                                           p.value
## 1 to 3: 0.31429738 12.376333 15 1772 0.000000000
## 2 to 3: 0.03980175 2.948647 8 1778 0.002806614
## 3 to 3: 0.01093238 2.167041 3 1784 0.090013176
p.asym(rho, n, p, q, tstat = "Pillai")
## Pillai-Bartlett Trace, using F-approximation:
##
                        approx df1 df2
                 stat
                                            p.value
## 1 to 3: 0.25424936 11.000571 15 1782 0.000000000
## 2 to 3: 0.03887348 2.934093 8 1788 0.002932565
## 3 to 3: 0.01081416 2.163421 3 1794 0.090440474
p.asym(rho, n, p, q, tstat = "Roy")
## Roy's Largest Root, using F-approximation:
```

approx df1 df2 p.value

F statistic for Roy's Greatest Root is an upper bound.

stat ## 1 to 1: 0.2153759 32.61008 5 594

##

#Step 10. Standardized canonical coefficients

```
# Psychological variables
s1 <- diag(sqrt(diag(cov(psych))))</pre>
std_xcoef <- s1 %*% cc1$xcoef</pre>
std_xcoef
                          [,2]
##
              [,1]
                                     [,3]
## [1,] -0.8404196 -0.4165639 -0.4435172
## [2,] 0.2478818 -0.8379278 0.5832620
## [3,] -0.4326685 0.6948029 0.6855370
# Academic variables
s2 <- diag(sqrt(diag(cov(acad))))</pre>
std_ycoef <- s2 %*% cc1$ycoef</pre>
std_ycoef
##
               [,1]
                            [,2]
                                         [,3]
## [1,] -0.45080116 -0.04960589 0.21600760
## [2,] -0.34895712  0.40920634  0.88809662
## [3,] -0.22046662 0.03981942 0.08848141
## [4,] -0.04877502 -0.82659938 -1.06607828
## [5,] -0.31503962  0.54057096 -0.89442764
```